

# Distinguishing WIMP-nucleon interactions with directional dark matter experiments

Bradley J. Kavanagh  
(LPTHE - Paris 06 & IPhT - CEA/Saclay)

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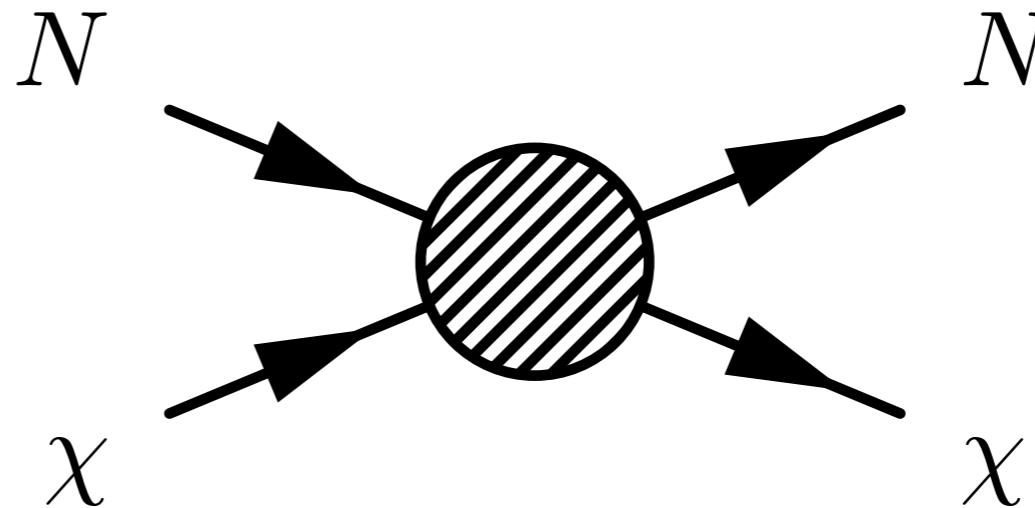
Based on arXiv:1505.07406

# Possible WIMP-nucleon operators

Direct detection:

$$m_\chi \gtrsim 1 \text{ GeV}$$

$$v \sim 10^{-3}$$



$$q \lesssim 100 \text{ MeV} \sim (2 \text{ fm})^{-1}$$

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Relevant non-relativistic (NR) degrees of freedom:

$$\vec{S}_\chi$$

$$\vec{S}_N$$

$$\frac{\vec{q}}{2m_N}$$

$$\vec{v}_\perp = \vec{v} + \frac{\vec{q}}{2\mu_{\chi N}}$$

# Non-relativistic effective field theory (NREFT)

Require Hermitian, Galilean invariant and time-translation invariant combinations:

$$\begin{array}{l} \text{SI} \rightarrow \boxed{\mathcal{O}_1 = 1} \\ \text{SD} \rightarrow \boxed{\mathcal{O}_4 = \vec{S}_\chi \cdot \vec{S}_N} \end{array}$$

[1008.1591, 1203.3542, 1308.6288, 1505.03117]

# Non-relativistic effective field theory (NREFT)

Require Hermitian, Galilean invariant and time-translation invariant combinations:

SI

$$\mathcal{O}_1 = 1$$

$$\mathcal{O}_3 = i\vec{S}_N \cdot (\vec{q} \times \vec{v}^\perp) / m_N$$

$$\mathcal{O}_4 = \vec{S}_\chi \cdot \vec{S}_N$$

SD

$$\mathcal{O}_5 = i\vec{S}_\chi \cdot (\vec{q} \times \vec{v}^\perp) / m_N$$

$$\mathcal{O}_6 = (\vec{S}_\chi \cdot \vec{q})(\vec{S}_N \cdot \vec{q}) / m_N^2$$

$$\mathcal{O}_7 = \vec{S}_N \cdot \vec{v}^\perp$$

$$\mathcal{O}_8 = \vec{S}_\chi \cdot \vec{v}^\perp$$

$$\mathcal{O}_9 = i\vec{S}_\chi \cdot (\vec{S}_N \times \vec{q}) / m_N$$

$$\mathcal{O}_{10} = i\vec{S}_N \cdot \vec{q} / m_N$$

$$\mathcal{O}_{11} = i\vec{S}_\chi \cdot \vec{q} / m_N$$

$$\mathcal{O}_{12} = \vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}^\perp)$$

$$\mathcal{O}_{13} = i(\vec{S}_\chi \cdot \vec{v}^\perp)(\vec{S}_N \cdot \vec{q}) / m_N$$

$$\mathcal{O}_{14} = i(\vec{S}_\chi \cdot \vec{q})(\vec{S}_N \cdot \vec{v}^\perp) / m_N$$

$$\mathcal{O}_{15} = -(\vec{S}_\chi \cdot \vec{q})((\vec{S}_N \times \vec{v}^\perp) \cdot \vec{q}) / m_N^2$$

⋮

[1008.1591, 1203.3542, 1308.6288, 1505.03117]

# Calculating the cross section

'Dictionaries' are available which allow us to translate from relativistic interactions to NREFT operators:

[e.g. 1211.2818, 1307.5955, 1505.03117]

$$\text{E.g. } \bar{\chi}\gamma^\mu\chi\bar{N}\gamma_\mu\gamma^5N \longrightarrow 8m_N(m_N\mathcal{O}_9 - m_\chi\mathcal{O}_7)$$

Then calculating the scattering cross section is straightforward:

$$\frac{d\sigma_i}{dE_R} = \frac{1}{32\pi} \frac{m_A}{m_\chi^2 m_N^2} \frac{1}{v^2} \sum_{N,N'=p,n} c_i^N c_i^{N'} F_i^{(N,N')}(v_\perp^2, q^2)$$

Nuclear response functions:  $F_i(v_\perp^2, q^2)$

*So how can we distinguish these different cross sections?*

# Distinguishing operators: approaches

- *Materials signal* - compare rates obtained in different experiments [1405.2637, 1406.0524, 1504.06554, 1506.04454]
  - ↳ May require a large number of experiments
- *Annual modulation* - due to different  $v$ -dependence annual modulation rate and phase can be different [1504.06772]
  - ↳ Annual modulation is a small effect
- *Energy spectrum* - look for an energy spectrum which differs from the standard SI case in a single experiment [1503.03379]

# Distinguishing operators: Energy-only

Consider three different operators:  $\mathcal{O}_1$ ,  $\mathcal{O}_5$ ,  $\mathcal{O}_7$

SI operator  $F_1 \sim q^0 v^0$

'Non-standard' operators

$F_5 \sim q^2(v_\perp^2 + q^2)$

$F_7 \sim v_\perp^2$

Generate mock data assuming either  $\mathcal{O}_5$  or  $\mathcal{O}_7$ .

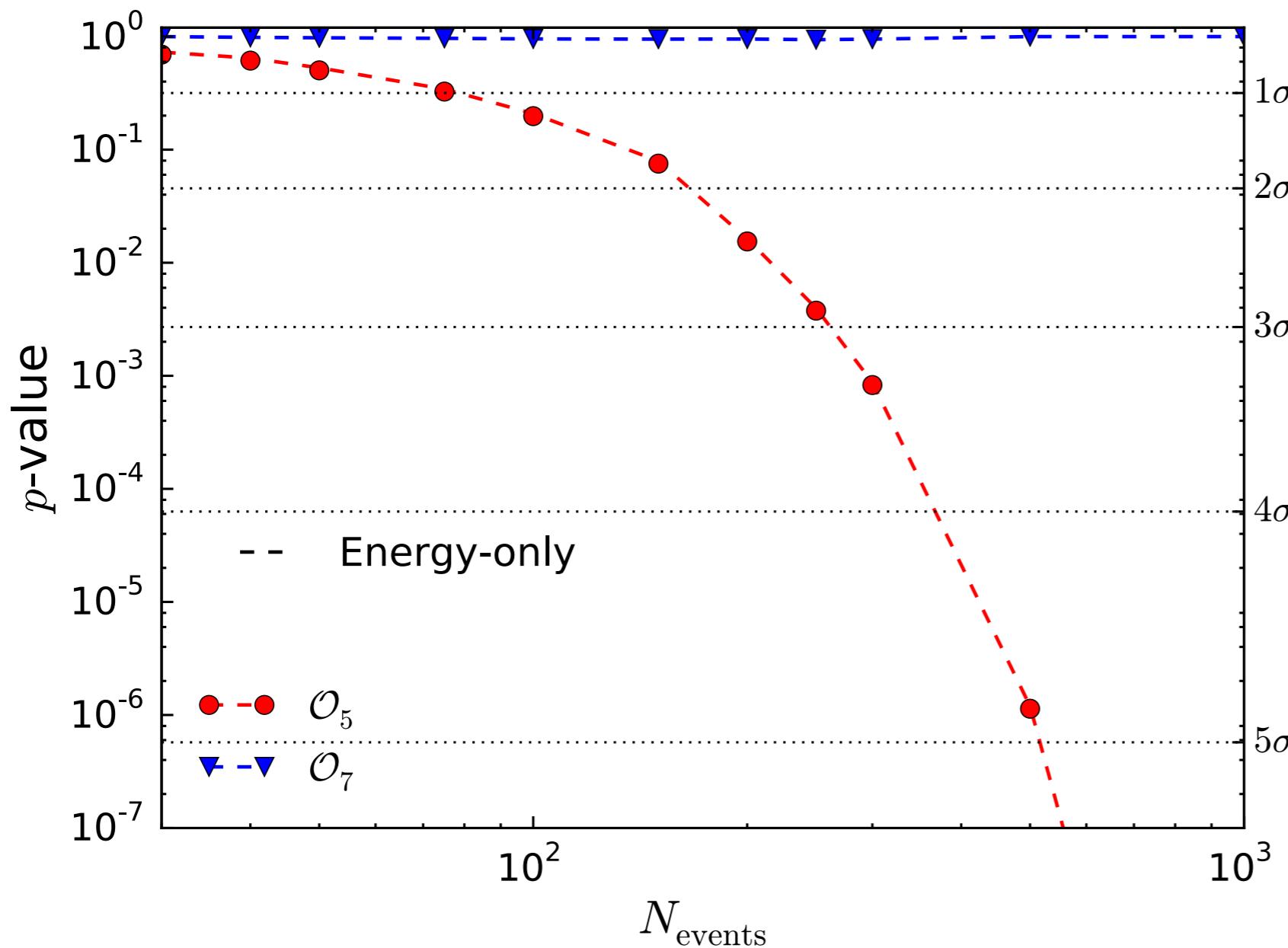
Assume the data is a mixture of events due to  $\mathcal{O}_1$  and the 'non-standard' operator (either  $\mathcal{O}_5$  or  $\mathcal{O}_7$ ).

Fit values of  $m_\chi$  and  $A$ , fraction of events due to 'non-standard' interactions.

*With what significance can we reject the SI-only scenario?*

# Distinguishing operators: Energy-only

With what significance can we reject ‘standard’ SI/SD interactions in 95% of experiments?



‘Perfect’ CF<sub>4</sub> detector

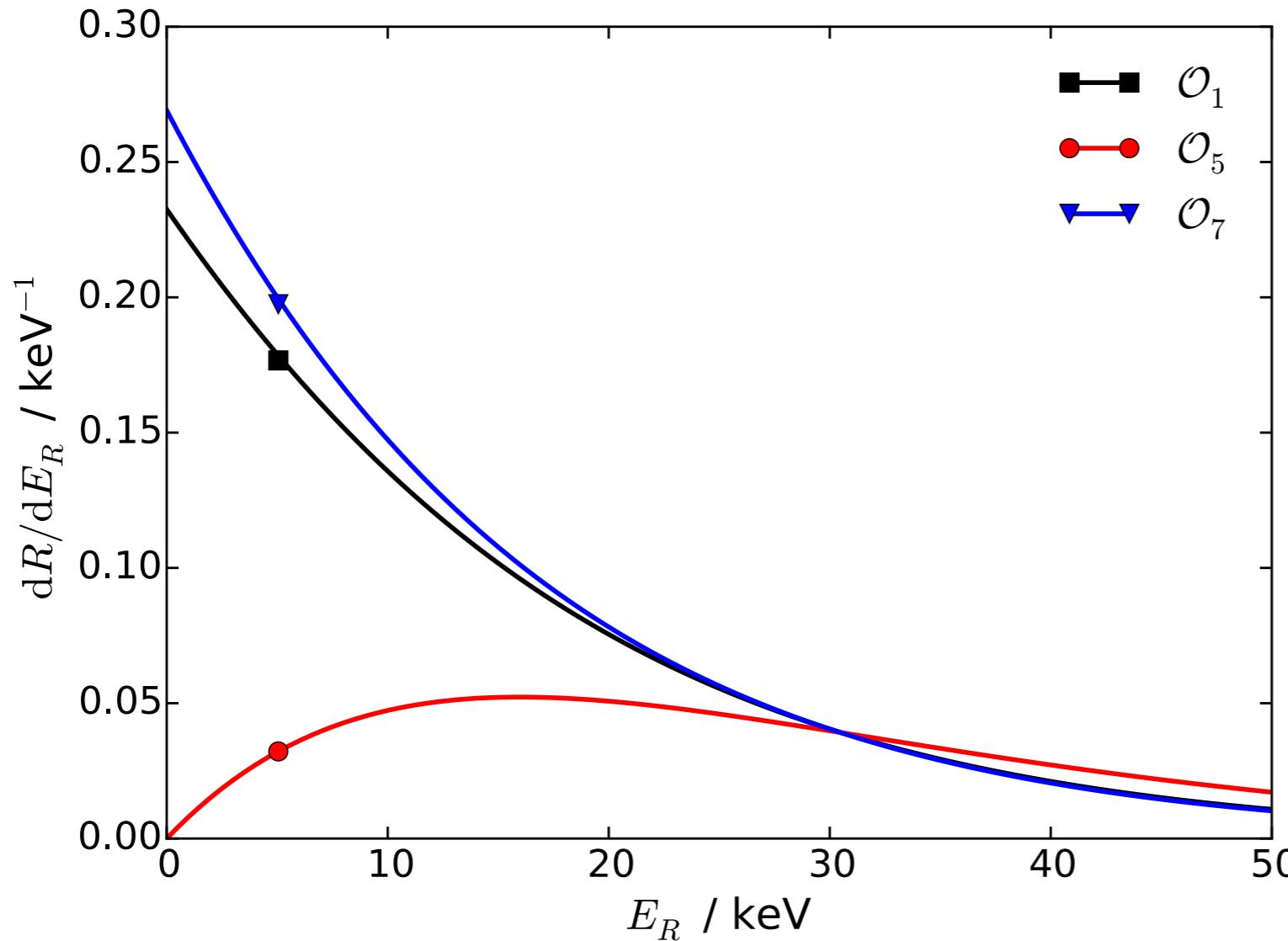
$E_R \in [20, 50]$  keV

Input WIMP mass:  
 $m_\chi = 50$  GeV

SHM velocity distribution

$$\begin{aligned} F_1 &\sim q^0 v^0 \\ F_5 &\sim q^2 (v_\perp^2 + q^2) \\ F_7 &\sim v_\perp^2 \end{aligned}$$

# Comparing energy spectra



$$F_1 \sim q^0 v^0$$
$$F_5 \sim q^2 (v_\perp^2 + q^2)$$
$$F_7 \sim v_\perp^2$$

Energy spectrum differences between  $\mathcal{O}_1$  and  $\mathcal{O}_7$  are smoothed out once we integrate over (smooth) DM velocity distribution.

