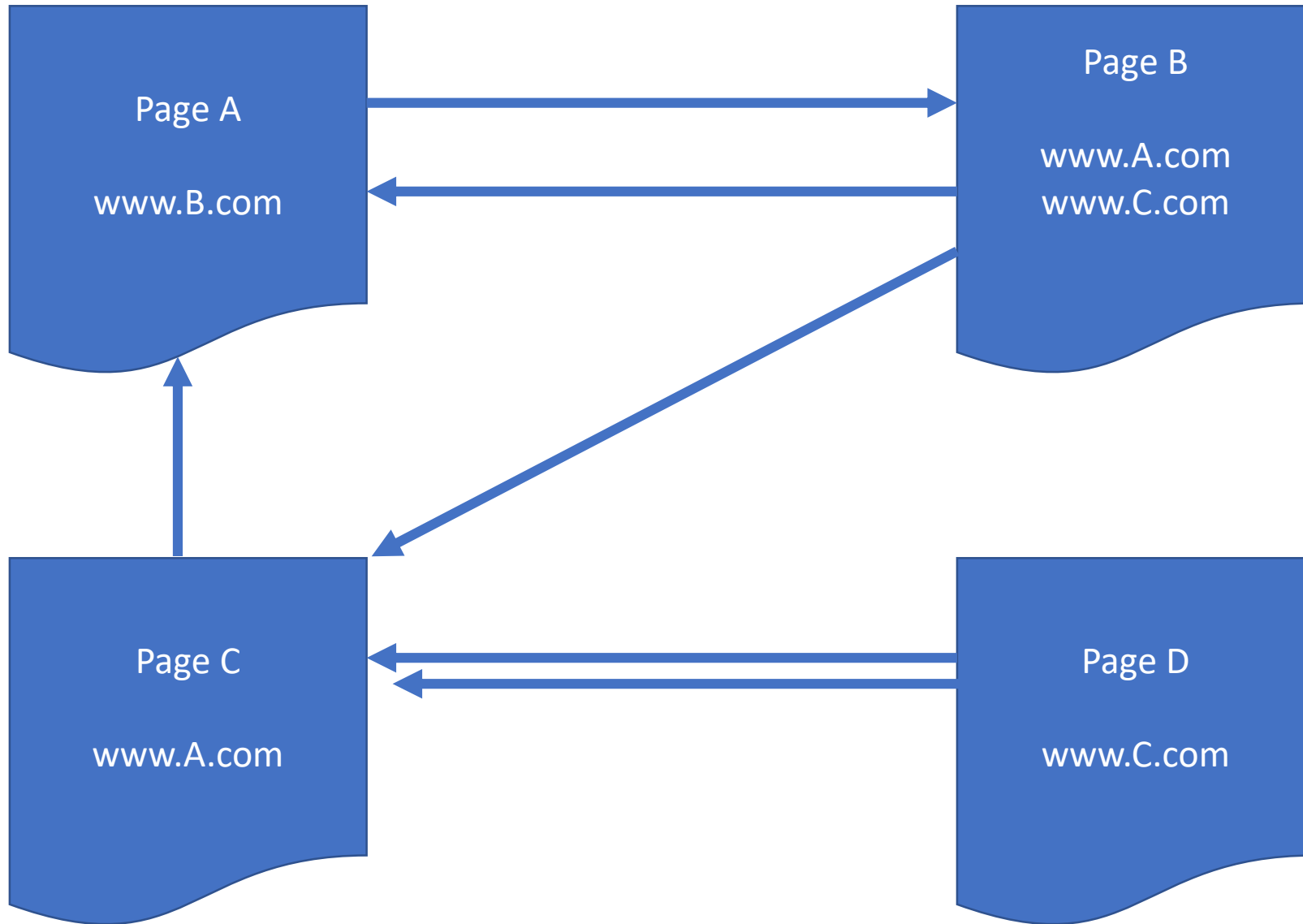


# PAGERANK ALGORITHM

RANK WEBSITES FROM SEARCH ENGINE RESULTS



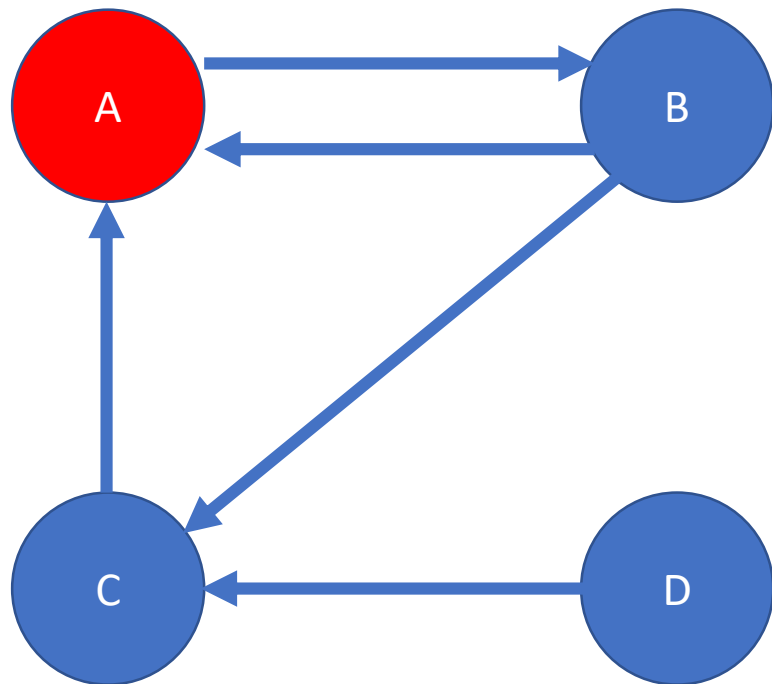


# PageRank

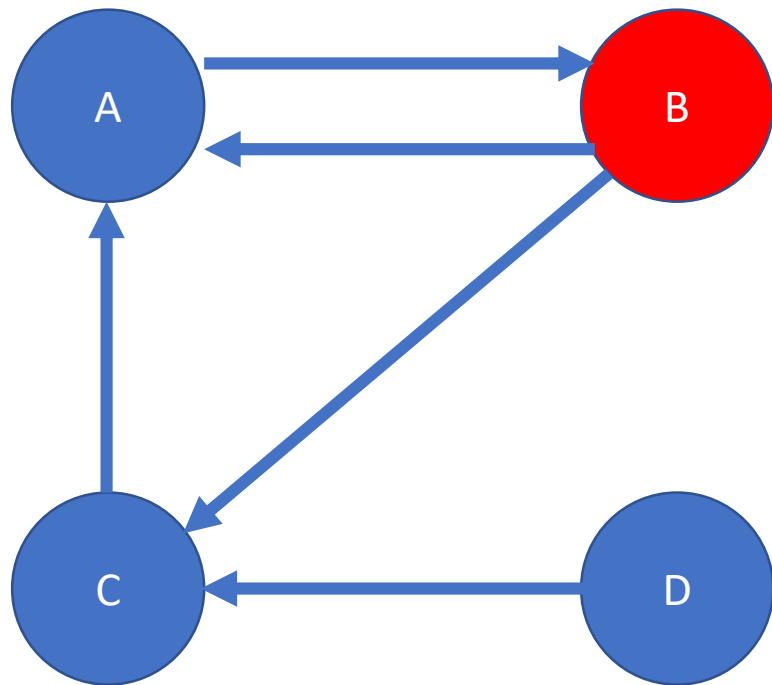
$$PR(p_i) = \frac{1-d}{N} + d \sum_{p_j \in M(p_i)} \frac{PR(p_j)}{L(p_j)}$$

