

# CONFRONTING ASTROPHYSICAL UNCERTAINTIES IN THE DIRECT DETECTION OF DARK MATTER

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## Abstract

# Published work

Parts of the work described in this thesis have appeared in the following published works:

1. *Parametrizing the local dark matter speed distribution: a detailed analysis*  
**B. J. Kavanagh**  
Submitted to Phys. Rev. D, arXiv:1312.1852
2. *WIMP physics with ensembles of direct-detection experiments*  
A. H. G. Peter, V. Gluscevic, A. M. Green, **B. J. Kavanagh**, S. K. Lee  
Submitted to Phys. Dark Universe, arXiv:1310.7039
3. *Model independent determination of the dark matter mass from direct detection*  
**B. J. Kavanagh** and A. M. Green  
Phys. Rev. Lett. 111, 031302 (2013), arXiv:1303.6868
4. *Improved determination of the WIMP mass from direct detection data*  
**B. J. Kavanagh** and A. M. Green  
Phys. Rev. D 86, 065027 (2012), arXiv:1207.2039

# Acknowledgements

*This is dedicated to all of those with big egos  
Never fakin', we get the dough and live legal*

—Dr. Dre

# Contents

<b>Contents</b>	<b>iv</b>
<b>List of Figures</b>	<b>v</b>
<b>List of Tables</b>	<b>vi</b>
<b>1 Introduction</b>	<b>1</b>
1.1 Evidence for dark matter . . . . .	2
1.2 Properties of dark matter . . . . .	8
1.3 Particle dark matter candidates . . . . .	12
1.4 Detection of dark matter . . . . .	14
<b>2 Direct detection of dark matter</b>	<b>19</b>
2.1 Introduction . . . . .	19
2.2 Direct detection formalism . . . . .	20
2.3 Direct detection experiments . . . . .	26
<b>3 Parameter Reconstruction</b>	<b>28</b>
3.1 Posterior distribution . . . . .	28
3.2 Parameter estimates . . . . .	29
<b>4 Parametrising the dark matter momentum distribution</b>	<b>30</b>
<b>5 A novel method for parametrising the speed distribution</b>	<b>31</b>
<b>6 Breaking the cross section degeneracy: neutrino telescopes</b>	<b>32</b>
<b>7 Speed parametrisation for directional experiments</b>	<b>33</b>
<b>8 Conclusions</b>	<b>34</b>
<b>Bibliography</b>	<b>35</b>

# List of Figures

1.1	CMB anisotropies measured by the Planck experiment . . . . .	3
1.2	Schematic illustration of galaxy rotation curves . . . . .	6
1.3	Schematic dark matter interactions . . . . .	15

# List of Tables

1.1	Cosmological parameters obtained by the Planck Collaboration	3
2.1	Summary of current WIMP detection experiments. . . . .	27

# Nomenclature

$\sigma_{SI(SD)}$  WIMP nucleon spin-independent (spin-dependent) cross section

$m_\chi$  WIMP mass



# Chapter 1

## Introduction

What and where is dark matter? For a question so central to cosmology and particle physics, the prospects for finding an answer do not at first glance seem promising. As with so many things in physics, we should not by all rights be able to answer the question, nature having hidden itself away in the dark recesses of the universe. But dark matter is all around us and we merely need a window through which to view it. In this work, I will discuss strategies for the direct detection of dark matter: how they offer us a window - however murky - into the dark universe; how they are faced with myriad uncertainties; and how those uncertainties can be overcome to help us to understand more about what dark matter is and how it is distributed in our tiny patch of the universe.

The question ‘*What is dark matter?*’ is perhaps best answered by reviewing the current evidence for its existence. Evidence for dark matter is found on scales from the Milky Way up to the cosmological horizon, with a range of observations which cannot be adequately explained with the observed constituents of the universe. Dark matter is an invisible component introduced to reconcile these observations with the known laws of physics - most importantly, General Relativity. Beyond this general definition, there are a wide range of particle physics candidates which may play the role of dark matter. These typically derive from theories of physics beyond the Standard Model, meaning that the study of the properties of dark matter can shed light on theories of high energy physics. Many of these proposed dark matter candidates have weak but non-zero interactions with particles of the Standard Model, leading to several avenues through which it is hoped the non-gravitational detection of dark matter may soon be achieved.

In this chapter, we summarise the evidence in support of the dark mat-

ter paradigm, including constraints from precision cosmology. We then describe some of the broad classes into which particle dark matter candidates can be categorised, as well as describing a few specific candidates in more detail. Finally, we discuss current progress and constraints from direct and indirect searches for particle dark matter.

## 1.1 Evidence for dark matter

Dark matter is a key component of the  $\Lambda$ CDM paradigm of modern cosmology. In this framework, the energy density of the universe today is dominated by the constant and uniform contribution of the vacuum,  $\Lambda$ , also referred to as Dark Energy. This contribution exerts a negative pressure and drives the accelerating expansion of the universe which was the subject of the 2011 Nobel Prize in Physics [1, 2]. However, the formation of structure in the early universe is driven by the clustering of an inert, slow moving and as yet undetected matter component [3]: Cold Dark Matter. In  $\Lambda$ CDM cosmology, baryonic matter makes up a much smaller fraction of the energy density of the universe. Cosmological experiments allow us to precisely determine the contributions of these various components (see e. g. WMAP [4], BOOMERanG [5], BOSS [6], BICEP2 [7] and CFHTLenS [8] to name just a few.)

A particularly sensitive probe for determining the dark matter contribution to the energy budget of the universe is the measurement of the temperature anisotropies of Cosmic Microwave Background (CMB) photons. These contain an imprint of the acoustic oscillations of the baryon-photon fluid during the era of recombination. The scale of these oscillations is sensitive to the size of the gravitational potential generated in the early universe by dark matter. **This is shite and needs fixing, am I talking about BAOs or what?** The recent Planck experiment [9] measured the angular power spectrum of these CMB temperature anisotropies. Figure 1.1 shows the results of these measurements, as well as the best fit 6-parameter  $\Lambda$ CDM model. The contribution of the cosmological constant, the total matter component, and the separate baryonic and dark matter components to the total energy density of the universe is shown in Table ??, constrained with an accuracy of less than 3%. We are lead to the conclusion that  $\sim 84\%$  of the matter content of the universe is in fact dark.

**Do more evidence - and less ‘problems’ - maybe move the**

Parameter	68% limits
$\Omega_\Lambda$	$0.686 \pm 0.020$
$\Omega_m h^2$	$0.1423 \pm 0.0029$
$\Omega_b h^2$	$0.02207 \pm 0.00033$
$\Omega_c h^2$	$0.1196 \pm 0.0031$

Table 1.1: Energy density of the cosmological constant ( $\Lambda$ ), total matter ( $m$ ), and separate baryonic ( $b$ ) and cold dark matter ( $c$ ) components in units of the critical density **define...**, as obtained by the Planck Collaboration [10]. The Hubble parameter is defined as  $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$ .