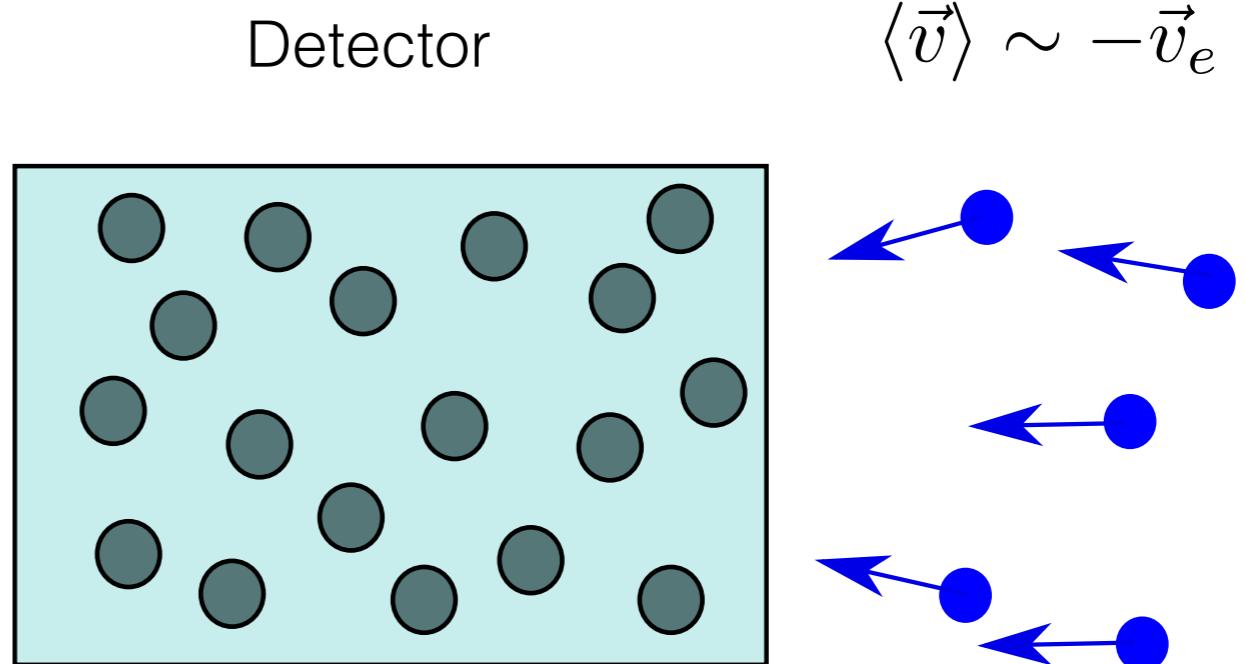
*True of any operators whose cross-sections differ only by  $v_\perp^2$ .*

# Directional detection

Different  $v$ -dependence could impact *directional* signal.

Mean recoil direction is parallel to incoming WIMP direction (due to Earth's motion).

$$\langle \vec{q} \rangle$$

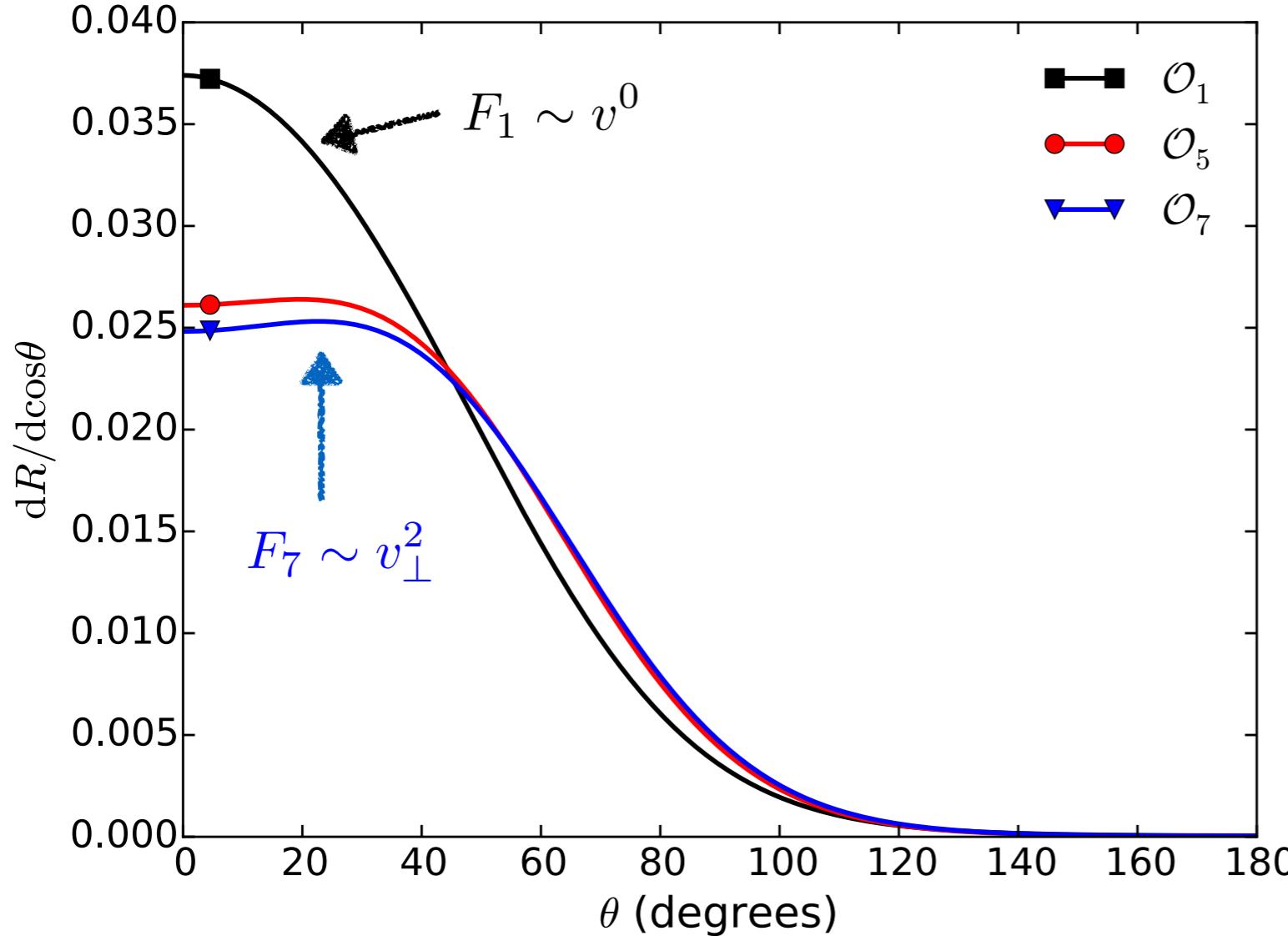


Convolve cross section with velocity distribution to obtain directional spectrum, as a function of  $\theta$ , the angle between the recoil and the peak direction.

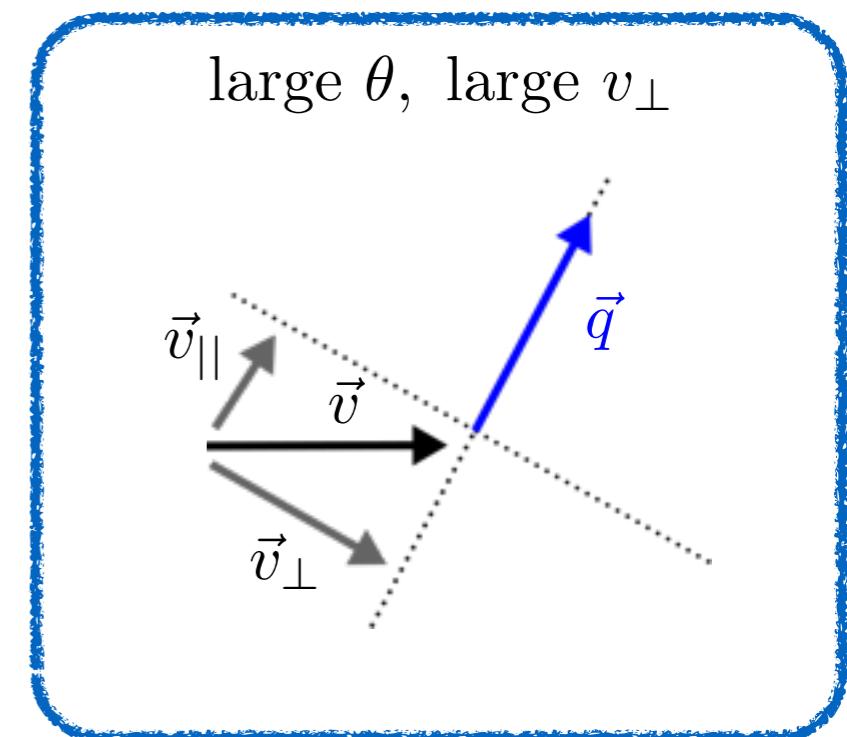
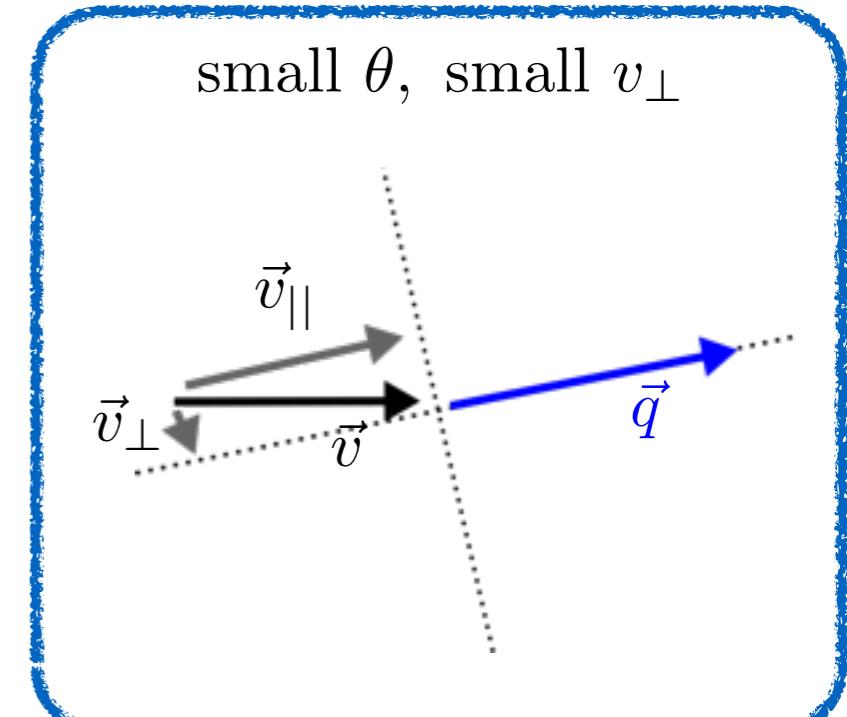
*So, what does the directional spectrum look like?*

# Directional spectra of NREFT operators

Total distribution of recoils as a function of  $\theta$ :

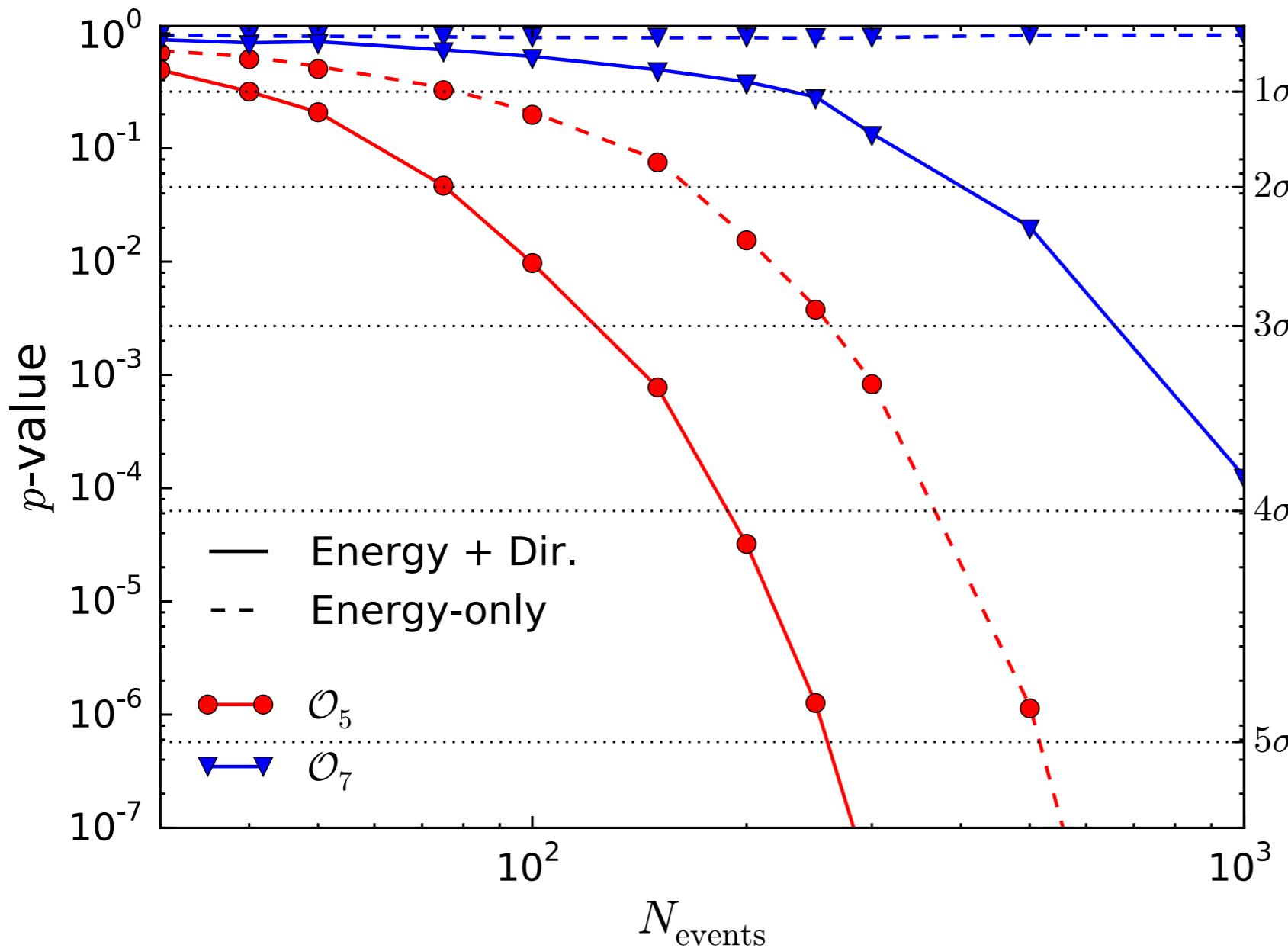


Spectra of all operators given in  
[1505.07406, 1505.06441].



