

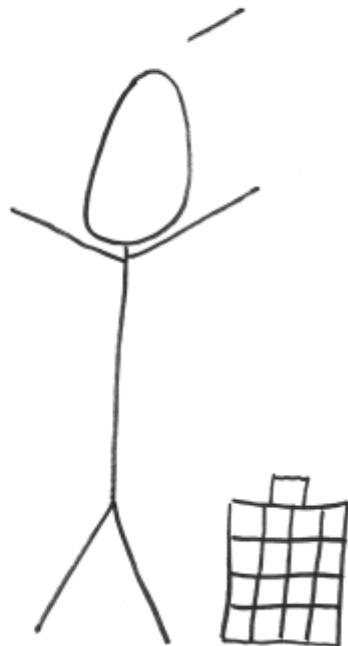
# A Stick Figure Guide to the Advanced Encryption Standard (AES)

Sep 22, 2009

**(A play in 4 acts. Please feel free to exit along with the stage character that best represents you. Take intermissions as you see fit. Click on the stage if you have a hard time seeing it. If you get bored, you can [jump to the code](#). Most importantly, enjoy the show!)**

Act 1: Once Upon a Time...

I handle petabytes\* of data every day. From encrypting juicy Top Secret intelligence to boring packets bound for your WiFi router, I do it all!

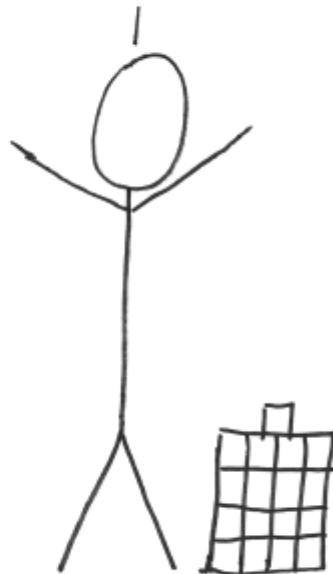


\* 1 petabyte ≈ a lot

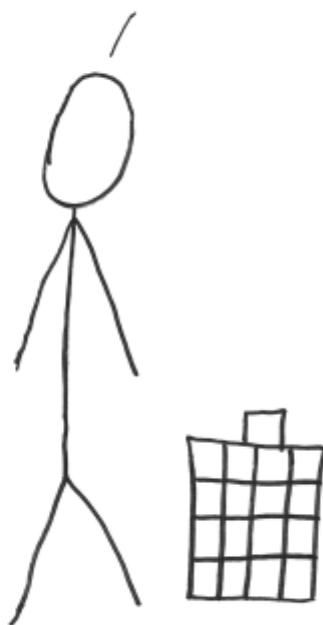
... and still no one seems to care about me or my story.



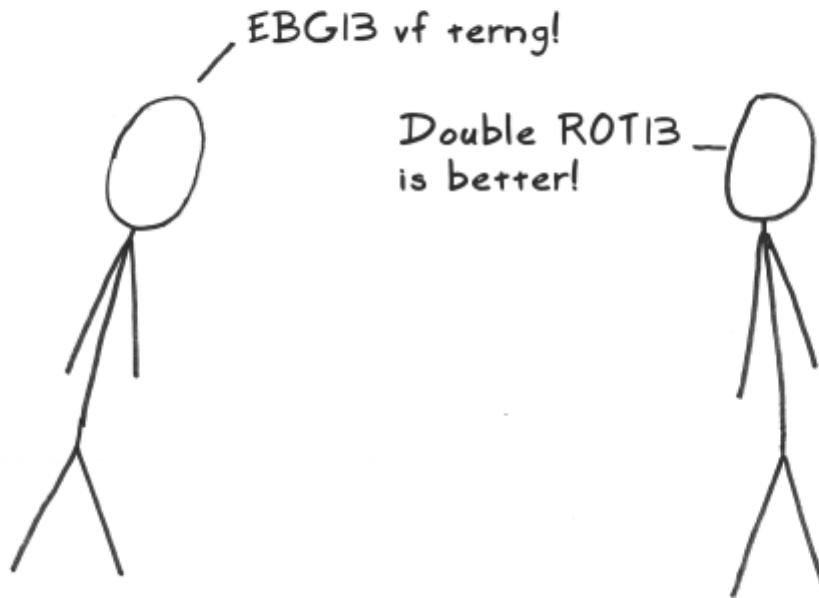
I've got a better-than-Cinderella story as I made my way to become king of the block cipher world.



Whoa! You're still there. You want to hear it? Well let's get started...



Once upon a time,\* there was no good way for people outside secret agencies to judge good crypto.