**BBN stuff here? Need to add more CMB and LSS stuff...** *Read for details: [arXiv:1404.5415](#)*

**CFHTLENS: [arXiv:1404.5469](#)**

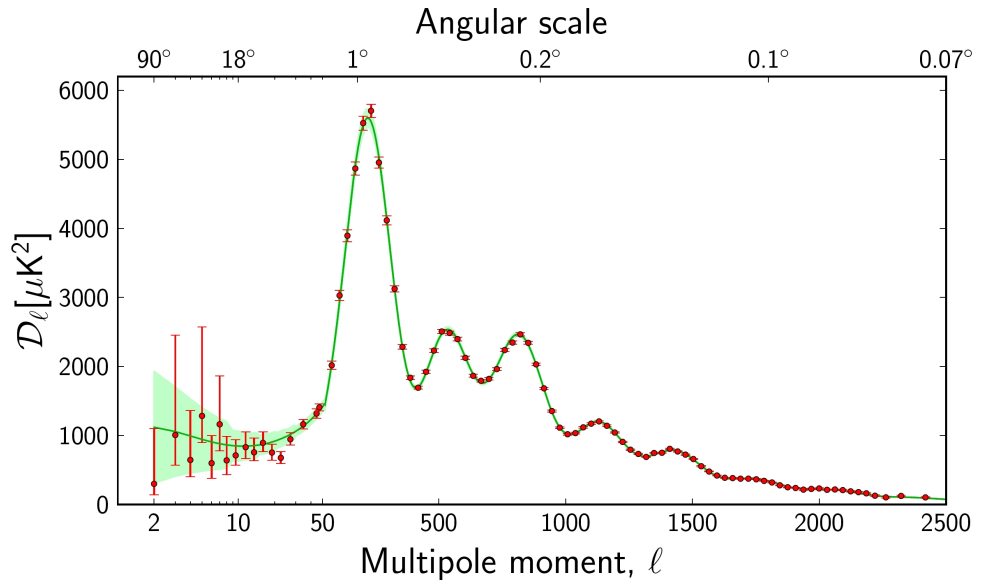


Figure 1.1: CMB anisotropies. **Need actual caption**

However, the evidence for dark matter is not purely cosmological. In 1933, Zwicky measured the velocity dispersion of galaxies in the Coma cluster [11]. An application of the Virial Theorem indicated a gravitational mass in the cluster which was several hundred times bigger than that expected from the luminosity of the member galaxies. It is now known that some of this mass is in the form of hot ( $\sim 1$  million K), X-ray emitting intracluster gas [12]. Nonetheless, a discrepancy remains; current estimates of

the mass-to-light ratio of the Coma cluster give a value of roughly 150 times that of the Sun [13, 14]. However, the Coma cluster does not appear to be unusual. Measurements of the masses of a large number of galaxy clusters using gravitational lensing [15], X-ray observations [16] and dynamical estimates [17] indicate that a significant fraction of a cluster's mass must be dark.

The validity of the  $\Lambda$ CDM paradigm is also borne out in results from N-body simulations. These simulations track the evolution of structure in the universe by accounting for the dynamics and gravitational interactions **only Newtonian?** of a large number of particles starting from some initial conditions. These may be horizon-scale cosmological simulations, tracing the collapse of the initial density perturbations after decoupling (such as the the Millenium simulation [18]), or galaxy-scale simulations, tracing the formation and growth of a small number of galaxies starting from initial conditions at intermediate redshift (such as the Via Lactea [19] and Aquarius [20] simulations).

**Maybe swap this paragraph with the next one - it makes more sense?** A variety of sophisticated computational techniques (such as smoothed particle hydrodynamics [21], adaptive mesh refinement [22] and moving mesh cosmology [23]) have been employed and refined to make such simulations computationally feasible and to allow higher and higher resolutions to be reached. In spite of this, computational limitations mean that the highest resolution simulations still use 'particle' masses of the order of  $10^5 M_\odot$  [24], many orders of magnitude more massive than the  $O(\text{GeV-TeV})$  particles expected to make up the universe's dark matter. **say more...**

Many N-body simulations are DM-only, simulating only the gravitational dynamics of collisionless particles. However, an increasing number are incorporating baryonic physics such as gas dynamics, as well as stellar evolution, chemical enrichment and a variety of feedback processes **Need some citations....** Appropriately accounting for these factors is extremely complex and in some cases the strength of these processes is unknown and must be tuned in the simulations to match observations (see for example Ref. [25]). **Mention some other problems - shock resolution etc.** Due in part to these difficulties, the impact of baryonic physics on the formation of galaxies and the properties of DM haloes is still uncertain (see for example Refs. [24, 26]). I will revisit this topic - and its consequences

for the direct detection of dark matter - in Chapter ??.

In spite of these limitations, a consistent picture has emerged from a vast array of N-body simulations. The size distribution of gravitational structures found in the universe is well matched over a range of distance scales with that obtained from N-body simulations **CITATION!**. In particular, the fact that DM is non-interacting means that it begins to collapse gravitationally earlier in cosmic time than baryonic matter. After decoupling, baryons then fall into the gravitational wells produced by the infalling DM structures. Without DM, the baryonic matter in the universe could not have had enough time to collapse to form the array of gravitationally bound structures we see today [3]. **Coldness...**

N-body simulations also suggest that galaxies such as the Milky Way should be embedded in a large, approximately spherical dark matter halo. This is corroborated by observations of the rotation curves of spiral **just spirals?** galaxies. In particular, the circular velocity of stars in these galaxies is observed to be approximately constant out to large galactocentric distances [27, 28]. This is shown schematically in Fig. 1.2. **Say something about gas, and 21cm emission (so that you can check the rotation beyond the luminous matter).** [Optical edge] The majority of the mass of the luminous disc is concentrated at small radii, suggesting that there should be a Keplerian decay of the circular velocity at large radii:  $v \sim r^{-1/2}$ . However, the inclusion of a non-luminous dark matter halo can reconcile this expectation with the observed flat rotation curves. The density profiles  $\rho(r)$  required to provide a good fit to rotation curve data are consistent with those obtained from N-body simulations, such as the Navarro-Frenk-White profile **Is this really true? Cusp/Core problem?**

$$\rho(r) = \frac{\rho_0}{r/R_s(1 + r/R_s)^2}, \quad (1.1)$$

which is described by the central density  $\rho_0$  and a scale radius  $R_s$ . This provides a good cross-check between the results of N-body simulations, which span scales up to the cosmological, and galactic-scale observations of the local universe. The rotation curve of the Milky Way itself has also been studied **[cite Mattia and others self-consistent distribution guys]**, as well as the ultralocal distribution of dark matter near the Sun's position. An understanding of this distribution has significant implications

for the study of dark matter detection and we defer a detailed discussion to Chapter ??.

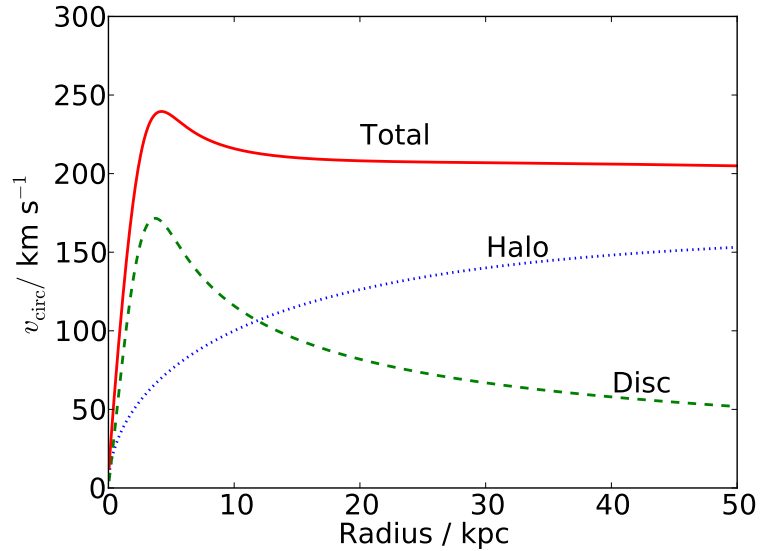


Figure 1.2: Schematic illustration of galaxy rotation curves (circular velocity as a function of galactocentric distance). The contribution to the circular velocity from the luminous disc (green dashed line) and dark matter halo (red dotted line) are shown, as well as the total circular velocity (solid blue line).