# Distinguishing operators: Energy + Directionality

With what significance can we reject ‘standard’ SI/SD interactions in 95% of experiments?



‘Perfect’ CF<sub>4</sub> detector

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Input WIMP mass:  
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SHM velocity distribution

$$\begin{aligned} F_1 &\sim q^0 v^0 \\ F_5 &\sim q^2 (v_\perp^2 + q^2) \\ F_7 &\sim v_\perp^2 \end{aligned}$$

# Summary: a final example

NREFT framework allows us to compare the different possible direct detection signals.

Some operators can be distinguished in a single experiment from their energy spectra alone (e.g. if the form factor goes as  $F \sim q^n$ )

*But*, this is not true for all operators. Consider:

$$\mathcal{L}_1 = \bar{\chi}\chi\bar{N}N \longrightarrow F \sim v^0$$

$$\mathcal{L}_6 = \bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}\gamma_\mu N \longrightarrow F \sim v_\perp^2$$

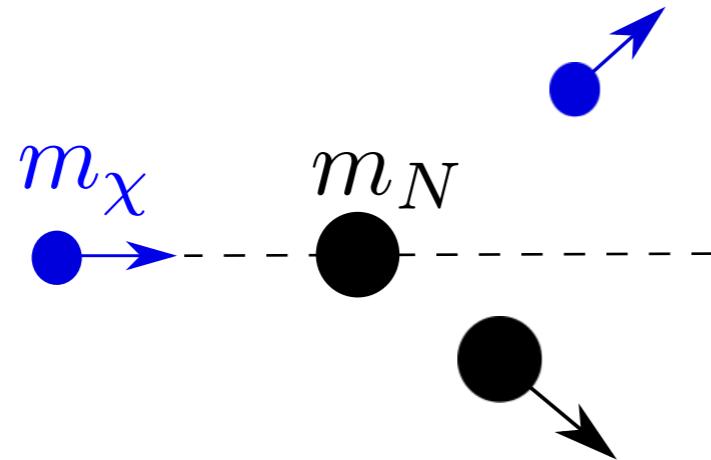
These operators cannot be distinguished in a single non-directional experiment.

*Directional detection will be powerful and crucial tool for determining how DM interacts with the Standard Model!*

# Backup Slides

# The Directional Spectrum

Recoil distribution for WIMP-nucleus recoils in direction  $\hat{q}$  with fixed WIMP speed  $\vec{v}$ :



$$\mu_{\chi N} = \frac{m_\chi m_N}{m_\chi + m_N}$$

$$v_{\min} = \sqrt{\frac{m_N E_R}{2 \mu_{\chi N}^2}}$$

$$\frac{dR}{dE_R d\Omega_q} = \frac{\rho_0 v}{m_\chi} \frac{\langle |\mathcal{M}|^2 \rangle}{32\pi m_N^2 m_\chi^2 v^2} \frac{v \delta(\vec{v} \cdot \hat{q} - v_{\min})}{2\pi}$$

↗ WIMP flux      ↑ Cross section      ↗ Kinematics

For standard SI and SD interactions:  $\langle |M|^2 \rangle \sim v^0 q^0$

# NREFT event rate

The matrix element for operator  $i$  can now be written as:

$$\langle |\mathcal{M}_i|^2 \rangle = |\langle c_i \mathcal{O}_i \rangle_{\text{nucleus}}|^2 = c_i^2 F_{i,i}(v_\perp^2, q^2)$$

[Assuming for now:  $c^p = c^n$  ]

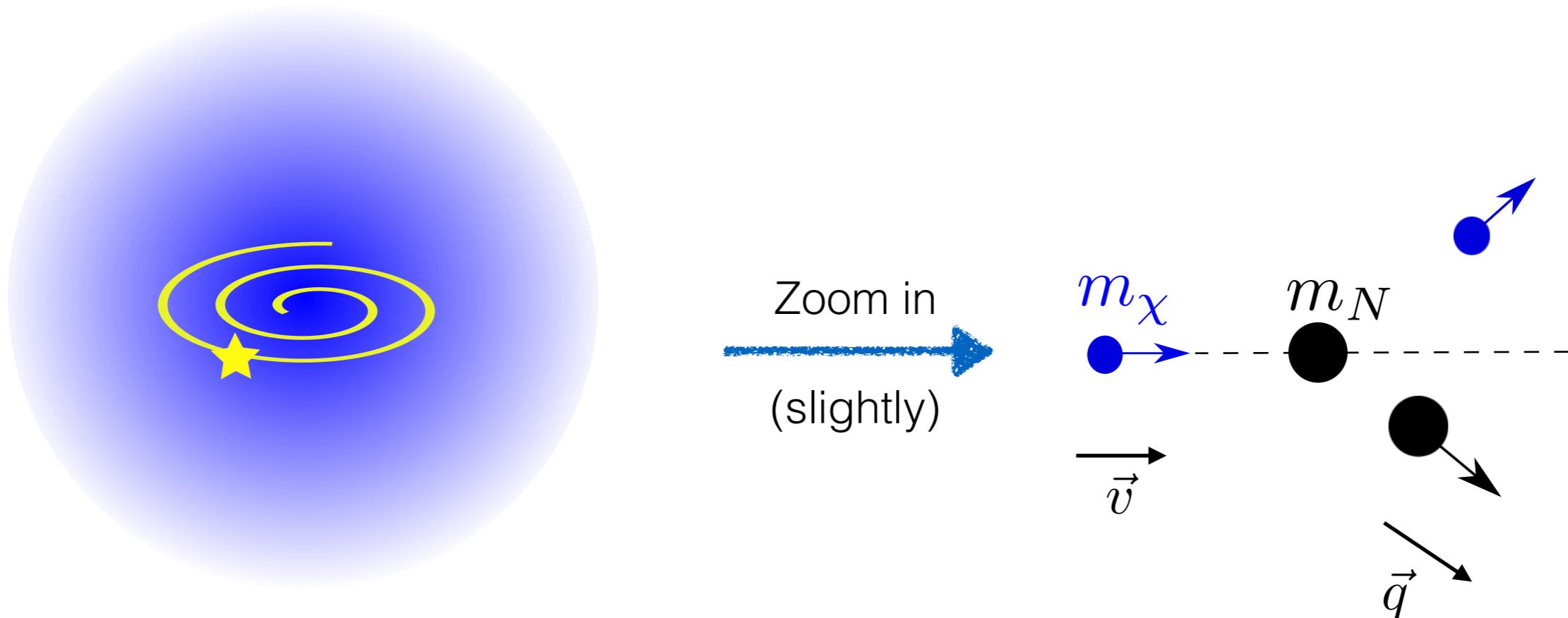
The nuclear response functions  $F_{i,i}(v_\perp^2, q^2)$  are the expectation values of the operators summed over all nucleons in the nucleus.

They are proportional to  $(v_\perp)^0$  or  $(v_\perp)^2$ .

$$\frac{dR_i}{dE_R d\Omega_q} = \frac{\rho_0}{64\pi^2 m_N^2 m_\chi^3} c_i^2 \int_{\mathbb{R}^3} F_{i,i}(v_\perp^2, q^2) f(\vec{v}) \delta(\vec{v} \cdot \hat{q} - v_{\min}) d^3 \vec{v}$$

Framework previously applied to non-directional direct detection and solar capture [[1211.2818](#), [1406.0524](#), [1503.03379](#), [1503.04109](#) and others].

# Direct detection

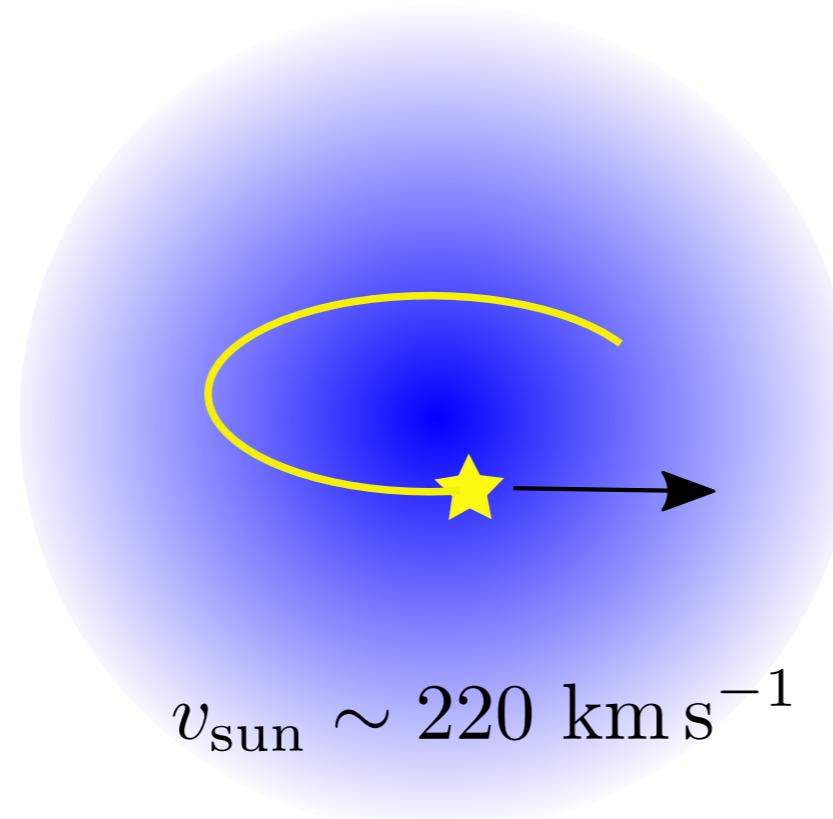


Look for interactions of DM particles from the halo with nuclei in a detector - measure **energy** of the recoiling nucleus.

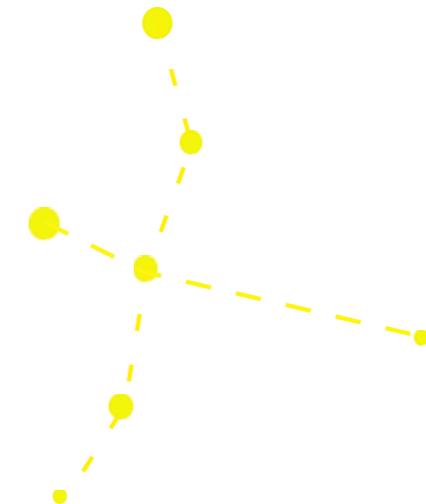
Expect lots of low energy backgrounds —> background discrimination can be...*problematic*...

# The WIMP Wind

In the halo:

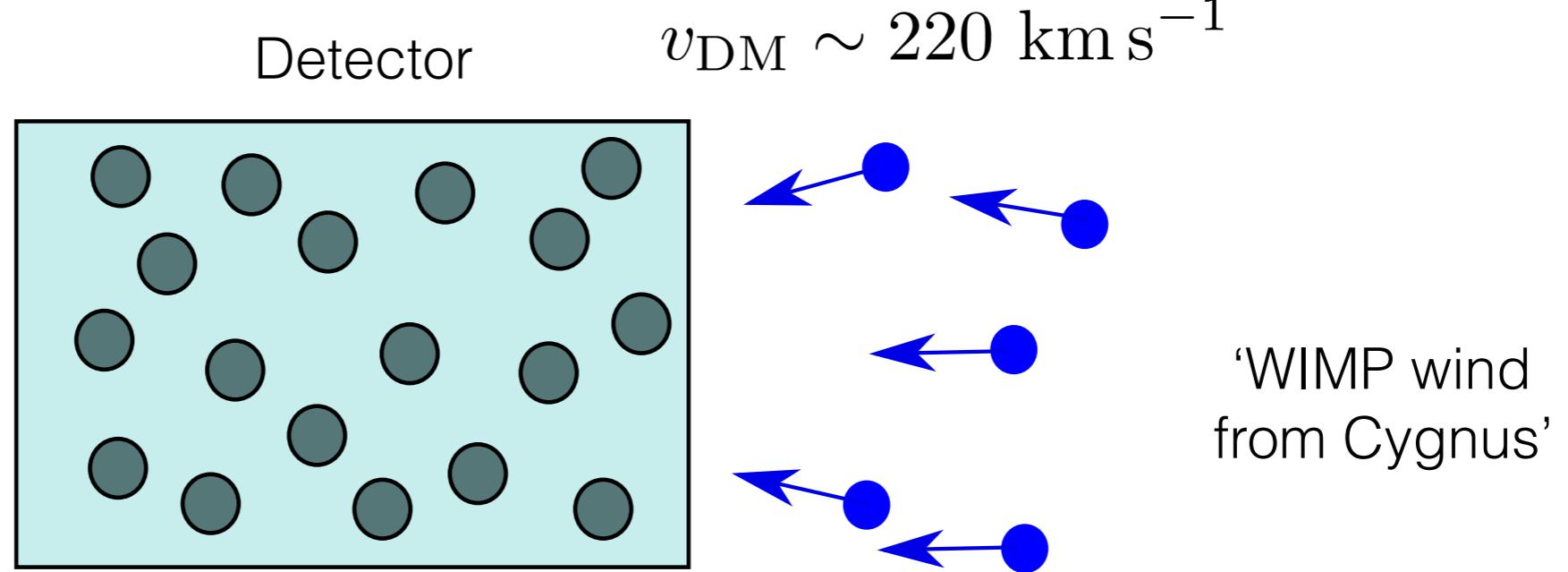


*WIMP*: Weakly Interacting  
Massive Particle



Cygnus constellation

In the lab:



# Radon Transform

For standard SI/SD, for fixed DM speed:

$$\frac{dR}{dE_R d\Omega_q} \propto \delta(\vec{v} \cdot \hat{q} - v_{\min})$$

So integrating over all DM speeds:

$$\frac{dR}{dE_R d\Omega_q} \propto \int_{\mathbb{R}^3} f(\vec{v}) \delta(\vec{v} \cdot \hat{q} - v_{\min}) d^3 \vec{v} \equiv \hat{f}(v_{\min}, \hat{q})$$