# General Formula

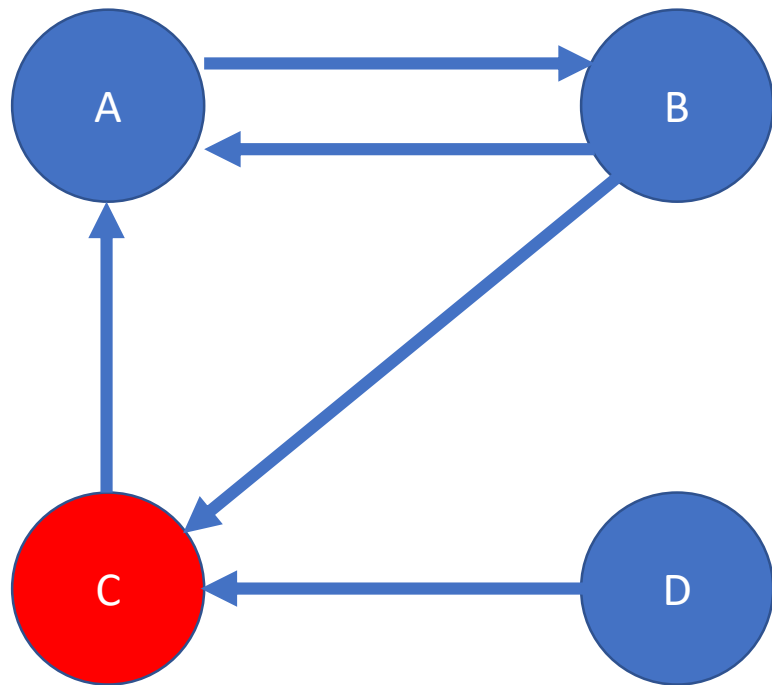
$$\text{PageRank}(A) = \frac{\text{PageRank}(B)}{\text{Outbound links}(B)} + \frac{\text{PageRank}(C)}{\text{Outbound links}(C)} + \frac{\text{PageRank}(D)}{\text{Outbound links}(D)} + \frac{\text{PageRank}(E)}{\text{Outbound links}(E)} + \dots$$