We see that evidence for dark matter appears over a wide range of distance scales, from the cosmological horizon down to our own Milky Way. Dark matter is required to explain the formation and growth of large scale structure, the dynamics of both galaxies and galaxy clusters and the anisotropic temperature distribution of the CMB among others. In spite of this, there remain several problems and unanswered questions with the dark matter paradigm.

*Cite Lyndzo! Lensing Tully-Fisher Bullet cluster*

### 1.1.1 Problems with dark matter

There have emerged several issues with the dark matter dominated model of structure formation as studied with N-body simulations. For example, DM-only simulations predict the existence of a large number of massive subhalos around Milky Way-size galaxies [20]. Using semi-analytical models of galaxy formation Kauffmann et al. [29] predicted that a Milky Way-size halo should host over 100 subhalos massive enough to support

observable satellite galaxies. However, the known population of dwarf spheroidal (dSph) satellite galaxies for the Milky Way is on the order of 20 [30], although more ultra-faint satellites are still being discovered (e.g. see Ref. [31]). This discrepancy between the predicted and observed amount of substructure in CDM structure formation is often referred to as the ‘missing satellite problem’ [32].

A related issue is the so-called ‘too big to fail’ problem, which concerns the density of dark matter subhalos. In particular, it is found that the most massive DM subhalos found in N-body simulations are too massive to host the brightest of the Milky Way’s dSph satellites [33]. If the observed dSph galaxies are hosted instead by less massive subhalos, this leaves a large number of more massive DM halos which have not yet been accounted for [34]. **NB: there are 11 well-known/bright/classical dSph satellites...**

Finally, there is also a discrepancy between the observed and simulated density profiles: the ‘Core-Cusp’ problem (for a review, see Ref. [35]). Cosmological simulations indicate that the DM density should be sharply peaked near the centre of low surface brightness and dSph galaxies [36, 37]. In contrast, observations of the rotation curves of a large number of galaxies suggests the presence of a core - a flat dark matter density profile near the centre [38, 39]. While these results are still under contention (for example, Ref. [40] find rotation curves consistent with *cuspy* density profiles), they may indicate a significant difference between the process of structure formation in the universe and that extracted from  $\Lambda$ CDM simulations.

A number of possible solutions to these issues have been suggested. Baryonic effects such as dynamical friction and stellar and supernova feedback (see for example Refs. [41–43]) can lead to the expulsion of DM from the centres of subhalos, reducing the total halo mass and leading to a flatter central density profile. **This bit could be better.** Others have suggested that a *warm* dark matter model may be a better fit to the data [44–46], reducing the amount of structure on small scales, as described in Sec. 1.2. **What about solutions about increasing the resolution of N-body simulations?** Whatever the ultimate resolution of these problems, it is clear that dark matter dominated structures such as dSph galaxies are testing ground for an even more precise understanding of structure formation in the DM paradigm.

There remains one problem which is of a much more theoretical nature. Dark matter is invoked to account for missing mass in a wide range of scenarios. However, this missing mass has not yet been observed indicating that it must interact only very weakly with photons and other particles of the standard model. In fact, as we shall see in Sec. 1.2, there is strong evidence that particles making up the universe's dark matter cannot be baryonic and must originate from beyond the Standard Model of particle physics. In the next section, we investigate what more can be inferred about the nature of particle dark matter and explore some well-motivated candidates.

*MACHOs? MOND?*

## 1.2 Properties of dark matter

Beyond its gravitational contribution to the universe, we appear to know little about the nature of particle dark matter. However, the success of modern cosmology and the lack of a confirmed detection so far means that we do have a grasp on some of the properties of any potential candidate. Taoso et al. [47] present a ‘10-point test’ which must be passed by any particle before it can be considered as a viable dark matter candidate. Here, I will briefly discuss four of these points, namely, that the DM candidate must be cold, neutral, produced with the appropriate relic density and compatible with primordial nucleosynthesis. **What about stability? THIS IS IMPORTANT FOR CANDIDATES - mention...**

### 1.2.1 Coldness

Results from N-body simulations indicate that dark matter should be *cold*. That is, DM should be travelling non-relativistically when it decouples from the thermal bath in the early universe. **Not quite true - could be warm...** In practise, this typically means that it cannot have a mass greater than around 1 keV [48]. **Watch out - this is actually the limit of WDM...** The typical speed of DM particles in the early universe defines the so-called *free-streaming length*. Below this length-scale, density perturbations are suppressed due to Landau damping [49]. For non-relativistic species, this free-streaming length scales as  $m_\chi^{-1/2}$  for thermal relics of mass  $m_\chi$  [50] **Why even say this...?** For particle candidates



which are too light - and which therefore travel too quickly after decoupling - small scale structures cannot form and cannot match the distribution of structures we see today. **Distinguish between warm and cold - what is the length scale?** *Warm* dark matter candidates with keV-scale masses have been suggested to explain the subhalo structures at the scale of dSph galaxies (as has already been discussed) However, *hot* dark matter, which decouples at relativistic speeds, is strongly-constrained and cannot make up more than around 1% of the total dark matter component [51, 52].

### 1.2.2 Neutrality

The possibility that charged massive particles (CHAMPs) may account for dark matter was proposed by De Rujula et al. [53]. Such particles be free and stable or may instead bind with electrons or positrons to form heavy neutral hydrogen-like objects. However, null searches for anomalous hydrogen in sea water [54] and anomalous heavy elements [55], as well as searches for CHAMPs in cosmic ray experiments [56] indicate that CHAMPs must be present in negligible densities in the Milky Way for masses in the range  $10 - 10^8$  GeV. **What about current constraints on ‘dark atoms’?** Millicharged DM is also strongly constrained. Searches for neutrino magnetic moments in reactor experiments exclude DM with charge greater than  $10^{-5}e$  for keV-scale masses and below [57]. Searches for distortions in the CMB caused by the interactions of millicharged particles limit the DM charge to be less than  $10^{-7}e$  for masses of 1 eV and below [58].

Could DM particles carry a colour charge? In this case, DM particles would interact strongly with particles of the SM. Such strong interactions may disrupt galaxy formation [59], distort the CMB due to scattering off baryons [60] and have been strongly constrained by experimental searches with the X-ray Quantum Calorimeter [61] and direct detection experiments [62]. **What about weak hypercharge?**

We are left with the conclusion that (without a mechanism for evading the above constraints [? ]) DM particles must carry no (or almost no) conventional electromagnetic, weak or strong charge. This rules out all SM particles (**does it...?**) as accounting for DM hinting strongly that these particles must derive from theories of physics beyond the Standard Model.

### 1.2.3 Relic density

In order to account for the dark matter in the universe, a good candidate must be produced in the early universe with sufficient abundance to match the currently observed value  $\Omega_c h^2 0.1196 \pm 0.0031$  (see Table 1.1). If produced with a smaller abundance, the candidate cannot account for the entirety of the universe's dark matter (though it could still contribute, along with other candidates, as in Ref. [63]). If on the other hand, it is produced with too great an abundance, it could threaten to exceed the DM density constraint set by Planck and overclose the universe.