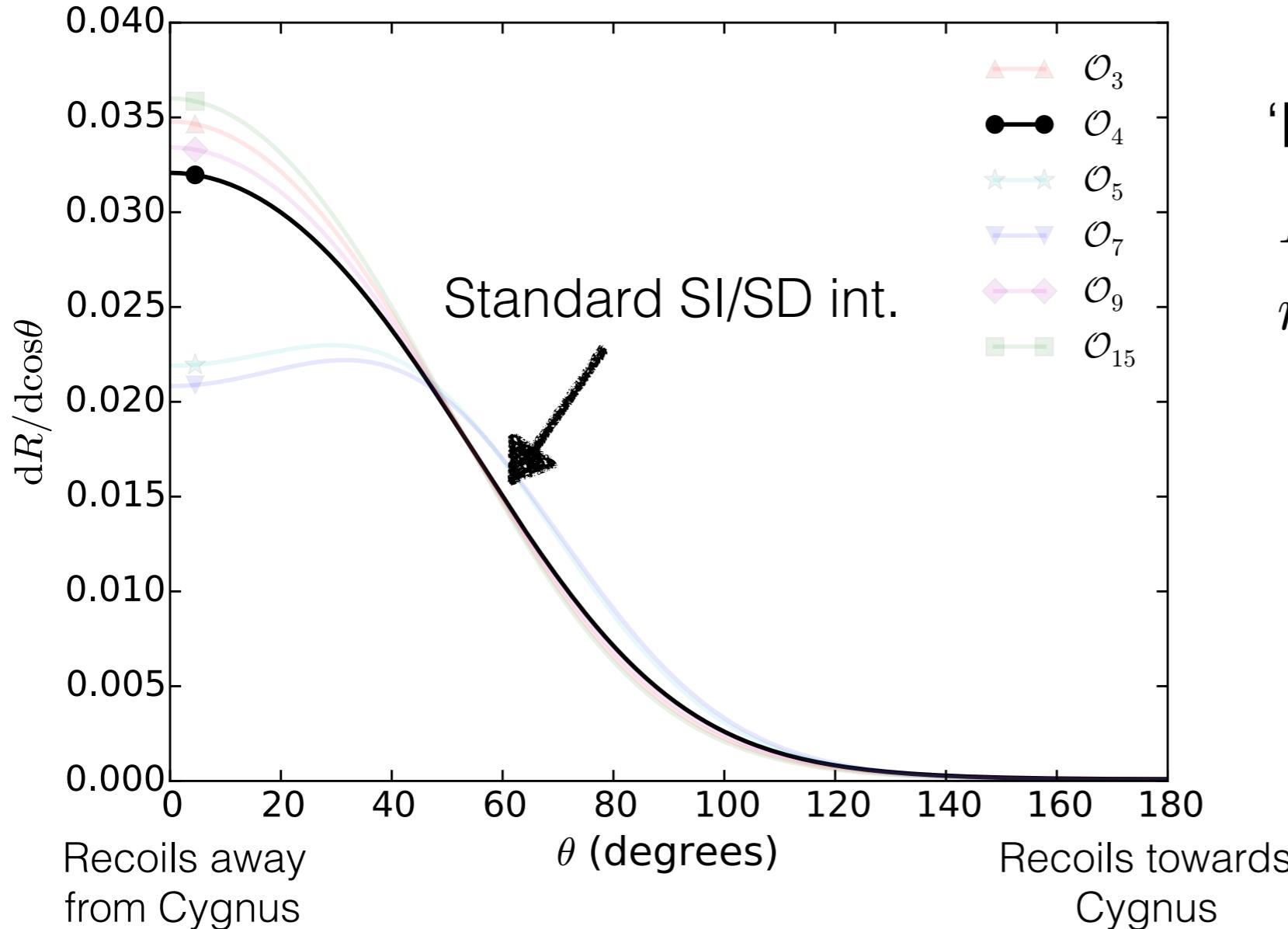
‘Radon Transform’ (RT)

For the SHM:

$$f(\vec{v}) = \frac{1}{(2\pi\sigma^2)^{3/2}} \exp\left[-\frac{(\vec{v} - \vec{v}_{\text{lag}})^2}{2\sigma_v^2}\right]$$

→  $\hat{f}(v_{\min}, \hat{q}) = \frac{1}{\sqrt{2\pi\sigma_v^2}} \exp\left[-\frac{(v_{\min} - \vec{v}_{\text{lag}} \cdot \hat{q})^2}{2\sigma_v^2}\right]$

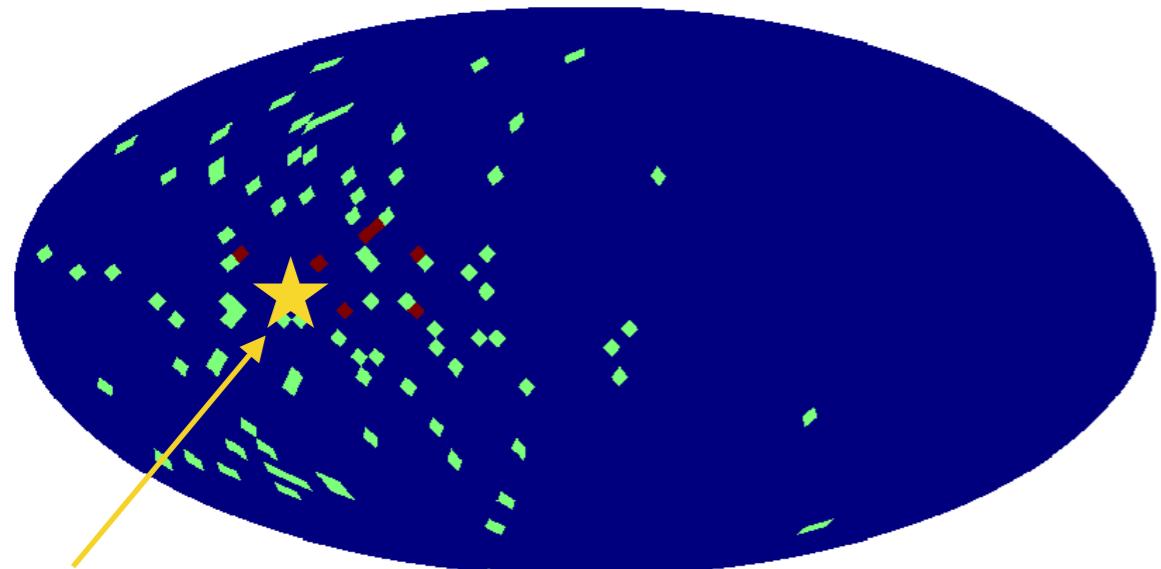
# Directional Spectra



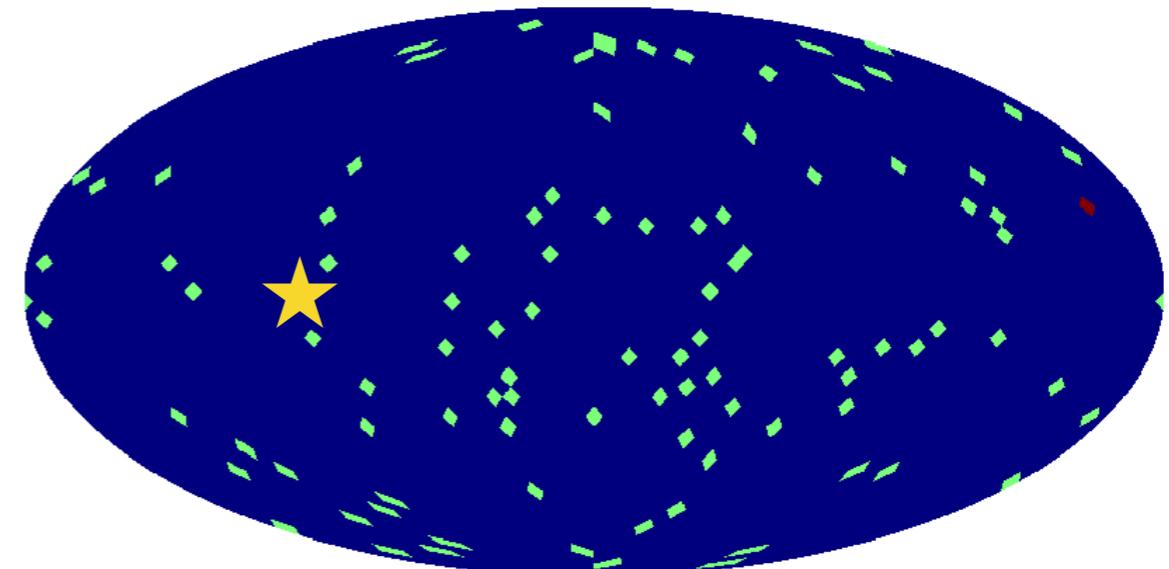
'Perfect'  $\text{CF}_4$  detector  
 $E_R \in [20, 50] \text{ keV}$   
 $m_\chi = 100 \text{ GeV}$

# The Smoking Gun

Aim to measure the **energy** and **direction** of the recoiling nucleus.



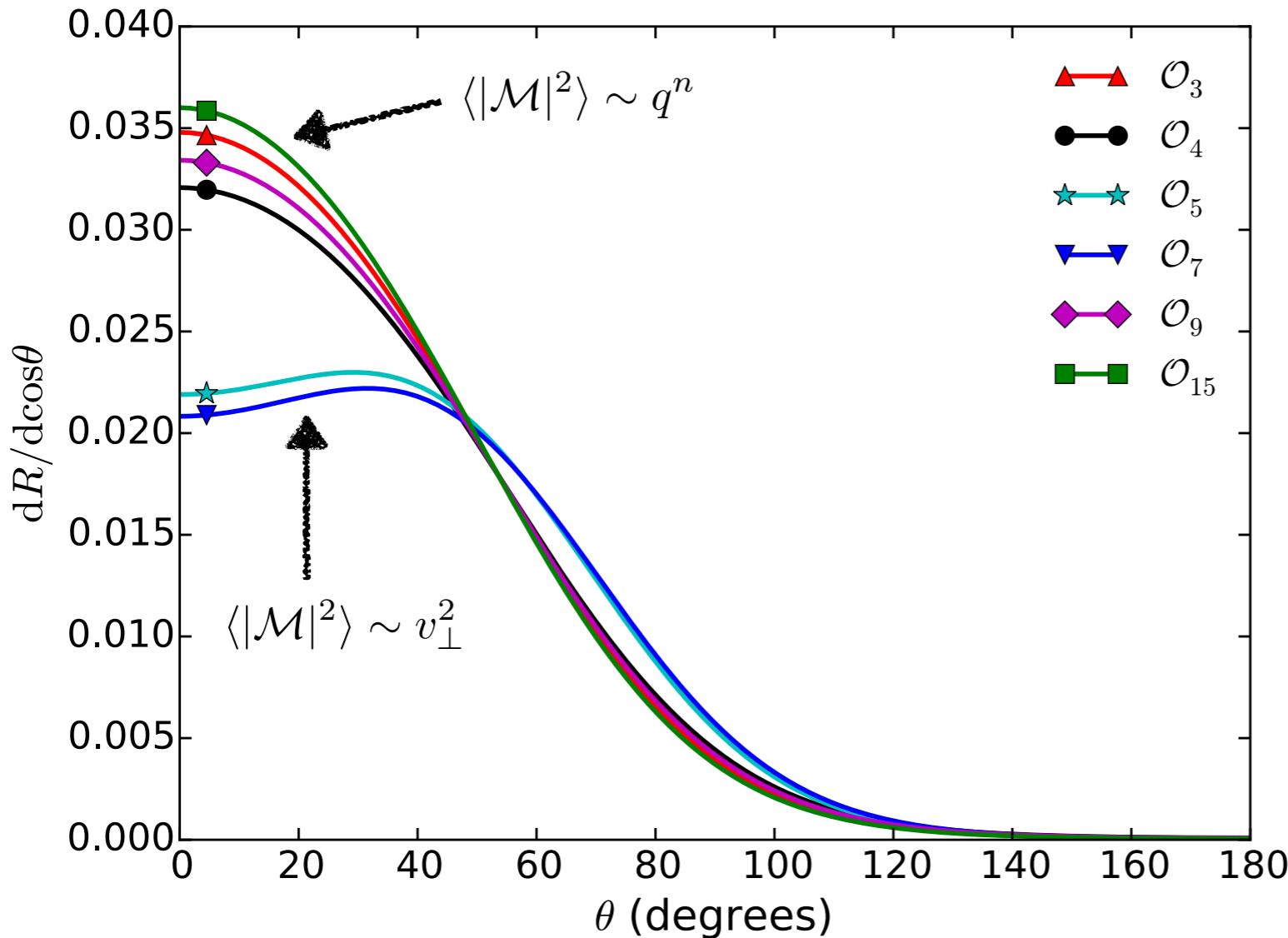
WIMP signal



Only need around 10 events to distinguish signal from background, and around 30 events to confirm the median direction of the flux [\[astro-ph/0408047, 1002.2717\]](#).

Can also exploit time-dependence of the signal due to the motion of the Earth around the Sun [\[1205.2333\]](#).

