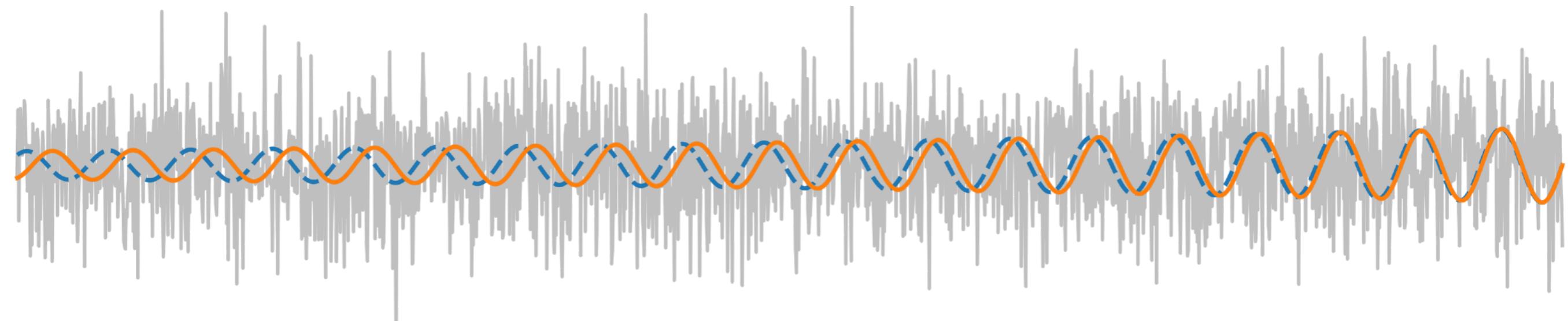


Detecting, Discovering and Measuring Dark Matter around Black Holes with Gravitational Waves



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 @BradleyKavanagh

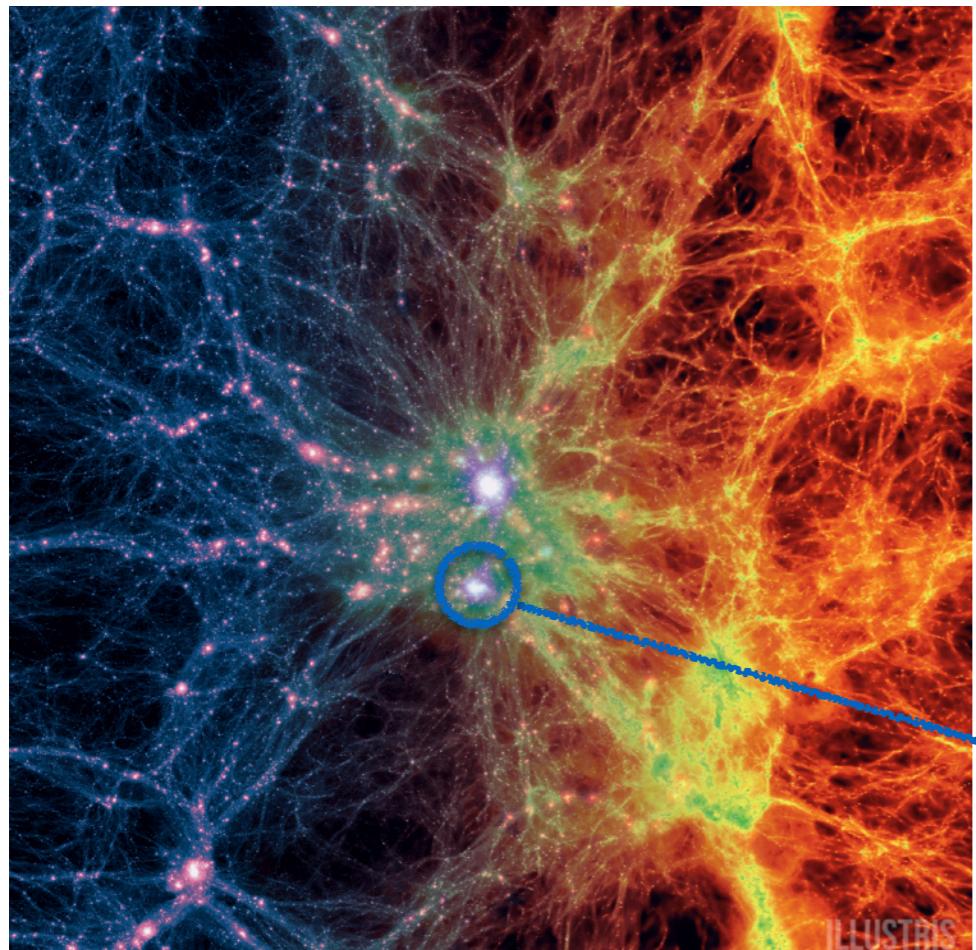
NBIA Astroparticle Seminar, 18th October 2021

Abstract. With growing agony of not finding a dark matter (DM) particle in direct search experiments so far (for example in XENON1T), frameworks where the freeze-out of DM is driven by number changing processes within the dark sector itself and do not contribute to direct search, like Strongly Interacting Massive Particle (SIMP) are gaining more attention. In this analysis, we ideate a simple scalar DM framework stabilised by \mathbb{Z}_2 symmetry to serve

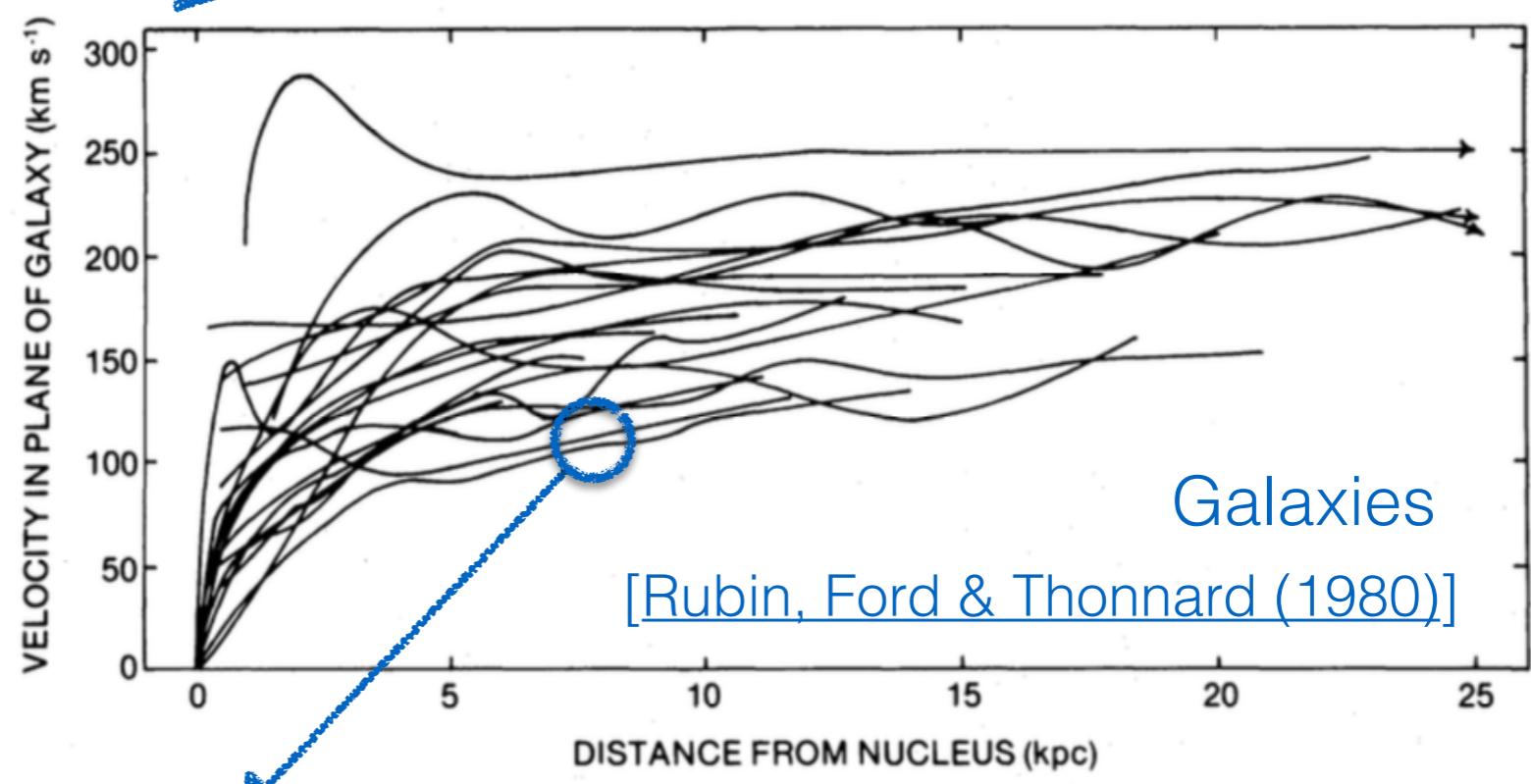
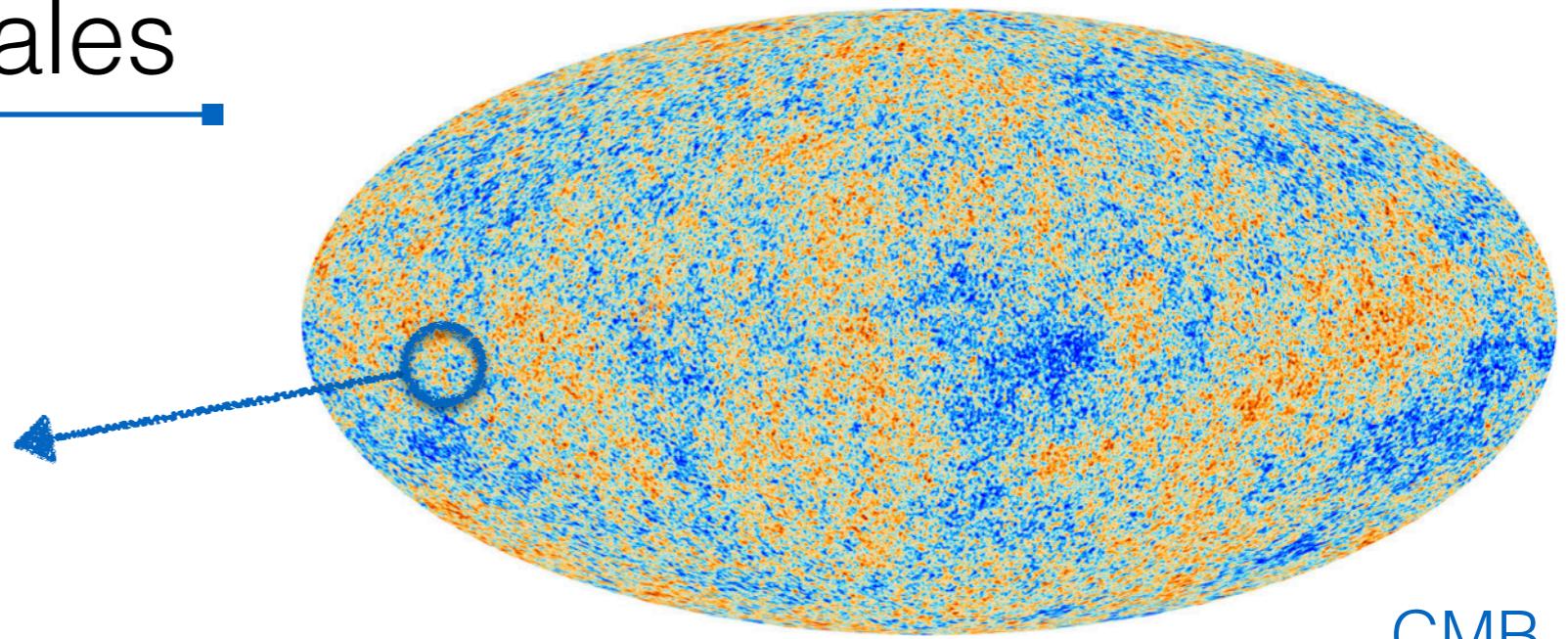
From ‘SIMPler realisation of Scalar Dark Matter’ [[1904.07562](#)]

[With thanks to @TimonEmken]

Dark Matter on all scales



Galaxy clusters
[Illustris, [1405.2921](#)]
[[astro-ph/0006397](#)]



Dark Matter at Earth

NOT TO SCALE



Global and local estimates of
DM at Solar radius give: $\rho_\chi \sim 0.2 - 0.8 \text{ GeV cm}^{-3}$

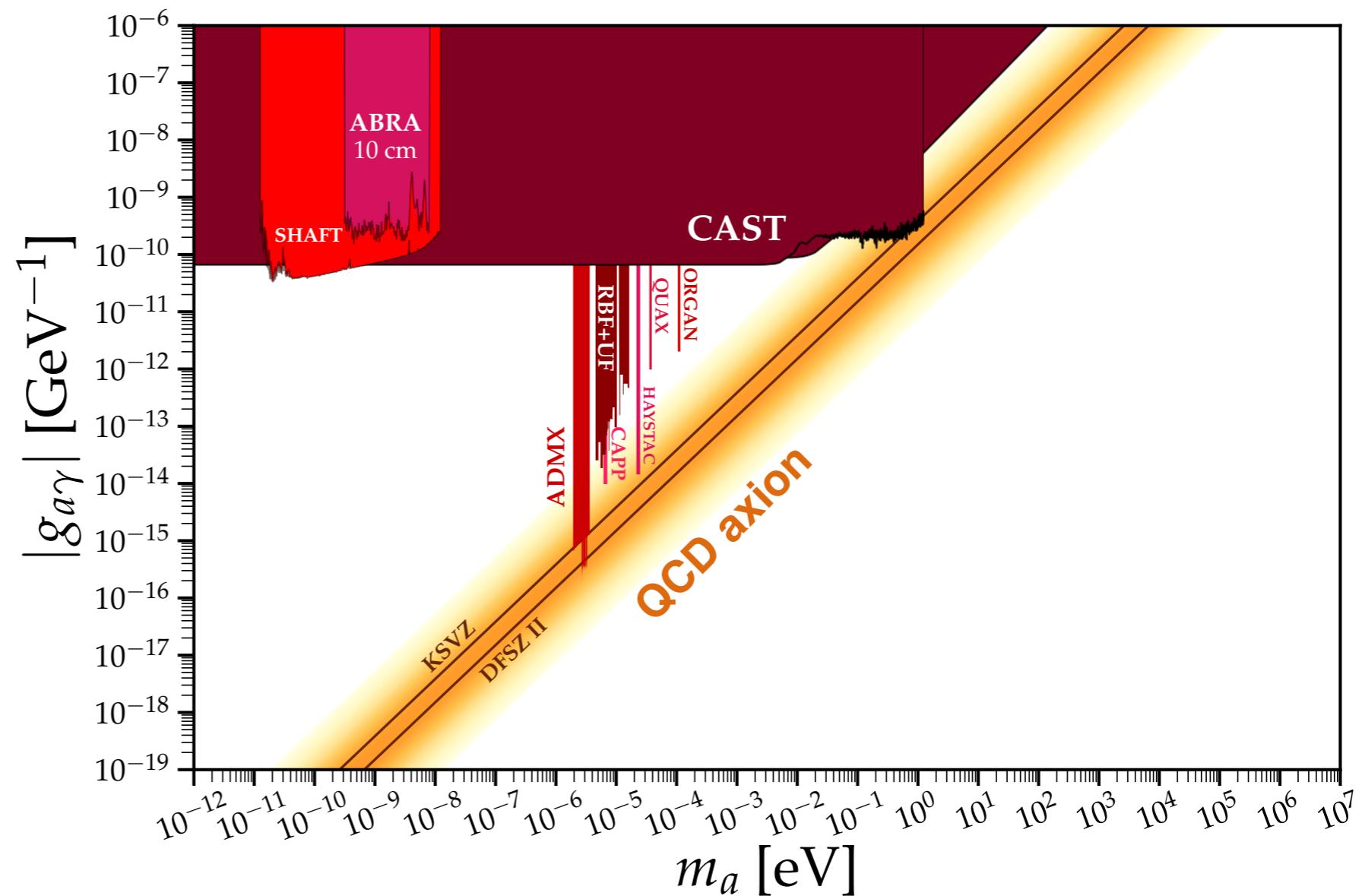
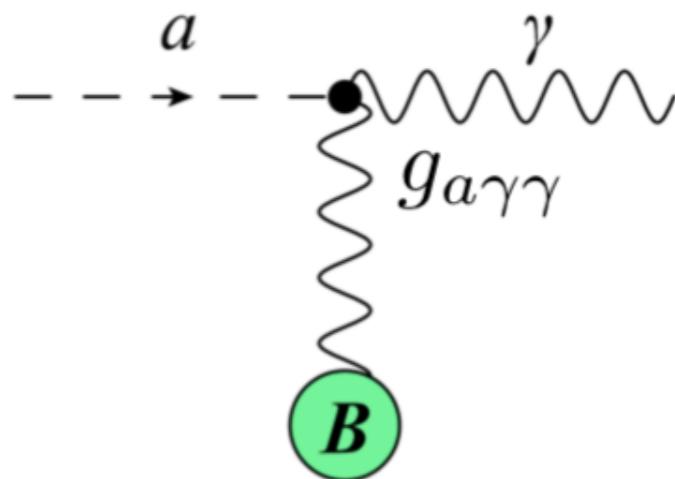
E.g. Iocco et al. [[1502.03821](#)],
Garbari et al. [[1206.0015](#)],
Read [[1404.1938](#)]

Axion Dark Matter

[Slide credit: Marco Chianese]

Dark Matter could be in the form of light pseudo scalar ‘axions’, which may convert to photons (and vice versa) in an external magnetic field:

$$\begin{aligned}\mathcal{L} &\supset -\frac{1}{4} g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu} \\ &= -\frac{1}{4} g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}\end{aligned}$$



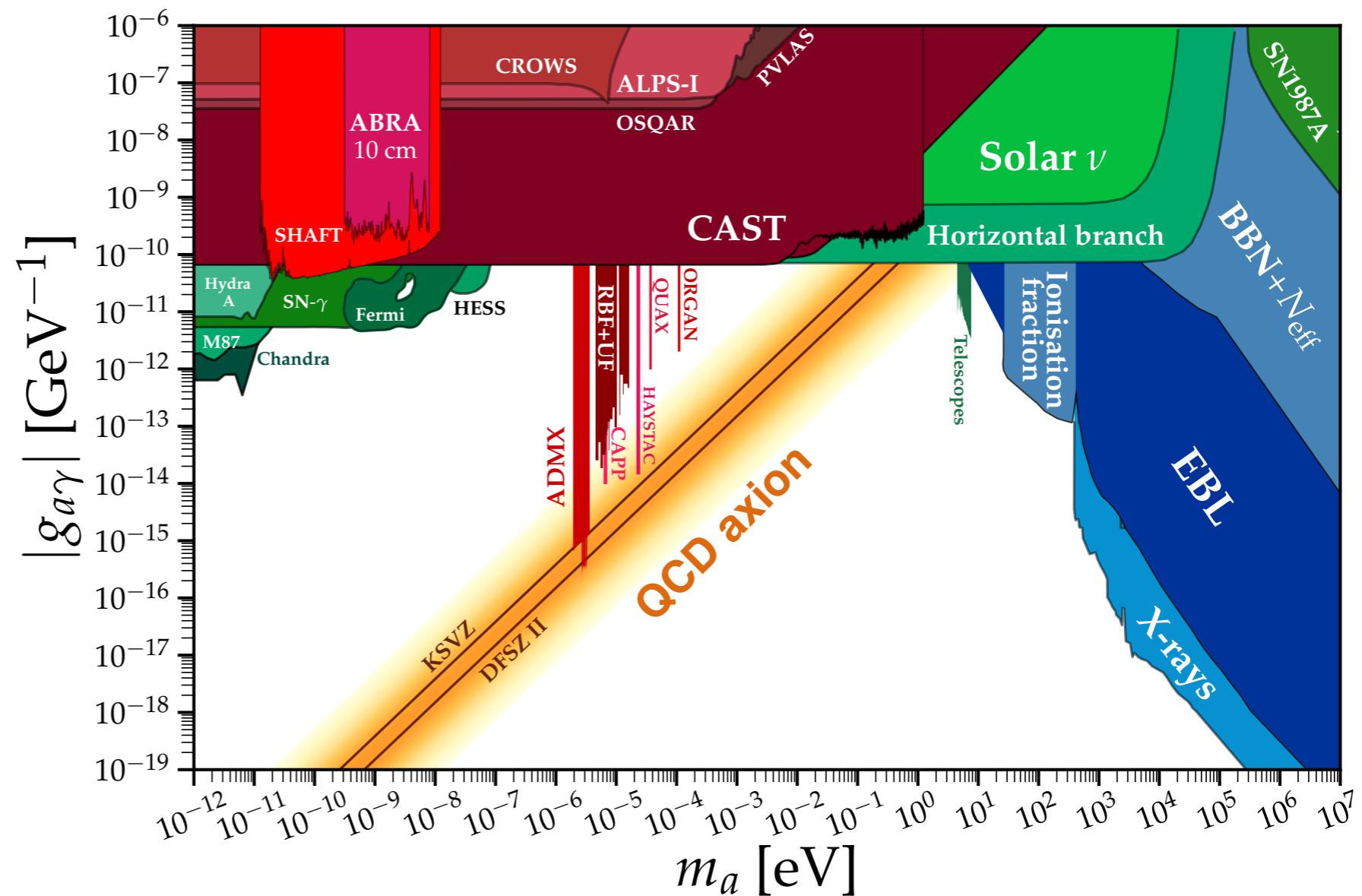
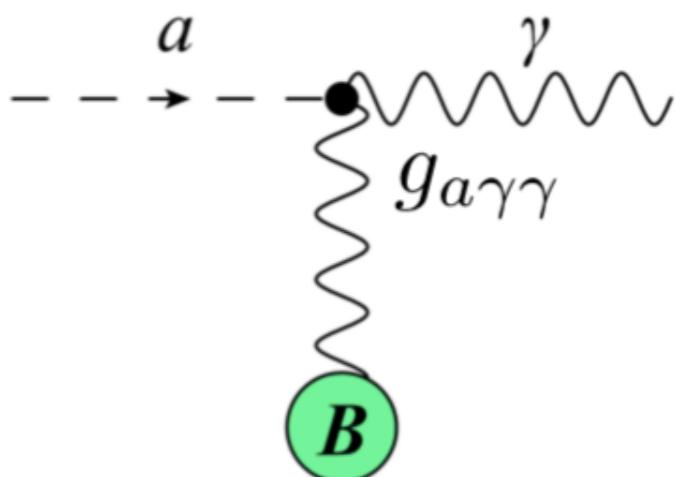
[O’Hare, <https://cajohare.github.io/AxionLimits/>]

Axion Dark Matter

[Slide credit: Marco Chianese]

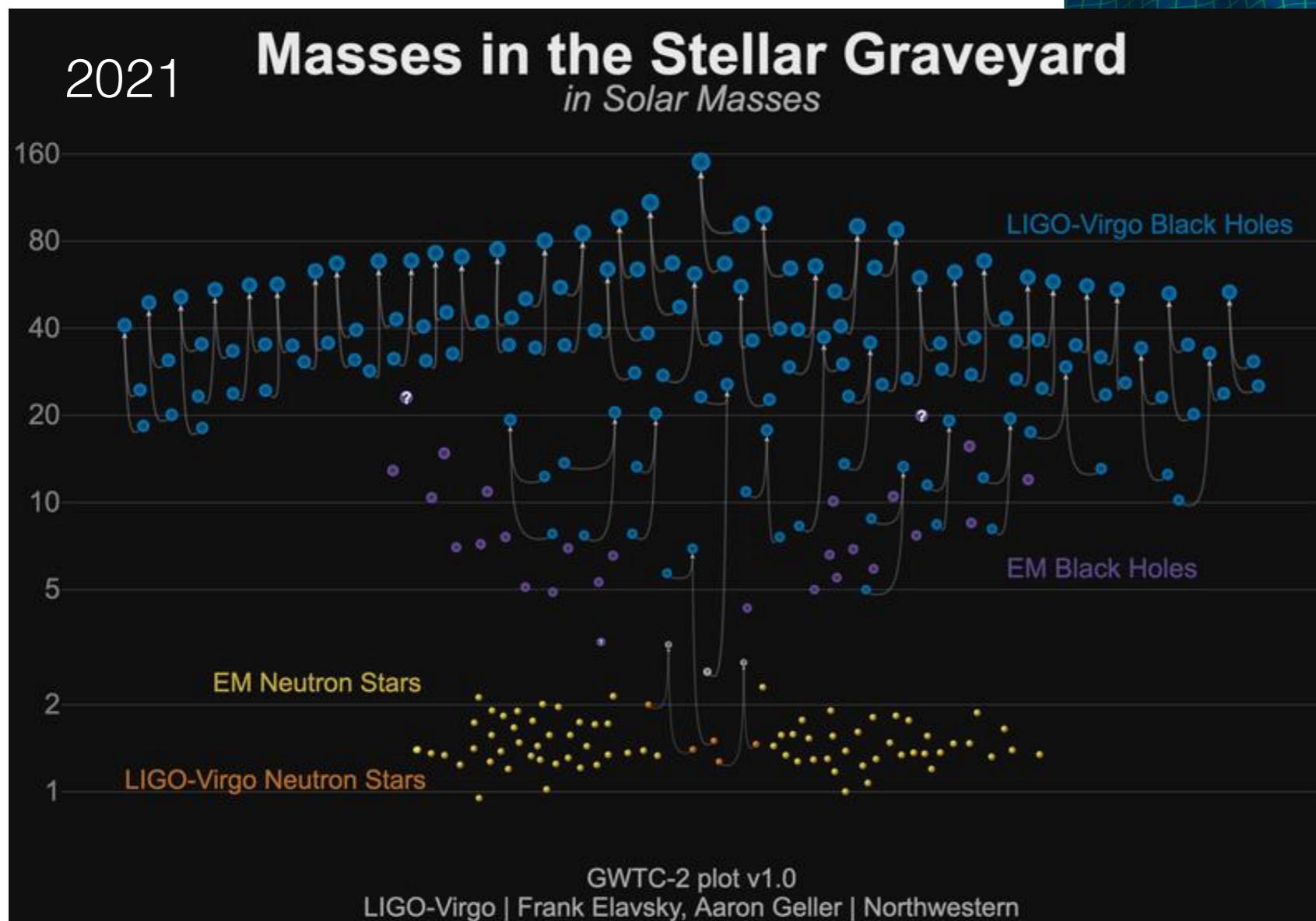
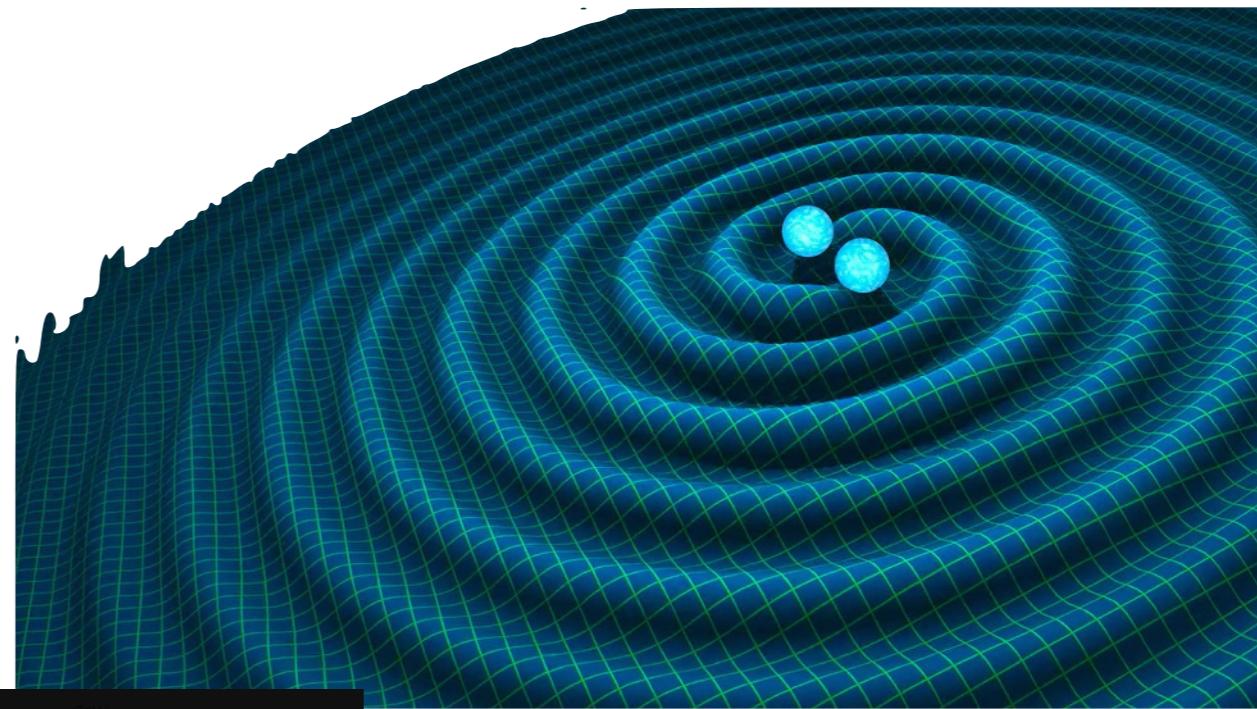
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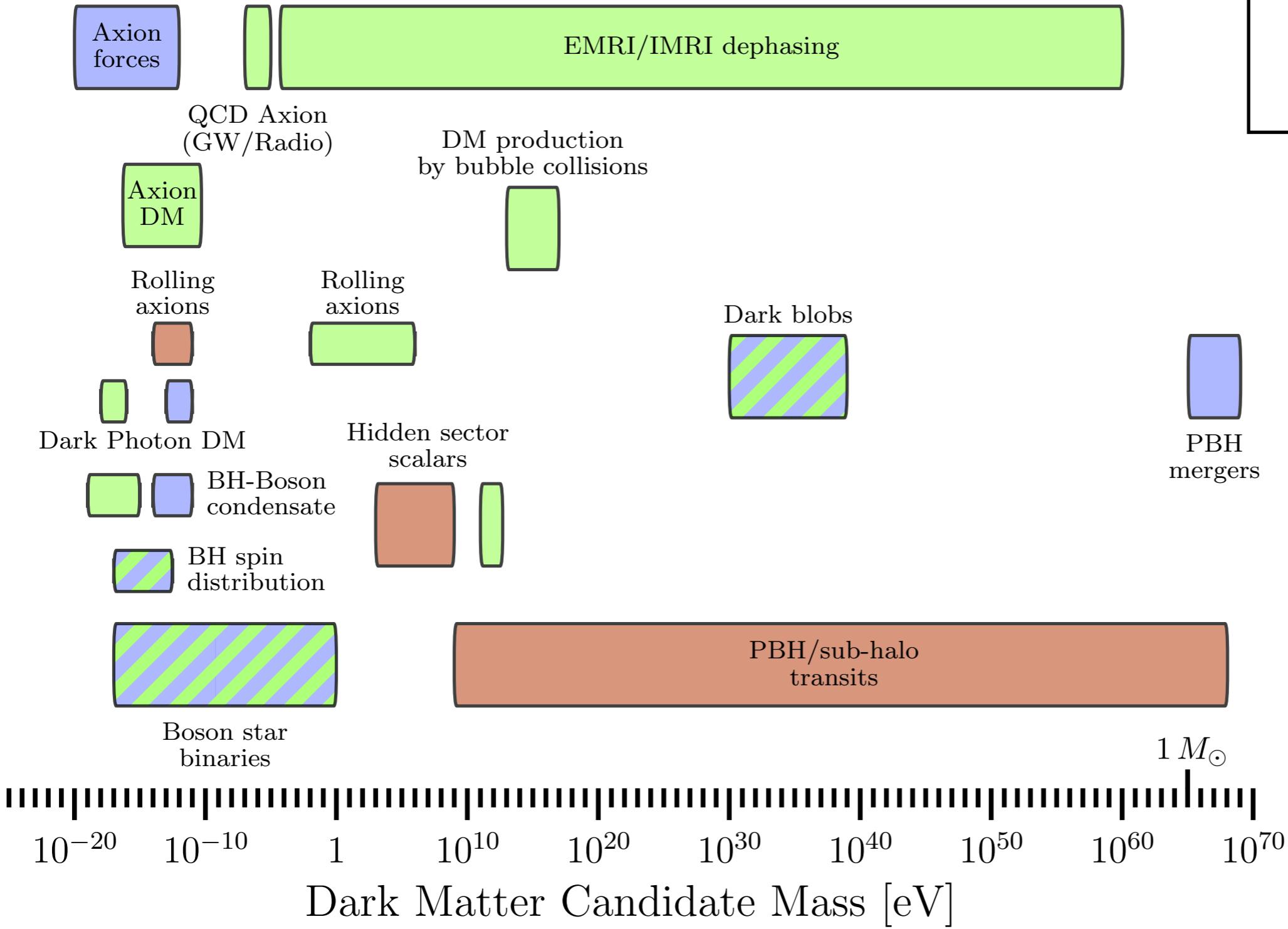
[O’Hare, <https://cajohare.github.io/AxionLimits/>]