#### Depends on coldness

The standard scenario for the production of dark matter is referred to as thermal freeze-out [3]. In this scenario, DM particles remain in kinetic and chemical equilibrium with SM particles in the very early universe by scattering and annihilation processes. Their abundance follows a Maxwell-Boltzmann distribution  $n \sim (m/T)^{3/2} \exp(-m/T)$  for a mass  $m$  and temperature  $T$ . As the universe expands, however, the particles become diluted, reducing the interaction rate **actually, the annihilation rate?** until eventually the DM particles become decoupled from the SM particles and are ‘frozen-out.’ They are then left with the abundance they had when they decoupled, which is further diluted by the expansion of the universe to become the abundance we see today. The exact relic abundance depends on  $\langle \sigma_{\text{ann}} v \rangle$ , the average annihilation cross section of the DM particles (weighted by the DM speed). If this is small, DM will decouple early when the temperature of the universe is still high, leading to a large relic abundance. If the annihilation cross section is large, DM will remain in equilibrium for longer, even as the particles become more and more diluted. The DM then freezes out later, with a lower temperature and lower relic abundance. This process is illustrated schematically in Fig. ?? *Make a simple figure for this.* The resulting relic abundance for GeV-scale DM is given approximately by:

$$\Omega_c h^2 \approx \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma_{\text{ann}} v \rangle}, \quad (1.2)$$

leading to a canonical value of around  $\langle \sigma_{\text{ann}} v \rangle \approx 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$  for the annihilation cross section. This coincides well with the value expected for particles with weak-scale interactions (so-called weakly interacting massive particles, or WIMPs), leading some to refer to this argument as the WIMP

miracle. **(Add in refs from page 121 of PDM.)** In reality, the full differential equations describing the DM number density must be solved [64], accounting for co-annihilations [65], which may boost the total cross section. However, the simplicity of this scenario make cold thermal relics an attractive candidate for DM.

Dark matter may also achieve the correct relic abundance through a variety of other mechanisms. ‘Freeze-in’ [66] involves particles which interact so weakly (termed feebly interacting massive particles, FIMPs) that they never reach equilibrium. Instead, a relic population is built up gradually through the production of FIMPs by annihilation of SM particles. In contrast to the freeze-out scenario, the relic abundance of FIMPs increases with increasing annihilation cross section. Dark matter may also be produced gravitationally from vacuum fluctuations during and after inflation [67, 68] or from the decays of heavier meta-stable particles (e.g. Refs [69? ]). These possibilities open up the range of candidates which may be considered to include much lighter or much heavier particles than the freeze-out scenario alone might allow.

### 1.2.4 Primordial nucleosynthesis

**Need more refs here...**

Primordial nucleosynthesis (or Big Bang Nucleosynthesis, BBN) describes the production of light nuclei in the first few minutes after the big bang. By solving a set of coupled Boltzmann equations describing the nuclear reactions of protons, neutrons and light nuclei, we can obtain the primordial abundances of these light nuclei and compare with the inferred values. **Citation** Significantly, these abundances depend strongly on the baryon-photon ratio  $\eta$  and therefore the total baryon density. Fits to data lead to the result  $\Omega_b h^2 = 0.017 - 0.024$  [70], independent of the value obtained from CMB measurements (Table 1.1). Thus, the dark matter of the universe cannot be baryonic. **Combine this with the ‘neutrality’ constraint and we see that there are no SM particles (or their spartners?) with the correct quantum numbers.** We are led to conclude that particle dark matter must consist of some as-yet undiscovered particle. **Link this to the next section...**

The results of BBN are also very sensitive to light new species, which can alter the number of relativistic degrees of freedom in the early universe

and therefore affect the expansion rate. These include, for example, gravitinos [71], right-handed neutrinos [72] and millicharged particles []. BBN therefore provides strong constraints on the parameters of such models. **What about stating some of the constraints on  $N_\nu$ ?** In addition, the decay of dark matter particles into electromagnetic or hadronic showers during nucleosynthesis can drastically change the primordial abundances of the light elements. BBN can therefore be used to constrain models in which dark matter undergoes early decays (or in which dark matter is produced by the decays of heavier particles) [73].

### 1.3 Particle dark matter candidates

#### **Make an explicit distinction between WIMPs and non-WIMPs?**

While *valid* DM candidates need only satisfy the conditions and constraints which have already been discussed, *well-motivated* candidates should derive sensibly from some as-yet undiscovered theory of physics. In fact, dark matter candidates can be found in a wide range of models of particle physics beyond the standard model. As has already been discussed, massive particles with GeV-scale masses and weak-scale interactions are attractive for obtaining the correct DM relic density. Such a WIMP candidate may be provided by the lightest supersymmetric particle (LSP) in supersymmetric theories [74]. In supersymmetry, each of the known SM particles has a supersymmetric partner (or ‘spartner’), with bosons having fermionic partners and vice versa - this additional symmetry is often invoked to help alleviate the hierarchy problem [75]. In models which possess R-parity [**say more?**], particles carry R-parity 1 while supersymmetric particles (‘sparticles’) carry R-parity -1. This means that the lightest sparticle cannot decay into SM particles and is therefore stable, making it a promising DM candidate.

#### **Does this hold JUST for the MSSM?**

Depending on the parameters of the supersymmetric theory, there are many possibilities for which sparticle will be the LSP. One popular and well-studied possibility is the neutralino  $\chi$  [76? ], which is a linear combination of the neutral supersymmetric partners of the  $W$ ,  $B$  and Higgs bosons [**These are the CP-even higgsinos of the MSSM**]. The properties of the neutralino can vary dramatically depending on the mixing between these different components and the underlying supersymmetric parameters

[77] **[This is a bad citation...]**. *Neutralino pros and cons...* In different scenarios **which are...?**, the LSP may be sneutrino [78], a partner of the standard model neutrino. *Say more about sneutrinos...are they excluded already by direct searches?* Another alternative is the gravitino, in which case it may be produced gravitationally in the early universe with a mass greater than  $10^{12}$  GeV, leading to the title ‘WIMPzilla’ [79].

WIMPs also arise in theories of universal extra dimensions, in which the additional dimensions are compactified, leading to a tower of excited states of the standard model particles [80]. These ‘Kaluza-Klein’ (KK) particles also possess a KK-parity, which means that the lightest KK particle (LKP) is stabilised [81]. One possibility for the LKP is the first excitation of the  $B$  weak hypercharge boson,  $B^{(1)}$ . In this case, the WIMP would be a spin-1 particle with a mass of around 1 TeV (in order to be produced thermally with the correct relic abundance) [82]. However, it has also been shown that the first KK excitations of the photon and neutrino are viable DM candidates if they also have masses at the TeV scale [83]. In contrast to the LSP, the LKP is described by a relatively small parameter space and may be more easily constrained by upcoming experiments [84].

In light of the problems with models of dark matter structure formation on small scales, there are several candidates which may be attractive for constituting warm dark matter. While standard neutrinos (with masses of a few eV [85]) cannot account for a large fraction of the dark matter **[see earlier]**, keV-scale sterile neutrinos may be viable [86]. Sterile neutrinos interact with ordinary matter via neutrino mixing rather than via electroweak interactions. **[Constraints in Ref.59 of <http://arxiv.org/pdf/0903.4849v4.pdf>]** While attractive for providing warm dark matter, non-thermal production [87] or multiple sterile neutrinos species [88] may be required to avoid many of these constraints.