# Directional Spectra



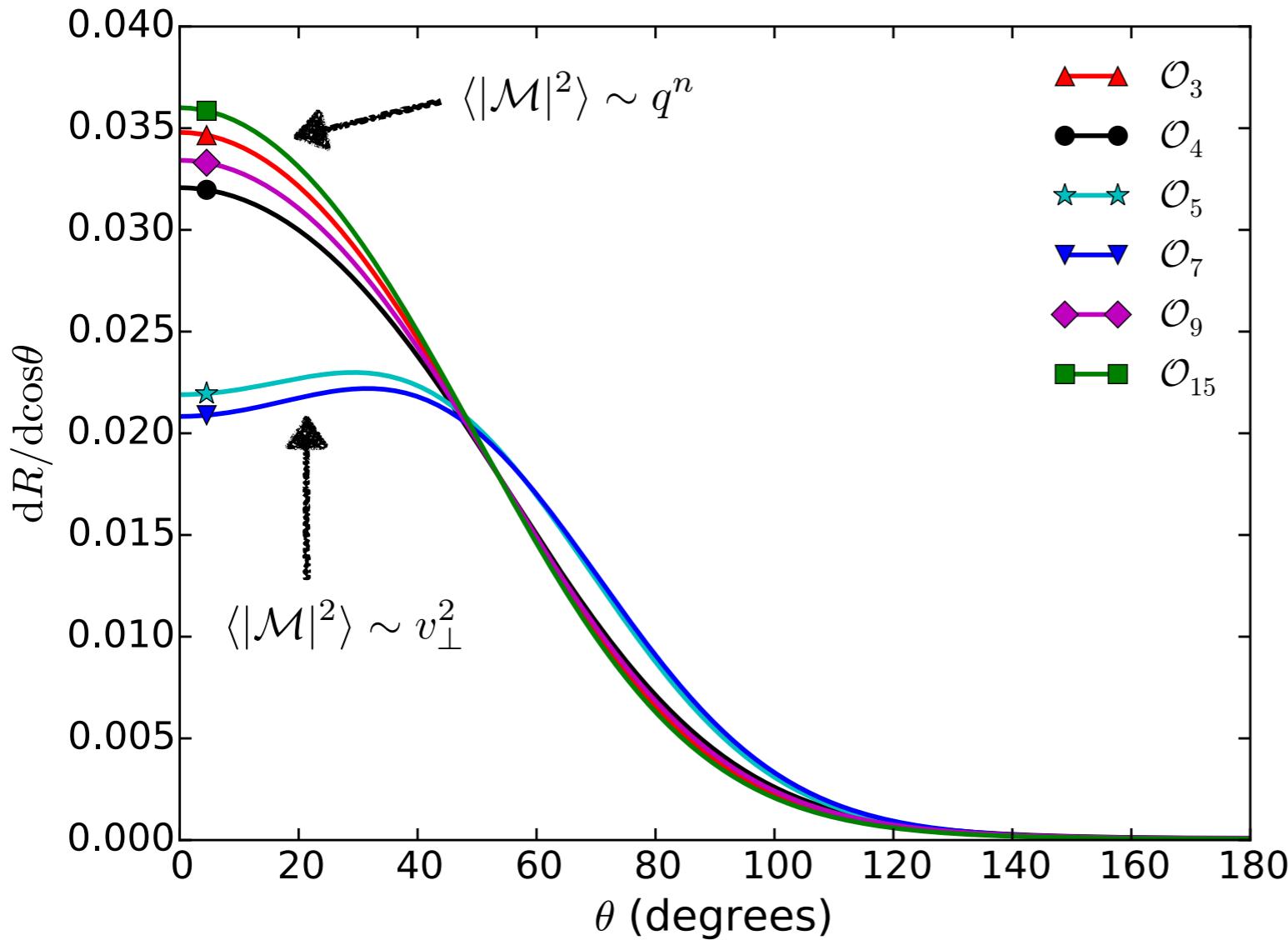
'Perfect'  $\text{CF}_4$  detector

$E_R \in [20, 50] \text{ keV}$

$m_\chi = 100 \text{ GeV}$

Note: 
$$\begin{aligned} q &= 2\mu_{\chi N} \vec{v} \cdot \hat{q} \\ &= 2\mu_{\chi N} v \cos \theta \end{aligned}$$

# Directional Spectra



'Perfect'  $\text{CF}_4$  detector

$E_R \in [20, 50] \text{ keV}$

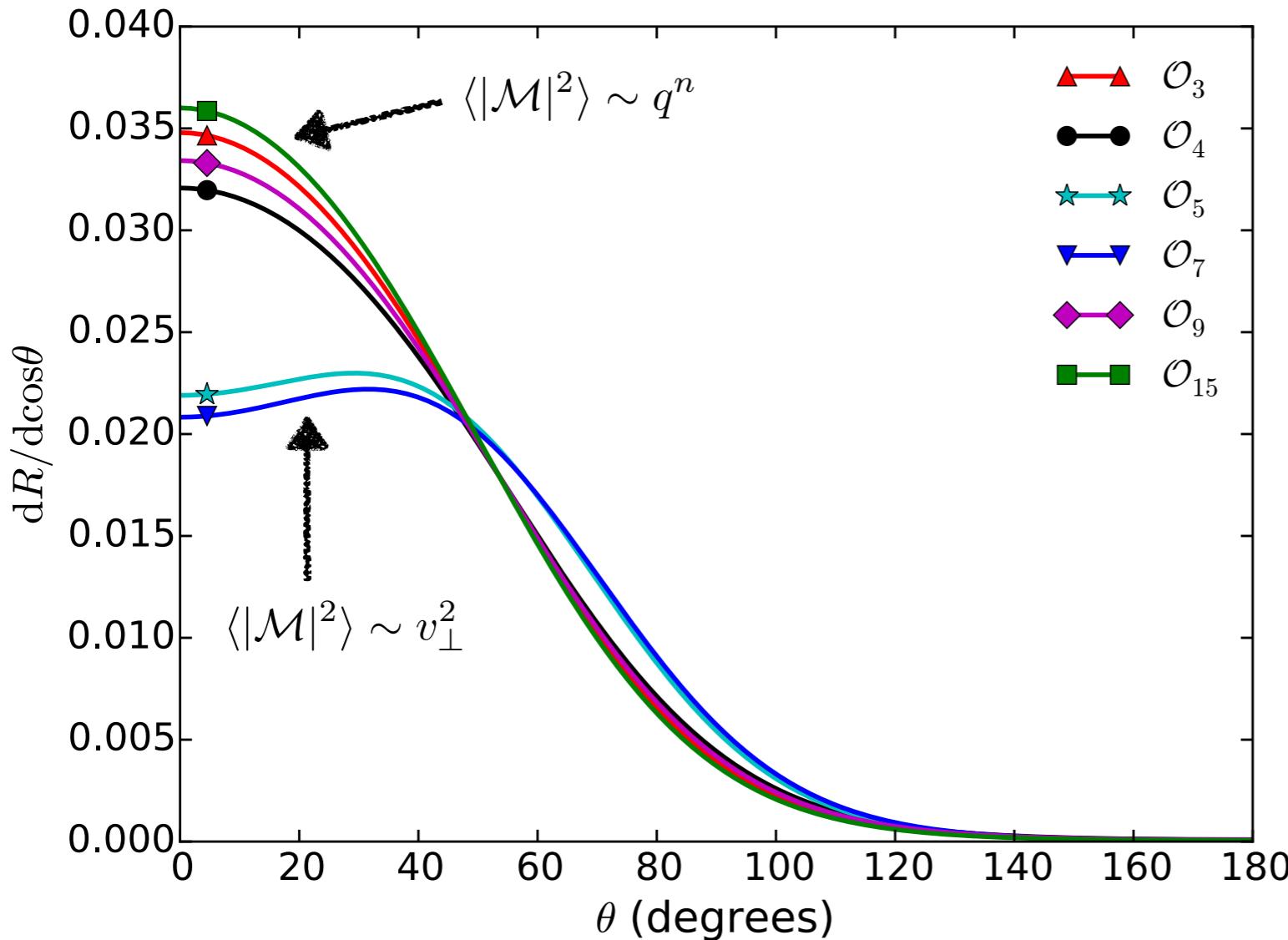
$m_\chi = 100 \text{ GeV}$

$$\begin{aligned} \text{Note: } q &= 2\mu_{\chi N} \vec{v} \cdot \hat{q} \\ &= 2\mu_{\chi N} v \cos \theta \end{aligned}$$

Most isotropic:  $\mathcal{O}_7 = \vec{S}_n \cdot \vec{v}_\perp \rightarrow \sigma_7 \sim v_\perp^2$

Least isotropic:  $\mathcal{O}_{15} = (\vec{S}_\chi \cdot \frac{\vec{q}}{m_n})((\vec{S}_n \times \vec{v}_\perp) \cdot \frac{\vec{q}}{m_n}) \rightarrow \sigma_{15} \sim q^4(q^2 + v_\perp^2)$

# A (new) ring-like feature



Operators which give  
 $\langle |\mathcal{M}|^2 \rangle \sim (v_\perp)^2$   
lead to a ‘ring’ in the  
directional rate.

A ring in the standard rate has been previously studied [Bozorgnia et al. - 1111.6361], but *this* ring occurs for lower WIMP masses (down to 10 GeV) and higher threshold energies (up to 10 keV).

# Likelihood Analysis

Generate mock data assuming an NREFT operator  
(  $\mathcal{O}_7$  or  $\mathcal{O}_{15}$  ).

Assume data is a combination of standard SD interaction and non-standard NREFT interaction. Fit to data with two free parameters  $m_\chi$  and  $A$ .

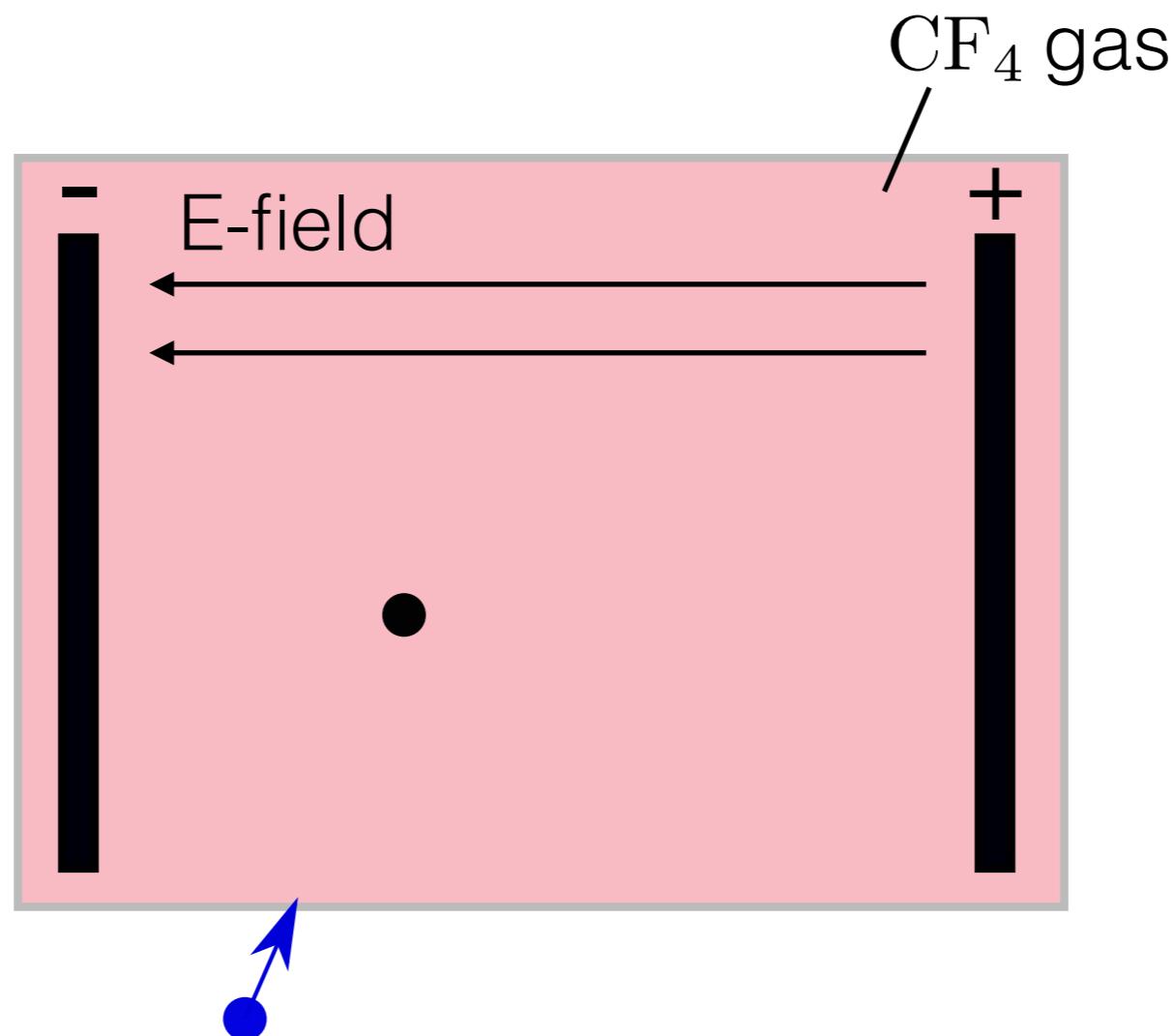
$A$  : fraction of events which are due to non-standard NREFT interaction.

Perform likelihood ratio test to determine the significance with which we can reject SD-only interactions (i.e. reject  $A = 0$ ) in 95% of pseudo-experiments.

Plot as a function of the number of signal events  $N_{\text{WIMP}}$ .

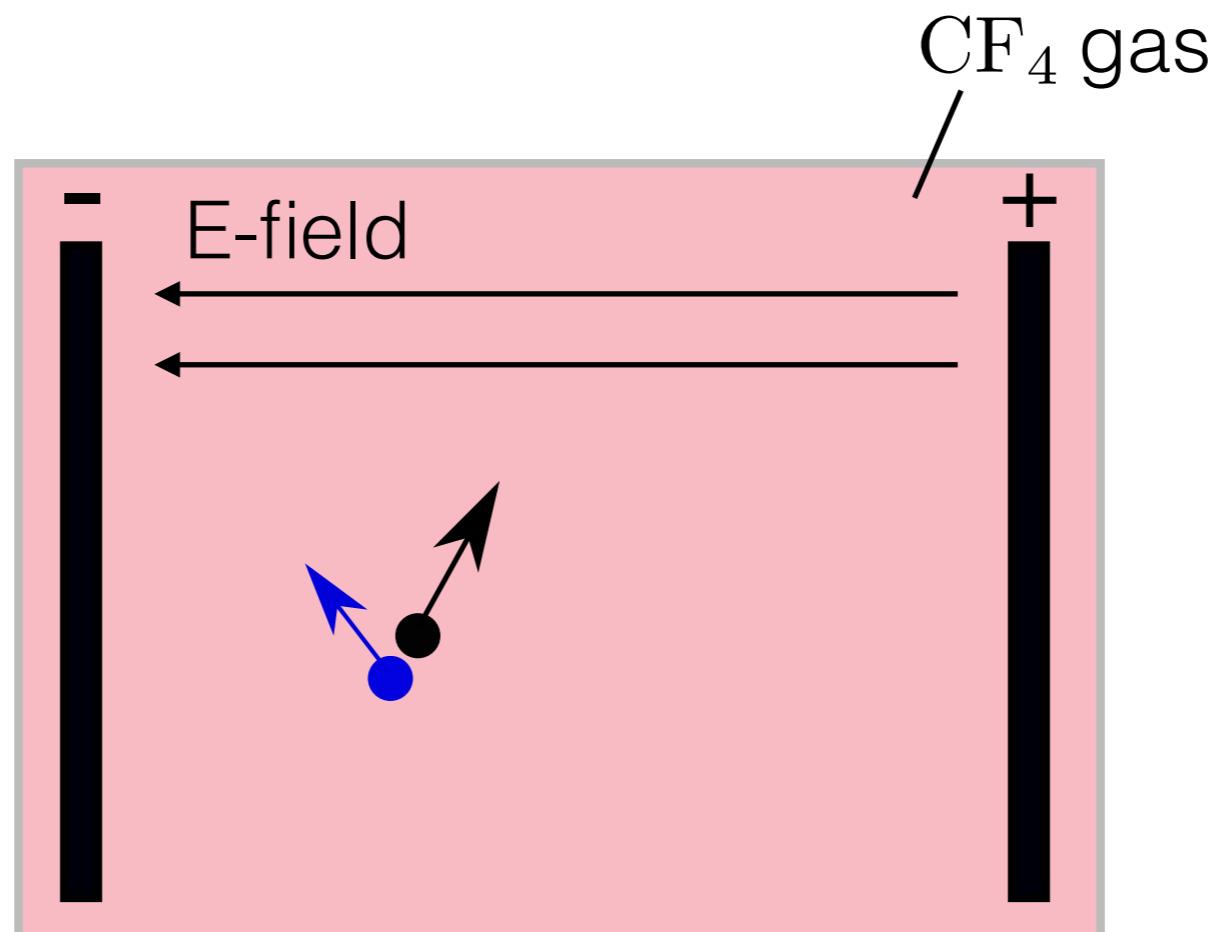
# Directional detection - TPCs

Most advanced technology is the gaseous Time Projection Chamber (TPC) : [e.g. DRIFT, MIMAC, DMTPC, NEWAGE, D3]