Gravitational Waves (GWs)



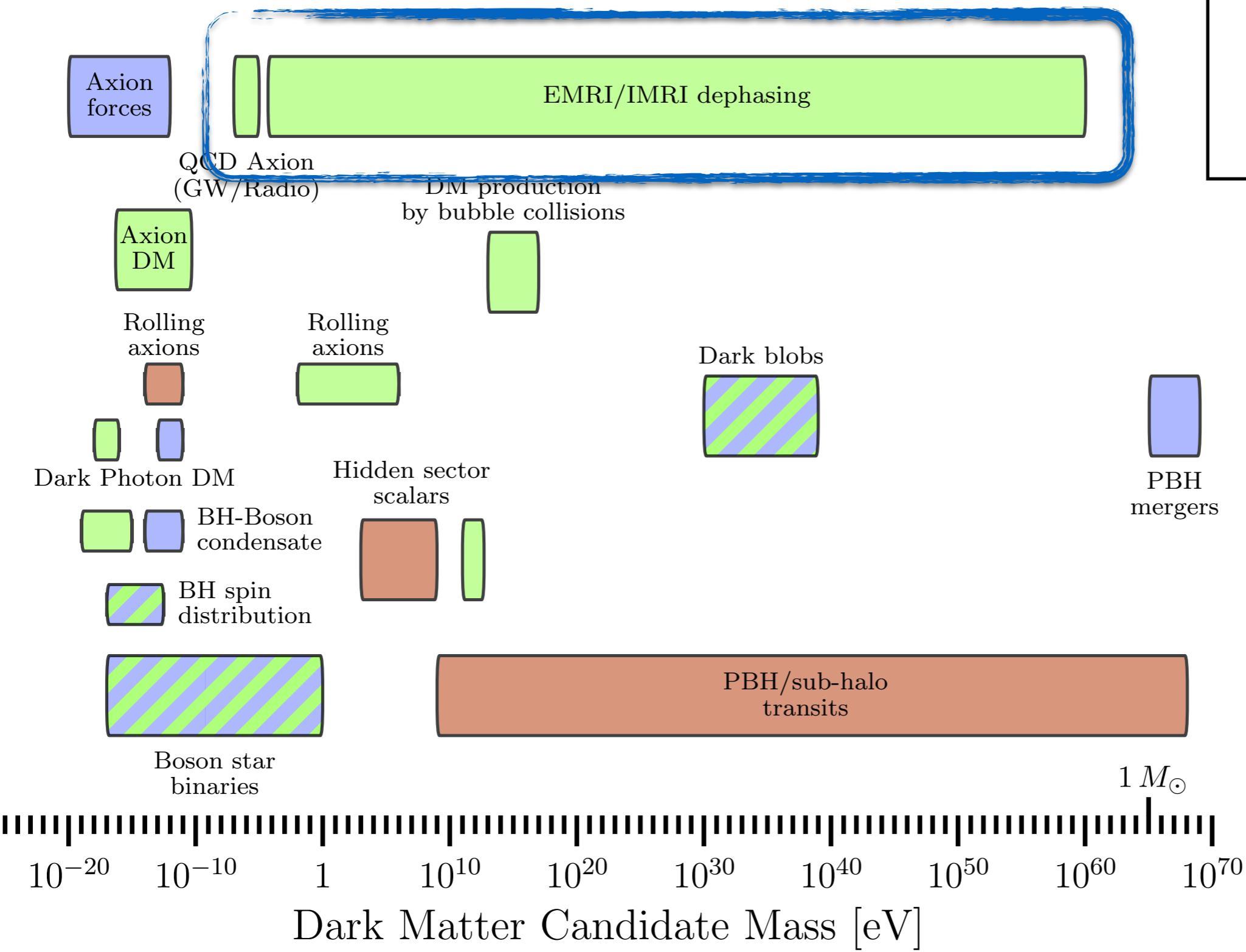
R. HURT / CALTECH-JPL /
HANDOUT/ ESA

GW probes of DM



[Bertone, Croon, et al (including **BJK**), [1907.10610](#)]

GW probes of DM

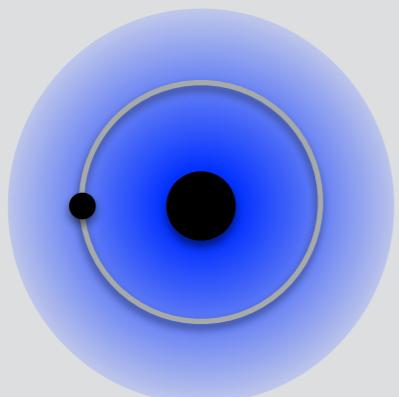
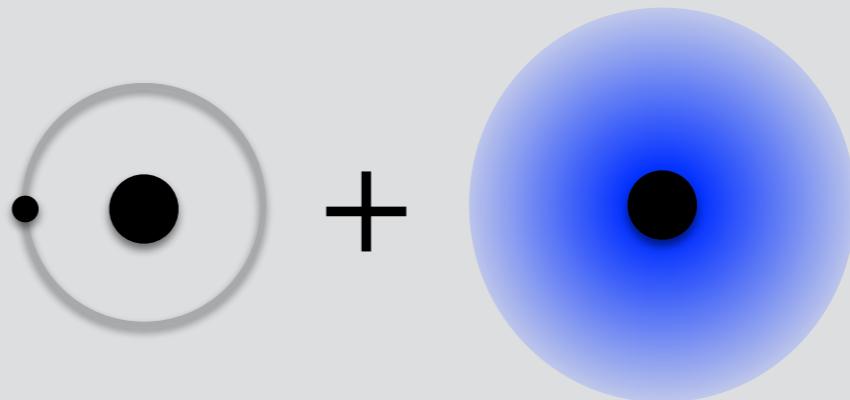


[Bertone, Croon, et al (including **BJK**), [1907.10610](#)]

Overview

Intermediate Mass-Ratio Inspirals (IMRIs) and Dark Matter spikes

[Eda et al, [1301.5971](#), and others]

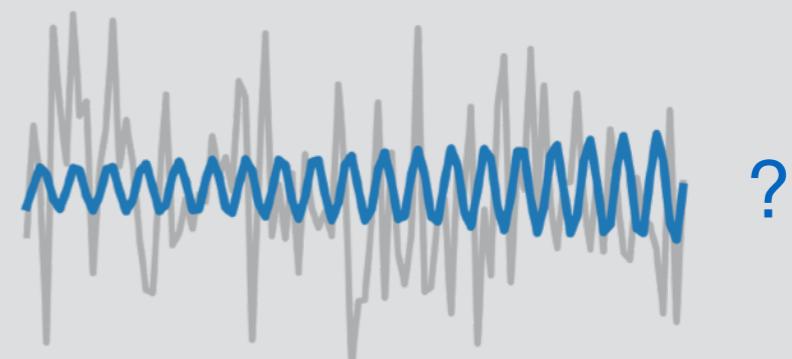


Dark Matter ‘de-phasing’ revisited

[**BJK**, Nichols, Gaggero, Bertone, [2002.12811](#)]

Measuring Dark Matter Around Black Holes

[Coogan, Bertone, Gaggero, **BJK** & Nichols,
[2108.04154](#)]



Intermediate Mass Ratio Inspiral (IMRI)

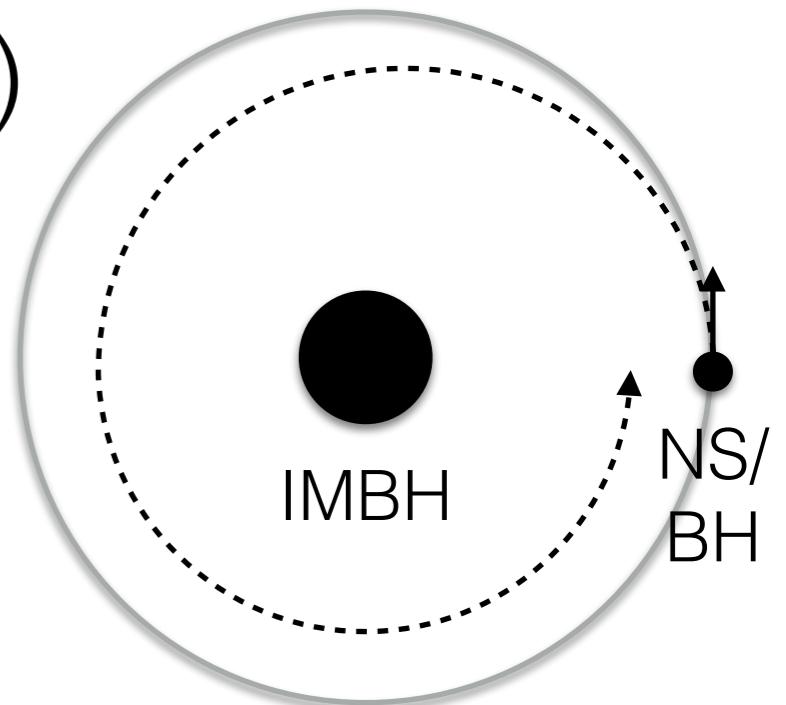
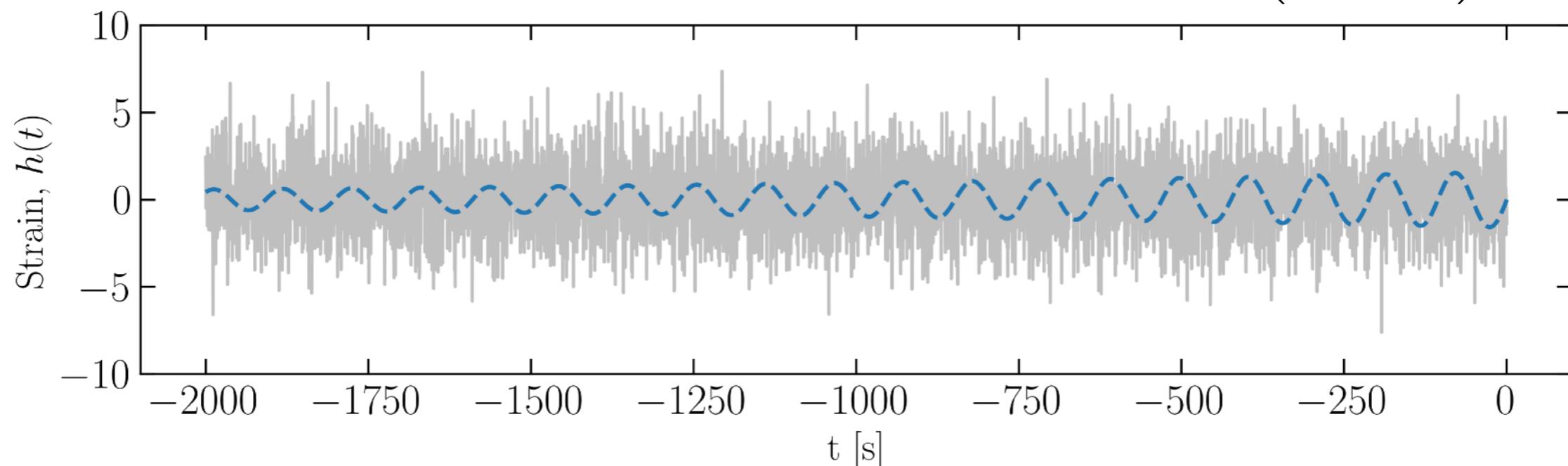
Stellar mass compact object (NS/BH) inspirals towards intermediate mass black hole (IMBH)

$$M_{\text{IMBH}} \sim 10^3 - 10^5 M_\odot$$

GW emission causes long, slow inspiral:

$$\dot{E}_{\text{GW}} \approx \frac{32G^4}{5c^5} \frac{M_{\text{IMBH}}^3 M_{\text{NS}}^2}{r^5} \propto (f_{\text{GW}})^{10/3}$$

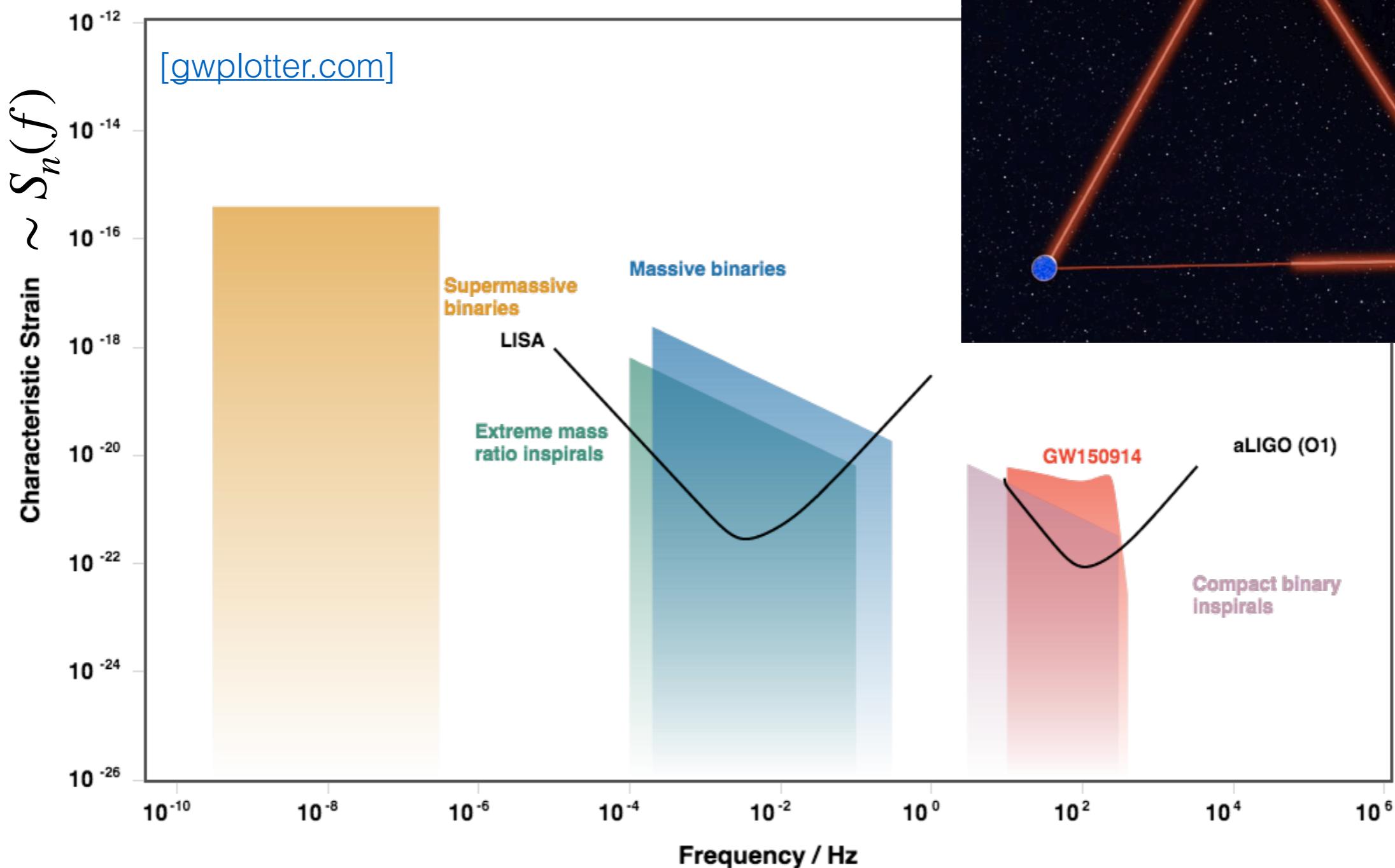
Until the innermost stable circular orbit: $f_{\text{ISCO}} = 0.44 \left(\frac{10^4 M_\odot}{M_1} \right) \text{ Hz}$



LISA: GWs in Space

© AEI / MM / exozet

Laser Interferometer Space Antenna
(planned for the 2030s) [\[1702.00786\]](#)



LISA could detect $\sim 3 - 10$ IMRIs per year

[\[1711.00483\]](#)

Dark Matter ‘spikes’ (1)

Depending on the formation mechanism of the IMBH,
expect an over-density of DM:

$$\rho_{\text{DM}} = \rho_6 \left(\frac{10^{-6} \text{ pc}}{r} \right)^{\gamma_{\text{sp}}}$$

For BH forming in an NFW halo,
from adiabatic growth expect:

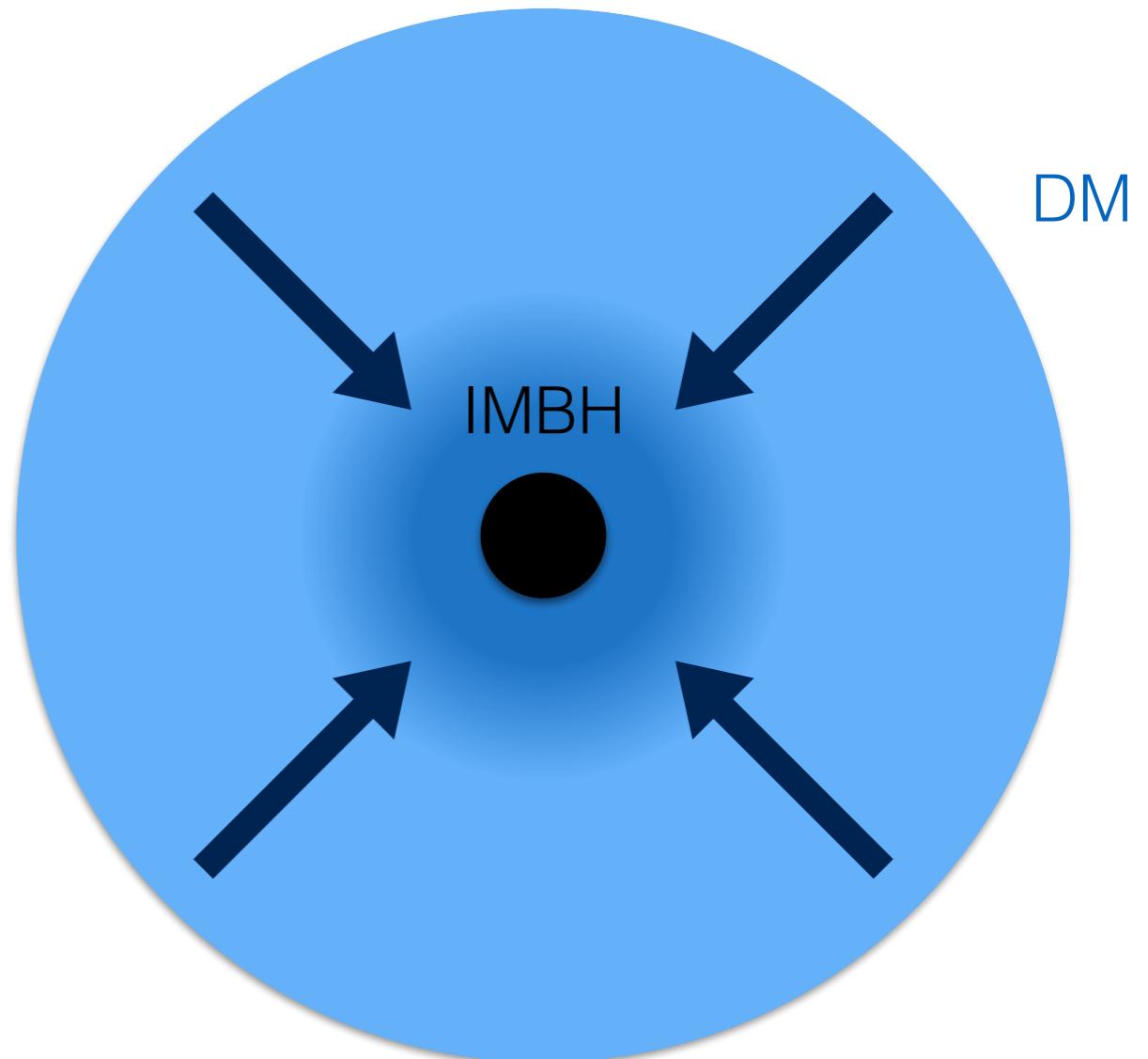
$$\gamma_{\text{sp}} = 7/3 \approx 2.333$$

For 10^5 Solar mass IMBH, forming at
 $z \sim 20$, get typical values:

$$\rho_6 \approx 5.45 \times 10^{15} M_{\odot} \text{pc}^{-3}$$

$$r_{\text{sp}} \approx 0.5 \text{ pc}$$

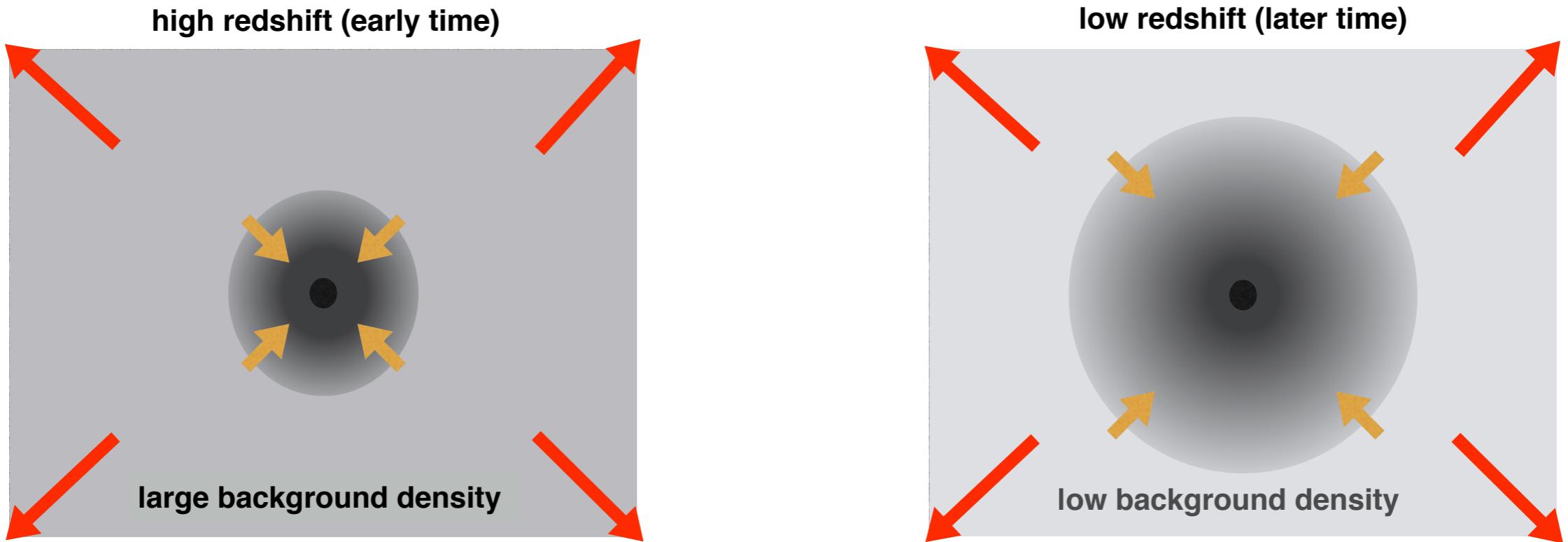
Density can reach $\rho \sim 10^{24} M_{\odot} \text{ pc}^{-3}$
($\sim 10^{24}$ times larger than local density)



[[astro-ph/9906391](#), [astro-ph/0501555](#), [astro-ph/0501625](#), [astro-ph/0509565](#), [0902.3665](#), [1305.2619](#)]

Dark Matter 'spikes' (2)

Primordial black holes seed the formation of 'local' DM halos:



$$R_{\text{tr}}(z) = 0.0063 \left(\frac{M_{\text{PBH}}}{M_{\odot}} \right) \left(\frac{1 + z_{\text{eq}}}{1 + z} \right) \text{ pc}$$

$$\rho(r) \propto r^{-9/4}$$

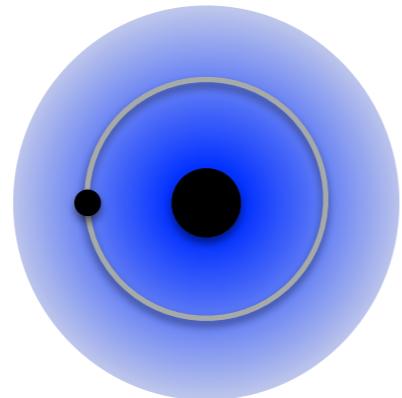
By matter-radiation equality, $M_{\text{halo}} \sim M_{\text{PBH}}$

[Slide shamelessly ripped off from Daniele Gaggero]

[\[Bertschinger \(1985\)\]](#)
[\[0706.0864, 1901.08528\]](#)

Benchmark Systems

Consider some benchmark systems with (detector frame) masses:



$$m_1 = 10^3 M_\odot$$

$$m_2 = 1 M_\odot$$

$$\rho_{\text{DM}} = \rho_6 \left(\frac{10^{-6} \text{ pc}}{r} \right)^{\gamma_{\text{sp}}}$$

Astrophysical benchmark

$$\gamma_{\text{sp}} = 7/3 \approx 2.3333\dots$$

$$\rho_6 \approx 5.45 \times 10^{15} M_\odot \text{ pc}^{-3}$$

PBH benchmark

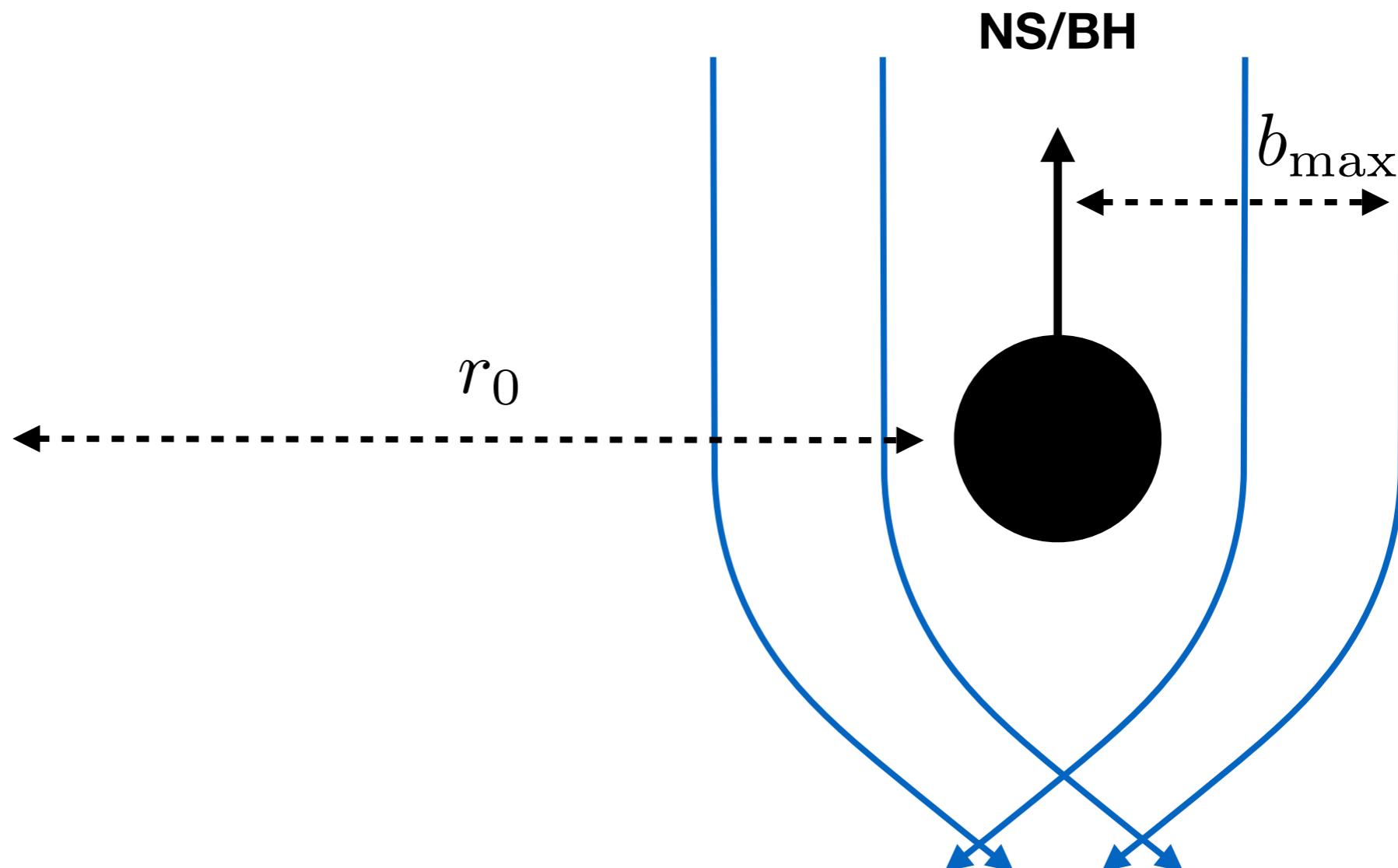
$$\gamma_{\text{sp}} = 9/4 \approx 2.25$$

$$\rho_6 \approx 5.35 \times 10^{15} M_\odot \text{ pc}^{-3}$$

For now we'll be agnostic about the nature of the lighter compact object...