Another non-WIMP candidate is the axion. The axion was originally introduced by Peccei and Quinn [89] to solve the strong CP problem. It was observed that this spin-zero particle should be produced in abundance in the early universe via the ‘misalignment mechanism’ and, for masses in the range  $10^{-5} - 10^{-3}$  eV, can account for the cosmological dark matter [90]. It was recently noted that axion dark matter would thermalise and form a Bose-Einstein condensate, acting as cold dark matter at late times [91], as well as explaining anomalies in the alignment of CMB multipoles [92]. Also of interest are axion-like particles (ALPs), which emerge naturally in

string theory and are expected to span many orders of magnitude in mass and coupling strength [93]. **[Be more explicit about mass ranges.]**

As is clear from this discussion, there are a wide range of well-motivated candidates for the dark matter in the universe. Some further examples include **[list some...]**, as well as minimal approaches to DM [94]**and others....** In this work, we focus on the WIMP, not only because of its popularity and generic nature, but because of the large number of experimental searches which provide sensitivity to WIMP dark matter.

**[Some overlap here in text...]** The final condition appearing in the ‘10-point test’ of Taoso et al. asks the question ‘Can it be probed experimentally?’ While there are viable DM candidates which interact only gravitationally (such as **WHAT?**), a wide variety of proposed candidates can interact (however weakly) with the particles of the standard model. While the experimental accessibility of a given DM candidate is not a strict necessity, it allows models to be tested (and either falsified or confirmed) beyond the hypothesis stage. In the next section, we explore the different avenues by which models of particle dark matter may be probed.

## 1.4 Detection of dark matter

Many of the candidates which have been discussed are expected to interact weakly with the particles of the Standard Model. Dark matter particles which are produced by thermal freeze-out in the early universe must have interactions with SM **[Define SM somewhere]** particles in order to maintain thermal and kinetic equilibrium. These interactions are mediated by Feynman diagrams which can be represented (schematically) as in Fig. 1.3. The existence of production, annihilation and scattering processes between DM and SM particles provides a window into the possible detection of particle DM. Each of these processes leads to a distinct detection strategy, often referred to as collider, indirect and direction detection.

### 1.4.1 Collider production

**Elaborate and actually explain more of this section. Add more from the PDM... What about actual current limits, nothing seen yet? What about kinematic endpoints...?**

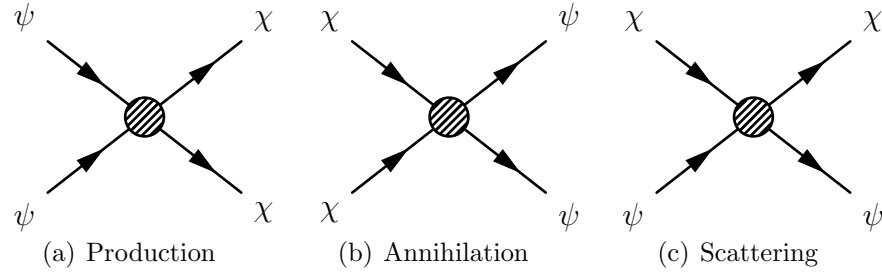


Figure 1.3: Schematic interactions between dark matter particles  $\chi$  and standard model particles  $\psi$ .

Searches for dark matter at the LHC **[What about LEP/Tevatron?]** rely on processes such as Fig. 1.3(a), in which SM particles annihilate to produce dark matter particles. However, the weak interactions of the DM means that once produced, it will escape the detectors of ATLAS and CMS. Thus, collider searches for dark matter must look for other signatures.

One approach is to look for signatures which are characteristic of a particular theory. For example, looking for evidence of KK states which are expected in theories of universal extra dimensions [95, 96], or searching for particle signatures from decay chains which are expected from supersymmetry [97, 98]. While this allows for tight constraints to be placed on specific models, the range of models may be large, making this approach unfeasible. **This is a bit harsh...**

An alternative approach is to look for deviations from the SM expectation and use this to place limits on the operators of an effective field theory [? ]. One possible signature is to look for the pair production of DM states, with initial state radiation of a SM particle. Combining the possibilities for what is in this initial state radiation (quarks, gluons, photons,  $Z$ s, etc.), we can perform a so-called **mono-everything** search [99]. **Mention actual results and mention effective operators...** It is also possible to look for more general missing energy signatures [100], in which energy is carried away by the dark matter particle produced. **So far nothing has been observed.**

One advantage of the effective operator approach is that these bounds can be translated into limits on signals at direct and indirect experiments, allowing collider results to be incorporated with other experimental searches in a complementary fashion [101]. However, it has been noted that caution must be exercised in naively applying the field theory approach at the LHC as well as in translating this to other search channels [102, 103].



*Improve, and talk about a future collider and how it might help.*

### 1.4.2 Indirect detection

*FINISH THIS SECTION!*

The possibility of dark matter annihilation into SM particles (as described in Fig. 1.3(b)) means that DM may be detected indirectly, by searching for these excess annihilation products (and related decay products). Some searches aim to look for the contribution of these products to signals obtained over large areas. The Fermi-LAT collaboration have published limits on searches for spectral lines and contributions to the diffuse background of gamma-rays [104]. Cosmic ray experiments such as PAMELA [105] **and ...** have aimed to measure the  $p^\pm$  and  $e^\pm$  abundances in cosmic rays. The AMS experiment [106] has recently reported a rise in the cosmic ray positron fraction at energies above 10 GeV, which has been interpreted as tentative evidence for dark matter annihilations (see e.g. Ref. [107] **and others**). In the case of charged particle cosmic rays, astrophysical magnetic fields deflect the paths of particles, meaning that it can be difficult to resolve individual sources [].

In contrast, photon searches allow specific locations to be targeted. Because the signal rate is proportional to the DM annihilation rate (along the line of sight), the potential signal scales as the square of the dark matter density. Thus, searching in areas where the DM density is expected to be high can boost the signal rate significantly [108]. As has already been discussed, dSph galaxies are dark matter dominated objects and thus represent promising targets for indirect searches. A survey of 25 Milky Way satellite galaxies by the Fermi-LAT telescope [109] has so far found no significant gamma-ray signal, however, again constraining the possible DM annihilation cross section *give values*. By optimising search regions near the centre of the Milky Way for maximum signal-to-noise, Weniger recently found a bump in the gamma-ray spectrum of Fermi-LAT data around 130 GeV [110]. However, subsequent analysis has found that this feature may be a systematic effect in the detector [111] and that it is difficult to reconcile with conventional models for dark matter [112, 113].

Perhaps more promising is a different gamma ray signal coming from the inner regions of the Galaxy, peaking at energies around 1-3 GeV [114, 115]. Fits of the data point towards a dark matter particle with a mass of 31-40



GeV, annihilating predominantly to  $b\bar{b}$  with a cross section of  $\langle\sigma v\rangle(1.4 - 2.0) \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$ , approximately matching the value required for a particle created by thermal freeze-out in the early universe. While it has been suggested that this signal is actually consistent with known sources [116] or as yet unresolved astrophysical sources [117], further analysis has shown that the signal matches the spectrum and morphology expected from DM annihilation [118]. **Mention the significance...** Confirmation of the signal may have to wait until it is corroborated by independent observations, for example a DM annihilation signal from dSph galaxies.

Another potentially rich source of DM annihilations are the Sun and Earth. DM particles may scatter with nuclei in these bodies, losing energy and eventually becoming captured. Eventually, the DM sinks to the centre of the object and annihilates. The only annihilation products which can escape are neutrinos which can then be detected at neutrino telescopes such as ANTARES [119] and IceCube [120]. Because the neutrino flux depends on the scattering rate of DM with nuclei, such signals can probe similar (but complementary) parameter spaces to direct detection experiments. We treat this subject in more detail in Chapter ??.