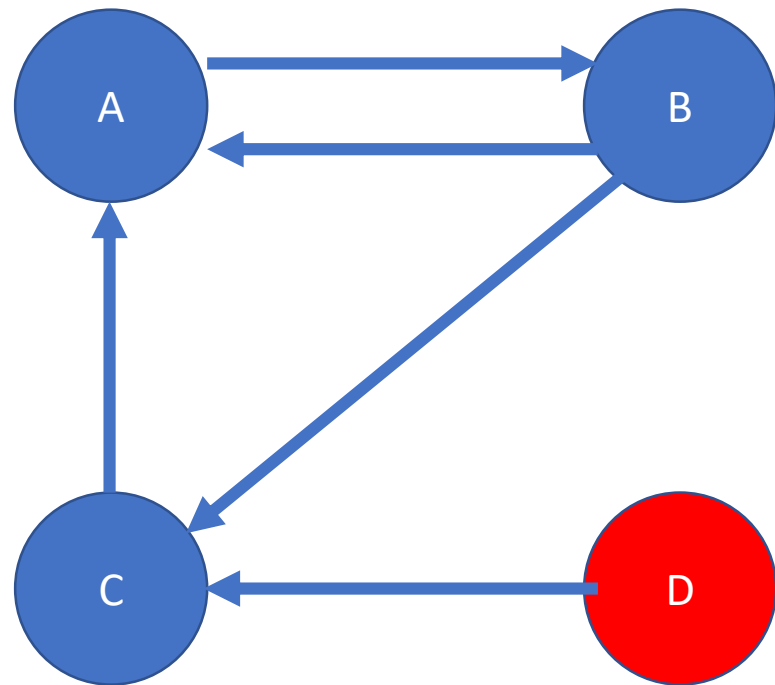
$$\text{PageRank}(A) = \frac{\text{PageRank}(B)}{\text{Count}(2)} + \frac{\text{PageRank}(C)}{\text{Count}(1)}$$



$$\text{PageRank}(B) = \frac{\text{PageRank}(A)}{\text{Count}(1)}$$



$$\text{PageRank}(C) = \frac{\text{PageRank}(B)}{\text{Count}(2)} + \frac{\text{PageRank}(D)}{\text{Count}(1)}$$