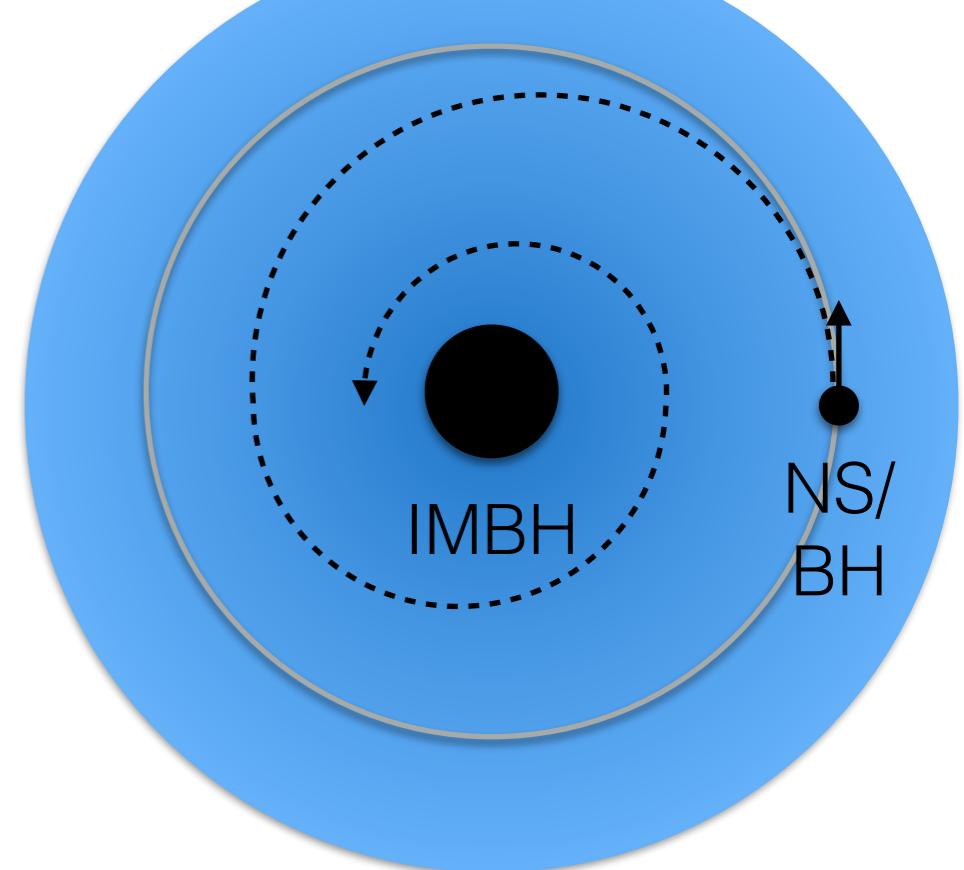
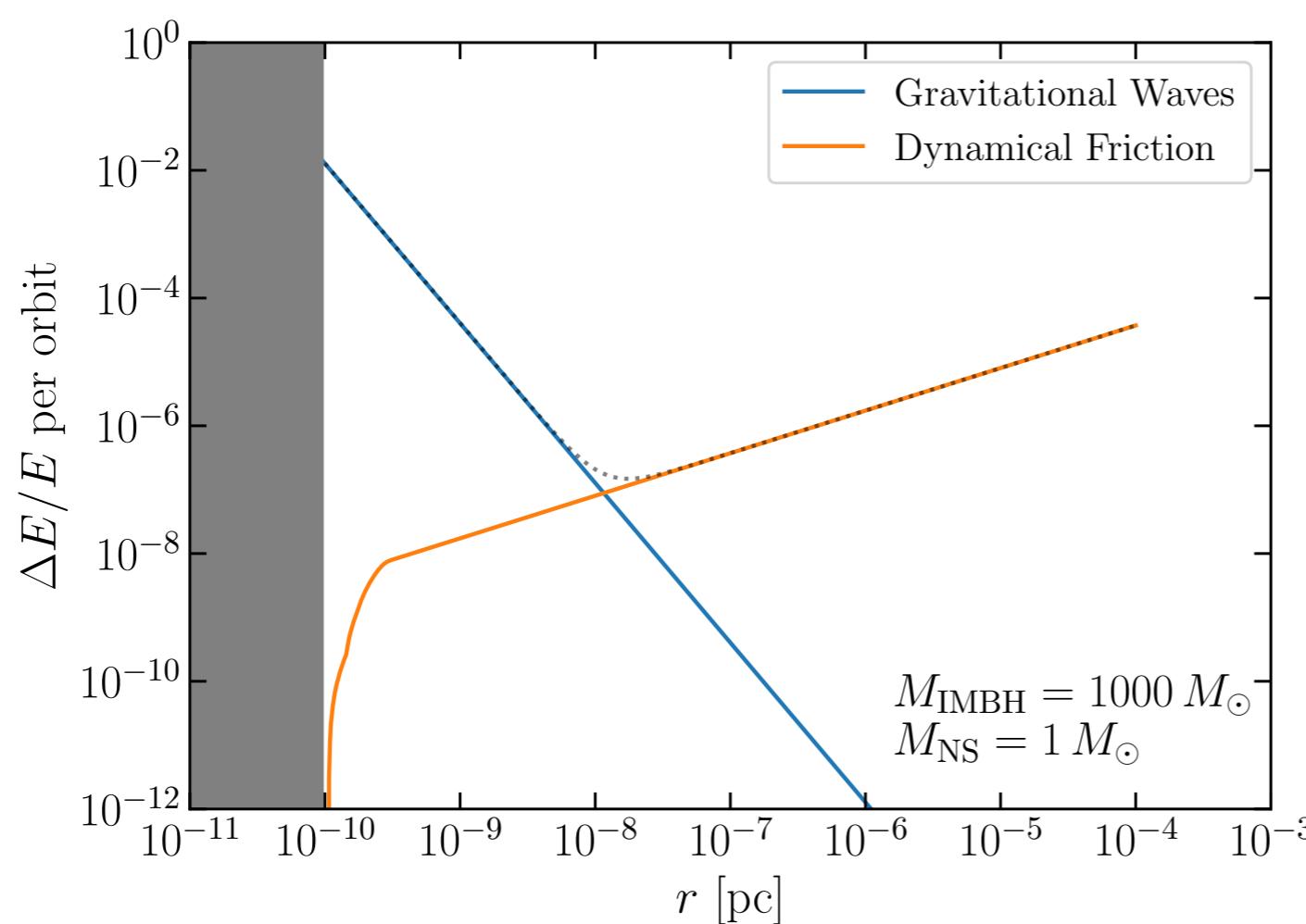
Dynamical Friction

[Chandrasekhar, 1943]

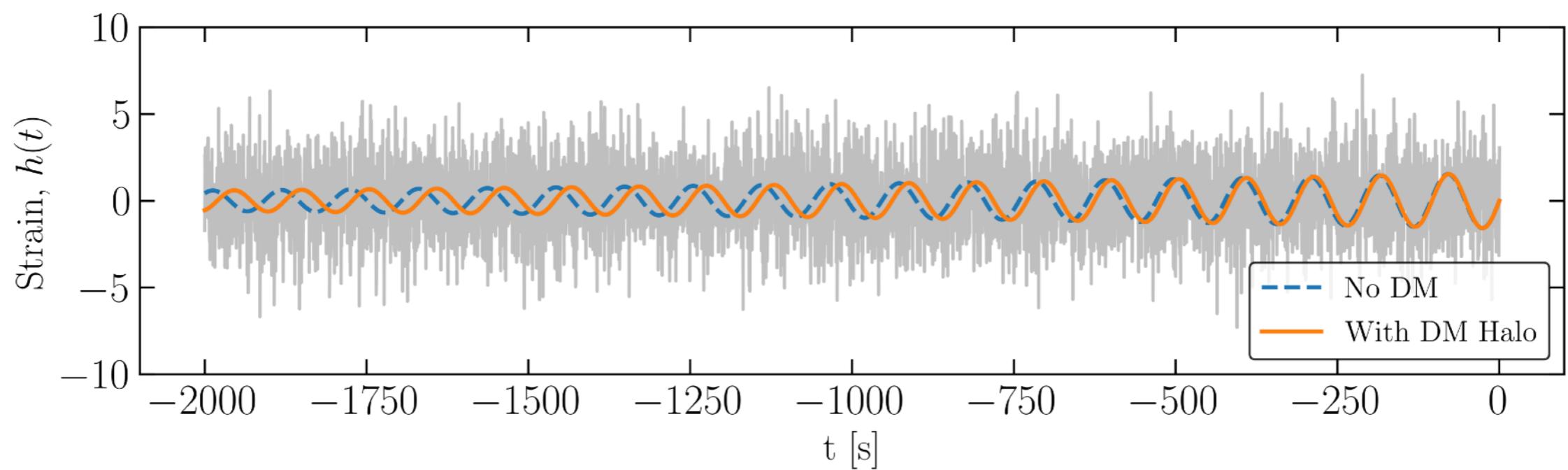


$$\dot{E}_{\text{DF}} \sim \frac{4\pi G^2 M_{\text{NS}}^2 \xi(v) \rho_{\text{DM}}(r)}{v_{\text{NS}}} \ln \Lambda \propto (f_{\text{GW}})^{\frac{2}{3}\gamma - 3}$$

IMRI + Dark Matter



$$-\dot{E}_{\text{orb}} = \dot{E}_{\text{GW}} + \dot{E}_{\text{DF}}$$



'De-phasing' signal

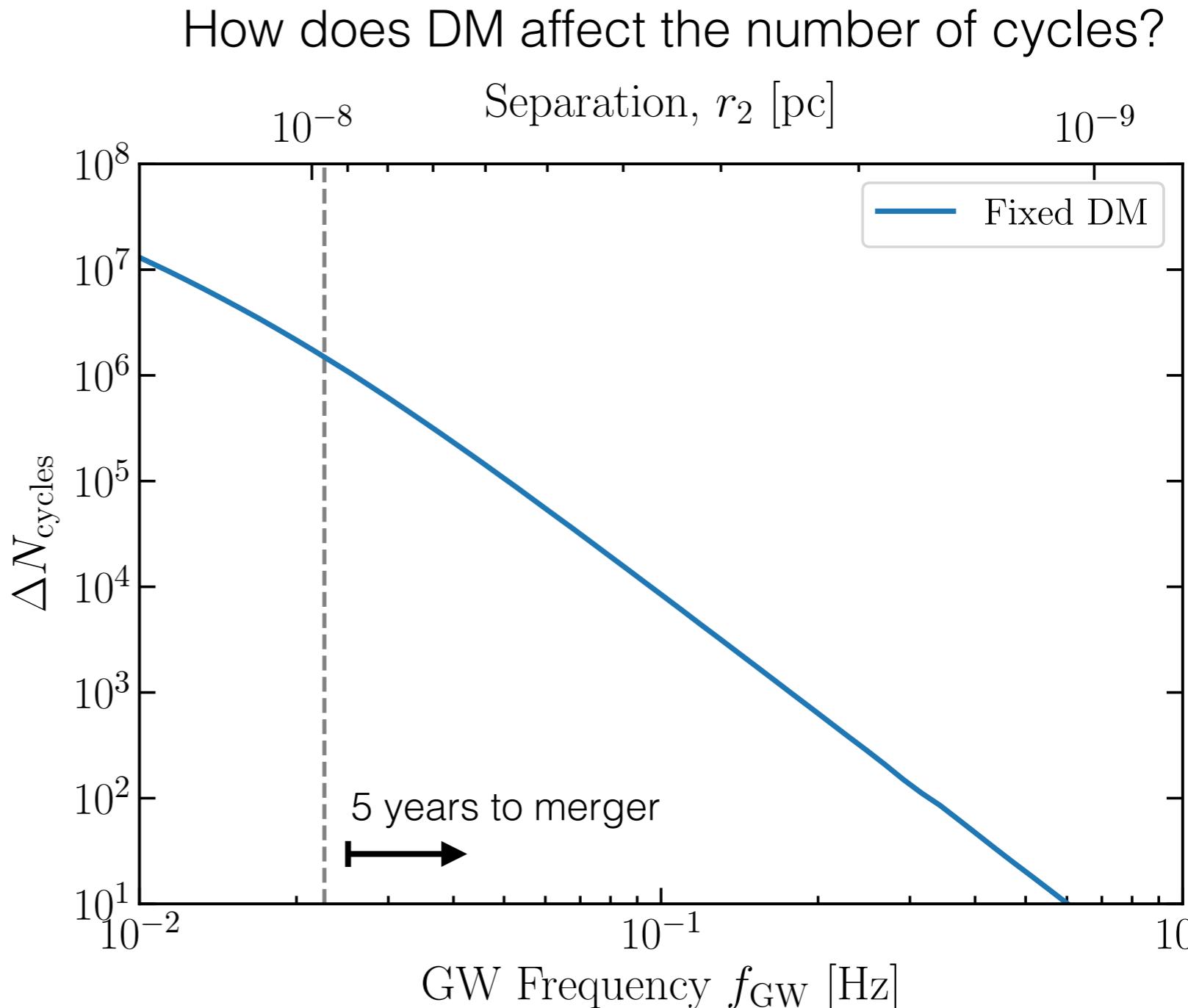
Consider our astro benchmark system, starting at some initial separation:

$$r_{\text{ini}} \sim 10^{-8} \text{ pc}$$



$$t_{\text{merge}}^{\text{vacuum}} \sim 5 \text{ yr}$$

$$N_{\text{cycles}}^{\text{vacuum}} \sim 6 \times 10^6$$



Need to know the signal to better than ~ 1 part in 10^6 !

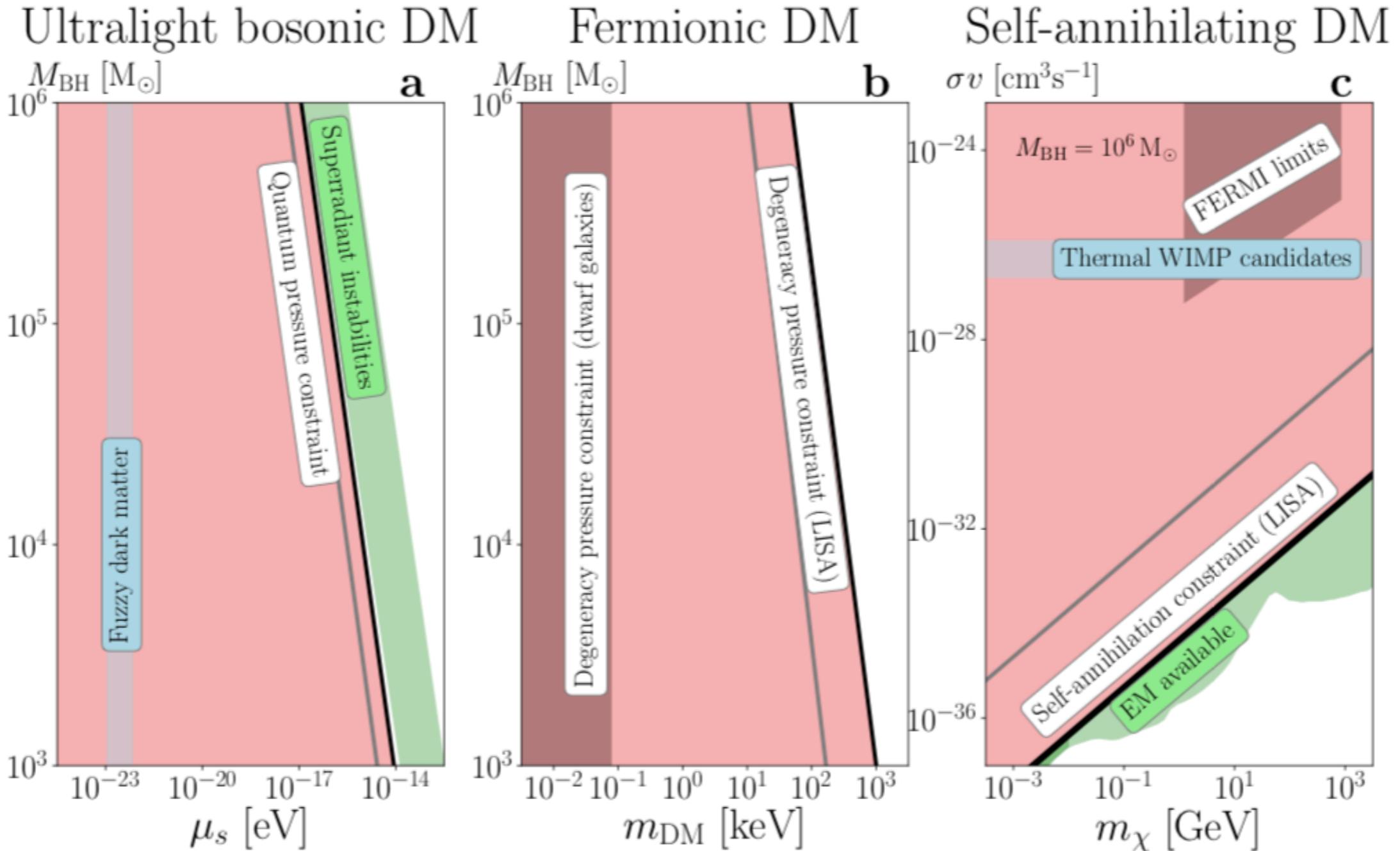
[Eda et al. [1301.5971](#), [1408.3534](#)]

[See also [1302.2646](#), [1404.7140](#), [1404.7149](#)]

Nature of Dark Matter

Red regions would be ruled out by observation of a DM spike!

[[1906.11845](#)]



[See also Bertone, Coogan, Gaggero, **BJK** & Weniger, [1905.01238](#)]

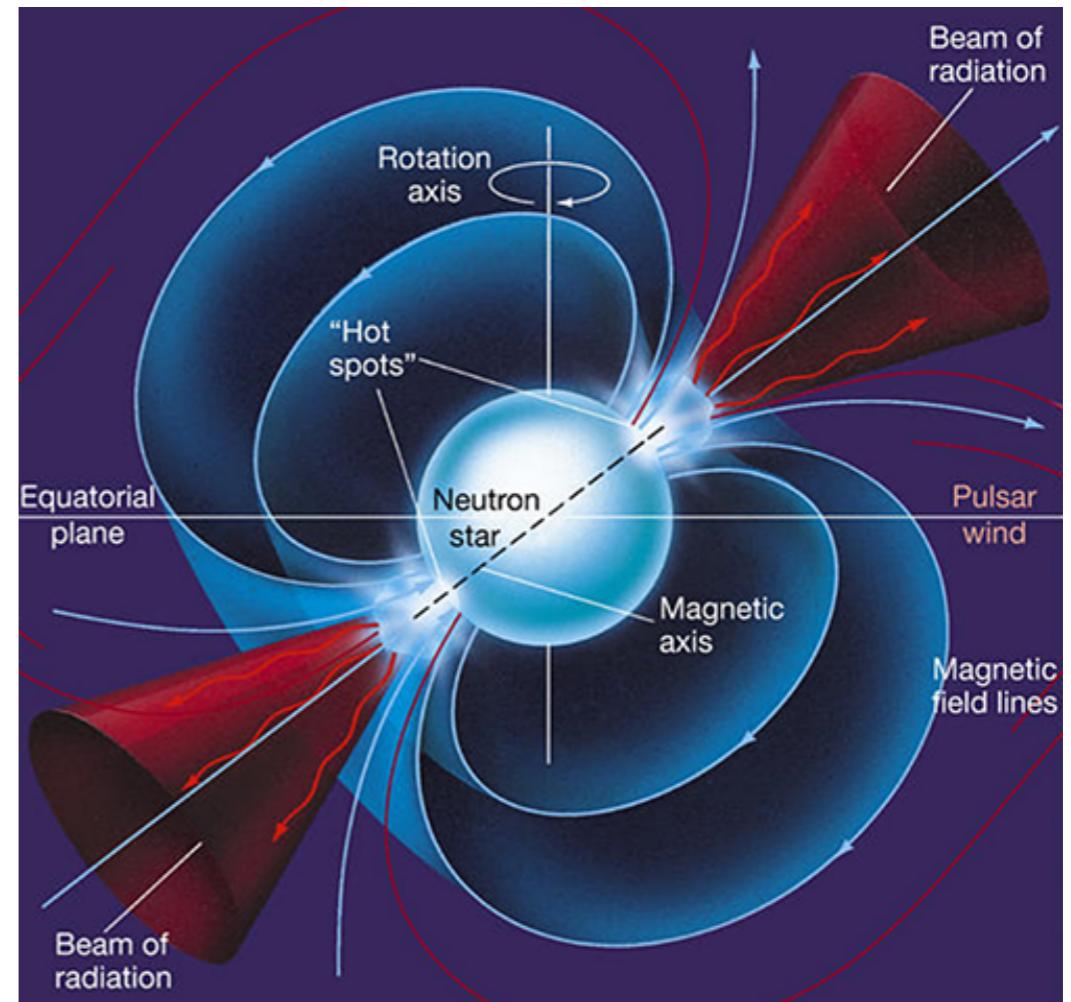
Axions and neutron stars

Old neutron stars can have extremely high magnetic fields:

$$B_0 = 10^{12} - 10^{15} G$$

Surrounded by a dense plasma which allows ‘resonant’ conversion when axion mass matches plasma mass:

$$\omega_p(B_0, P) = m_a/2\pi$$



© 2005 Pearson Prentice Hall, Inc

Magnetic field and plasma frequency varies as a function of radius from NS; NS can effectively ‘scan’ over a range of axion masses:

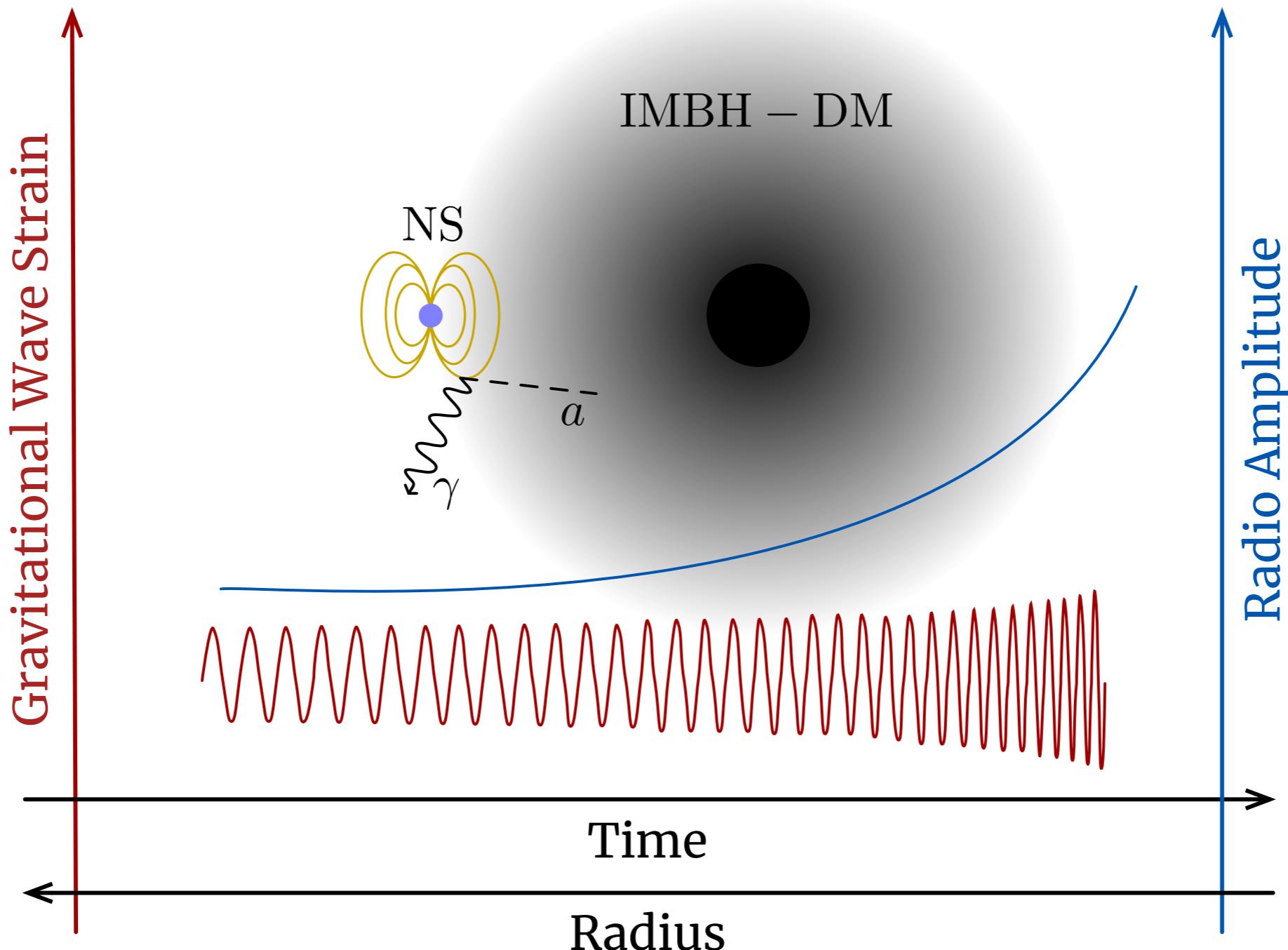
$$m_a \sim 10^{-7} \text{ eV} \quad \text{up to} \quad m_a \sim 10^{-5} \text{ eV}$$

Frequency range of radio telescopes

Require conversion *outside* NS

[\[1803.08230\]](#), [\[1804.03145\]](#), [\[1811.01020\]](#), [\[1910.11907\]](#)

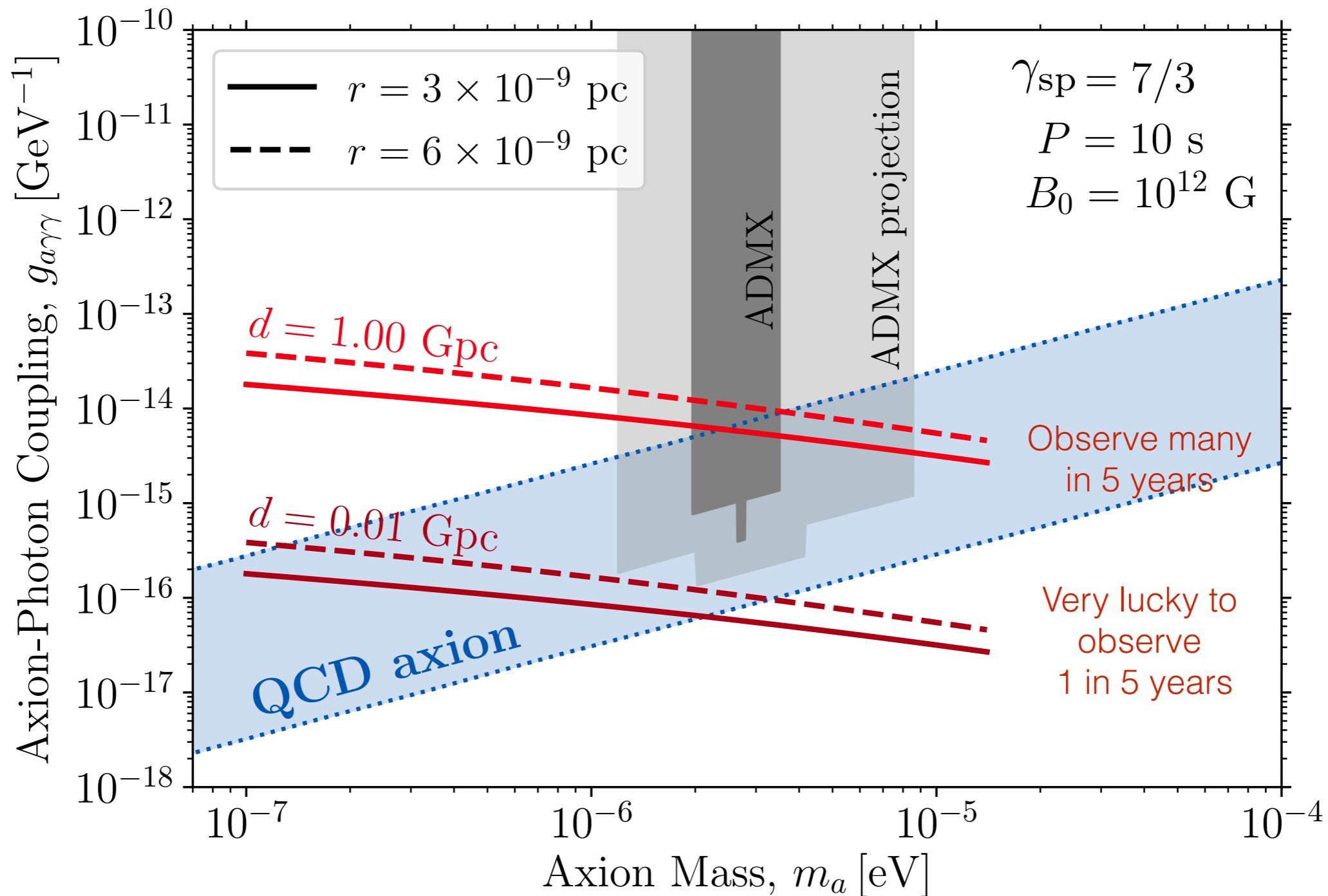
A unique signature



[Edwards, Chianese, **BJK**, Nissanke & Weniger, [1905.04686](#)]

QCD Axion Reach

SKA should be able to probe QCD axion DM in the range $10^{-7} - 10^{-5}$ eV.



[Edwards, Chianese, **BJK**, Nissanke & Weniger, [1905.04686](#)]

Promising Signal

Dark Matter de-phasing is a very exciting signal. It's on long timescales (with LISA planned for 2030s), but it would allow us to:

Detect Dark Matter in
Gravitational waves

[Eda et al. [1301.5971](#), [1408.3534](#)]

Probe the nature of Dark Matter

[\[1906.11845\]](#)

Predict EM signals from Dark Matter

[Edwards, Chianese, **BJK**, Nissanke
& Weniger, [1905.04686](#)]

But doing the calculation **correctly** isn't easy...

A red curtain stage with a decorative banner in the center.

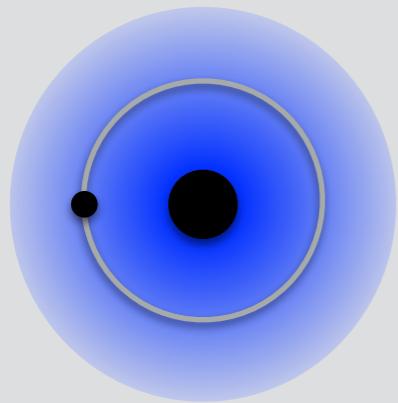
INTERMISSION



A red curtain stage with a decorative white ornate border. The word "INTERMISSION" is written in large, bold, white capital letters within the border. The stage floor is made of dark wood planks.