*Give some solid results and talk about future experiments.*

*ICECUBE SEARCHES FOR DM ANNIHILATION IN GALAXIES AND CLUSTERS [121]*

*IACTS: HESS, MAGIC, VERITAS and CTA [122]*

### 1.4.3 Direct detection

Processes described by the diagram in Fig. 1.3(c) lead to the possibility of scattering between DM and SM particles. The principle of direct detection is to look for nuclear recoils due to this scattering in a dedicated detector [? ? ]. However, WIMPs with GeV-scale masses and speeds  $v \sim 10^{-3}c$  (as predicted by N-body simulations [? ] and direct calculations []) are expected to produce keV-scale nuclear recoils. In addition, due to the expected low cross section for such interactions, the predicted rate is less than around 1 event per year per kg of detector mass **Check and cite**. Detecting such rare, low energy recoils requires not only large ton-scale detectors, but also sophisticated methods for discriminating signal from background.

*Write one paragraph about the tentative signals. Start with the refer-*

*ences in here arXiv:1207.2039. Go back and do this after I've done the DD chapter.*

The interpretation of direct detection data will be the main focus of this work and we will therefore defer a more detailed discussion until Chapter ??.

*Say something about complementarity between these 3.*

#### 1.4.4 Conclusions

The  $\Lambda$ CDM paradigm has enjoyed great success in explaining observations from galactic to cosmological scales. While discrepancies with observations on smaller scales remain, these are being actively pursued and may prove to be valuable testing grounds for the process of dark matter structure formation. The identity of dark matter is unknown and cannot be accounted for by any of the known standard model particles. Even so, we know that it must be neutral, long-lived and cold (or possibly warm) and that it must pass a variety of stringent tests coming from BBN and the CMB. There is no lack of well-motivated CDM candidates, including the lightest supersymmetric and Kaluza-Klein particles, sterile neutrinos, axions and many more. We have focussed on the search for weakly interacting massive particles (WIMPs) and shown that tight limits have been set by a wide range of direct, indirect and collider experiments and that the prospects for detecting WIMPs in the near future are good.

# Chapter 2

## Direct detection of dark matter

### 2.1 Introduction

The idea that particle dark matter (DM) may be observed in terrestrial detectors was first proposed by Goodman and Witten in 1985 [123] and by Drukier, Freese and Spergel in 1986 [124]. If DM can interact with particles of the Standard Model, the flux of DM from the halo of the Milky Way should be large enough to cause measureable scattering from nuclei. If the subsequent recoils can be detected and their energy spectrum measured, it should be possible to infer some properties of the DM particles.

However, the expected event rate for keV-scale recoils at such a detector would be of the order of  $10^{-10}$  events per kg of detector material per day per keV recoil energy [125]. With such a low event rate, it is imperative that backgrounds can be reduced as much as possible. In addition, detectors should be as large as possible and sensitive to as wide a range of recoil energies as possible, in order to maximise the total number of events observed. Thus, specialised detectors are required to shield the active detector material from backgrounds and to discriminate between these backgrounds and signal events.

There exist at present a wide range of detectors using a variety of different sophisticated techniques for detecting such a weak signal against ubiquitous backgrounds, each probing a slightly different range of DM parameter space. Several of these experiments - such as DAMA/LIBRA [126], CoGeNT [127, 128] and CRESST-II [129] - claim to have observed a signal

indicative of a WIMP with mass  $\sim 10$  GeV. However, a number of other experiments have reported null results creating tension for a dark matter interpretation of these tentative signals. It remains to be seen whether this discrepancy is an experimental effect or physically meaningful result.

There remain a number of uncertainties in the direct detection of dark matter. These come from a variety of sources and can be approximately partitioned into experimental, nuclear, particle and astrophysical uncertainties. Understanding these uncertainties is imperative for properly interpreting the results of direct detection experiments and understanding whether a coherent picture can emerge from a number of different experimental efforts.

In this chapter, I will review the formalism for direct detection which was introduced by Goodman, Witten, Drukier, Freese and Spergel in the 1980s (and subsequently refined). I will then briefly discuss some of the experimental techniques which are used to achieve the required sensitivity for DM searches, as well as summarising current experimental constraints and results. I will outline some of the uncertainties which afflict the interpretation of direct detection data.

I will focus on astrophysical uncertainties in direct detection. In particular, I will discuss the local density and distribution of dark matter impacts the direct detection event rate, how well we understand these different factors and review approaches which have been developed in the past to mitigate these uncertainties.

## 2.2 Direct detection formalism

*Make sure I get the right citations and stuff in here... Generalise to many nuclei etc... Make the distinction NOW about f1 or f or f3 and what I mean by that...*

**ELASTIC SCATTERING - what about the alternatives? Form factor DM, higher order stuff, effective operator, inelastic?**

**This only applies to fermionic dark matter!!!**

**Introduce the term WIMPs**

We wish to obtain the rate of nuclear recoils per unit detector mass.

The differential event rate  $R$  can be written straightforwardly as

$$\frac{dR}{dE_R} = N_T \Phi_\chi \frac{d\sigma}{dE_R}, \quad (2.1)$$

for recoils of energy  $E_R$ ,  $N_T$  target particles, a DM flux of  $\Phi_\chi$  and a differential scattering cross section of  $\frac{d\sigma}{dE_R}$ . Per unit detector mass, the number of target particles is simply  $N_T = 1/m_N$ , for nuclei of mass  $m_N$ . The DM flux for particles with speed in the range  $v \rightarrow v + dv$  is  $\Phi_\chi = n_\chi v f(v) dv$ . Here,  $n_\chi$  is the number density of dark matter particles  $\chi$  and  $f(v)$  is the speed distribution for the dark matter. This distribution function describes the fraction of DM particles having a given speed. Finally, we can convert from the number density to the mass density  $\rho_0$  by dividing by DM particle mass  $m_\chi$ :  $n_\chi = \rho_0/m_\chi$ . By integrating over all DM speeds, we therefore obtain

$$\frac{dR}{dE_R} = \frac{\rho_0}{m_N m_\chi} \int_0^\infty v f(v) \frac{d\sigma}{dE_R} dv. \quad (2.2)$$

The differential scattering cross section per solid angle in the zero-momentum frame (ZMF),  $\Omega^*$ , is given by:

$$\frac{d\sigma}{d\Omega^*} = \frac{1}{64\pi^2 s} \frac{p_f^*}{p_i^*} |\mathcal{M}|^2, \quad (2.3)$$

where  $\mathcal{M}$  is the scattering amplitude obtained from the Lagrangian. For elastic scattering, the final and initial momenta in the ZMF are equal:  $p_f^* = p_i^*$ . The centre-of-mass energy squared,  $s$ , can be written  $s \approx (m_\chi + m_N)^2$ , where we have used the non-relativistic approximation **This is only justified later**. The recoil energy can be written in terms of the ZMF scattering angle  $\theta^*$  as [125]

$$E_R = \frac{\mu_{\chi N}^2 v^2}{m_N} (1 - \cos \theta^*). \quad (2.4)$$

Noting that  $d\Omega^* = d\cos \theta^* d\phi$ , we can write:

$$\frac{dE_R}{d\Omega^*} = \frac{\mu_{\chi N}^2 v^2}{2\pi m_N}, \quad (2.5)$$

and therefore

$$\frac{d\sigma}{dE_R} = \frac{1}{32\pi m_N m_\chi^2 v^2} |\mathcal{M}|^2. \quad (2.6)$$

The matrix element  $\mathcal{M}$  is obtained from interaction terms in the lagrangian between the DM particle and quarks. This will depend on the particular DM model under consideration and the full form of these interaction terms is not known. However, because the WIMPs have speeds of order  $10^{-3}c$ , the scattering occurs in the non-relativistic limit, leading to some important simplifications. In this limit, the axial-vector interaction simply couples the spins of the WIMP and quark. The scalar interaction induces a coupling of the WIMP to the number of nucleons in the nucleus, with the vector<sup>1</sup> and tensor interactions assuming the same form as the scalar in the non-relativistic limit [74]. All other interactions are typically suppressed by powers of  $v/c$  and so will be subdominant (though we will consider briefly scenarios where this is not the case in Sec. ??). **Check and cite...** Generically, then, the cross section is typically written in terms of spin-independent (SI) and spin-dependent (SD) interactions [123] **Talk a bit more here about effective field theories - find the right paper - there's one that has all the v/c dependences - mentioned in [130]... - only considering contact interactions, slow moving spin-1/2,...[131–134] - axial-vector and scalar currents do not interfere...**

$$\frac{d\sigma}{dE_R} = \frac{d\sigma_{SI}}{dE_R} + \frac{d\sigma_{SD}}{dE_R}. \quad (2.7)$$

We now discuss the form of the SI and SD cross sections in turn.