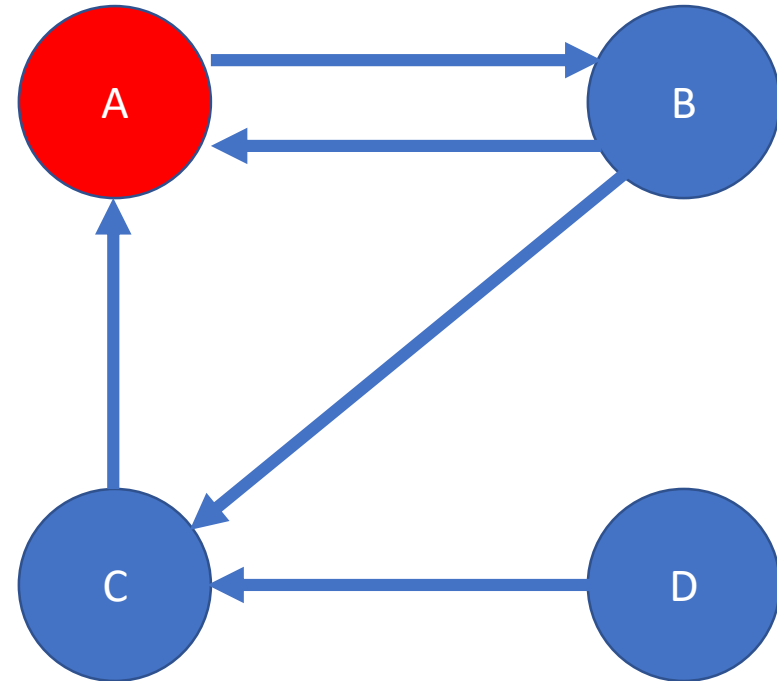
PageRank(D) = 0



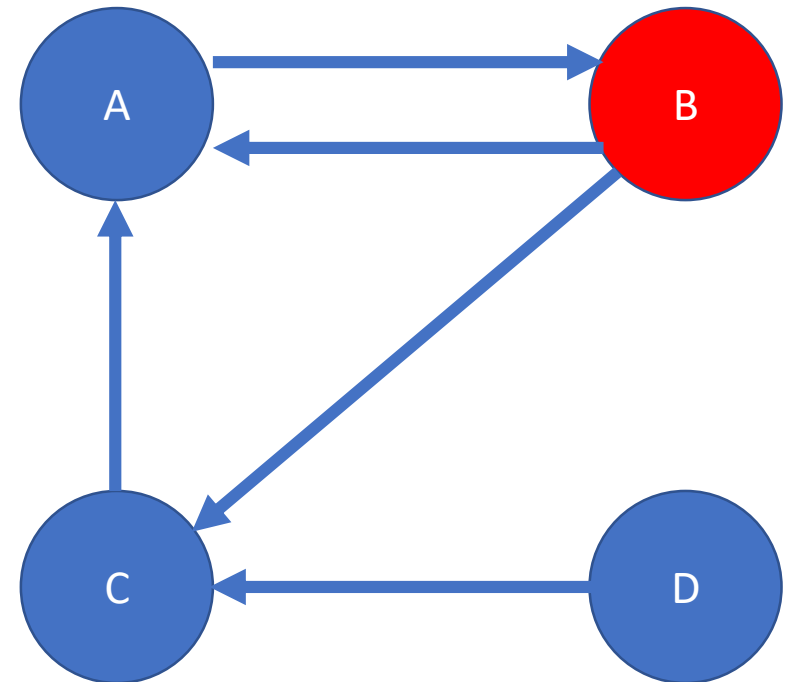
# Damping Factor

- The probability that a user will loose interest in following a chain of links and do another search.
- The recommended default value is 0.85.

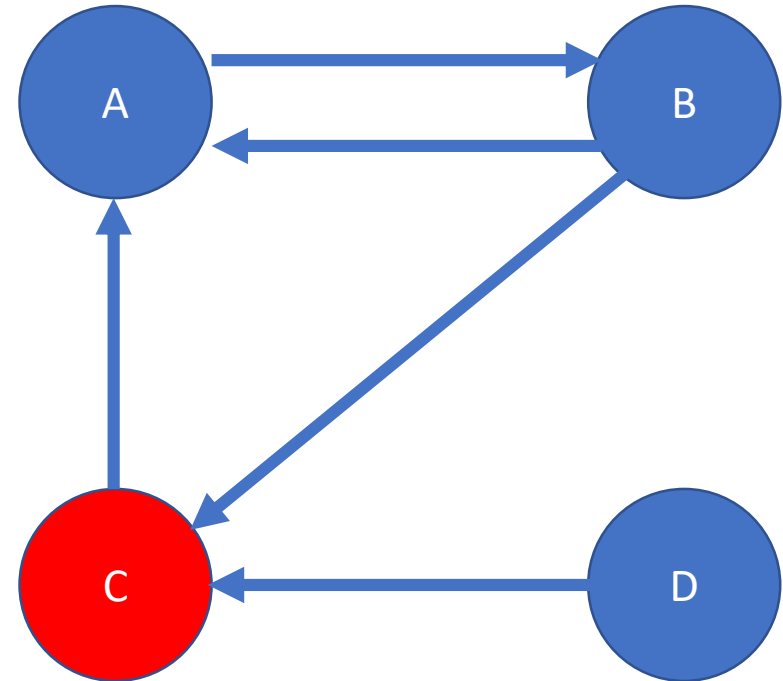
$$\begin{aligned} \text{PR}(A) &= (1-d) + d * (\text{PR}(T1)/C(T1) + \dots + \text{PR}(TN)/C(TN)) \\ &= (1-0.85) + 0.85 * (\text{PR}(B)/2 + \text{PR}(C)/1) \\ &= (1-0.85) + 0.85 * (1 / 2 + 1 / 1) \\ &= 1.425 \end{aligned}$$