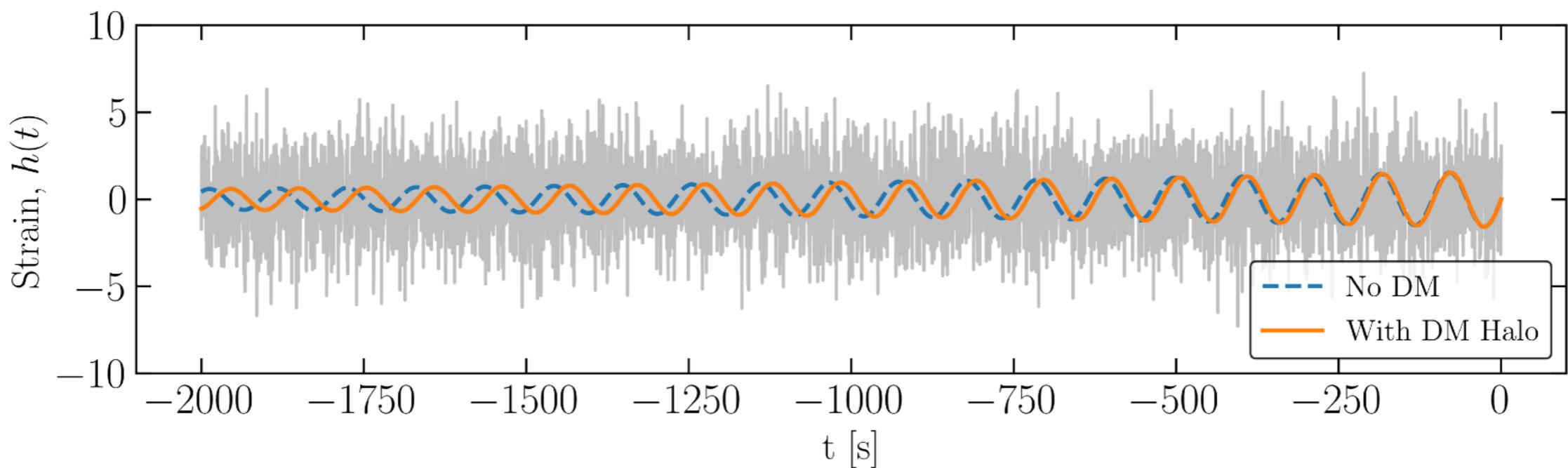
INTERMISSION





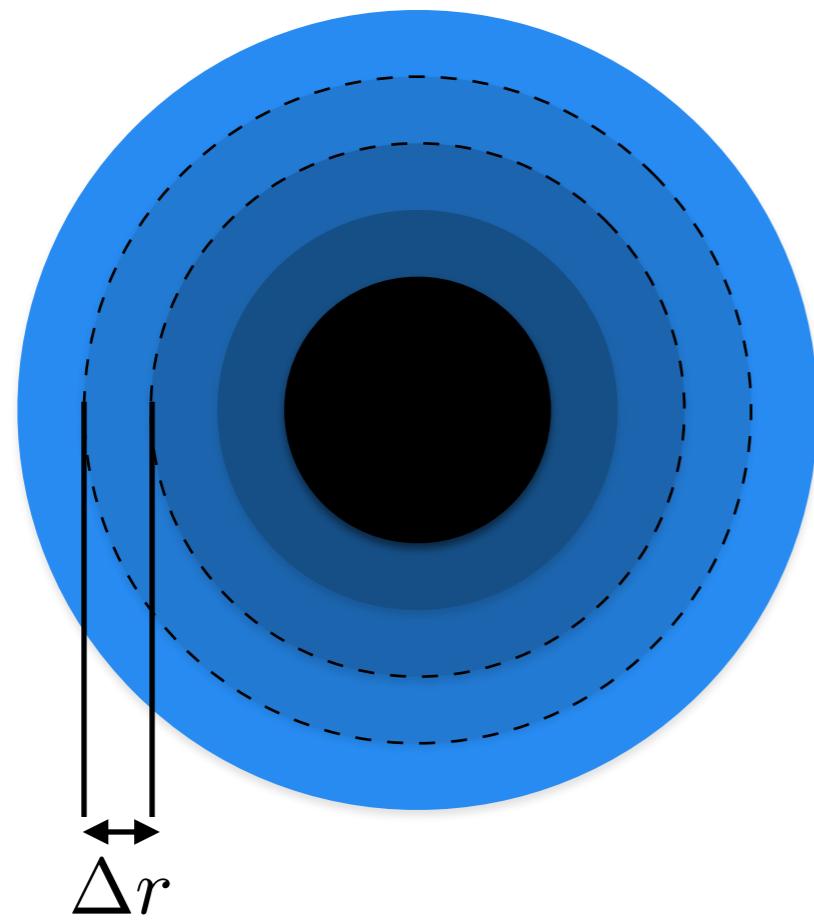
Dark Matter ‘de-phasing’ revisited

[BJK, Nichols, Gaggero, Bertone, [2002.12811](#)]

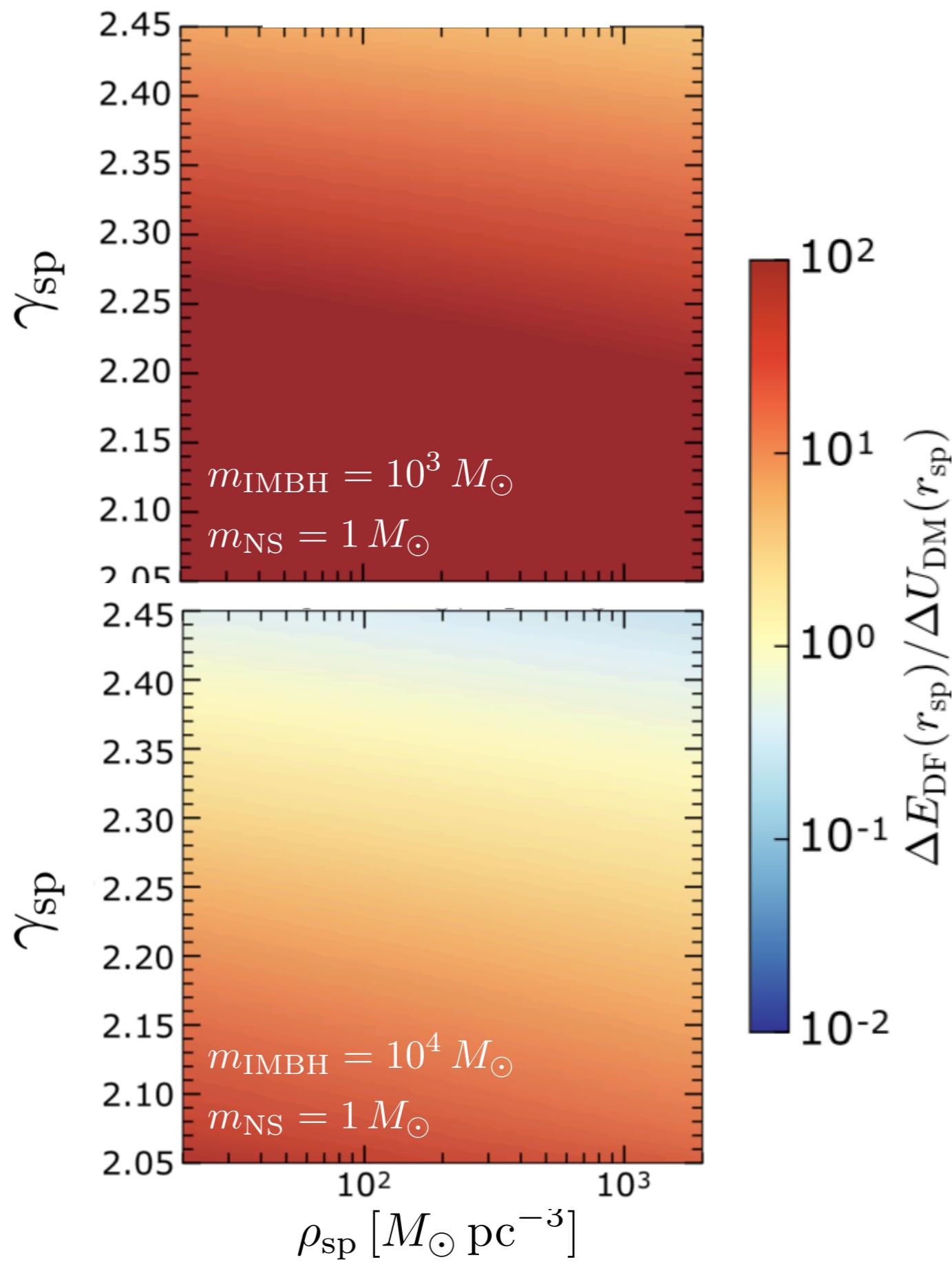


Energy Budget

Q: How much energy is *available* for dynamical friction?

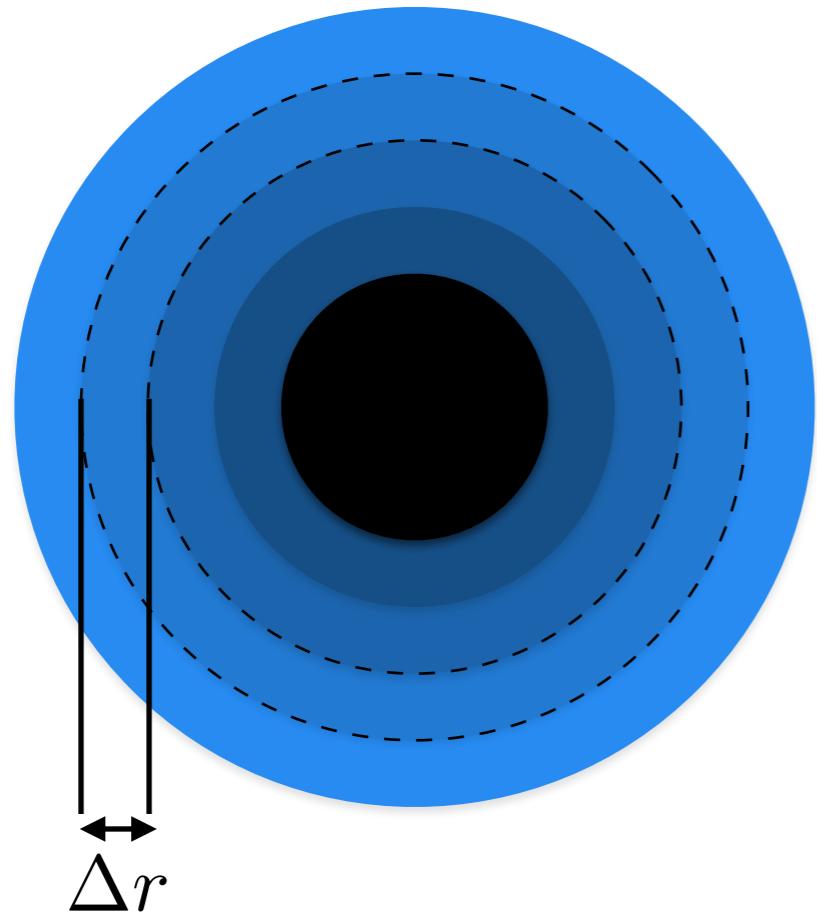


A: Binding energy of DM ΔU_{DM} over radius Δr



Energy Budget

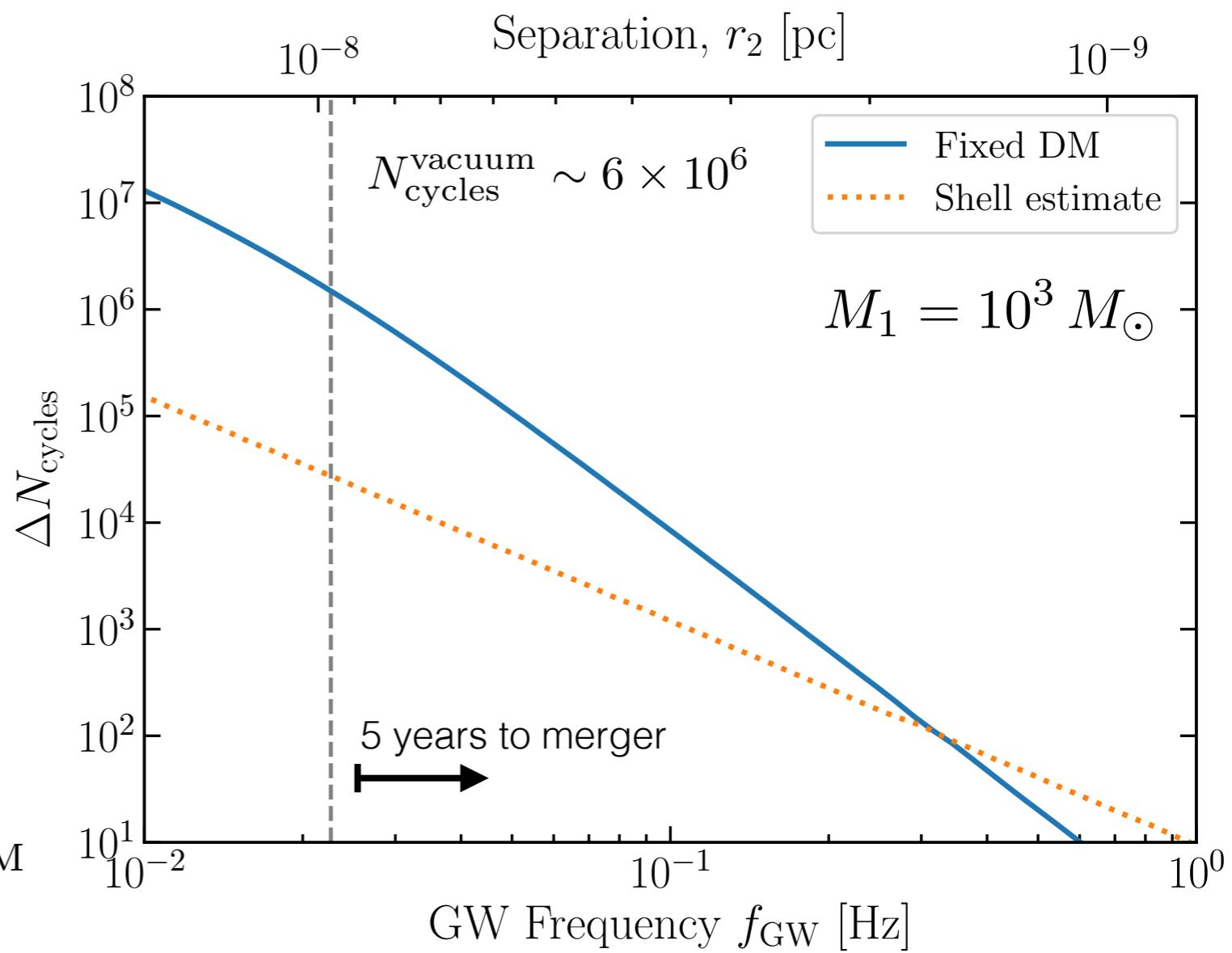
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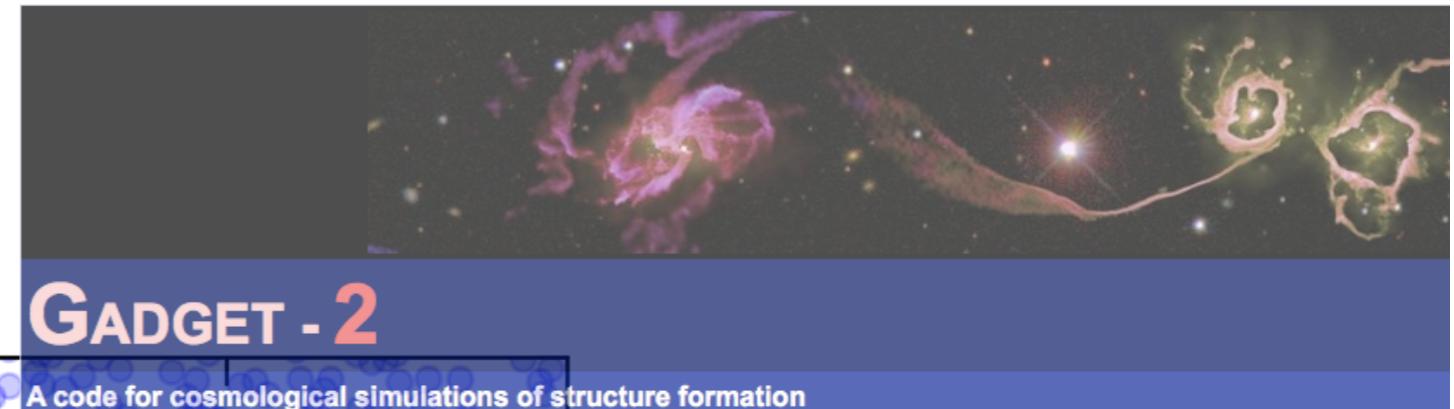
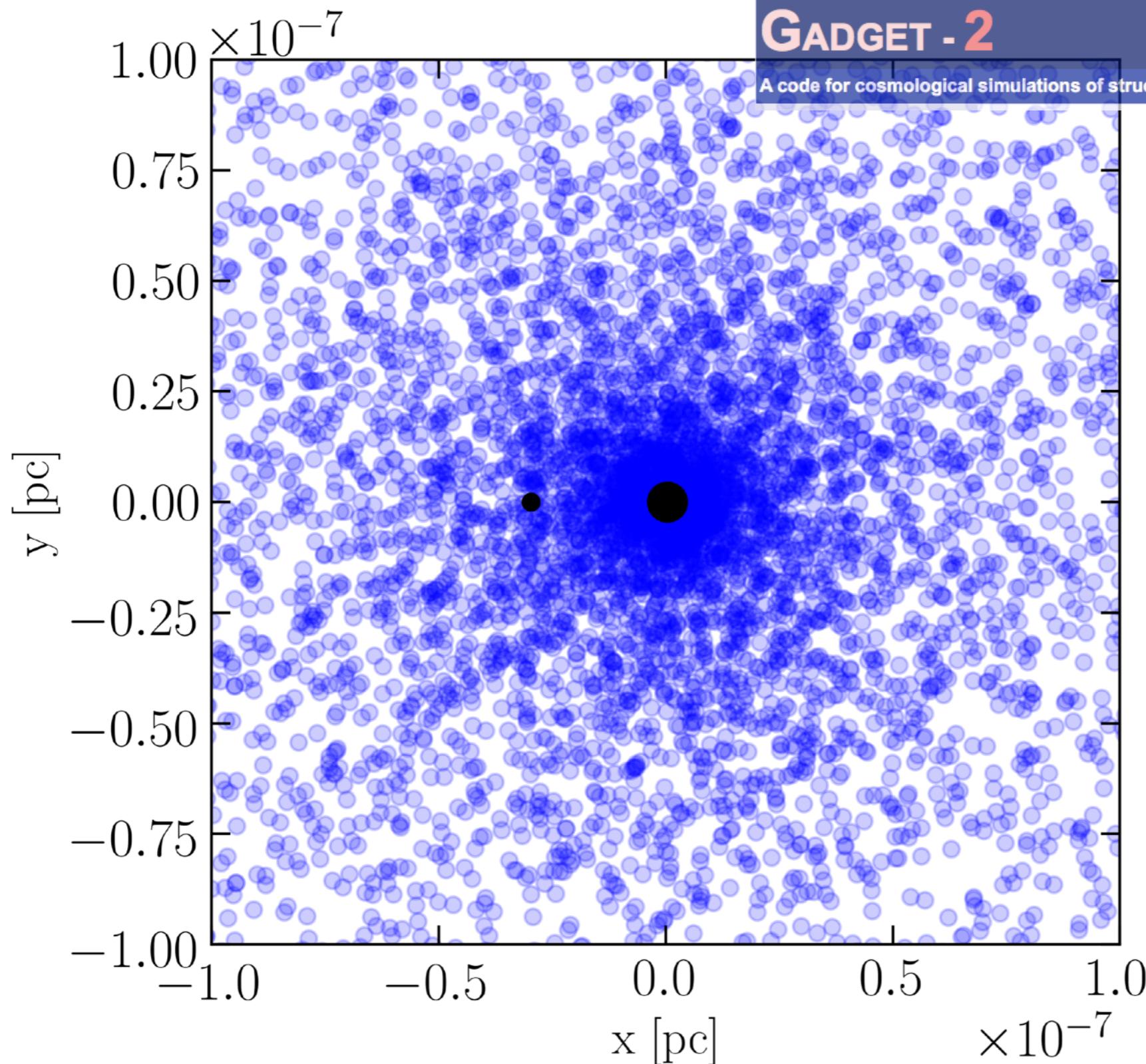
A: Binding energy of DM ΔU_{DM} over radius Δr

Evolve the system by fixing the dynamical friction force to extract *all* binding energy from a shell at a given radius:

$$\dot{E}_{\text{DF}} = \dot{r} \frac{dU_{\text{DM}}}{dr}$$



N-body Simulations



[astro-ph/0505010]

High Precision N-body Sims

Gadget-II code:

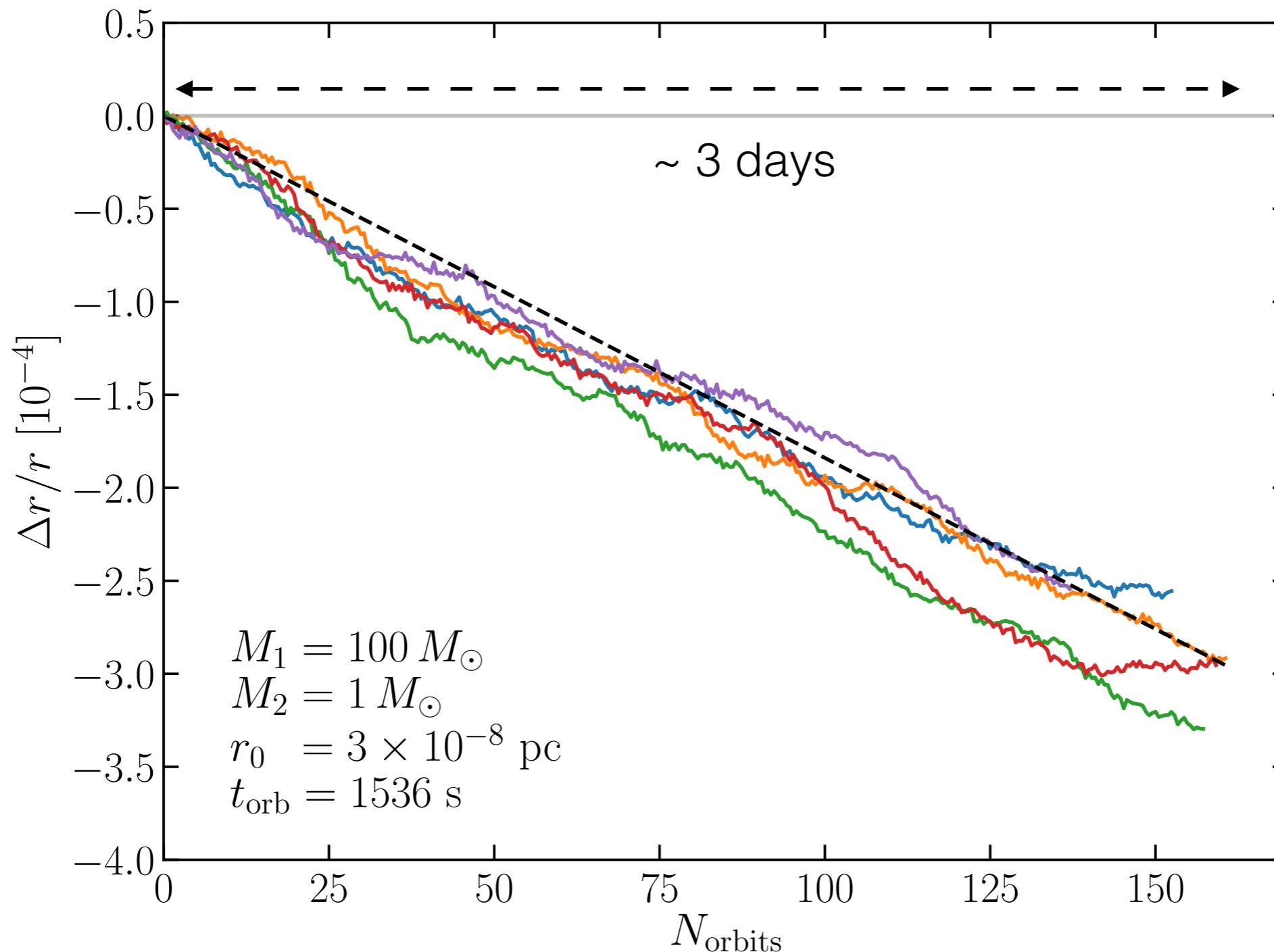
```
58
59  /* Some physical constants in cgs units */
60
61 #define GRAVITY      6.672e-8    /*!< Gravitational constant (in cgs units) */
62 #define SOLAR_MASS   1.989e33
63 #define SOLAR_LUM    3.826e33
64 #define RAD_CONST    7.565e-15
65 #define AVOGADRO    6.0222e23
66 #define BOLTZMANN   1.3806e-16
67 #define GAS_CONST   8.31425e7
68 #define C           2.9979e10
69 #define PLANCK      6.6262e-27
70 #define CM_PER_MPC  3.085678e24
71 #define PROTONMASS  1.6726e-24
72 #define ELECTRONMASS 9.10953e-28
73 #define THOMPSON    6.65245e-25
74 #define ELECTRONCHARGE 4.8032e-10
75 #define HUBLEE     3.2407789e-18    /* in h/sec */
76
```

The Universe:

$$G_N = 6.674 \times 10^{-8} \text{ m}^3 \text{ g}^{-1} \text{ s}^{-2}$$

N-body Results

Purely dynamical friction,
no GW emission



Allows us to check assumptions and fix normalisation of DF force ($\ln \Lambda$),
but can't simulate the whole 5 year inspiral!

Self-consistent evolution

Follow semi-analytically the phase space distribution of DM:

$$f = \frac{dN}{d^3\mathbf{r} d^3\mathbf{v}} \equiv f(\mathcal{E})$$

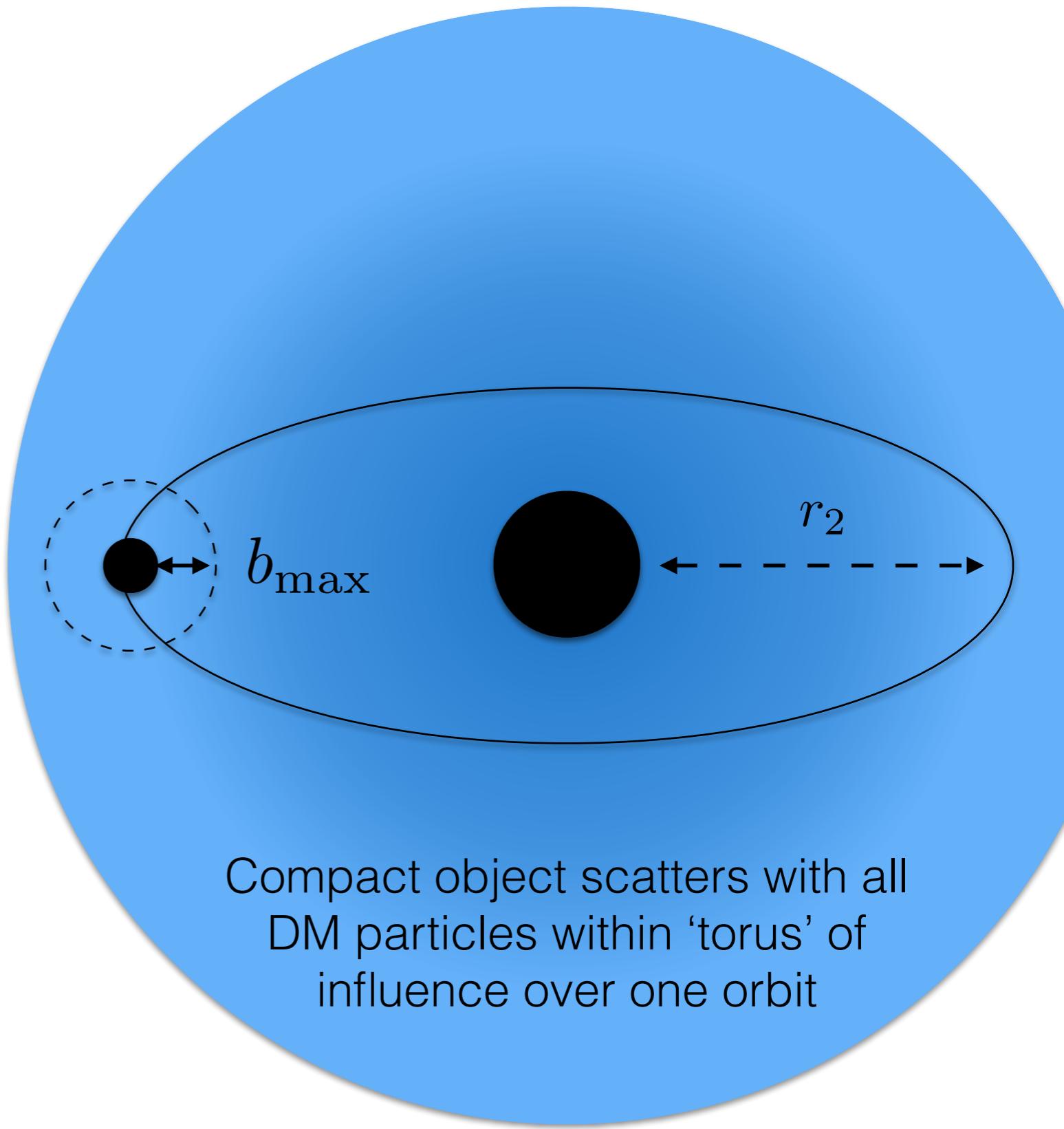
$$\mathcal{E} = \Psi(r) - \frac{1}{2}v^2$$

Each particle receives a ‘kick’ through gravitational scattering

$$\mathcal{E} \rightarrow \mathcal{E} + \Delta\mathcal{E}$$

Reconstruct density from distribution function:

$$\rho(r) = \int d^3\mathbf{v} f(\mathcal{E})$$



Self-consistent evolution

Assuming everything evolves slowly compared to the orbital period:

$$\Delta f(\mathcal{E}) = -p_{\mathcal{E}} f(\mathcal{E}) + \int \left(\frac{\mathcal{E}}{\mathcal{E} - \Delta\mathcal{E}} \right)^{5/2} f(\mathcal{E} - \Delta\mathcal{E}) P_{\mathcal{E}-\Delta\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$$

$P_{\mathcal{E}}(\Delta\mathcal{E})$ - probability for a particle with energy \mathcal{E} to scatter and receive a 'kick' $\Delta\mathcal{E}$

$p_{\mathcal{E}} = \int P_{\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$ - total probability for a particle with energy \mathcal{E} to scatter

Self-consistent evolution

Assuming everything evolves slowly compared to the orbital period:

$$\Delta f(\mathcal{E}) = -p_{\mathcal{E}} f(\mathcal{E}) +$$

Particles scattering from
 $\mathcal{E} \rightarrow \mathcal{E} + \Delta\mathcal{E}$

$$\int \left(\frac{\mathcal{E}}{\mathcal{E} - \Delta\mathcal{E}} \right)^{5/2} f(\mathcal{E} - \Delta\mathcal{E}) P_{\mathcal{E}-\Delta\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$$

Particles scattering from
 $\mathcal{E} - \Delta\mathcal{E} \rightarrow \mathcal{E}$

$P_{\mathcal{E}}(\Delta\mathcal{E})$ - probability for a particle with energy \mathcal{E} to scatter and receive a 'kick' $\Delta\mathcal{E}$

$$p_{\mathcal{E}} = \int P_{\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$$

- total probability for a particle with energy \mathcal{E} to scatter

Self-consistent evolution

Assuming everything evolves slowly compared to the orbital period:

$$T_{\text{orb}} \frac{df(\mathcal{E})}{dt} = -p_{\mathcal{E}} f(\mathcal{E}) +$$

Particles scattering from
 $\mathcal{E} \rightarrow \mathcal{E} + \Delta\mathcal{E}$

$$\int \left(\frac{\mathcal{E}}{\mathcal{E} - \Delta\mathcal{E}} \right)^{5/2} f(\mathcal{E} - \Delta\mathcal{E}) P_{\mathcal{E}-\Delta\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$$

Particles scattering from
 $\mathcal{E} - \Delta\mathcal{E} \rightarrow \mathcal{E}$

$P_{\mathcal{E}}(\Delta\mathcal{E})$ - probability for a particle with energy \mathcal{E} to scatter and receive a 'kick' $\Delta\mathcal{E}$