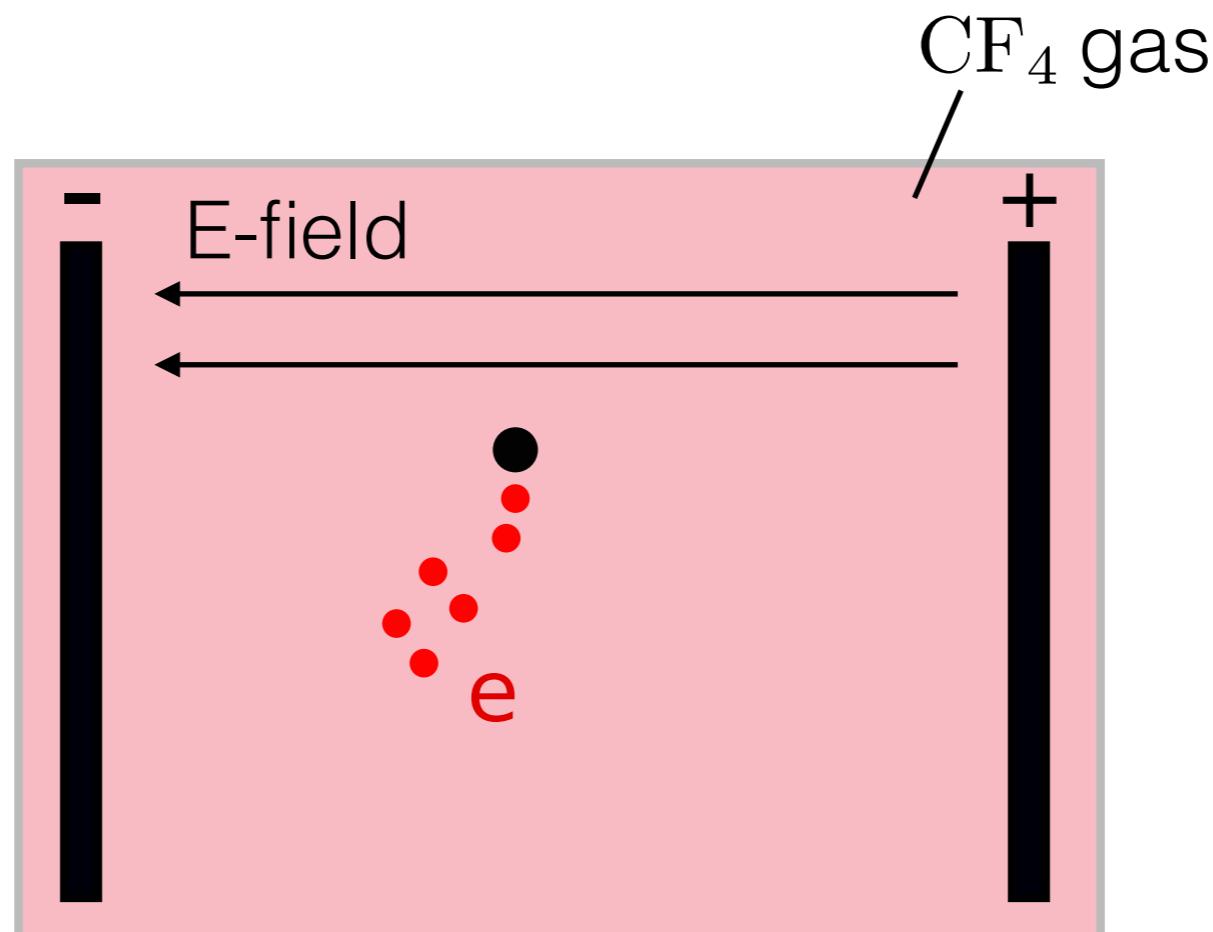
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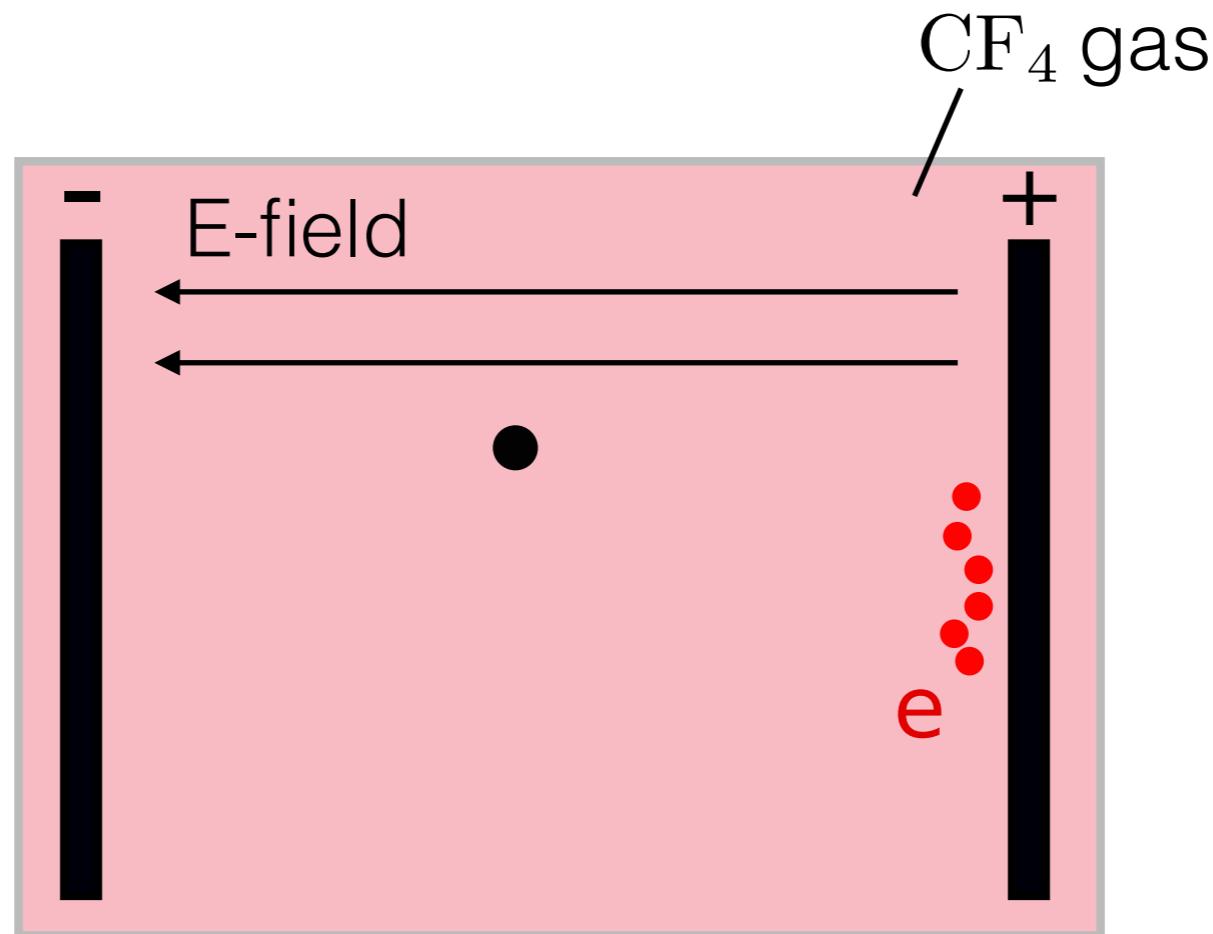
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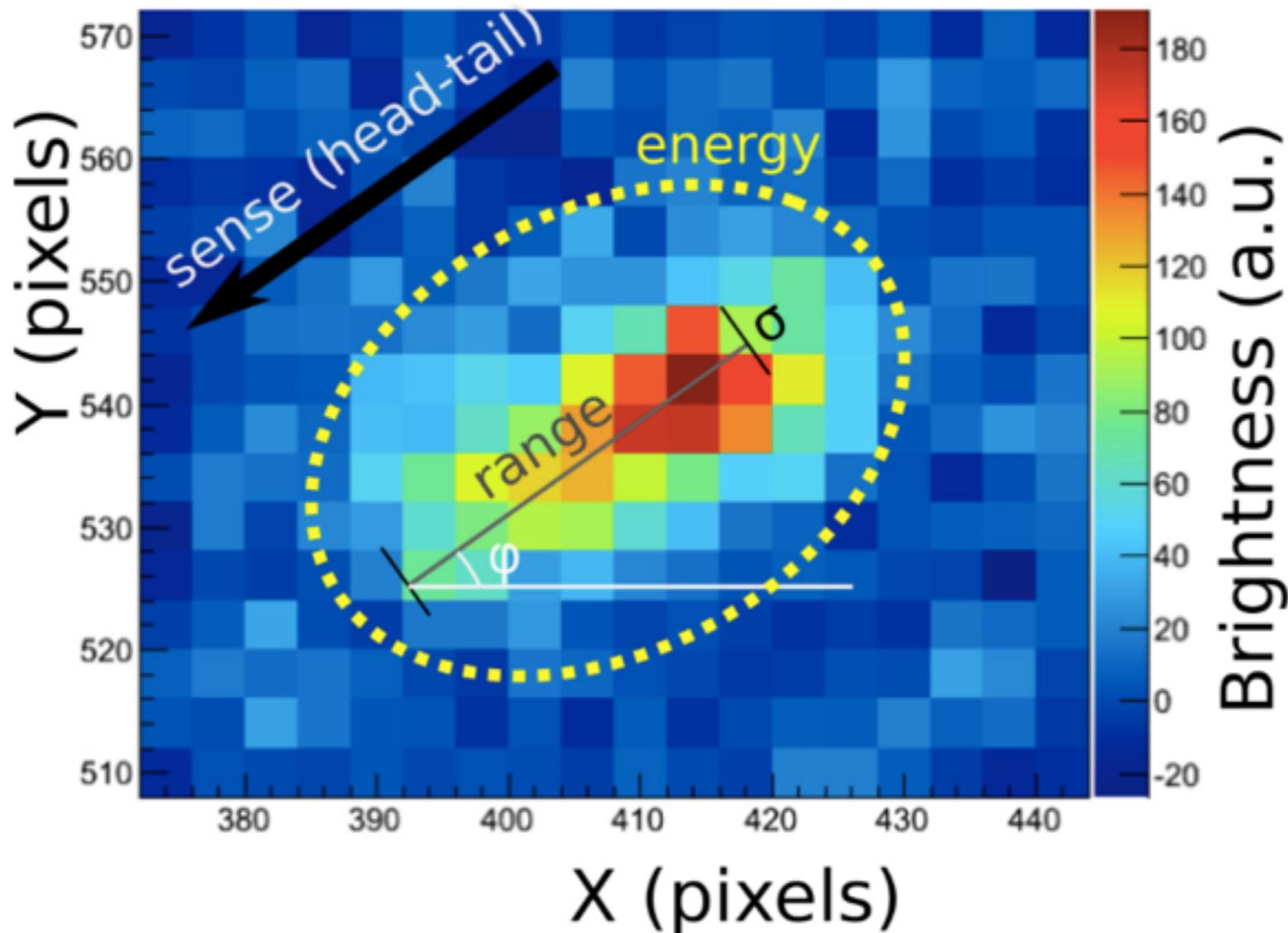


Get x,y of track from distribution of electrons hitting anode

Get z of track from timing of electrons hitting anode

# A ‘Real’ Signal

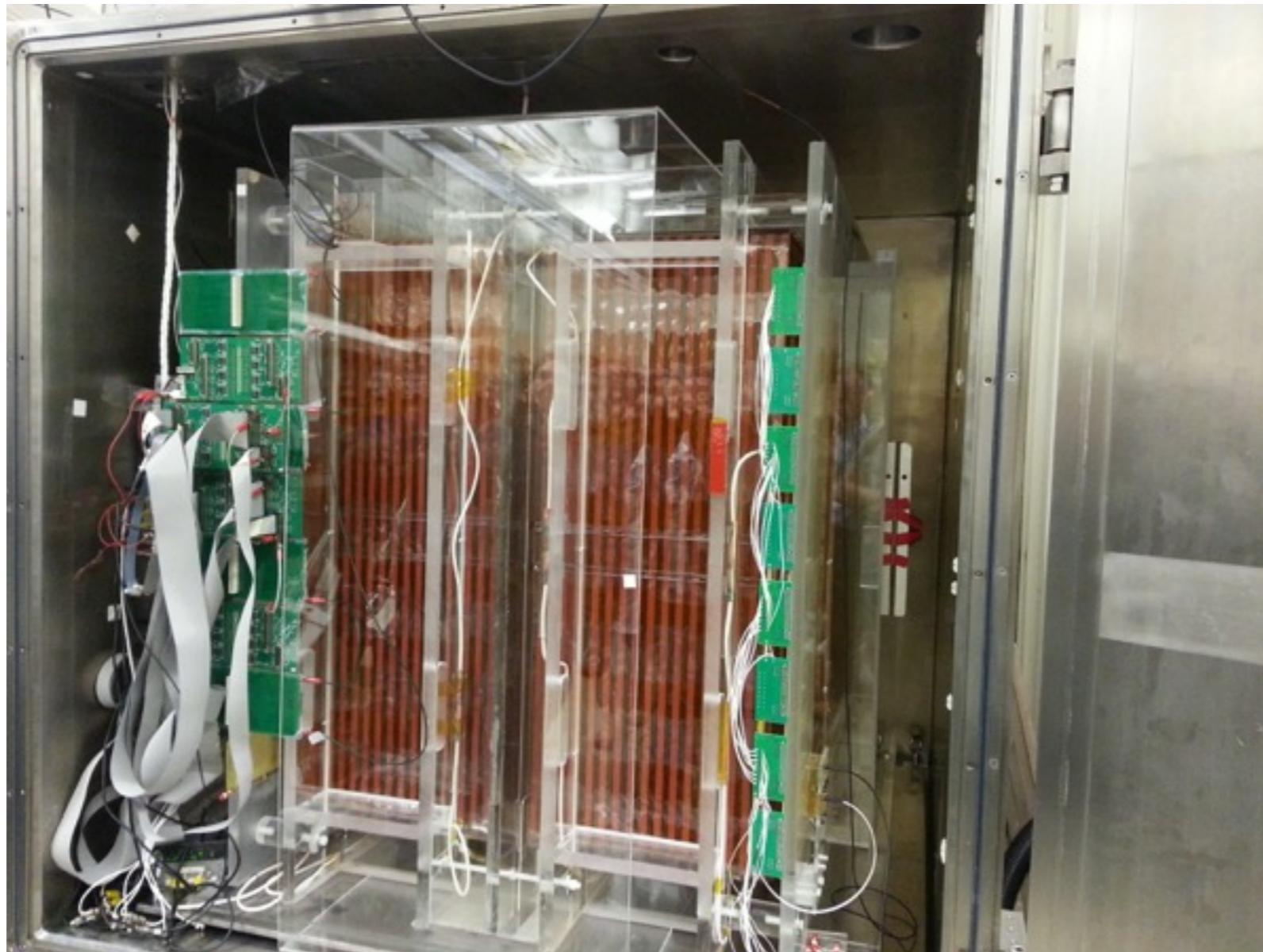
Deaconu et al. (DMTPC, 2015)