### 2.2.1 SI interactions

Spin-independent interactions are generated predominantly by scalar terms in the effective lagrangian **NB: Contact interactions in some effective field theory - what about loop diagrams...?**

$$\mathcal{L} \supset \alpha_S^{(q)} \bar{\chi} \chi \bar{q} q, \quad (2.8)$$

for interactions with a quark species  $q$  with coupling  $\alpha_S^{(q)}$ . The operator  $\bar{q}q$  is simply the quark number operator, which couples to the quark density. However, we should recall that the quarks are in nucleon bound states  $|n\rangle$ , so we should evaluate  $\langle n | \bar{q}q | n \rangle$ , adding coherently the contributions from both valence and sea quarks. These matrix elements are obtained

---

<sup>1</sup>For the case of a Majorana fermion, the vector current vanishes and we need not consider it.

from chiral perturbation theory [135] or Lattice QCD [136]. These matrix elements can be parametrised in terms of their contribution to the nucleon mass in the form:

$$m_n f_{Tq}^n \equiv \langle n | m_q \bar{q}q | n \rangle. \quad (2.9)$$

Adding the contributions of the light quarks, as well as the heavy quarks and gluons (which contribute through the chiral anomaly [137]), we obtain

$$\langle n | \sum_{q,Q,g} \bar{q}q | n \rangle = \left( \sum_{q=u,d,s} \frac{m_n}{m_q} f_{Tq}^n \alpha_S^q + \frac{2}{27} f_{TQ}^n \sum_{q=c,b,t} \frac{m_n}{m_q} \alpha_S^q \right) \equiv f^n. \quad (2.10)$$

The parameters describing the contributions of the different quarks to the nucleon mass be determined experimentally. The uncertainties this produces will be discussed shortly in Sec. ?? **Check - what exactly is this equal to...**

We now consider the matrix elements of the nucleon operators within a nuclear state,  $|\Psi_N\rangle: \langle \Psi_N | f^n \bar{n}n | \Psi_N \rangle$ . These operators now simply count the number of  $n$  nucleons in the nucleus, along with a momentum-dependent form factor,  $F(\mathbf{q})$ , corresponding to the Fourier transform of the nucleon density. This takes into account the loss of coherence for nuclear scattering due to the fact that the nucleus is not point-like. We therefore obtain:

$$\langle \Psi_N | f^n \bar{n}n | \Psi_N \rangle = \langle \Psi_N | \Psi_N \rangle f^n N_n F_n(\mathbf{q}) = 2m_N f^n N_n F_n(\mathbf{q}), \quad (2.11)$$

where we note that we require the wavefunctions to be normalised to  $2E \approx 2m_N$  for a nucleus of mass  $m_N$ . We now add the contribution from protons to the matrix element, noting that  $F_n \approx F_p = F$  (see Sec. ??)

$$\langle \Psi_N | f^n \bar{n}n + f^p \bar{p}p | \Psi_N \rangle = 2m_N (f^n N_n + f^p N_p) F(\mathbf{q}), \quad (2.12)$$

where  $N_n$  and  $N_p$  are the neutron and proton numbers of the nucleus respectively.

The corresponding matrix element for the scalar WIMP operator  $\bar{\chi}\chi$  is simple in the non-relativistic limit, evaluating to  $2m_\chi$  []. Combining these, we obtain the scalar matrix element

$$|\mathcal{M}_S|^2 = 16m_\chi^2 m_N^2 |f^p Z + f^n (A - Z)|^2 F_{SI}^2(\mathbf{q}), \quad (2.13)$$

and the SI cross section

$$\frac{d\sigma_{SI}}{dE_R} = \frac{m_N}{2\pi v^2} |f^p Z + f^n (A - Z)|^2 F^2(\mathbf{q}), \quad (2.14)$$

where we have used the atomic number  $Z$  and mass number  $A$  to describe the composition of the nucleus. It is conventional to write this in terms of the **total** WIMP-proton SI cross section, which does not depend on the particular  $(A, Z)$  of the target nucleus and thus allows easy comparison between experiments. This cross section is given by

$$\sigma_{SI}^p = \frac{\mu_{\chi p}^2}{\pi} (f^p)^2, \quad (2.15)$$

meaning that

$$\frac{d\sigma_{SI}}{dE_R} = \frac{m_N}{2\mu_{\chi p}^2 v^2} |Z + (f^n/f^p)(A - Z)|^2 F^2(E_R). \quad (2.16)$$

*TALK ABOUT  $f_n/f_p$ .*

*Talk about the vector contribution - subdominant*

*Mention spin 0 and spin 1*

**Distinguish between nucleon and neutron with  $n$**

### 2.2.2 SD interactions

The spin-dependent interaction is typically sourced by axial-vector currents of the form

$$\mathcal{L} \supset \alpha_{AV}^{(q)} (\bar{\chi} \gamma^\mu \gamma_5 \chi) (\bar{q} \gamma_\mu \gamma_5 q). \quad (2.17)$$

These result in a coupling of the spins of the WIMP and nucleus. In analogy with the SI case, we can write the nucleon quark matrix elements in the form [130, 138]

$$\langle n | \bar{q} \gamma_\mu \gamma_5 q | n \rangle = 2s_\mu^n \Delta_q^n, \quad (2.18)$$

where  $s_\mu$  is the nucleon **/neutron** spin 4-vector and  $\Delta_q^n$  parametrises the contribution of quark  $q$  to this total spin. Adding the contributions of the different quarks, we can define

$$a_{p,n} = \sum_{q=u,d,s} \frac{\alpha_{AV}^{(q)}}{\sqrt{2}G_F} \Delta_q^{p,n}, \quad (2.19)$$

which are the effective proton and neutron spin couplings.



The full nuclear matrix elements can then be written in the form

$$\langle \Psi_N | \sum_{q=u,d,s} \bar{q} \gamma_\mu \gamma_5 q | \Psi_N \rangle = 4\sqrt{2} G_F \frac{a_p \langle S_p \rangle + a_n \langle S_N \rangle}{J} \langle \Psi_N | \hat{J} | \Psi_N \rangle F_{SD}^2(E_R) \quad (2.20)$$

where  $J$  is the total nuclear spin,  $\langle S_{p,n} \rangle$  the expectation value of the total proton and neutron spin in the nucleus and  $F_{SD}^2$  is a form factor, as in the SI case, which is determined by the internal spin structure of the nucleus.