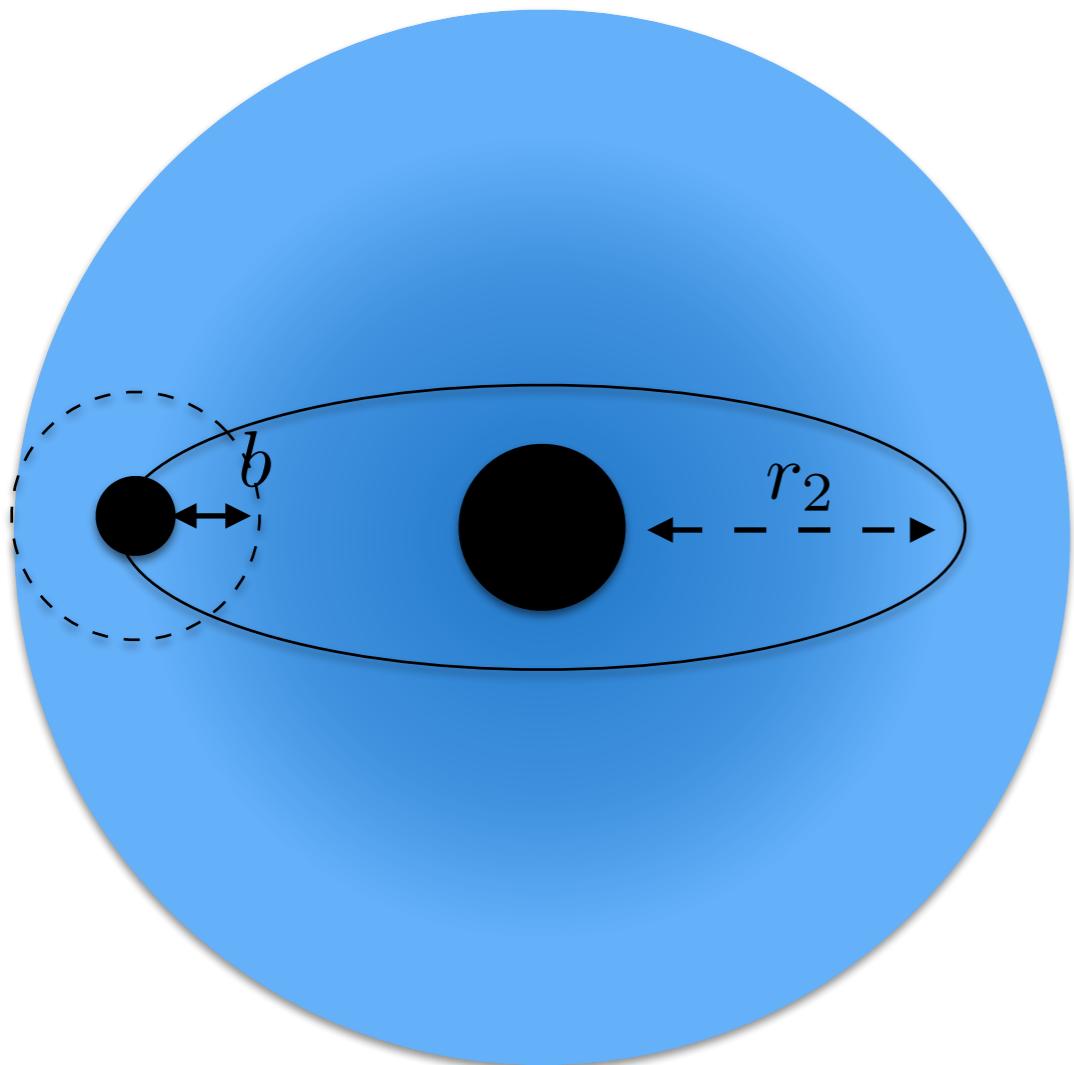
$$p_{\mathcal{E}} = \int P_{\mathcal{E}}(\Delta\mathcal{E}) d\Delta\mathcal{E}$$

- total probability for a particle with energy \mathcal{E} to scatter

Scattering probability $P_{\mathcal{E}}(\Delta\mathcal{E})$

Two body scattering problem relates energy exchange to impact parameter:

$$\Delta\mathcal{E}(b) = -2v_0^2 \left[1 + \frac{b^2 v_0^4}{G^2 m_2^2} \right]^{-1}$$



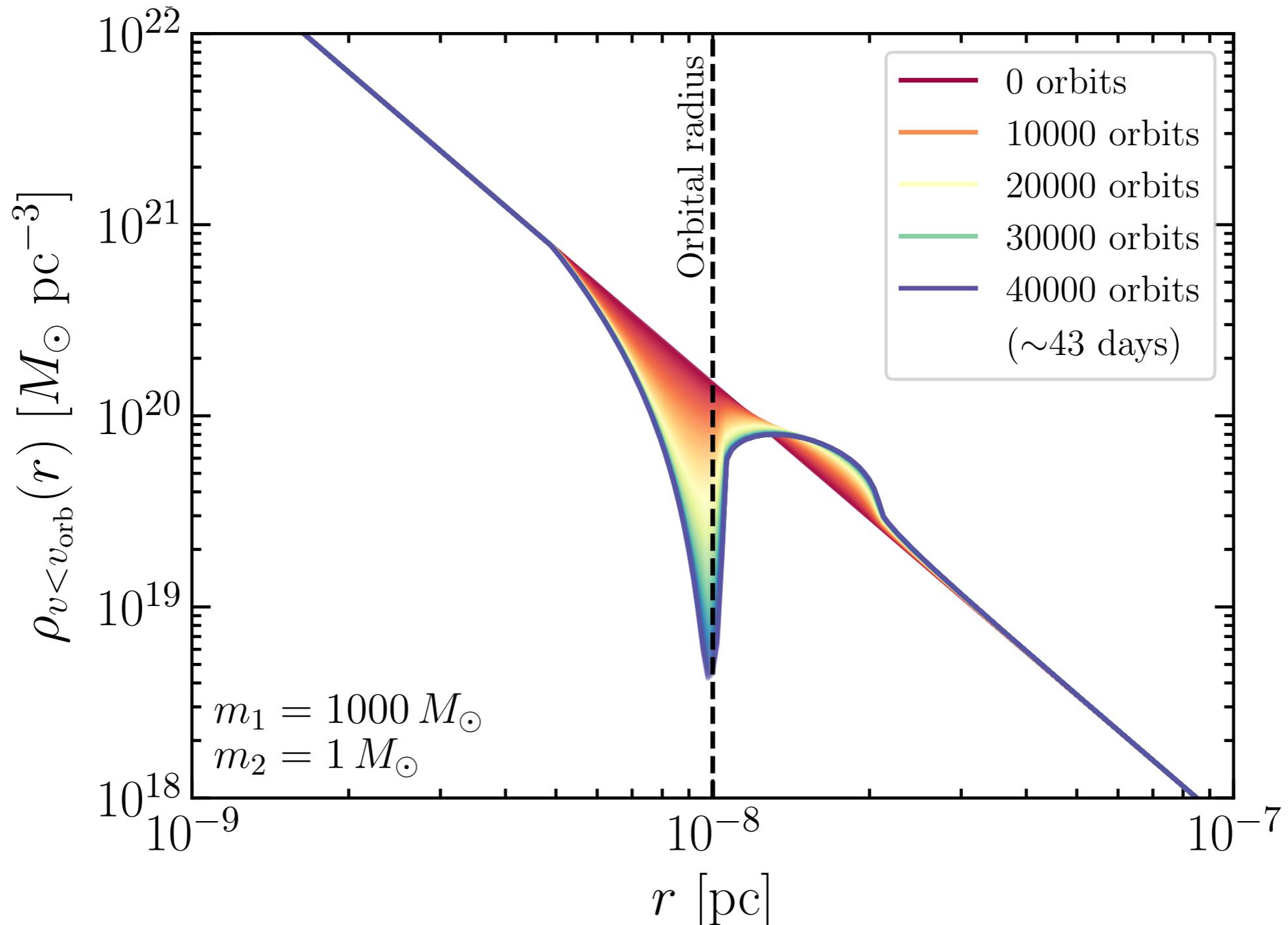
Integrate over the surface of the
'torus of influence'

Working to first order in b/r , $P_{\mathcal{E}}(\Delta\mathcal{E})$
can be written in terms of elliptic integrals

Code available online:
github.com/bradkav/HaloFeedback

Evolution of density profile

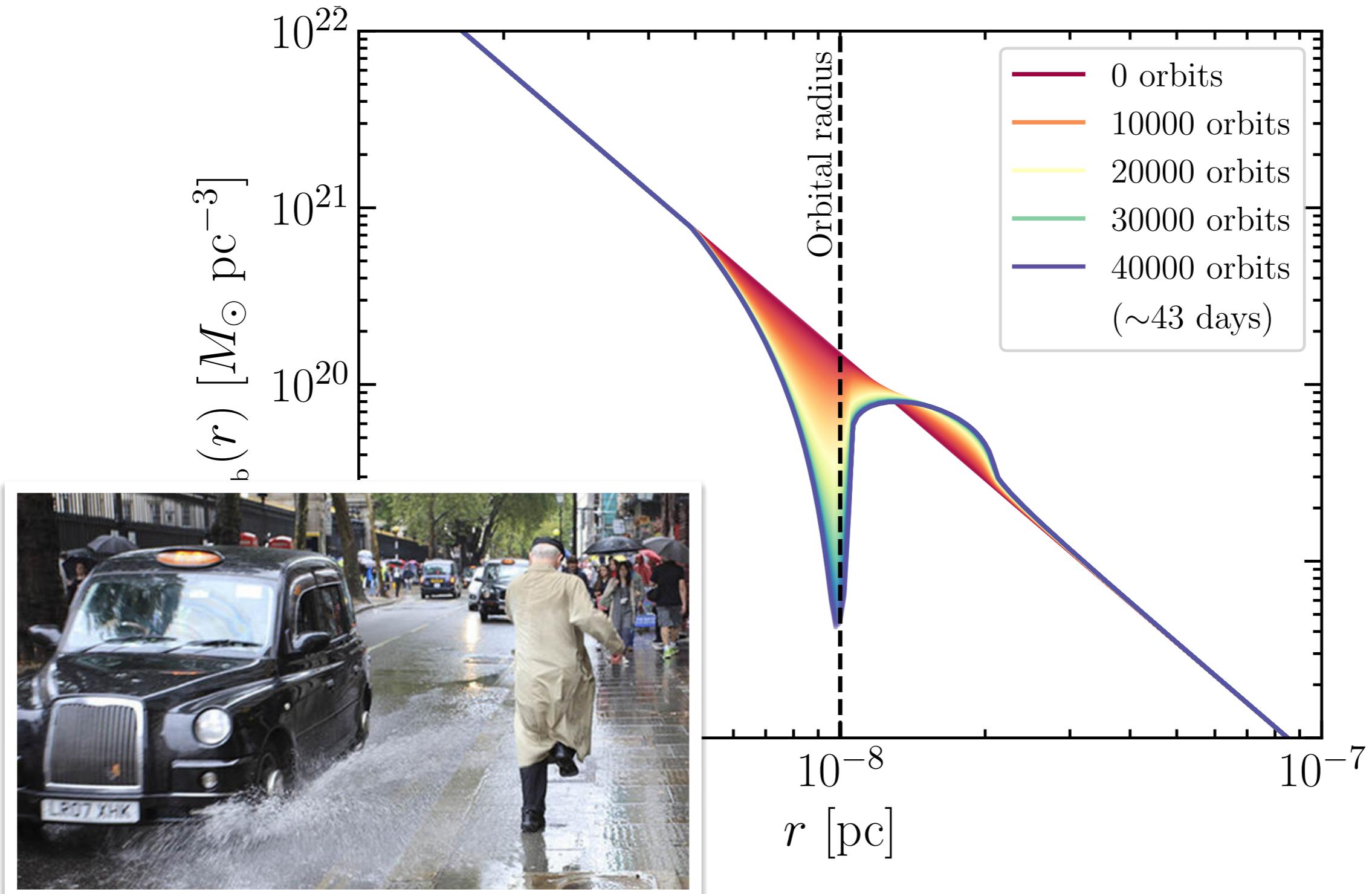
How does the DM halo ‘react’ to the orbiting compact object?



Subtlety: plotting here only ‘slow moving’ particles

Evolution of density profile

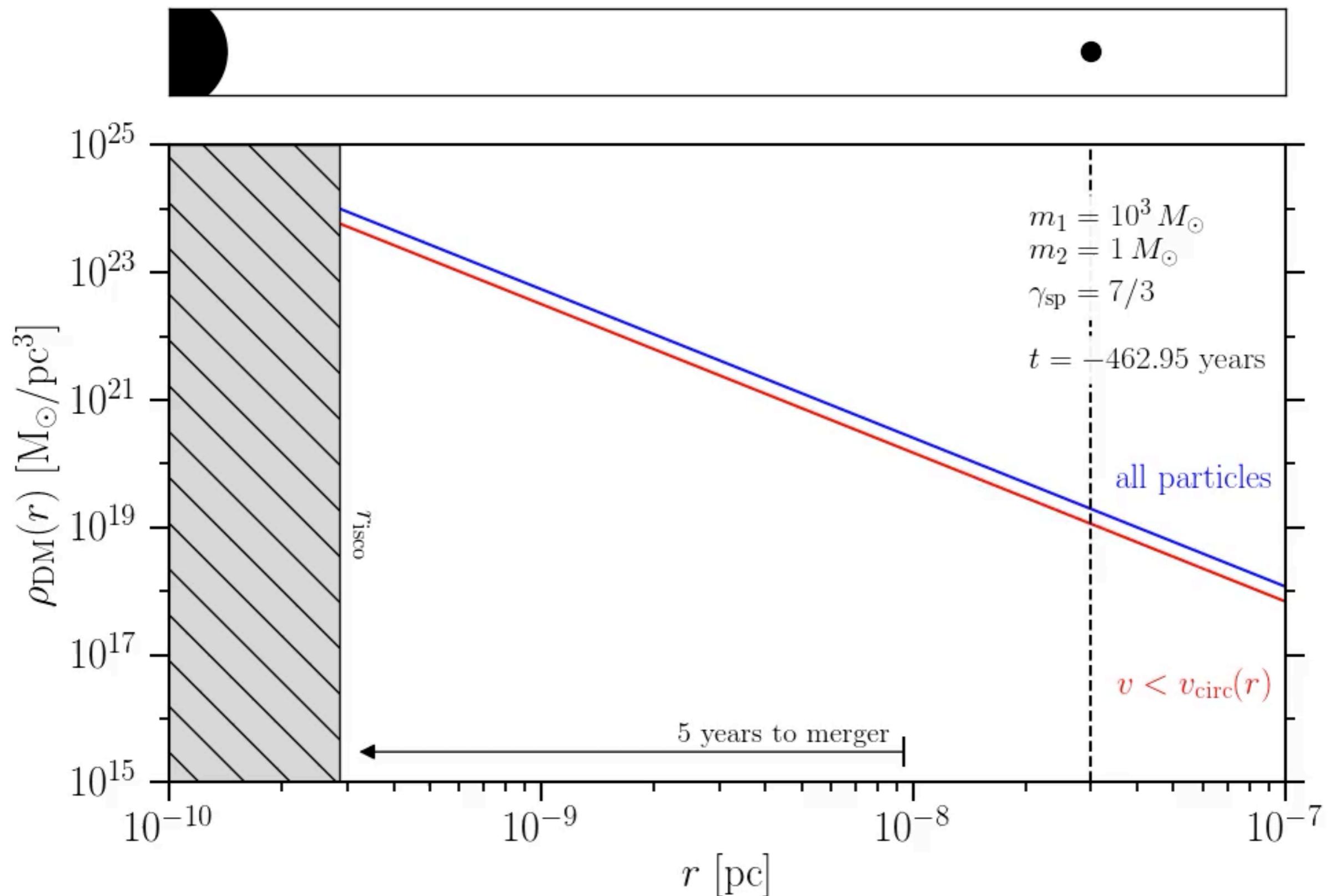
How does the DM halo ‘react’ to the orbiting compact object?



Subtlety: plotting here only ‘slow moving’ particles

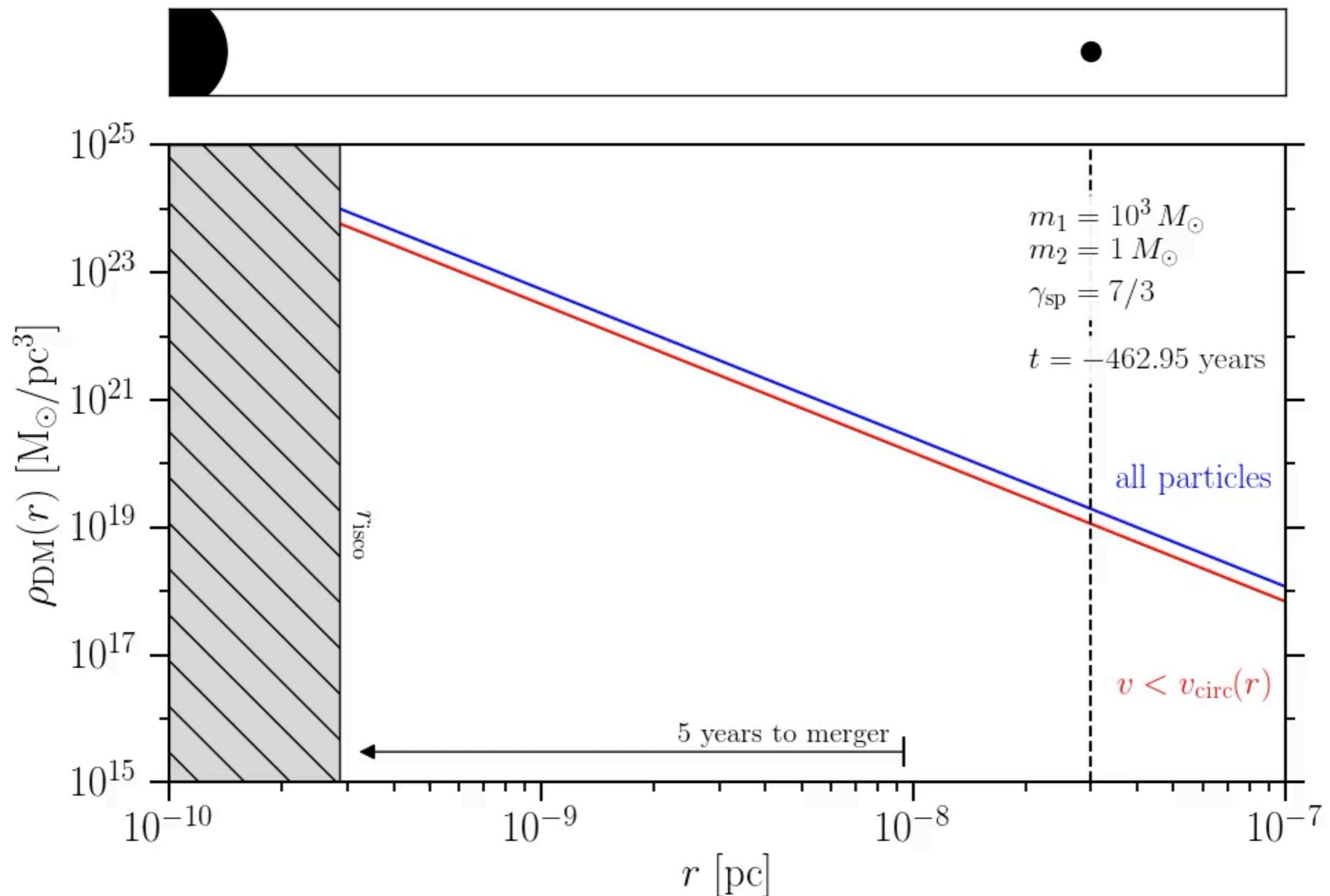
Full evolution of the system

Movies: tinyurl.com/GW4DM

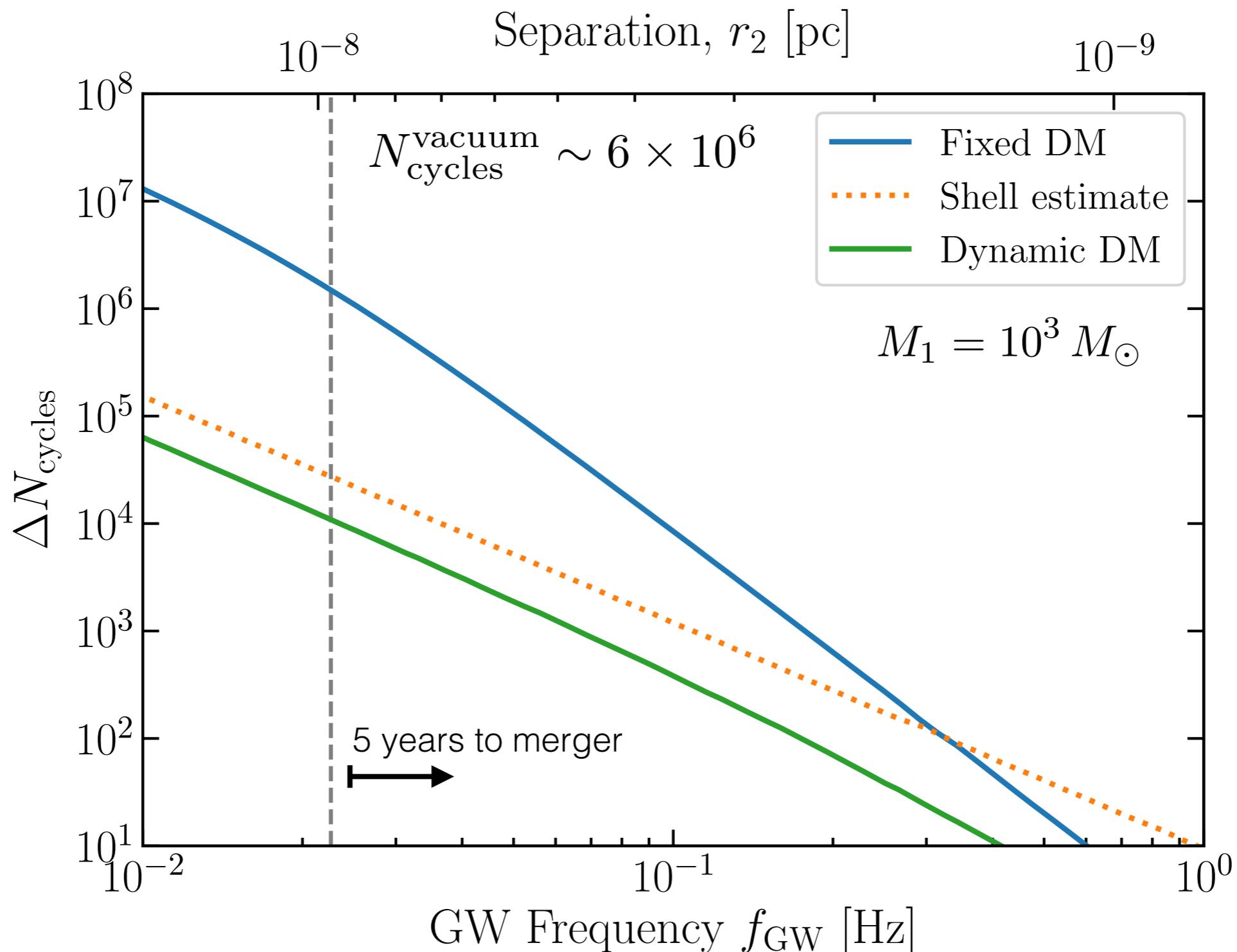


Full evolution of the system

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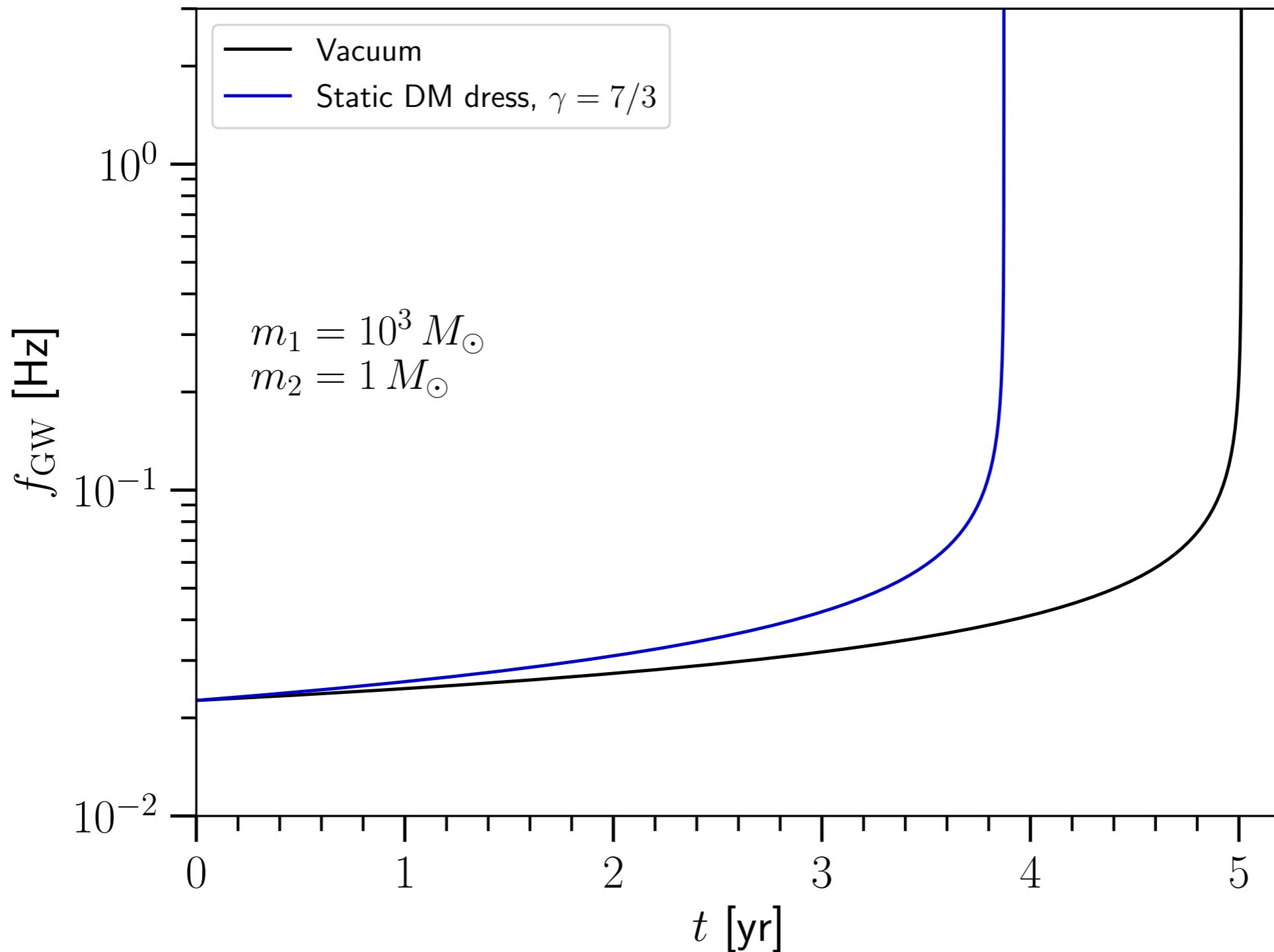
Self-consistent results



$$\Delta N_{\text{cycles}}(\text{static}) \approx 10^6 \rightarrow \Delta N_{\text{cycles}}(\text{dynamic}) \approx 10^4$$

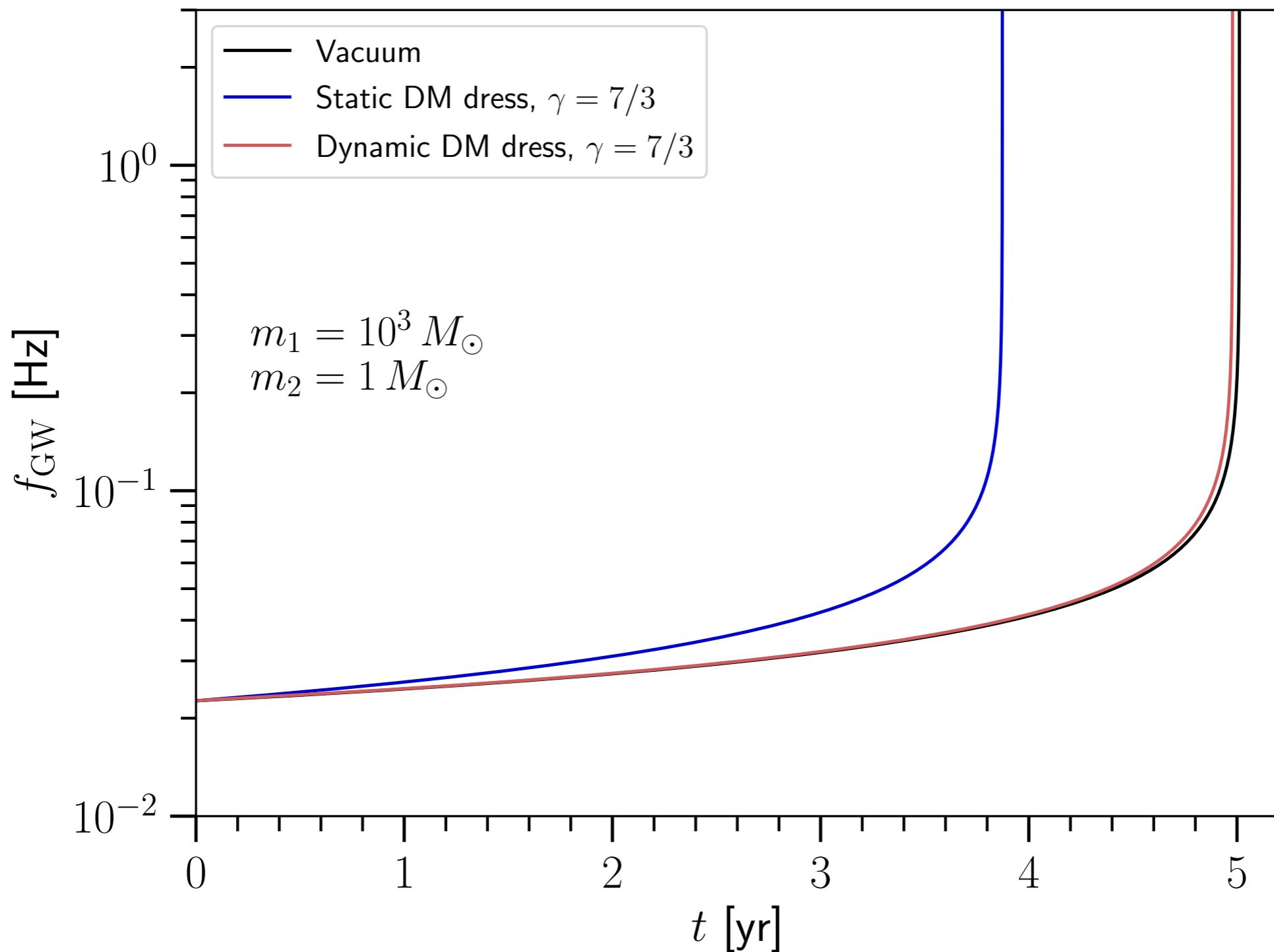
Spectrograms: $m_{\text{IMBH}} = 10^3 M_\odot$

$$\rho_{\text{DM}} = \rho_6 \left(\frac{10^{-6} \text{ pc}}{r} \right)^{\gamma_{\text{sp}}}$$



Spectrograms: $m_{\text{IMBH}} = 10^3 M_\odot$

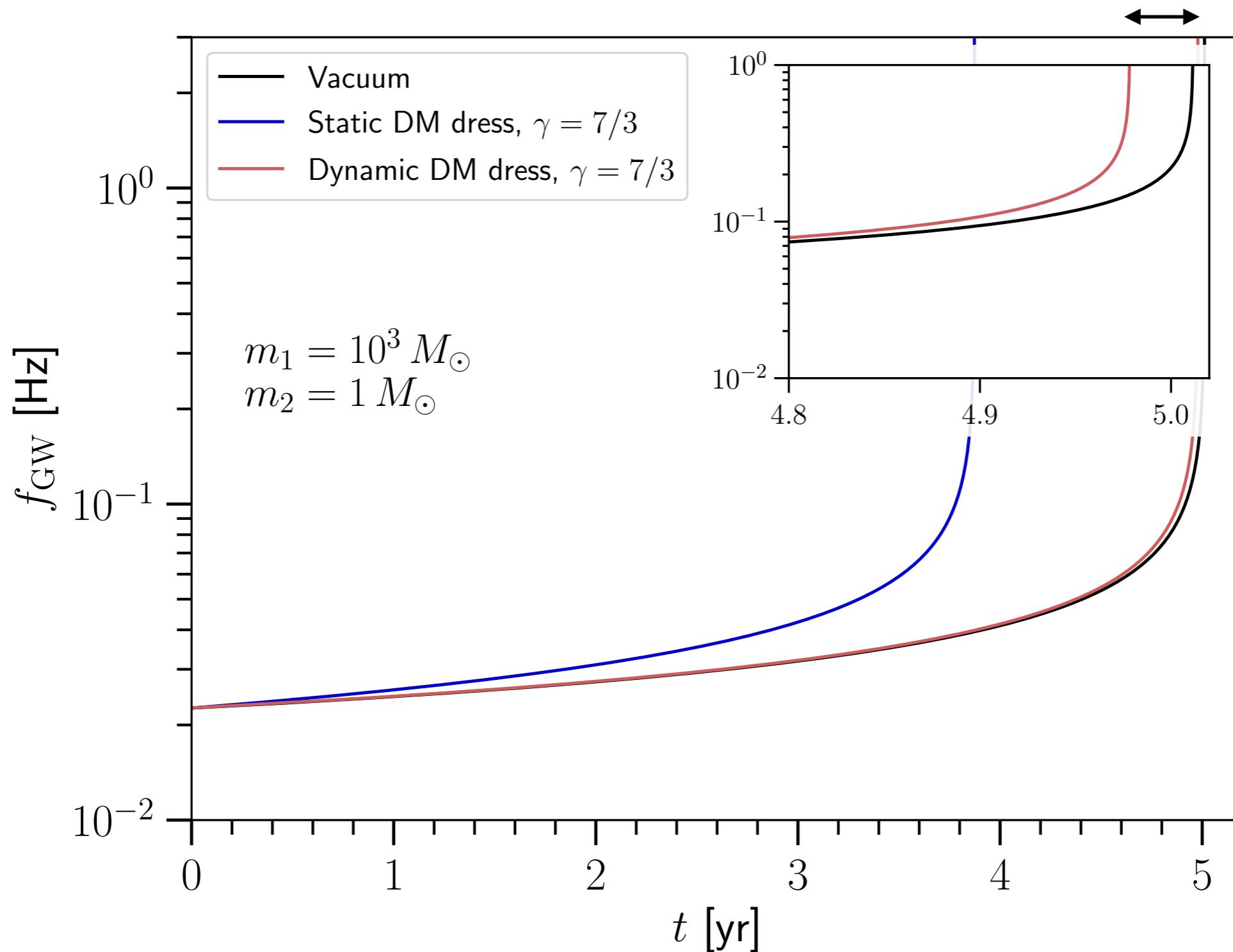
$$\rho_{\text{DM}} = \rho_6 \left(\frac{10^{-6} \text{ pc}}{r} \right)^{\gamma_{\text{sp}}}$$