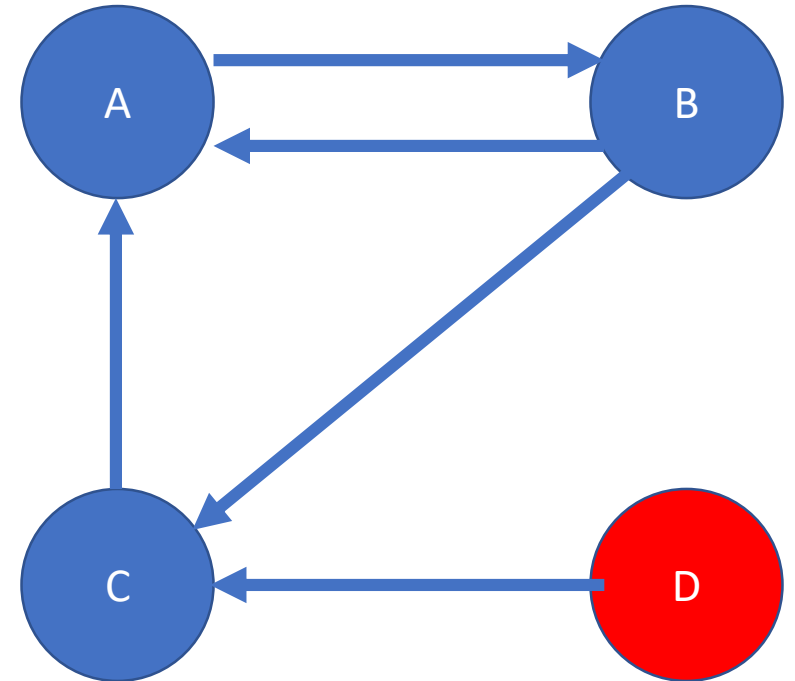
$$\begin{aligned} \text{PR}(B) &= (1 - 0.85) + 0.85 * ( \text{PR}(A) / 1 ) \\ &= (1 - 0.85) + 0.85 * ( 1.425 / 1 ) \\ &= 1.361 \end{aligned}$$



$$\begin{aligned} \text{PR}(C) &= (1-0.85) + 0.85 * (\text{PR}(B)/2 + \text{PR}(D)/1) \\ &= (1-0.85) + 0.85 * (1.361 / 2 + 1 / 1) \\ &= 1.597 \end{aligned}$$