**Should that be  $4\sqrt{2}$  or  $2\sqrt{2}$ ?** Noting that  $\langle \Psi_N | \hat{J} | \Psi_N \rangle = 2J(J+1)m_N$ , we obtain for the SD cross section

$$\frac{d\sigma_{SD}}{dE_R} = \frac{16m_N}{\pi v^2} G_F^2 \frac{J+1}{J} |a_p \langle S_p \rangle + a_n \langle S_n \rangle|^2 F_{SD}^2(E_R). \quad (2.21)$$

*Say something about the form factor - and about the ‘alternate’ non-form factor version....Also what about the neutralino axial vector matrix element - is that just 2 mx?*

Again, as in the SI case, it is convenient to rewrite this expression in terms of the proton cross section  $\sigma_{SD}^p$ , which is given by **be more explicit about how we obtain the cross section - i.e. using the  $\frac{d\sigma}{d\Omega^*}$  equation...**

$$\sigma_{SD}^p = \frac{96}{4} G_F^2 \frac{\mu_{\chi p}^2}{\pi} (a_p)^2. \quad (2.22)$$

This leads to the final expression for the SD cross section

$$\frac{d\sigma_{SD}}{dE_R} = \frac{2m_N \sigma_{SD}^p}{3\mu_{\chi p}^2 v^2} \frac{J+1}{J} |\langle S_p \rangle + (a_n/a_p) \langle S_n \rangle|^2 F_{SD}^2(E_R). \quad (2.23)$$

### 2.2.3 The final event rate

It is helpful to collect these various results together to form a coherent picture of the event rate. Combining the SI and SD rates together, we can write

$$\frac{d\sigma}{dE_R} = \frac{m_N}{2\mu_{\chi p}^2 v^2} (\sigma_{SI}^p \mathcal{C}_{SI} F_{SI}^2(E_R) + \sigma_{SD}^p \mathcal{C}_{SD} F_{SD}^2(E_R)), \quad (2.24)$$

where the proton cross sections  $\sigma_{SI,SD}^p$  were defined in the previous section, the form factors  $F_{SI,SD}^2$  will be discussed in more detail in Sec. ?? and we have defined the enhancement factors as

$$\mathcal{C}_{SI} = |Z + (f^n/f^p)(A - Z)|^2 \quad (2.25)$$

$$\mathcal{C}_{SD} = \frac{4}{3} \frac{J+1}{J} |\langle S_p \rangle + (a_n/a_p) \langle S_n \rangle|^2. \quad (2.26)$$

We can now incorporate these into the full event rate:

$$\frac{dR}{dE_R} = \frac{\rho_0}{2\mu_{\chi p}^2 m_x} (\sigma_{SI}^p \mathcal{C}_{SI} F_{SI}^2(E_R) + \sigma_{SD}^p \mathcal{C}_{SD} F_{SD}^2(E_R)) \int_0^\infty \frac{f(v)}{v} dv. \quad (2.27)$$

For a given experiment, which is sensitive to recoil energies in the range  $E_{\min}$  to  $E_{\max}$ , the total number of events expected is obtained by integrating over this range of recoil energies and multiplying by the exposure time  $t_{\text{exp}}$ , detector mass  $m_{\text{det}}$  and efficiency (which may also be a function of the recoil energy  $E_R$ )  $\epsilon(E_R)$ :

$$N_e = m_{\text{det}} t_{\text{exp}} \int_{E_{\min}}^{E_{\max}} \epsilon(E_R) \frac{dR}{dE_R} dE_R. \quad (2.28)$$

For the case of a more realistic experiment in which the measurement of energy has only a finite resolution  $\sigma(E_R)$ , we convolve the event rate with a resolution function to obtain the observed recoil spectrum  $\frac{d\tilde{R}}{dE_R}$ ,

$$\frac{d\tilde{R}}{dE_R}(E) = \int_{E'=0}^\infty \frac{e^{-(E-E')^2/(2\sigma(E'))}}{\sqrt{2\pi}\sigma(E')} \frac{dR}{dE_R}(E') dE'. \quad (2.29)$$

We now turn our attention to the discussion of such ‘realistic experiments’ and the current state of dark matter direct searches.

**SI good for heavier detectors... Annual modulation**

## 2.3 Direct detection experiments

### 2.3.1 Directional experiments

*Add in some plots of event rates etc...* PION-NUCLEON sigma term [135, 150, 151]

Experiment	Target	Status
CDMS-II [139–141]	Ge, Si	Null result
CoGeNT [127, 128]	Ge	Excess & annual modulation observed
XENON100 [142]	Xe	
CRESST-II [143]	CaWO <sub>4</sub>	Excess observed
DAMA/LIBRA [126]	NaI(Tl)	Annual modulation observed
EDELWEISS-II [144]	Ge	Null result
ZEPLIN-III [145]	Xe	Null result
KIMS [146]	CsI(Tl)	Null result
PICASSO [147]	<sup>19</sup> F	Null result
SIMPLE-II [148]	C <sub>2</sub> ClF <sub>5</sub>	Null result
COUPP [149]	CF <sub>3</sub> I	Null result

Table 2.1: Summary of current WIMP detection experiments.

# Chapter 3

## Parameter Reconstruction

### 3.1 Posterior distribution

Using the above techniques, we can obtain an estimate of the posterior distribution, or likelihood, for the  $N$  model parameters  $\mathcal{L}(\mathbf{D}|\{\theta_i\})$ .

It is sometimes necessary to calculate or plot the posterior distribution as a function of only a subset of parameters - say 1 or 2. While the full  $N$ -dimensional likelihood is unambiguous, the likelihood as a function of 1 or 2 parameters can be obtained in several ways, each of which encode different information. We discuss some of these ways below for the case of constructing a  $k$ -dimensional likelihood from the full  $N$ -dimensional parameter space.

**Profile likelihood (PL)** The profile likelihood is obtained by taking a  $k$ -dimensional slice of the full  $N$ -D likelihood. The choice of slice is somewhat arbitrary, but typically we choose to maximise the likelihood along the  $N - k$  remaining dimensions:

$$\mathcal{L}_{\text{PL}}(\theta_1, \theta_2, \dots, \theta_k) = \max_{k+1, \dots, N} \mathcal{L}(\theta_1, \theta_2, \dots, \theta_k, \theta_{k+1}, \dots, \theta_N). \quad (3.1)$$

**Marginalised posterior** The marginalised likelihood, or marginalised posterior,  $\mathcal{L}_{\text{M}}$  is obtained by integrating the full likelihood over the remaining  $N - k$  dimensions.

$$\mathcal{L}_{\text{M}}(\theta_1, \theta_2, \dots, \theta_k) = \int \mathcal{L}(\theta_1, \theta_2, \dots, \theta_k, \theta_{k+1}, \dots, \theta_N) d\theta_{k+1} \dots d\theta_N. \quad (3.2)$$

## 3.2 Parameter estimates

While the entire posterior distribution is required to assess the fit of a single point, it can be helpful to report as single value for a given parameter as a measure of the location of the distribution. As before, reduction from one to zero dimensions can be ambiguous and we describe several possible options below.

**Best fit** The best fit parameter, or maximum likelihood estimator, is the parameter value which gives the largest likelihood over the entire parameter range.

**Do the likelihoods for various things in here as well...poisson likelihood etc.**

## Chapter 4

# Parametrising the dark matter momentum distribution

## Chapter 5

### A novel method for parametrising the speed distribution

## Chapter 6

Breaking the cross section  
degeneracy: neutrino  
telescopes



## Chapter 7

### Speed parametrisation for directional experiments

# Chapter 8

## Conclusions

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