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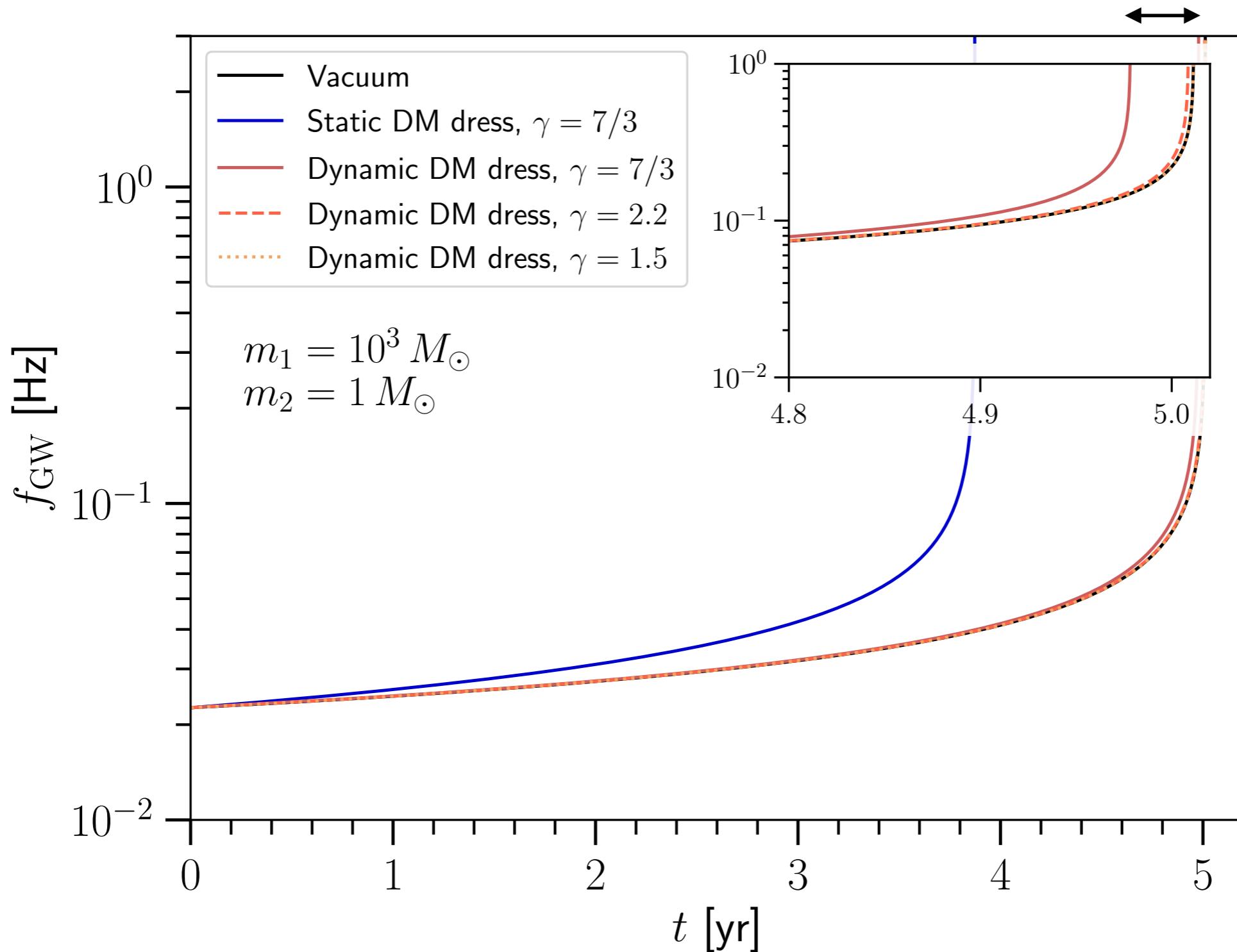
~ 12 days



Spectrograms: $m_{\text{IMBH}} = 10^3 M_\odot$

$$\rho_{\text{DM}} = \rho_6 \left(\frac{10^{-6} \text{ pc}}{r} \right)^{\gamma_{\text{sp}}}$$

~ 12 days

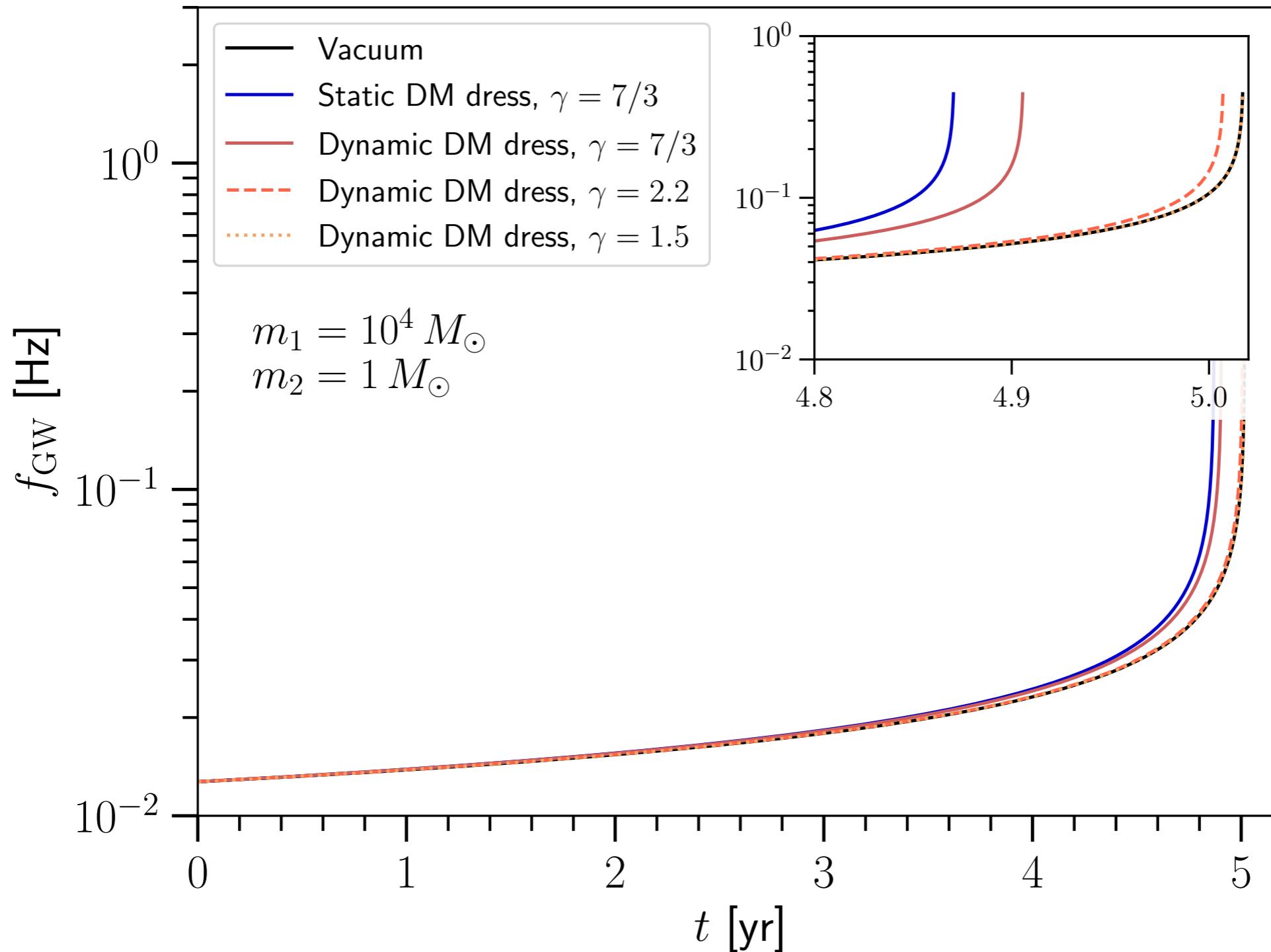


NB: $7/3 \approx 2.333$

Spectrograms: $m_{\text{IMBH}} = 10^4 M_\odot$

$$\rho_{\text{DM}} = \rho_6 \left(\frac{10^{-6} \text{ pc}}{r} \right)^{\gamma_{\text{sp}}}$$

As we increase the IMBH mass, the correction from having a dynamic DM halo decreases (but can still be very relevant)



NB: $7/3 \approx 2.333$

Detectability?

$$\Delta N_{\text{cycles}}(\text{static}) \approx 10^6 \rightarrow \Delta N_{\text{cycles}}(\text{dynamic}) \approx 10^4$$

In many systems, a more realistic treatment leads to a huge reduction in the size of the ‘de-phasing’ effect.

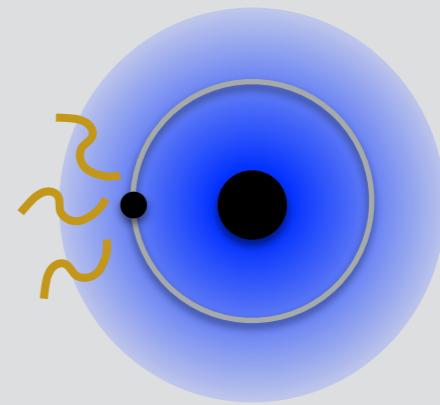
Even for very massive BHs, small corrections can spoil our ability to find the signal in data (so they must be accounted for)

The ‘rule of thumb’: *LISA should be able to detect a de-phasing as small as one radian.*

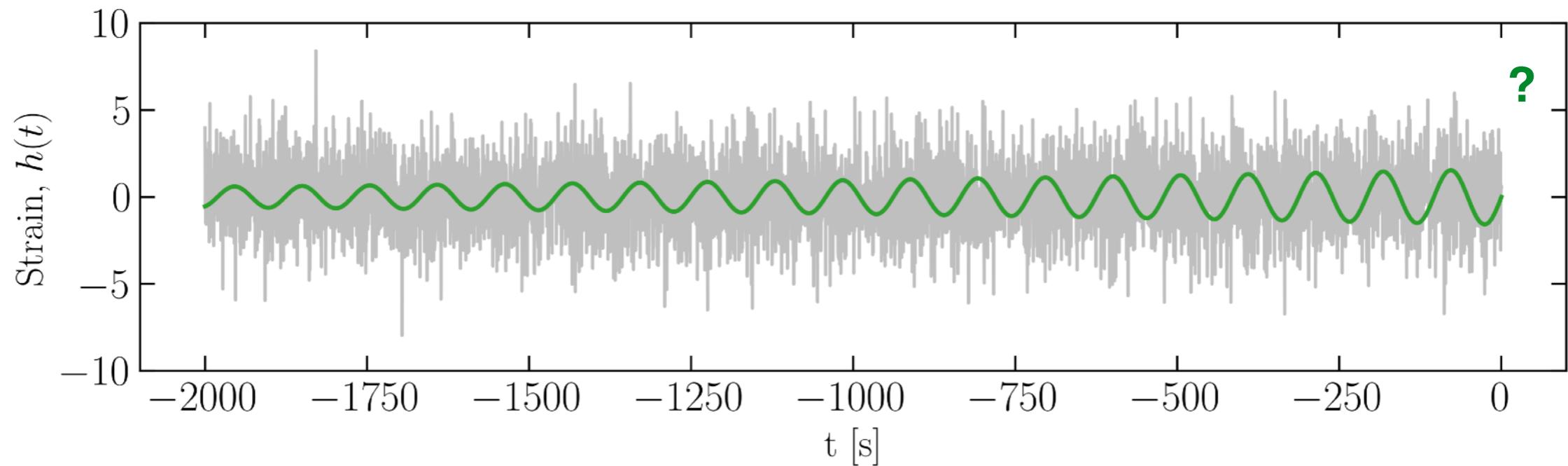
For a 1000 or 10000 solar mass IMBH, a de-phasing of ~10,000 cycles would still be easily detectable.

Measuring Dark Matter around Black Holes

[Coogan, Bertone, Gaggero, **BJK** & Nichols,
2108.04154]



A more realistic scenario



Want to address questions of:

- **Detectability** - is the event loud enough to detect?
- **Discoverability** - can we tell it apart from a *vacuum* waveform?
- **Measurability** - can we pin down the properties of the system
(especially *the DM*)?

Detectability

A signal may be *detectable* with LISA using matched filtering with a signal-to-noise ratio (SNR) $\gtrsim 15\dots$

[\[1905.11998\]](#)

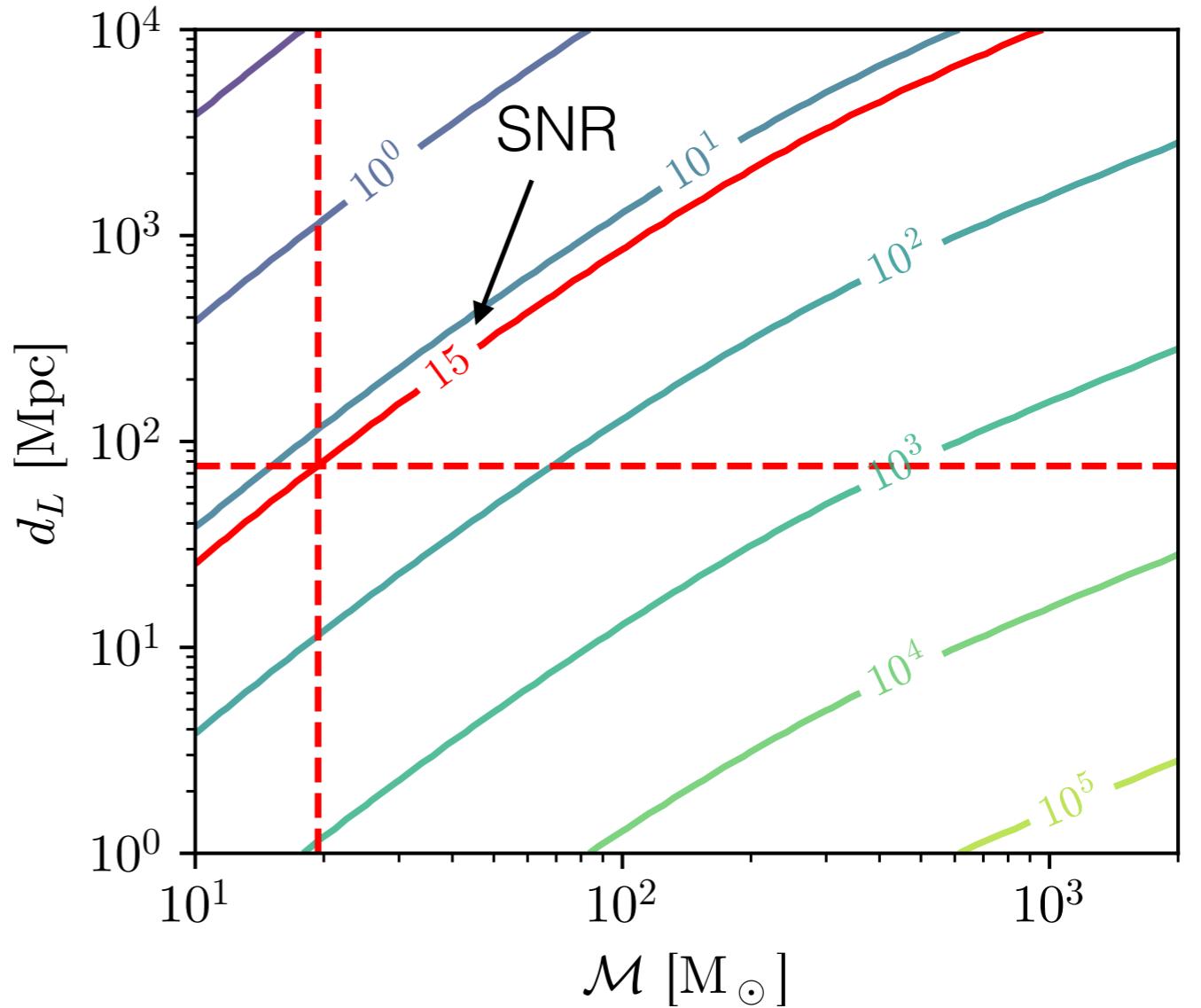
Match between waveforms a and b defined as:

$$\langle a | b \rangle = 4 \operatorname{Re} \int_0^\infty df \frac{\tilde{a}(f)^* \tilde{b}(f)}{S_n(f)}$$

Optimal SNR for waveform s is then:

$$\text{SNR}(s) = \sqrt{\langle s | s \rangle}$$

NB: Presence of the dark dress does not substantially affect SNR



$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$

Discoverability (1)

$$q = m_2/m_1$$

We'll call a DM spike *discoverable* if it can be distinguished from a vacuum-only system.

Compare Bayesian evidence for **V**acuum and **D**ressed systems:

$$\text{BF}(d) \equiv \frac{p(d|\text{D})}{p(d|\text{V})}$$

$$p(d) = \int d\boldsymbol{\theta} \mathcal{L}(\boldsymbol{\theta}) p(\boldsymbol{\theta})$$

Likelihood
Prior

$$\boldsymbol{\theta}_{\text{V}} = \{\mathcal{M}\}$$

$$\boldsymbol{\theta}_{\text{D}} = \{\gamma_{\text{sp}}, \rho_6, \mathcal{M}, \log_{10} q\}$$

$$\boldsymbol{\theta}_{\text{ext}} \equiv \{D_L, \phi_c, \tilde{t}_c\}$$

Solving the whole system is *slow*. Instead use an approximate parametrisation of $h(f)$ in terms of $\boldsymbol{\theta}_{\text{D}}$...
(see backup slides)

[<https://github.com/adam-coogan/pydd>]

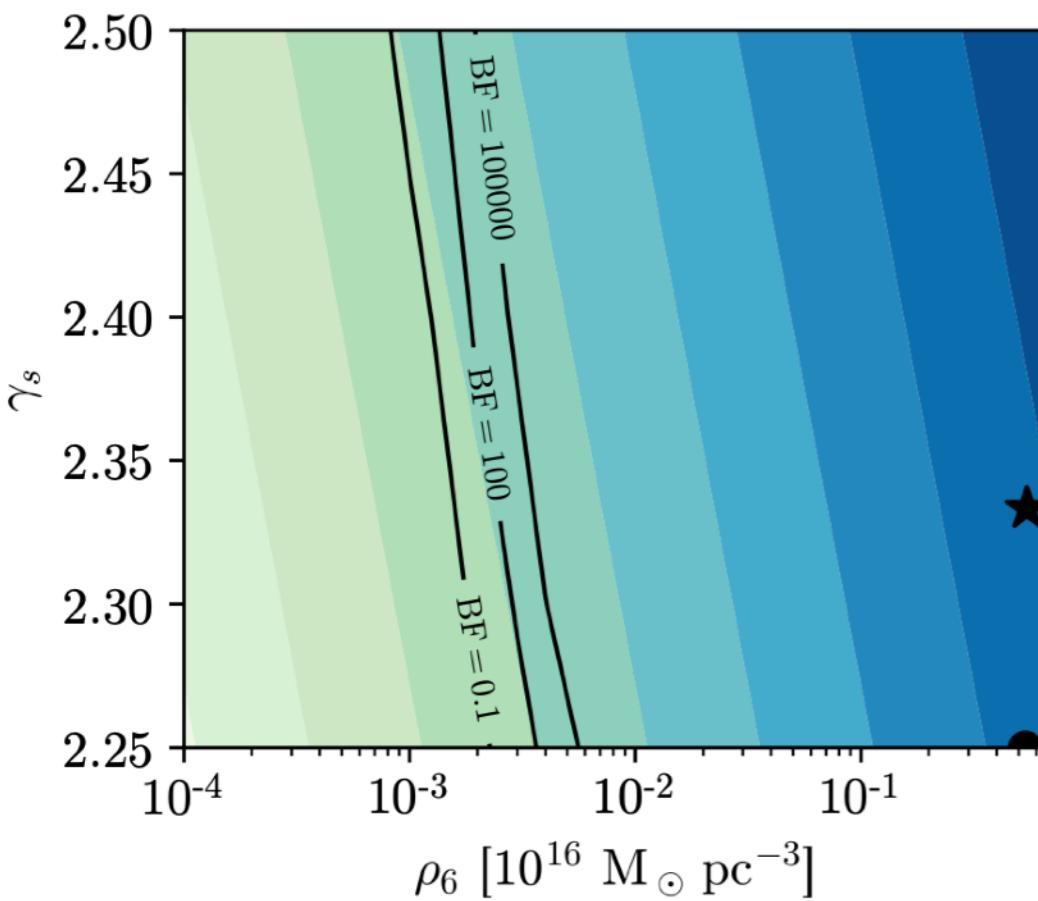
Discoverability (2)

$$q = m_2/m_1$$

We'll call a DM spike *discoverable* if it can be distinguished from a vacuum-only system.

Compare Bayesian evidence for **V**acuum and **D**ressed systems:

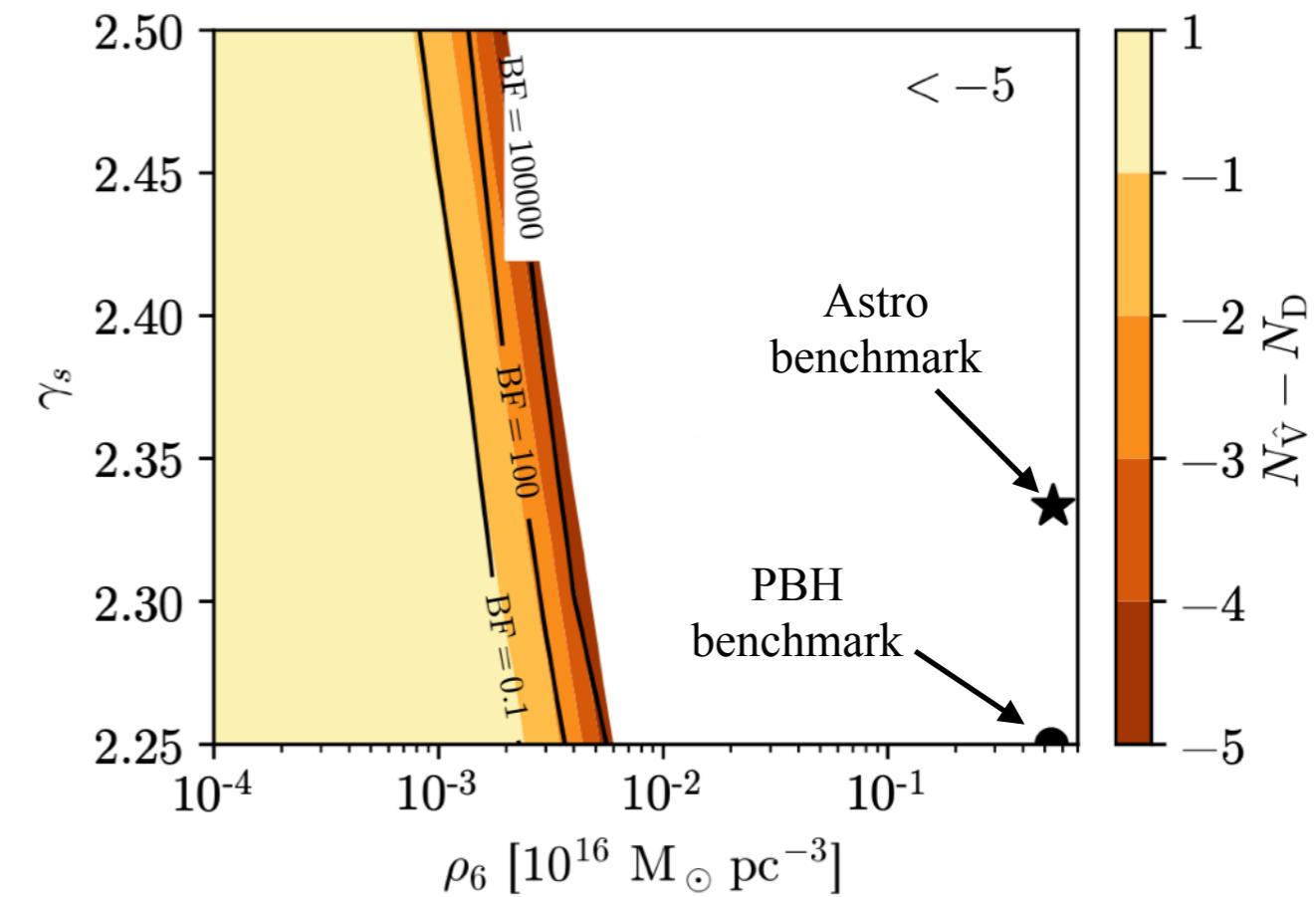
$$\text{BF}(d) \equiv \frac{p(d|\text{D})}{p(d|\text{V})}$$



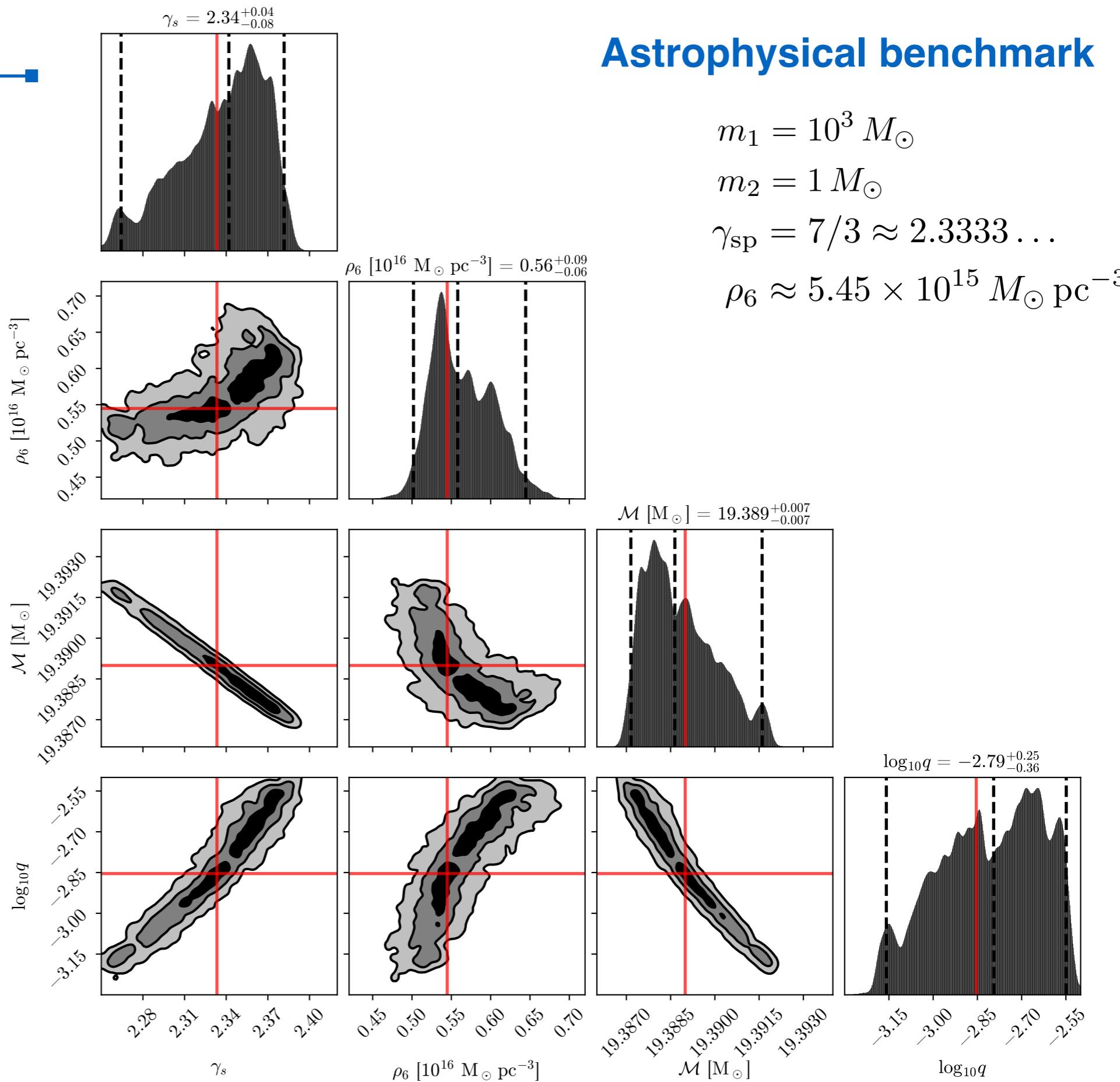
$$p(d) = \int d\theta \mathcal{L}(\theta) p(\theta)$$

Likelihood

Prior



Measurability



Astrophysical benchmark

$$m_1 = 10^3 M_\odot$$

$$m_2 = 1 M_\odot$$

$$\gamma_{\text{sp}} = 7/3 \approx 2.3333\dots$$

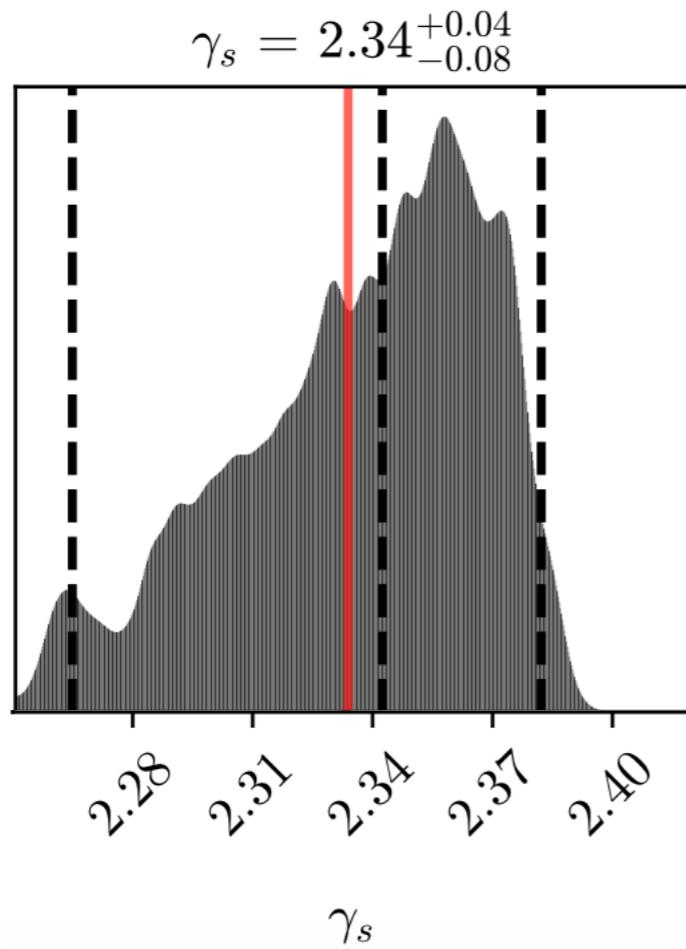
$$\rho_6 \approx 5.45 \times 10^{15} M_\odot \text{ pc}^{-3}$$

Discriminability?