$$\begin{aligned} \text{PR}(D) &= (1-0.85) + 0.85 * 0 \\ &= 0.15 \end{aligned}$$



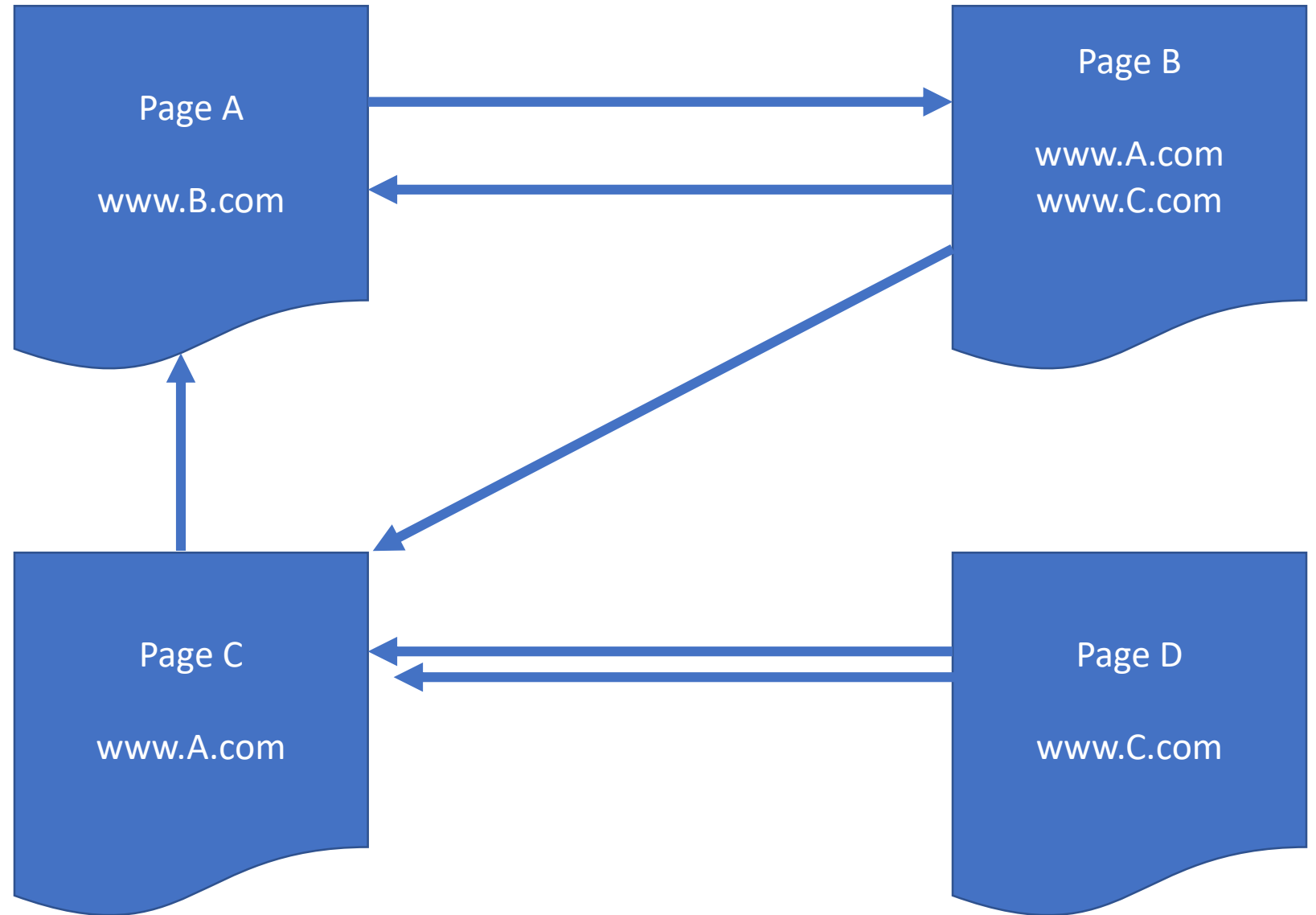
Iteration 1

$PR(A) = 1.425$

$PR(B) = 1.361$

$PR(C) = 1.597$

$PR(D) = 0.15$