- Finite angular resolution -  $\Delta\theta \sim 20^\circ - 80^\circ$
- May not get full 3-D track information
- May not get head-tail discrimination

# A Real TPC

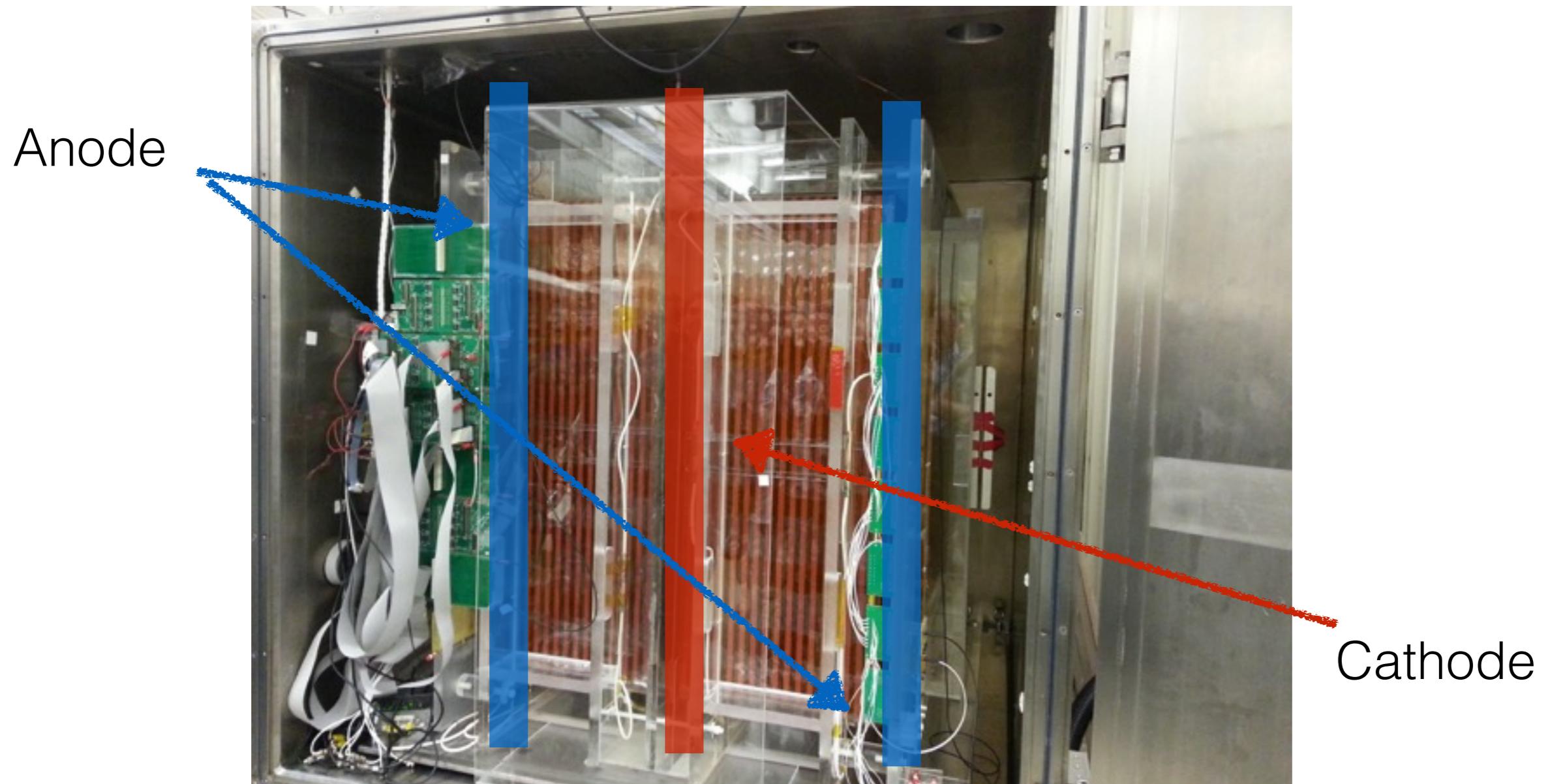
DRIIFT-IIe prototype detector @ Occidental College, LA



Two back-to-back TPCs

# A Real TPC

DRIIFT-IIe prototype detector @ Occidental College, LA



Two back-to-back TPCs

# Nuclear response functions

$$F_{1,1} = F_M$$

$$F_{3,3} = \frac{1}{8} \frac{q^2}{m_n^2} \left( v_\perp^2 F_{\Sigma'} + 2 \frac{q^2}{m_n^2} F_{\Phi''} \right)$$

$$F_{4,4} = \frac{C(j_\chi)}{16} (F_{\Sigma'} + F_{\Sigma''})$$

$$F_{5,5} = \frac{C(j_\chi)}{4} \frac{q^2}{m_n^2} \left( v_\perp^2 F_M + \frac{q^2}{m_n^2} F_\Delta \right)$$

$$F_{6,6} = \frac{C(j_\chi)}{16} \frac{q^4}{m_n^4} F_{\Sigma''}$$

$$F_{7,7} = \frac{1}{8} v_\perp^2 F_{\Sigma'},$$

$$F_{8,8} = \frac{C(j_\chi)}{4} \left( v_\perp^2 F_M + \frac{q^2}{m_n^2} F_\Delta \right)$$

$$F_{9,9} = \frac{C(j_\chi)}{16} \frac{q^2}{m_n^2} F_{\Sigma'}$$

$$F_{10,10} = \frac{1}{4} \frac{q^2}{m_n^2} F_{\Sigma''}$$

$$F_{11,11} = \frac{1}{4} \frac{q^2}{m_n^2}$$

$$F_{12,12} = \frac{C(j_\chi)}{16} \left( v_\perp^2 \left( F_{\Sigma''} + \frac{1}{2} F_{\Sigma'} \right) + \frac{q^2}{m_n^2} (F_{\tilde{\Phi}'} + F_{\Phi''}) \right)$$

$$F_{13,13} = \frac{C(j_\chi)}{16} \frac{q^2}{m_n^2} \left( v_\perp^2 F_{\Sigma''} + \frac{q^2}{m_n^2} F_{\tilde{\Phi}'} \right)$$

$$F_{14,14} = \frac{C(j_\chi)}{32} \frac{q^2}{m_n^2} v_\perp^2 F_{\Sigma'}$$

$$F_{15,15} = \frac{C(j_\chi)}{32} \frac{q^4}{m_n^4} \left( v_\perp^2 F_{\Sigma'} + 2 \frac{q^2}{m_n^2} F_{\Phi''} \right)$$

$F_{M,\Sigma',\Sigma'',\tilde{\Phi}',\Phi'',\Delta}(q^2)$  are standard form factors encoding the distribution of nucleons in the nucleus - suppression at high  $q$ .

*Coupling to  $q^2$  does not affect the intrinsic directional rate.*

*But, each term in the response function is proportional to either  $(v_\perp)^0$  or  $(v_\perp)^2$ .*

# Transverse Radon Transform

For response functions coupling to  $(v_{\perp})^2$  we need to calculate the *Transverse Radon Transform* (TRT):

$$\hat{f}^T(v_{\min}, \hat{q}) = \int_{\mathbb{R}^3} \frac{(v_{\perp})^2}{c^2} f(\vec{v}) \delta(\vec{v} \cdot \hat{q} - v_{\min}) d^3 \vec{v}$$

In the case of a Maxwell-Boltzmann distribution (e.g. SHM):

$$\hat{f}^T(v_{\min}, \hat{q}) = \frac{\left(2\sigma_v^2 + v_{\text{lag}}^2 - (\vec{v}_{\text{lag}} \cdot \hat{q})^2\right)}{\sqrt{2\pi}\sigma_v c^2} \exp\left[-\frac{(v_{\min} - \vec{v}_{\text{lag}} \cdot \hat{q})^2}{2\sigma_v^2}\right]$$

If we measure recoil angles  $\theta$  from the mean recoil direction  $\vec{v}_{\text{lag}}$ :

$$\hat{f}^T(v_{\min}, \hat{q}) = \frac{\left(2\sigma_v^2 + v_{\text{lag}}^2 \sin^2 \theta\right)}{\sqrt{2\pi}\sigma_v c^2} \exp\left[-\frac{(v_{\min} - v_{\text{lag}} \cos \theta)^2}{2\sigma_v^2}\right]$$

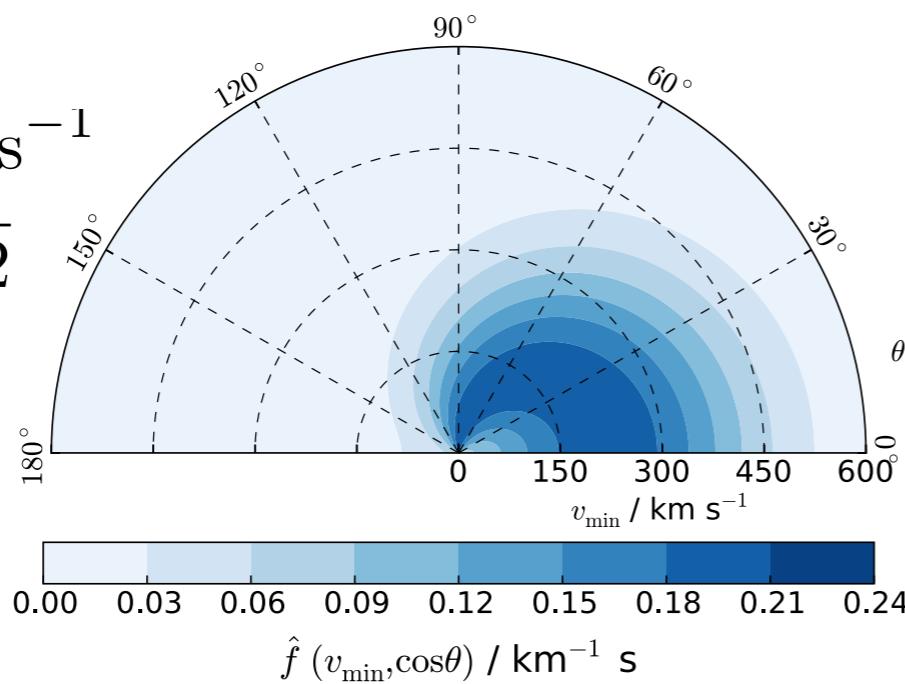
# Transverse Radon Transform (examples)

$$\hat{f}(v_{\min}, \hat{q})$$

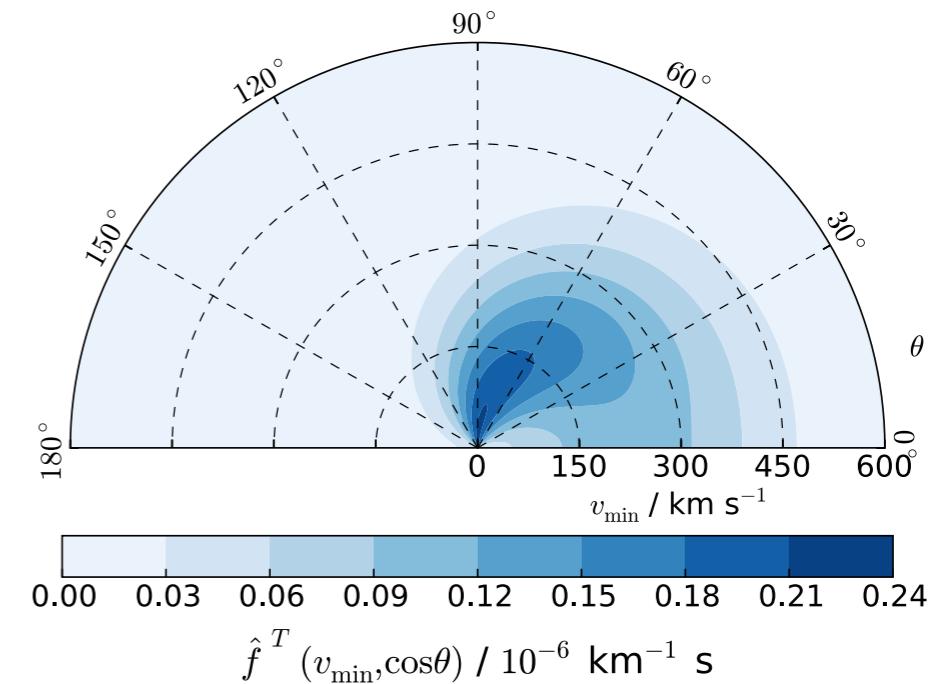
SHM:

$$v_{\text{lag}} = 220 \text{ km s}^{-1}$$

$$\sigma_v = v_{\text{lag}} / \sqrt{2}$$



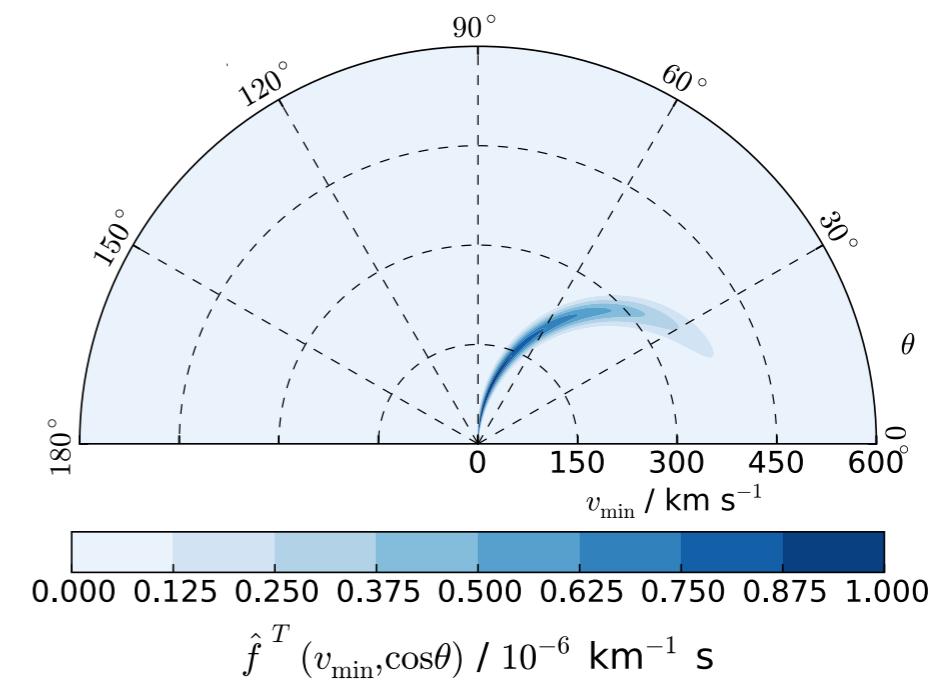
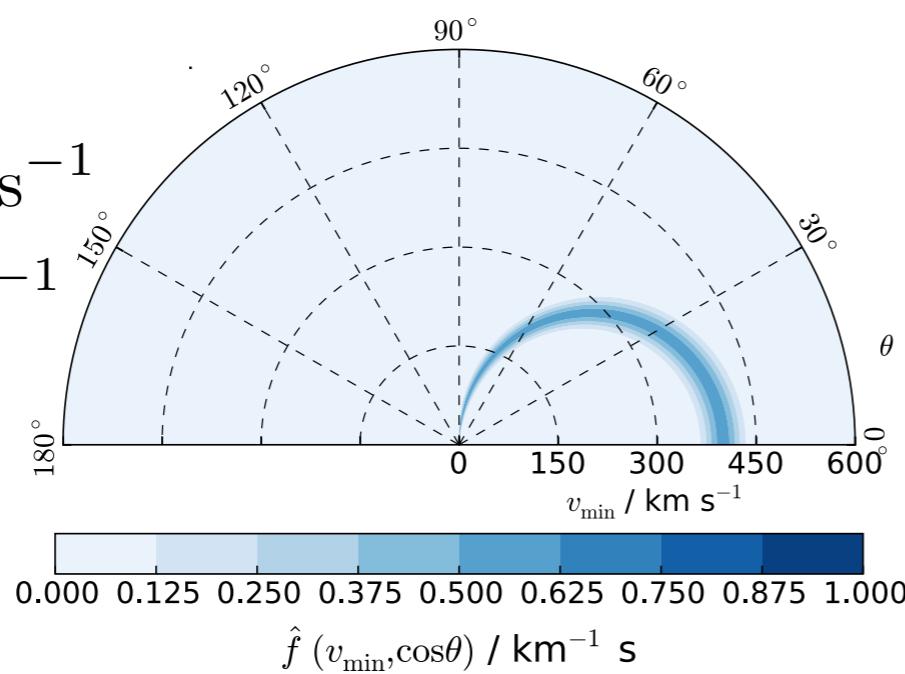
$$\hat{f}^T(v_{\min}, \hat{q})$$



Stream:

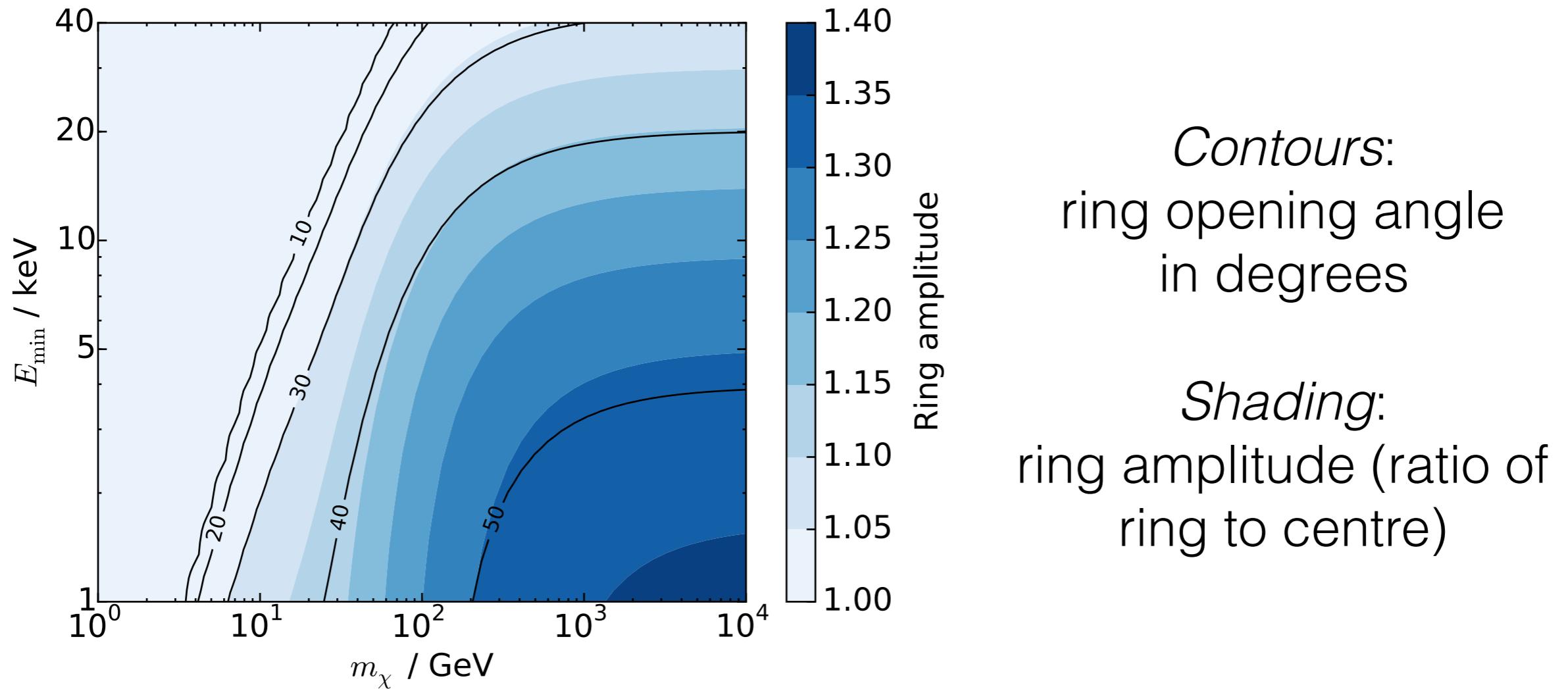
$$v_{\text{lag}} = 400 \text{ km s}^{-1}$$

$$\sigma_v = 20 \text{ km s}^{-1}$$



# A (new) ring-like feature

Operators with  $\langle |\mathcal{M}|^2 \rangle \sim (v_\perp)^2$  lead to a ‘ring’ in the directional rate.

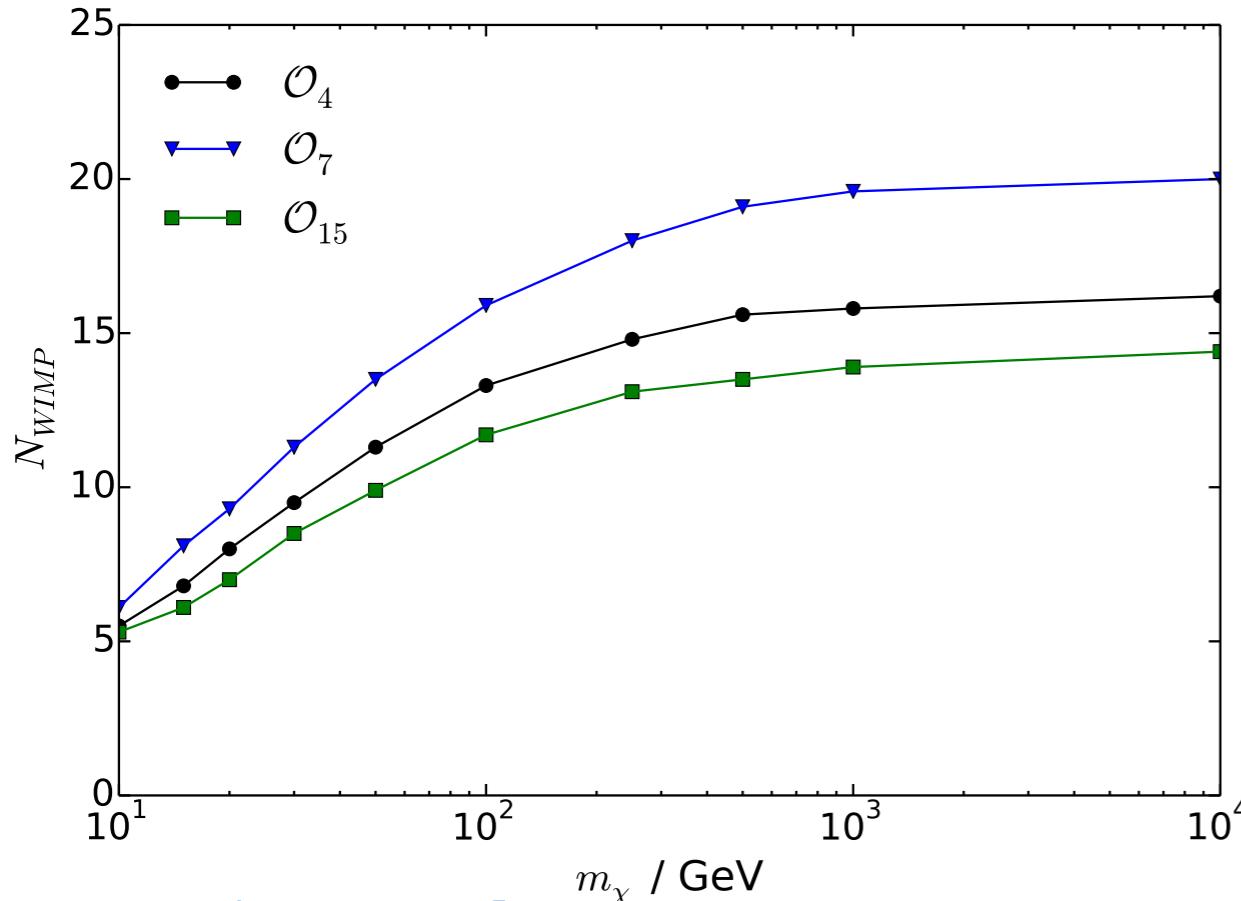


A ring in the standard rate has been previously studied [Bozorgnia et al. - 1111.6361], but *this* ring occurs for lower WIMP masses and higher threshold energies.

# Statistical tests

$$F_{4,4} \sim 1$$
$$F_{7,7} \sim v_\perp^2$$
$$F_{15,15} \sim q^4(q^2 + v_\perp^2)$$

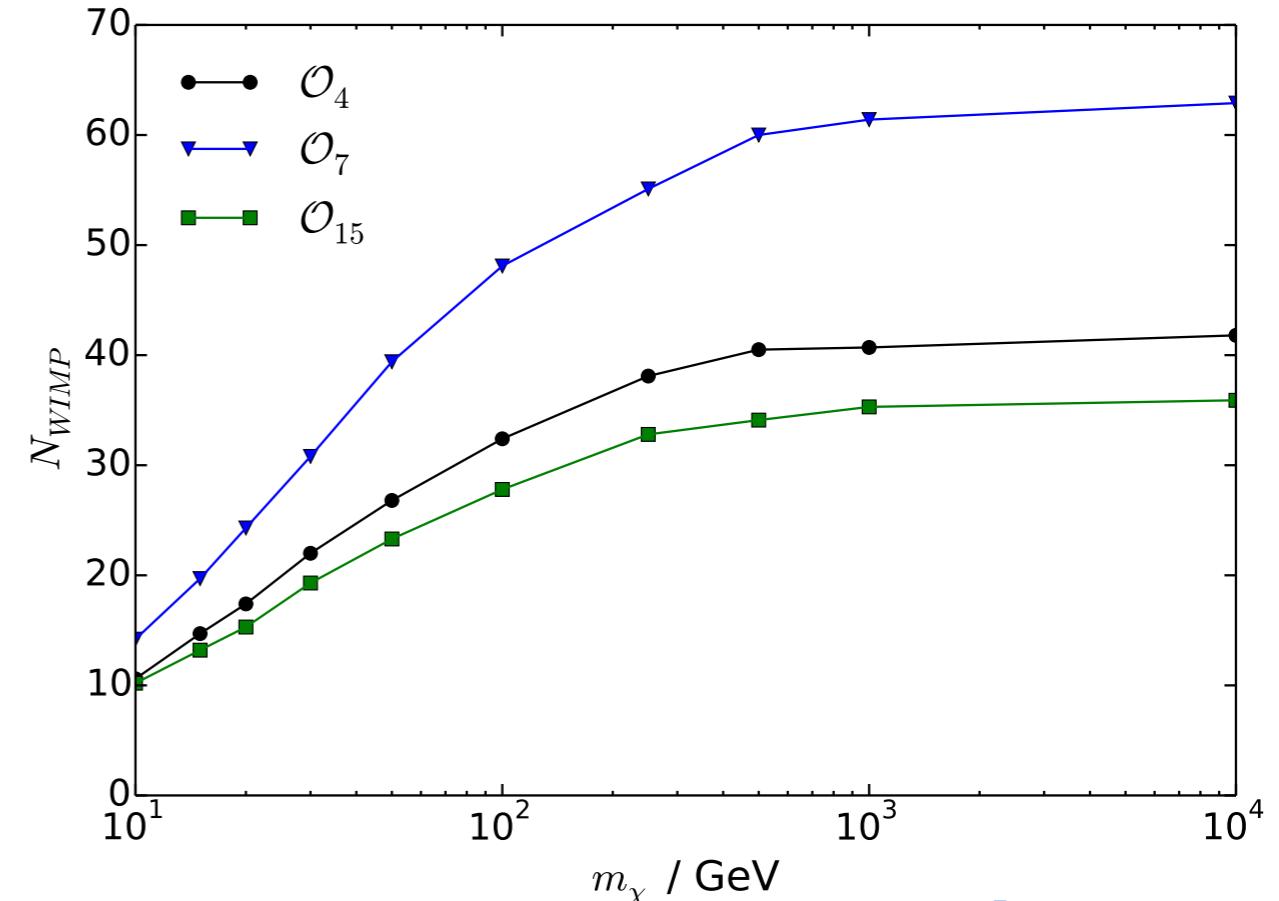
...reject isotropy...



[astro-ph/0408047]

Calculate the number of signal events required to...

...confirm the median recoil dir...



[1002.2717]

...at the  $2\sigma$  level in 95% of experiment.