Focus for now on the initial slope of the spike γ_s .
Can we tell different spikes apart?

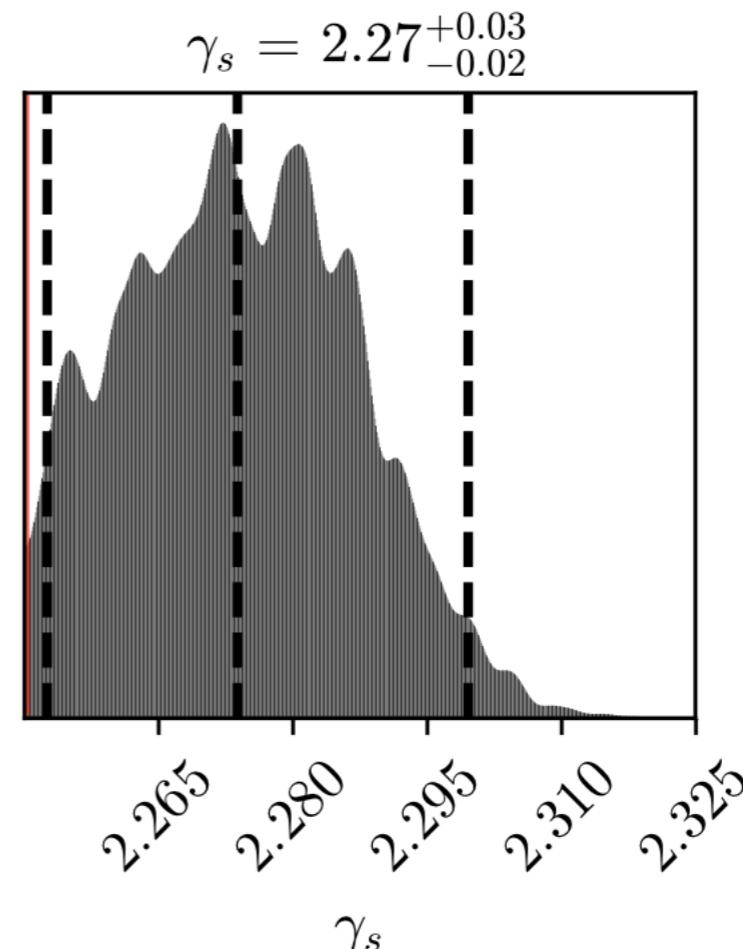
Astrophysical benchmark

$$\gamma_{\text{astro}} = 2.333$$



PBH benchmark

$$\gamma_{\text{PBH}} = 2.25$$



We may be able to distinguish different *shapes* of spike
→ Different DM models and formation mechanisms!

Growing interest

Gianfranco Bertone
(GRAPPA, Amsterdam)



Daniele Gaggero
(IFT, Madrid)



Pippa Cole
(GRAPPA, Amsterdam)



Pratibha Jangra
(IFCA, Santander)



Adam Coogan
(Mila, Montreal)



David Nichols
(U. Virginia)



Jose Maria Diego
(IFCA, Santander)



Francesca Scarcella
(IFT, Madrid)



and others...

Working on many inter-related ideas and projects
on PBHs, IMRIs and Gravitational Waves...

Plans for the future

Improved modelling

- Injection and evolution of angular momentum in the DM halo
- Post-Newtonian corrections
- Better N-body approaches [[AMUSE?](#)]

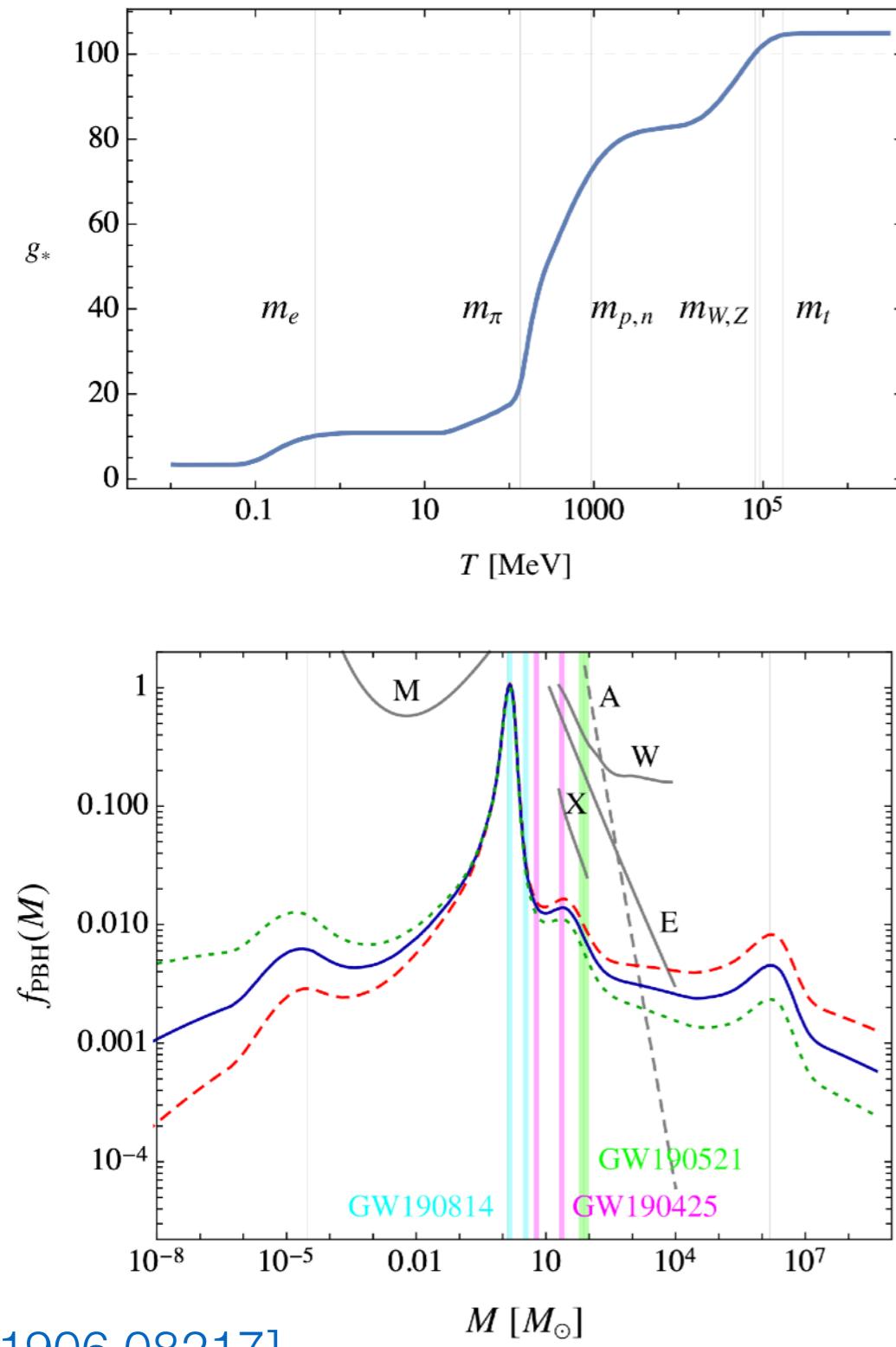
Detection methods

- Producing template banks for LISA searches
- Surrogate models for waveform generation
- Incoherent searches for continuous GWs
- ‘General’ de-phased waveform templates [[2004.06729](#)]

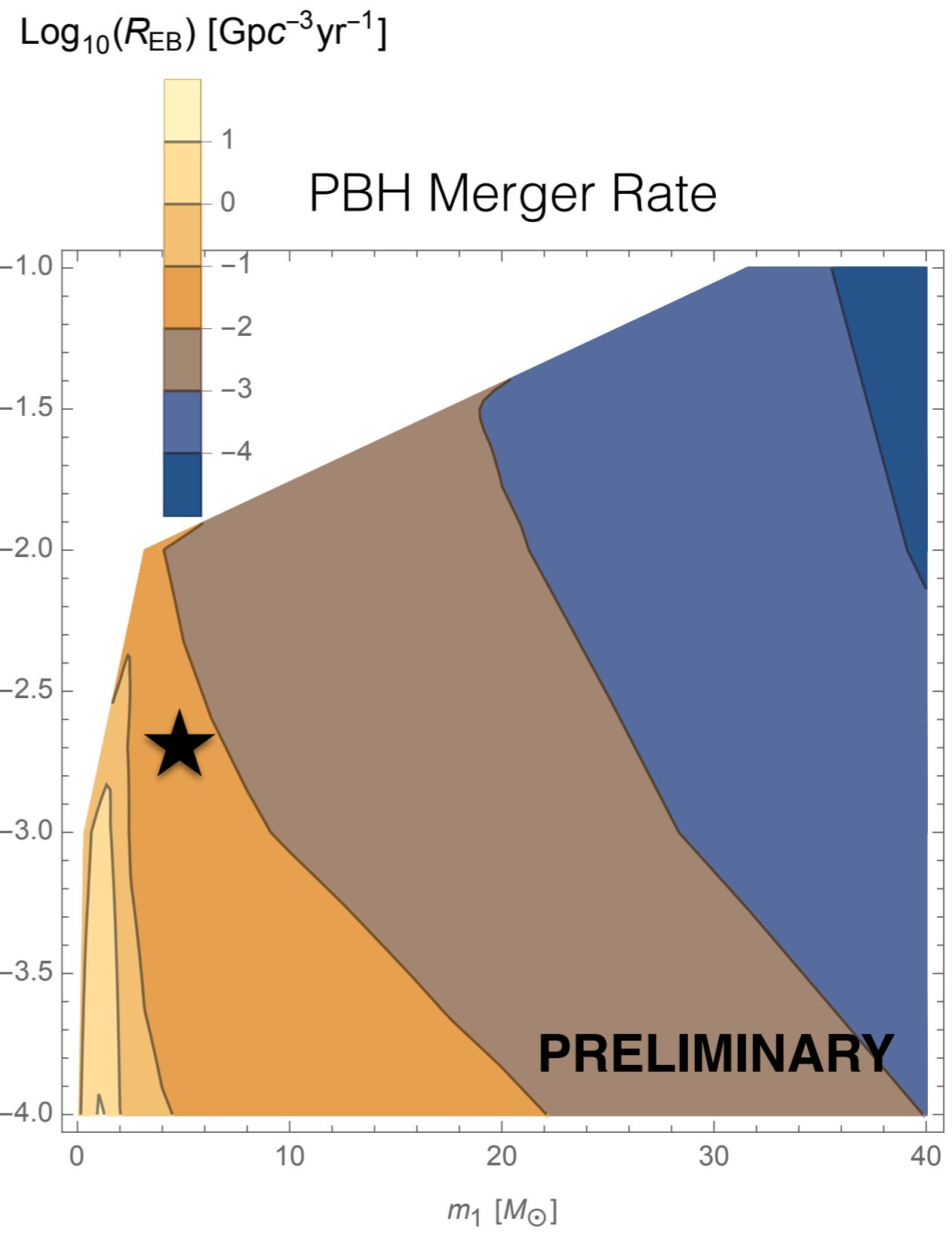
Detection prospects

- How many IMRI systems form? How many with BH/NSs?
- How many systems have a (surviving) spike?
- *What about ground-based detectors?*

Low mass PBH binaries



[1906.08217]

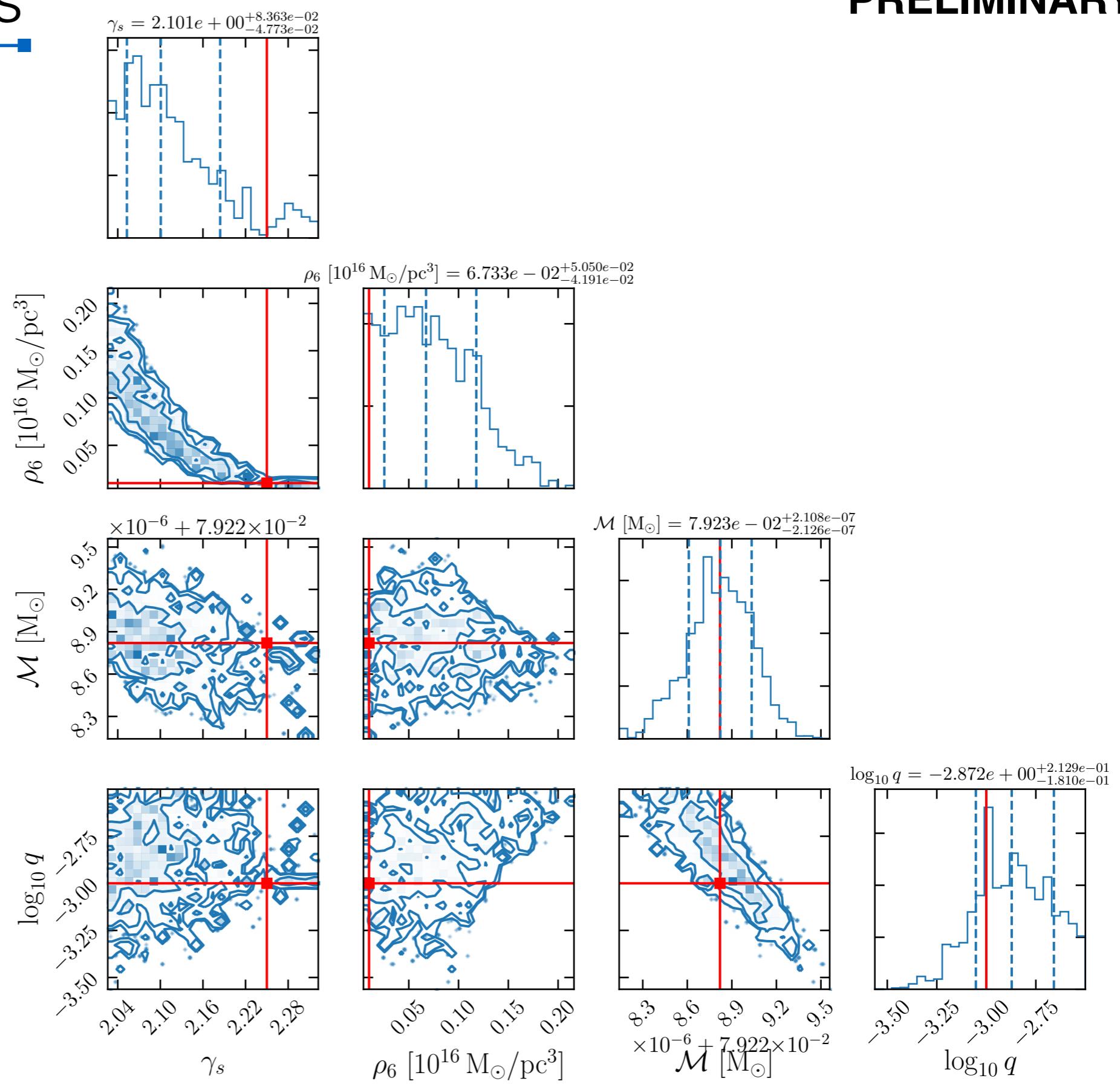


Need ground-based detectors (LIGO, Einstein Telescope, ...) to detect

Low mass PBHs

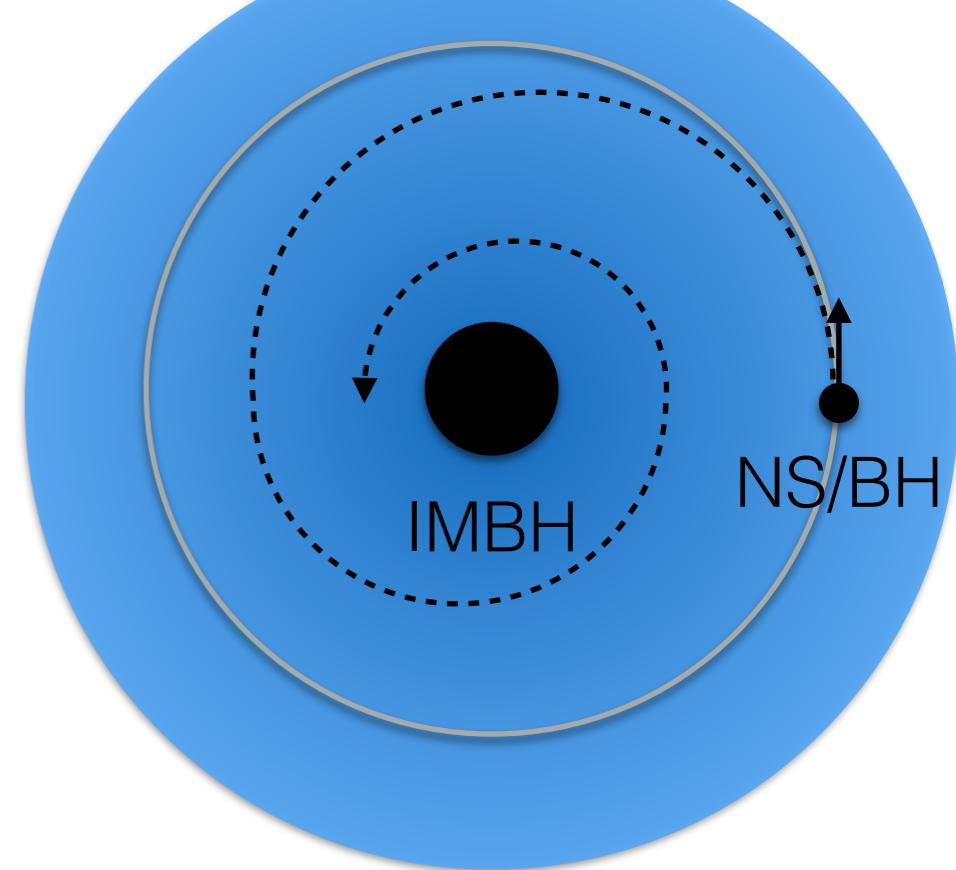
$m_1 = 5 M_\odot$; $m_2 = 0.005 M_\odot$; aLIGO

PRELIMINARY



Conclusions

Dark Matter ‘de-phasing’ is an extremely promising GW signature, which needs to be **modelled carefully**



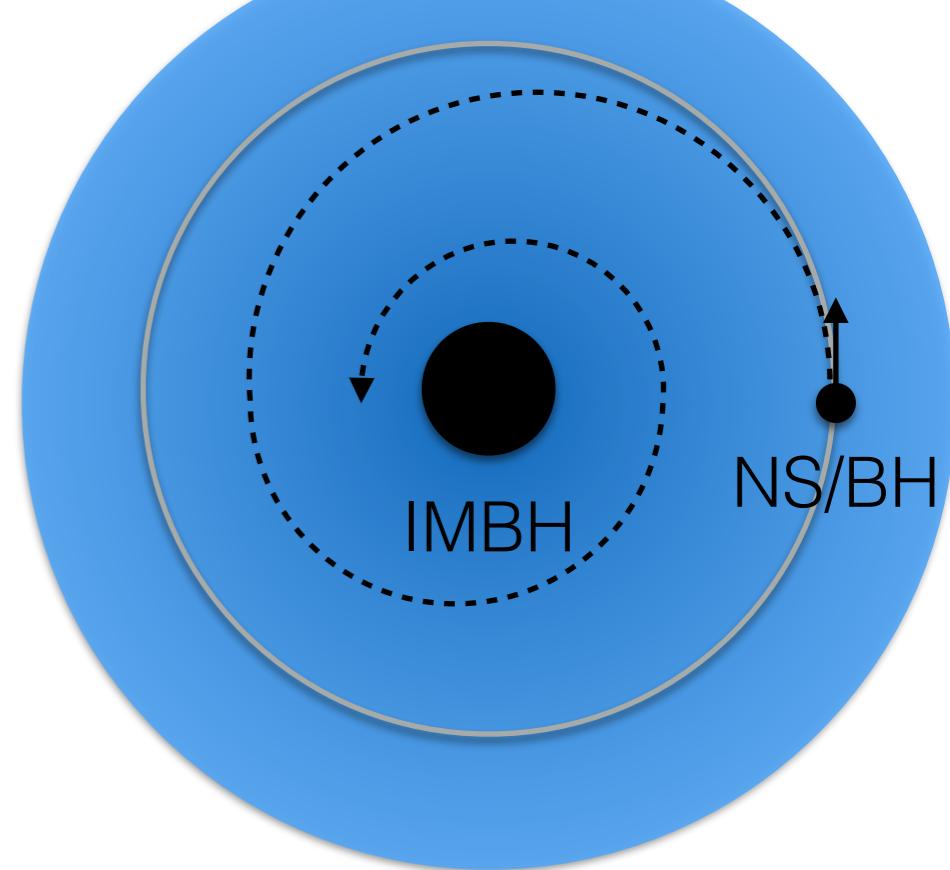
For light IMBHs, the **correction due to DM halo feedback** can be huge!

More calculations are needed to refine the modelling, to build template banks, and to understand the prospects for detection

These signals could probe the **nature of Dark Matter** and pave the way towards a **multi-messenger detection** of (Axion?) Dark Matter

Conclusions

Dark Matter ‘de-phasing’ is an extremely promising GW signature, which needs to be **modelled carefully**



For light IMBHs, the **correction due to DM halo feedback** can be huge!

More calculations are needed to refine the modelling, to build template banks, and to understand the prospects for detection

These signals could probe the **nature of Dark Matter** and pave the way towards a **multi-messenger detection** of (Axion?) Dark Matter

Thank you!

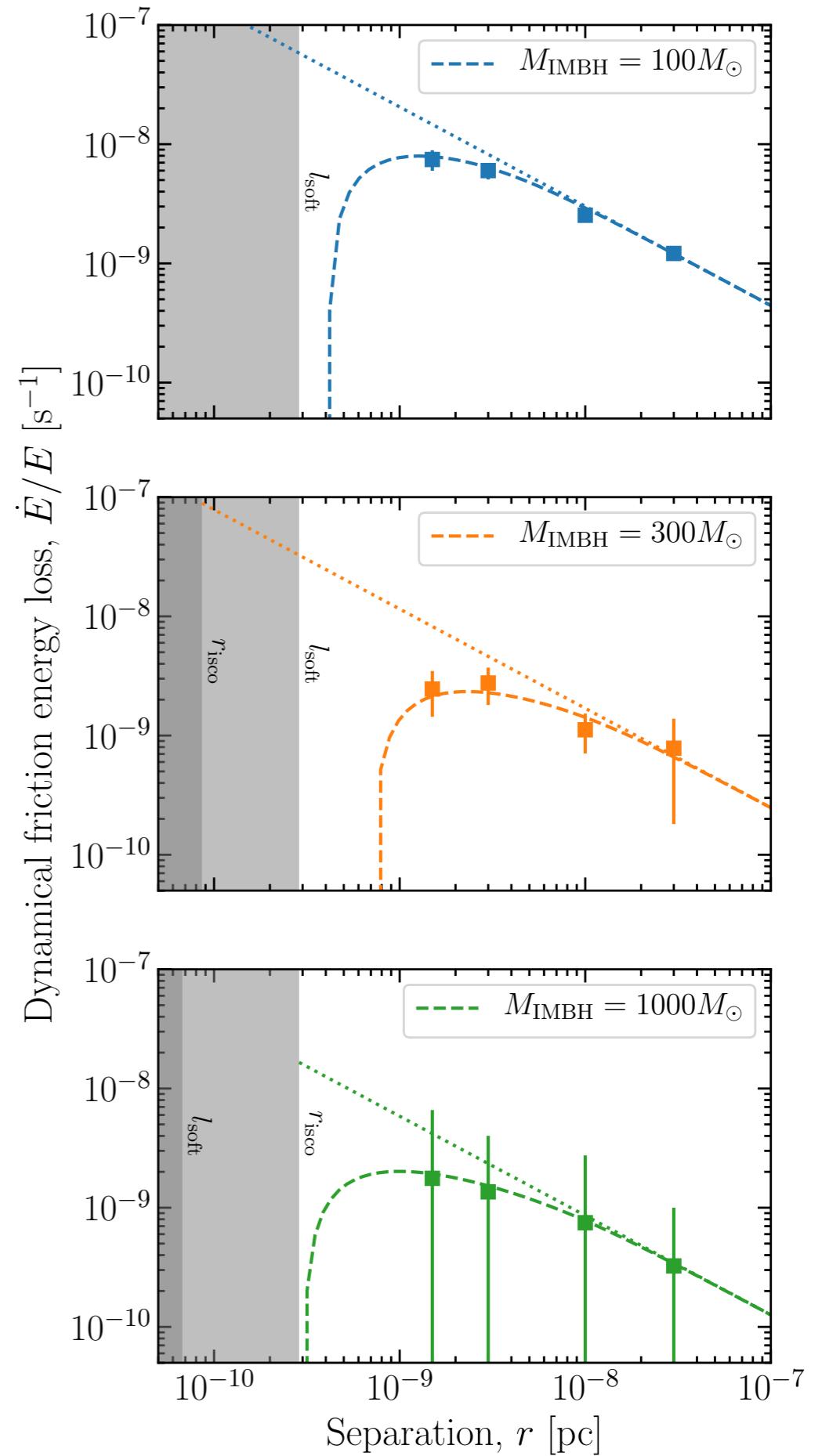
Backup Slides

N-body results

Dependence of dynamical friction force on mass and separation matches expectations

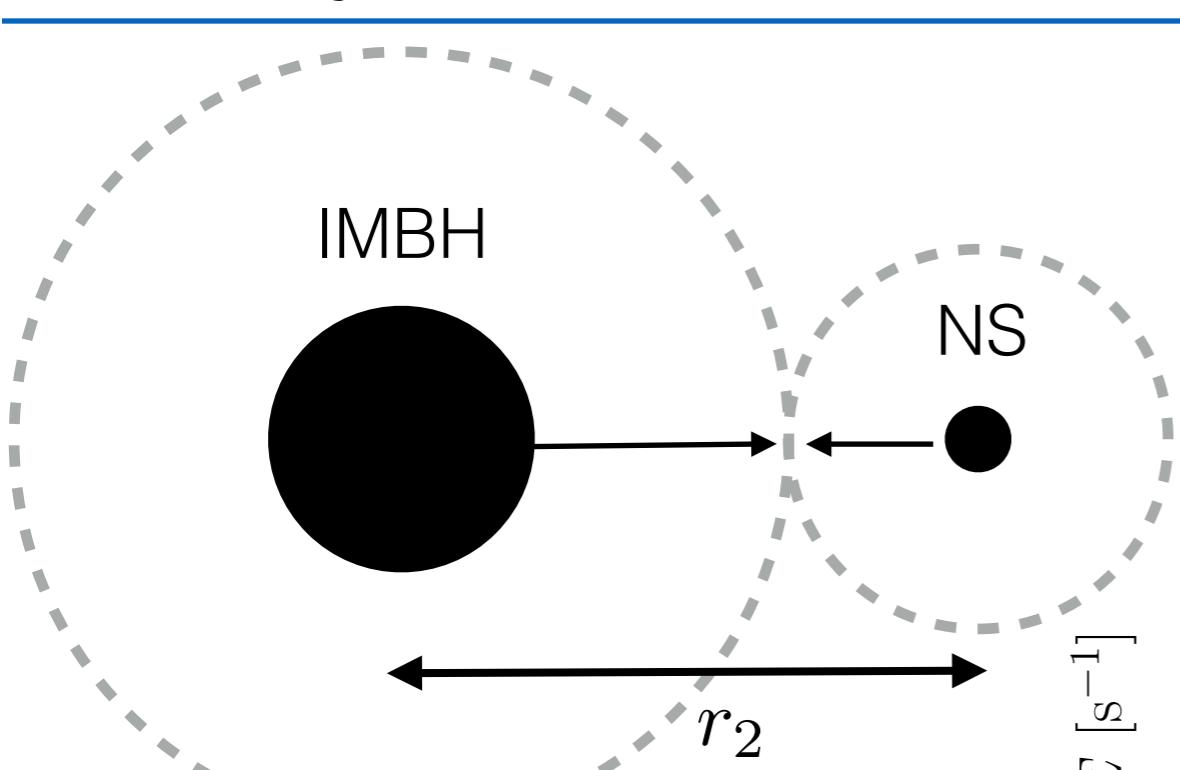
Dynamical friction traces local DM density (to better than 1%)

Drop off in DF force at small separations due to softening of simulations



N-body results

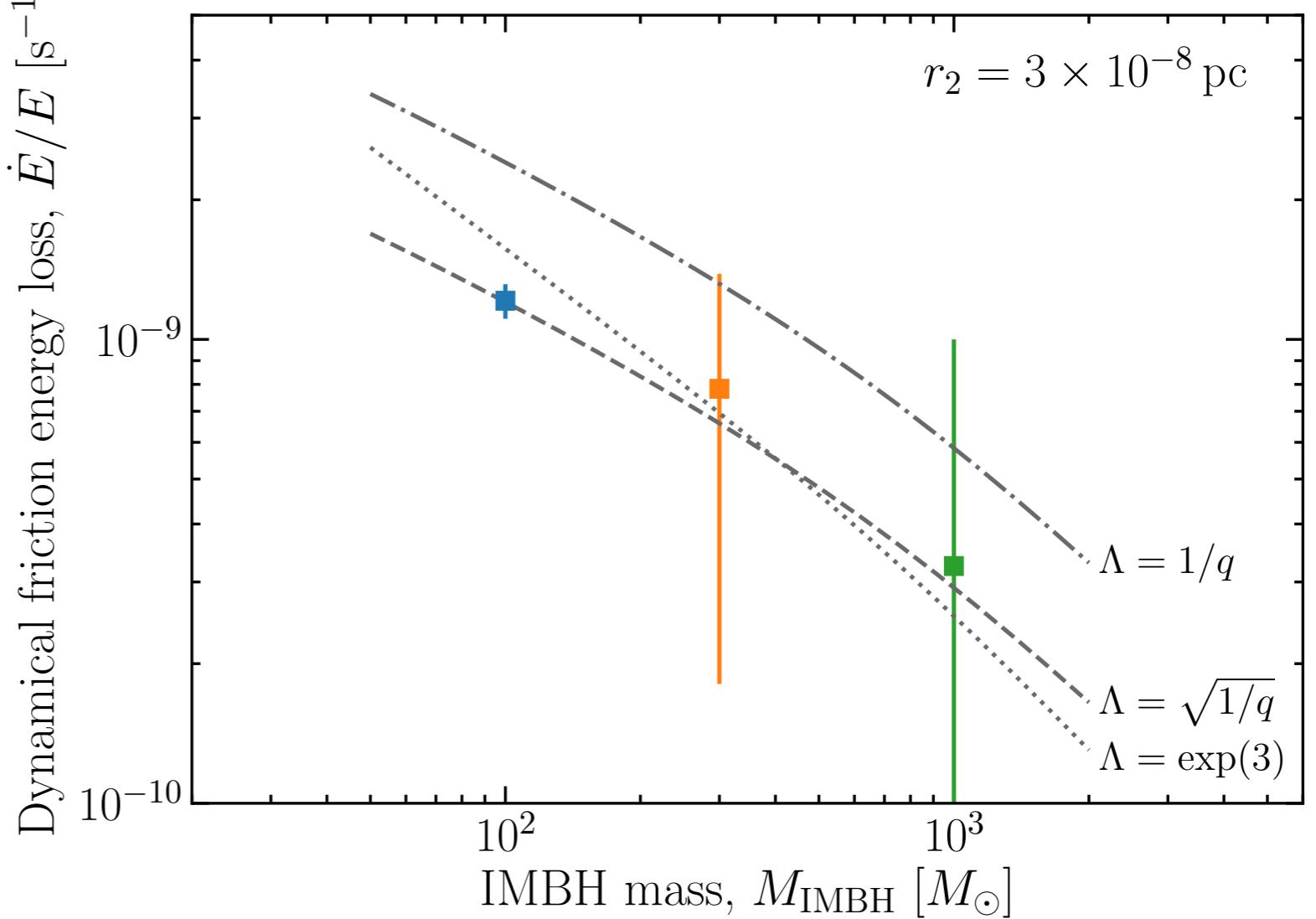
$$q \equiv m_{\text{NS}}/m_{\text{IMBH}} \ll 1$$



$$\begin{aligned}\Lambda &= b_{\max} \frac{v_0^2}{G m_{\text{NS}}} \\ &= \frac{b_{\max}}{q r_2} \\ &= 1/\sqrt{q}\end{aligned}$$