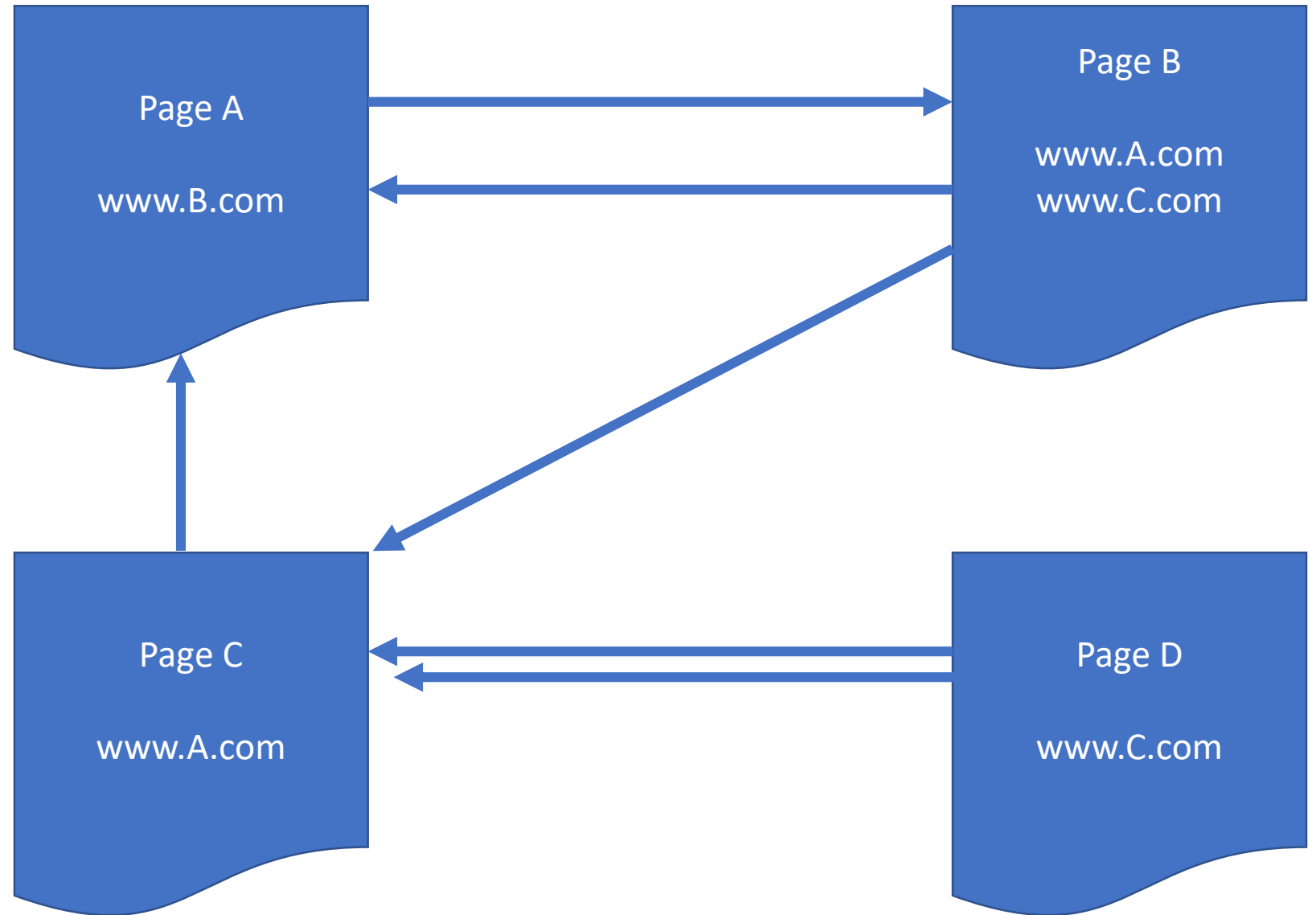
Iteration 2

$PR(A) = 2.070$

$PR(B) = 1.909$

$PR(C) = 1.087$

$PR(D) = 0.15$



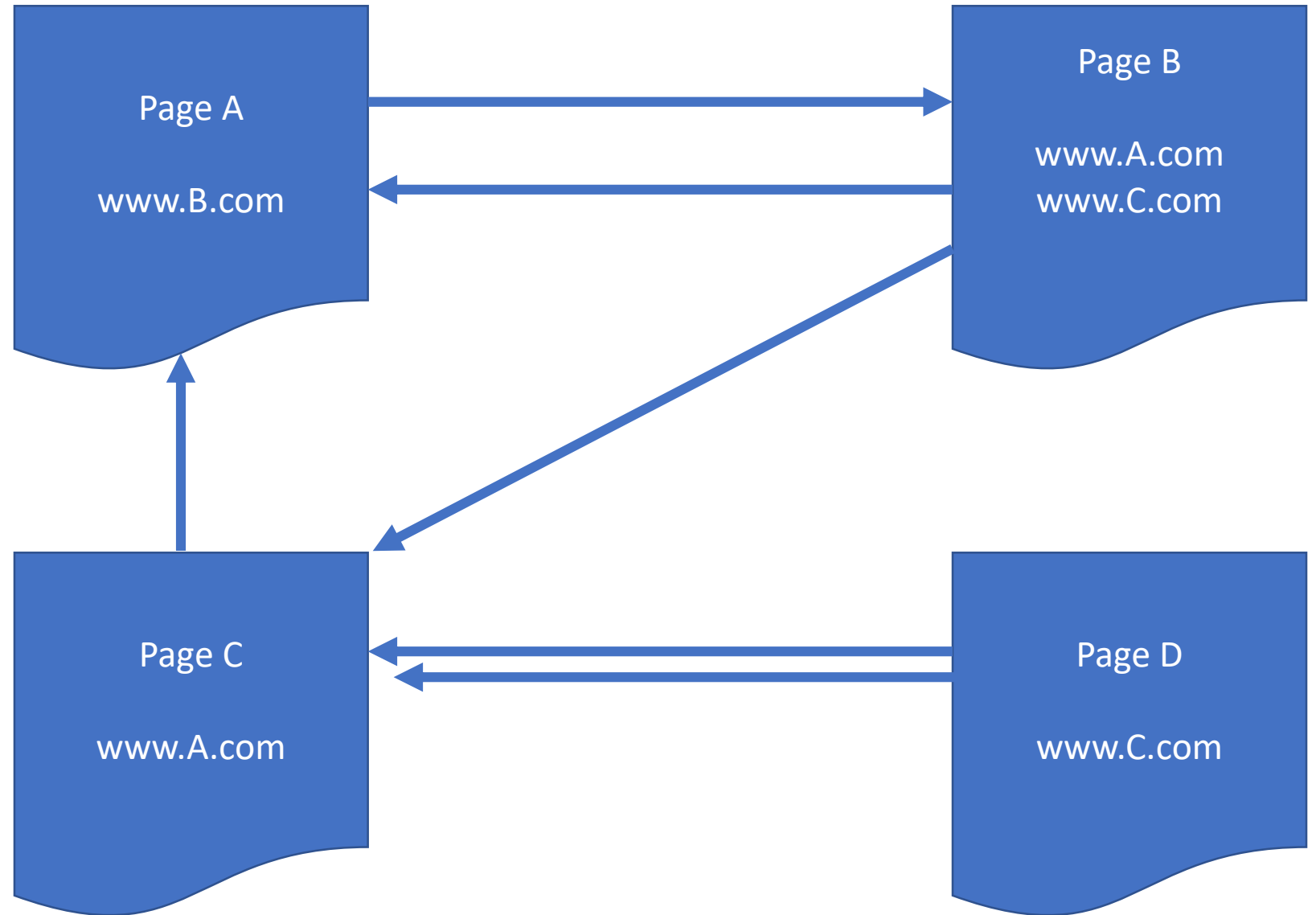
Iteration 3

$PR(A) = 1.887$

$PR(B) = 1.754$

$PR(C) = 1.023$

$PR(D) = 0.15$





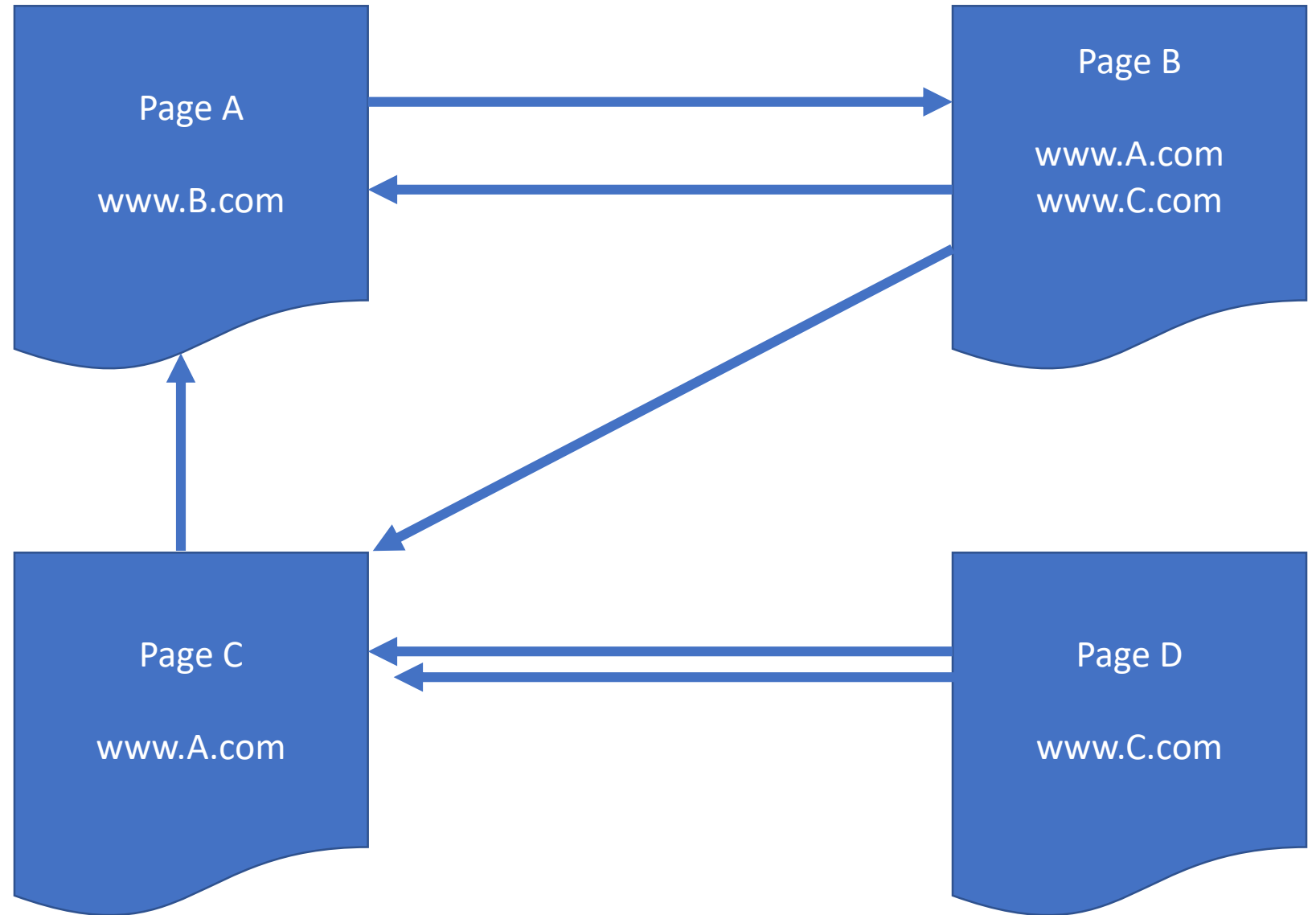
Iteration 4

$PR(A) = 1.765$

$PR(B) = 1.650$

$PR(C) = 0.979$

$PR(D) = 0.15$



Equilibrium  
(iteration 17)

$PR(A) = 1.519$

$PR(B) = 1.441$

$PR(C) = 0.890$

$PR(D) = 0.15$