Allows us to calibrate the maximum impact parameter; tells us which particles scatter with the NS.

$$b_{\max} = \sqrt{q} r_2 \sim 3\% r_2$$



Assumptions

- Spherical symmetry and isotropy of the DM halo
- DM particles only scatter within an impact parameter

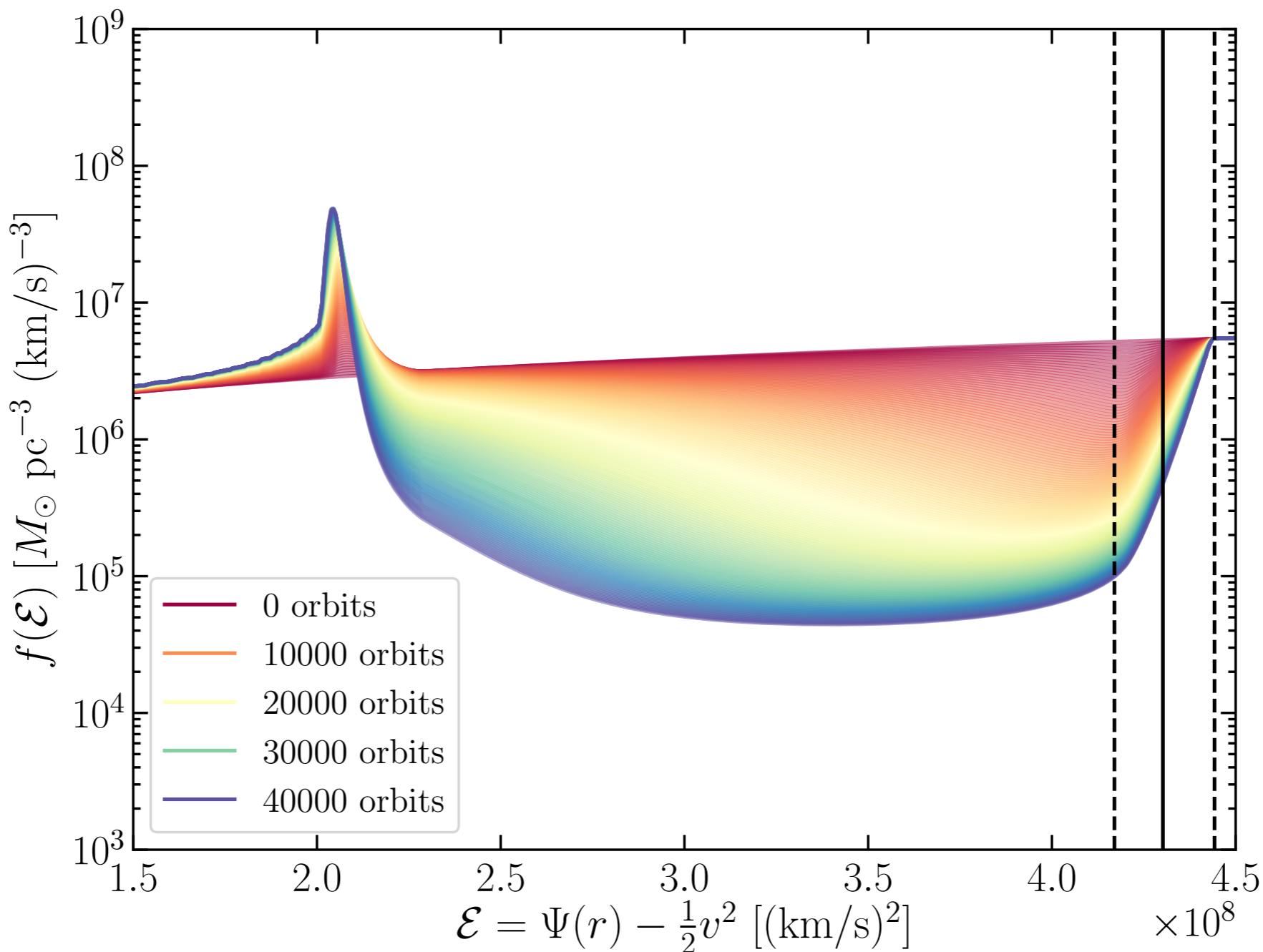
$$b < b_{\max} = \Lambda \times G_N M_{\text{NS}} / v_{\text{NS}}^2$$

- DM distribution is ‘locally’ uniform

$$b_{\max} \ll r_0$$

- Halo ‘relaxation’ is instantaneous
- Orbital properties evolve slowly compared to the orbital period

Distribution function



Self-consistently reconstruct density from distribution function:

$$\rho(r) = 4\pi \int_0^{v_{\max}(r)} v^2 f(\mathcal{E}) dv$$

Numbers of cycles

$$m_1 = 10^3 M_\odot, N_{\text{cycles}} = 5.71 \times 10^6 \text{ in vacuum}$$

	$\gamma_{\text{sp}} = 1.5$	$\gamma_{\text{sp}} = 2.2$	$\gamma_{\text{sp}} = 2.3$	$\gamma_{\text{sp}} = 2.\bar{3}$
Static	< 1	2.4×10^4	1.6×10^5	2.9×10^5
Dynamic	< 1	2.7×10^2	1.9×10^3	3.5×10^3

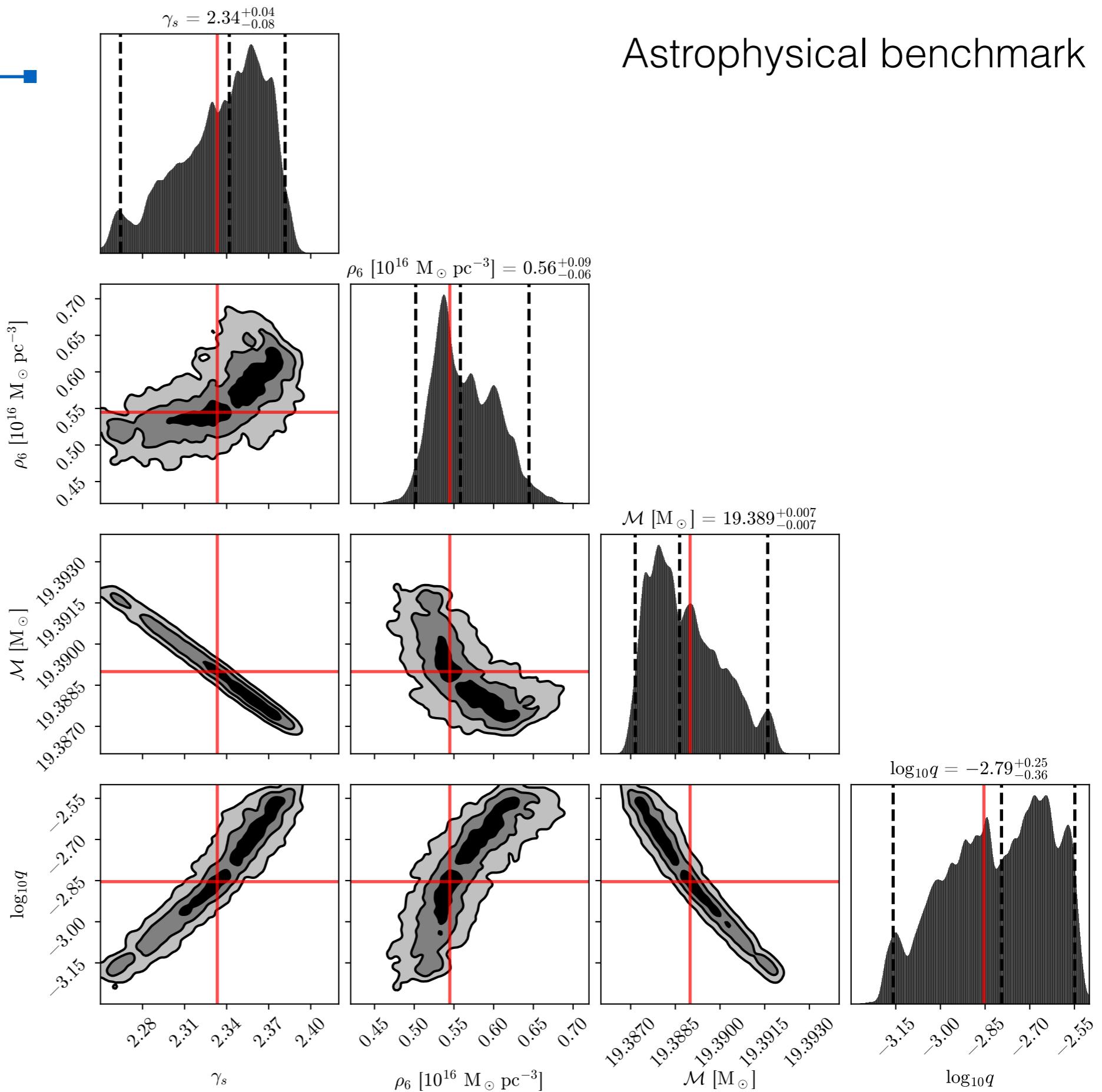
$$m_1 = 10^4 M_\odot, N_{\text{cycles}} = 3.20 \times 10^6 \text{ in vacuum}$$

	$\gamma_{\text{sp}} = 1.5$	$\gamma_{\text{sp}} = 2.2$	$\gamma_{\text{sp}} = 2.3$	$\gamma_{\text{sp}} = 2.\bar{3}$
Static	< 1	1.4×10^3	8.7×10^3	1.6×10^4
Dynamic	< 1	6.2×10^2	4.0×10^3	7.4×10^3

TABLE I. **Change in the number of cycles ΔN_{cycles} during the inspiral.** Change in the total number of GW cycles due to dynamical friction, starting 5 years from the merger.

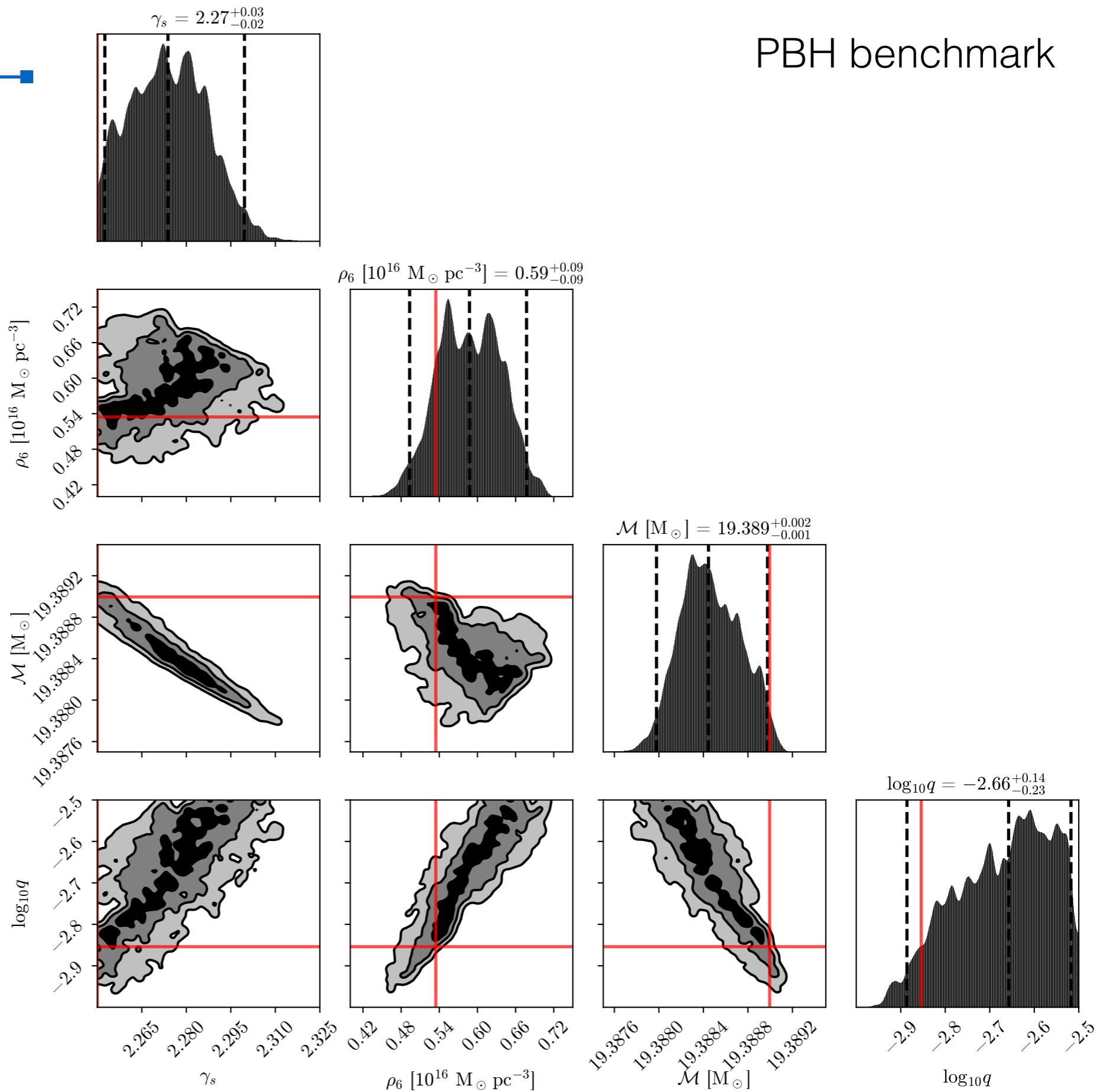
Measurability

Astrophysical benchmark



Measurability

PBH benchmark



Phase parametrisation

$$\hat{\Phi}(f) \equiv \Phi^V(f)$$

$$\times \left\{ 1 - \eta y^{-\lambda} \left[1 - {}_2 F_1 \left(1, \vartheta, 1 + \vartheta, -y^{-\frac{5}{3\vartheta}} \right) \right] \right\}$$

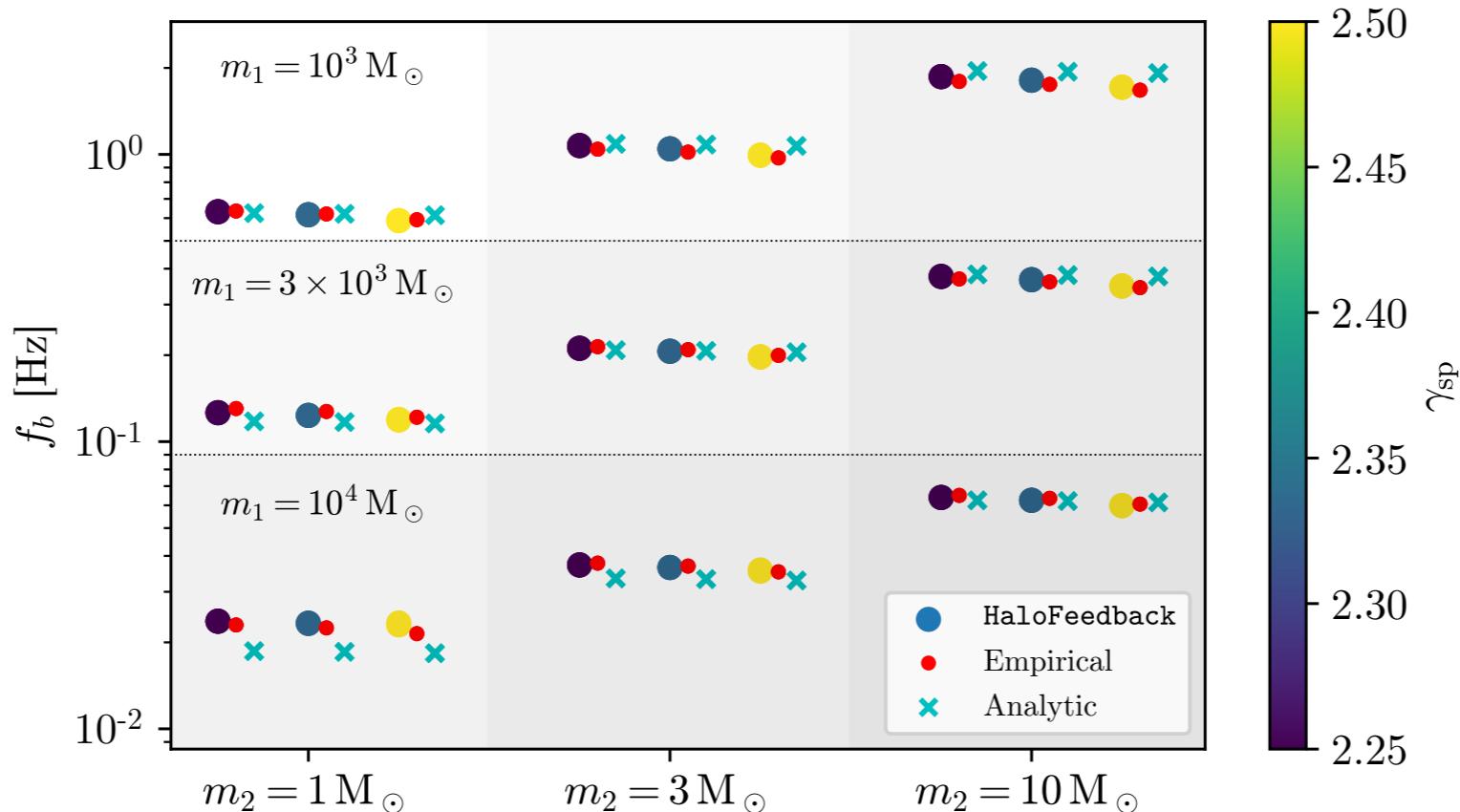
$$\vartheta = \frac{5}{2\gamma_e},$$

$$\lambda = \frac{11 - 2(\gamma_{\text{sp}} + \gamma_e)}{3},$$

$$\eta = \frac{5 + 2\gamma_e}{2(8 - \gamma_{\text{sp}})} \left(\frac{f_{\text{eq}}}{f_b} \right)^{\frac{11 - 2\gamma_{\text{sp}}}{3}}$$

$$f_b = \beta \left(\frac{m_1}{1000 M_\odot} \right)^{-\alpha_1} \left(\frac{m_2}{M_\odot} \right)^{\alpha_2} \left[1 + \zeta \log \frac{\gamma_{\text{sp}}}{\gamma_r} \right], \quad (35)$$

where $\alpha_1 = 1.4412$, $\alpha_2 = 0.4511$, $\beta = 0.8163 \text{ Hz}$, $\zeta = -0.4971$ and $\gamma_r = 1.4396$.



Axions and neutron stars

Produce a photon with axion energy $m_a \sim 10^{-6} \text{ eV} \sim 240 \text{ MHz}$



Conversion happens at a radius r_c , with probability: $p_{a\gamma} \propto \frac{g_{a\gamma\gamma}^2 B(r_c)^2}{2v_c}$

Radiated power is given by: $\frac{d\mathcal{P}}{d\Omega} \sim 2 \times p_{a\gamma} \rho_{\text{DM}}(r_c) v_c r_c^2$

Probe axions in the mass range

$$m_a \sim 10^{-7} \text{ eV} \quad \text{up to} \quad m_a \sim 10^{-5} \text{ eV}$$

Frequency range of
radio telescopes

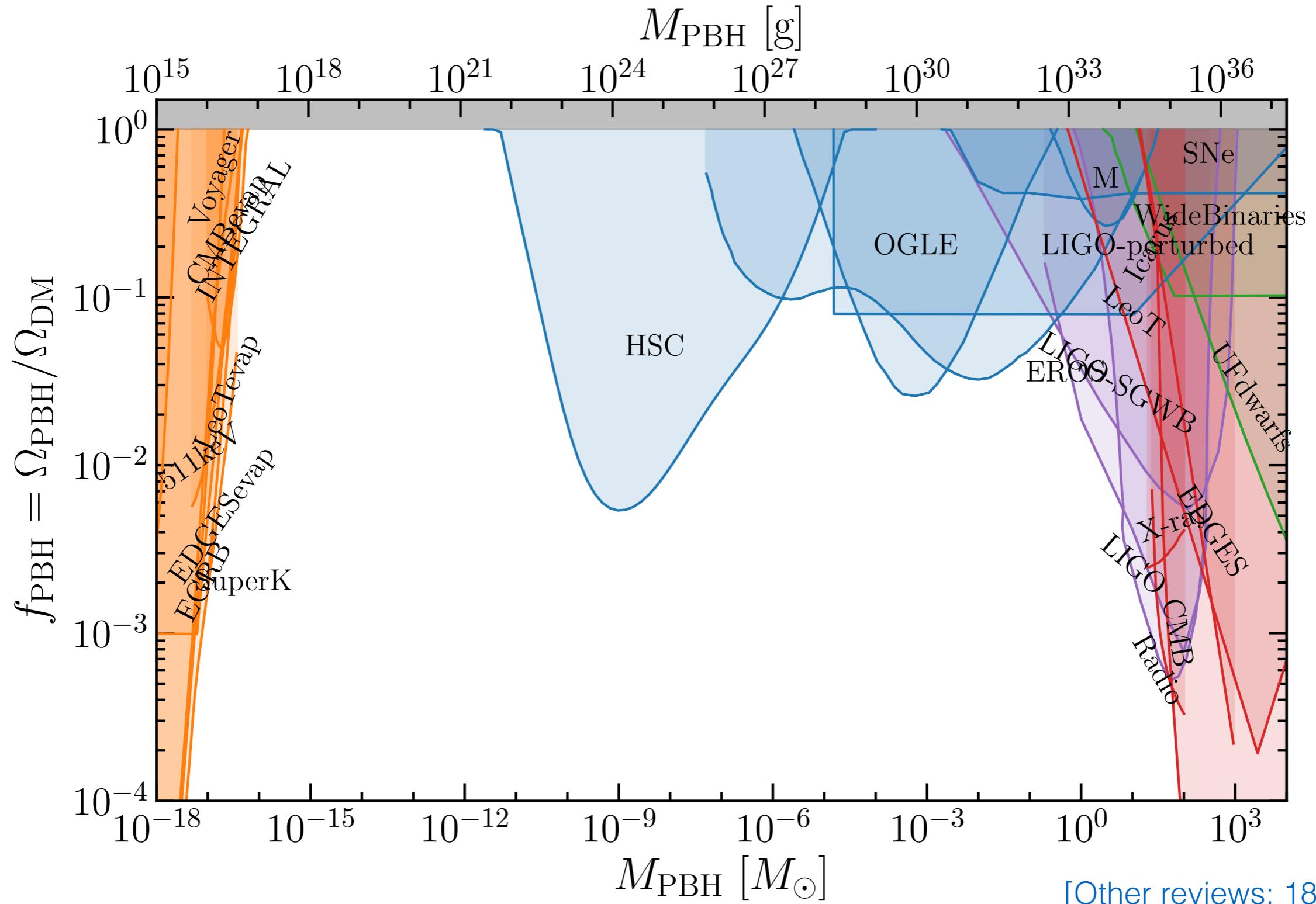
Require conversion
outside NS

[\[1803.08230\]](#), [\[1804.03145\]](#), [\[1811.01020\]](#), [\[1910.11907\]](#)

PBH Constraints

[Green & BJK, 2007.10722]

[Code online: github.com/bradkav/PBHbounds]

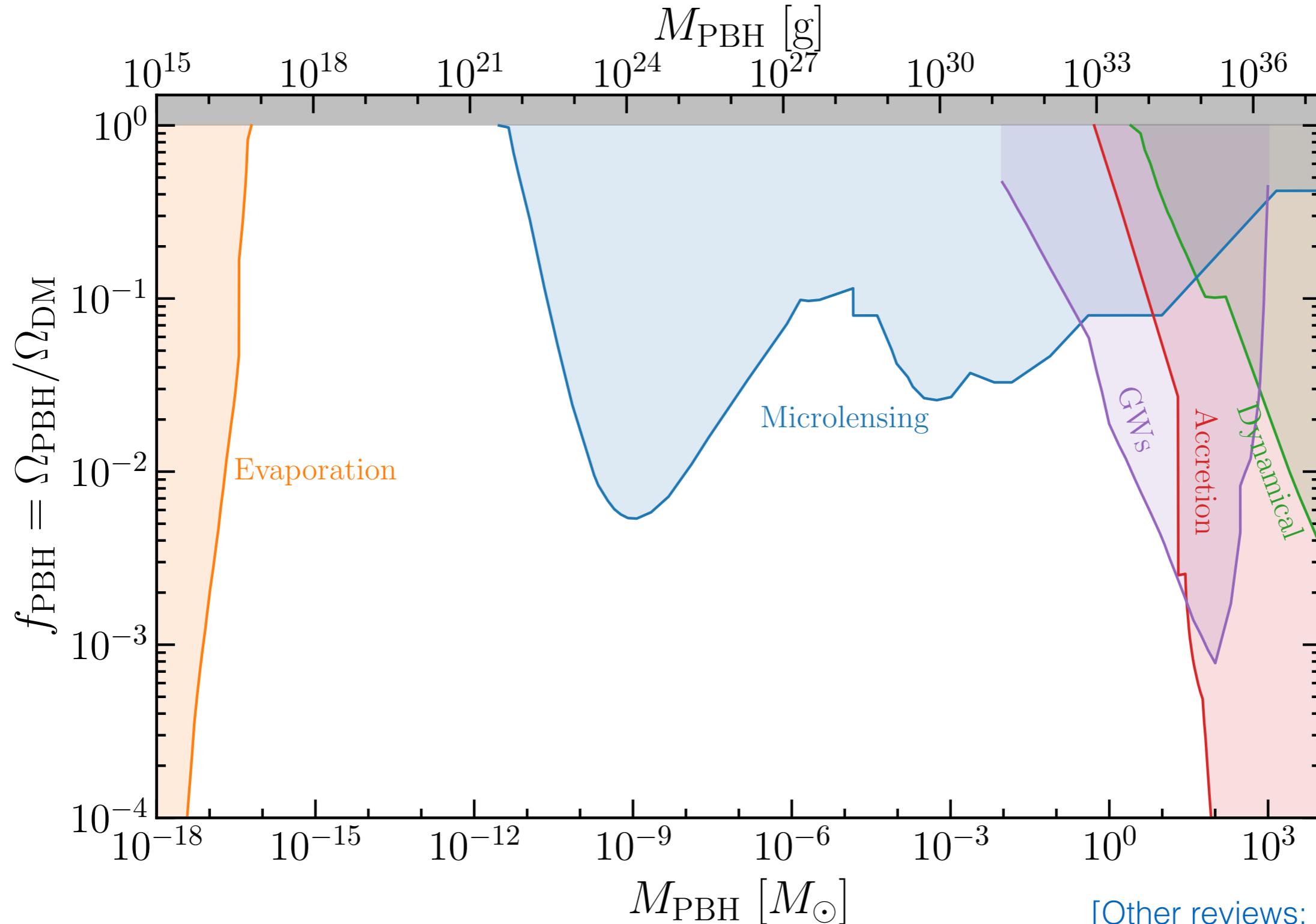


[Other reviews: [1801.05235](#),
[2002.12778](#), [2006.02838](#)]

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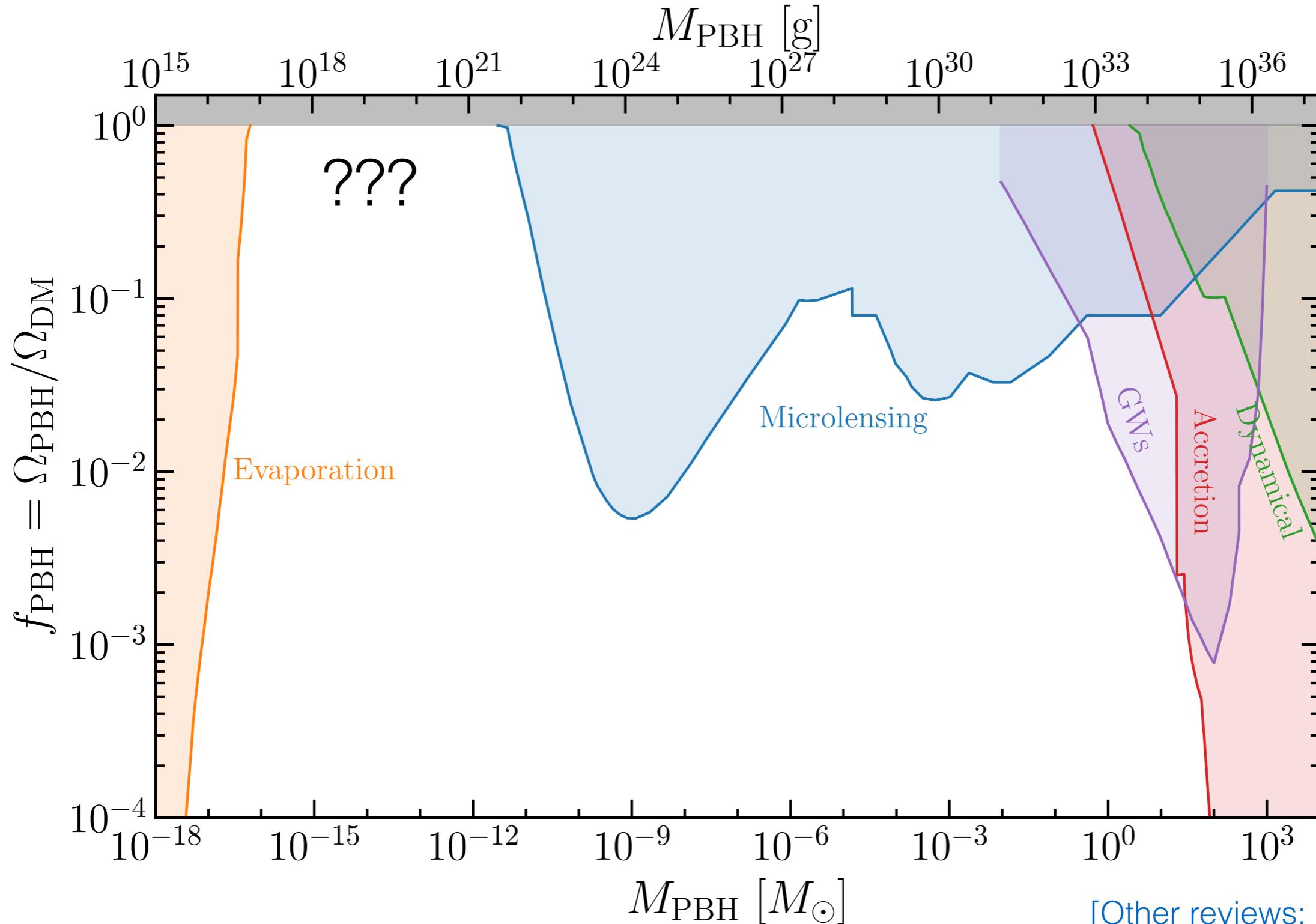


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