\* ~ pre-1975 for the general public

A decree went throughout the land to find a good, secure, algorithm.

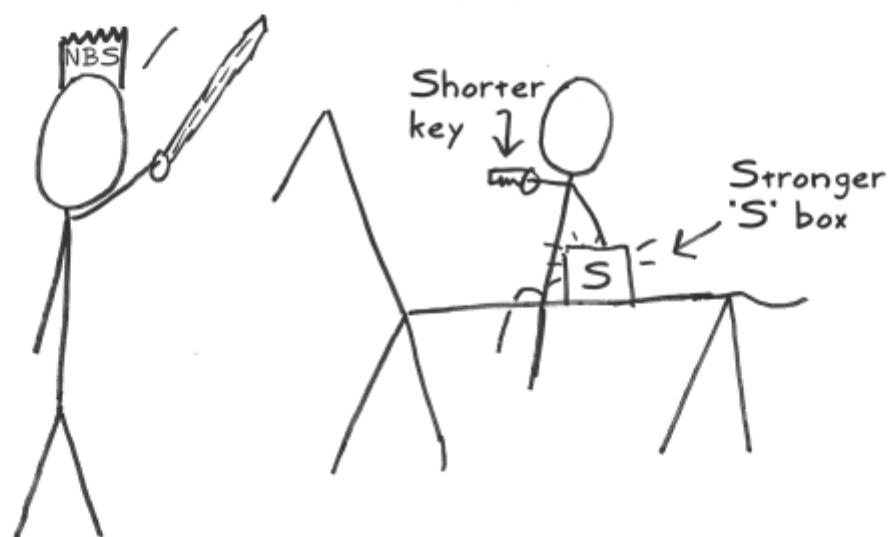


One worthy competitor named Lucifer came forward.



After being modified by the National Security Agency (NSA), he was anointed as the Data Encryption Standard (DES).

I anoint thee as DES!



DES ruled in the land for over 20 years. Academics studied him intently. For the first time, there was something specific to look at. The modern field of cryptography was born.

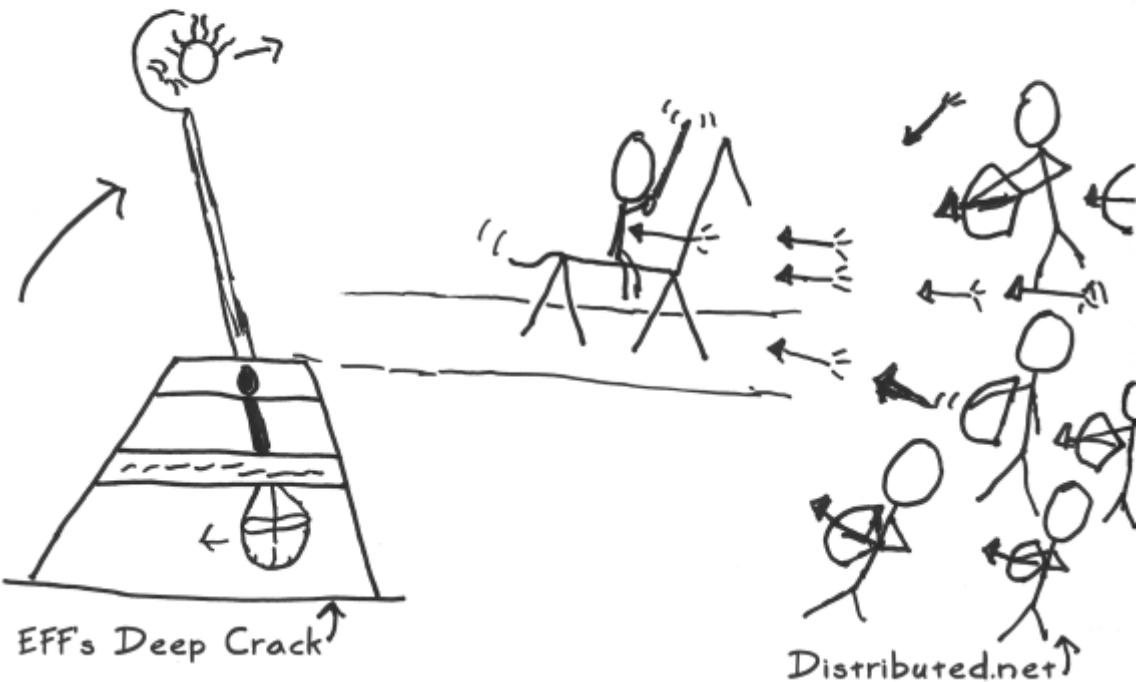
'... to the best of our knowledge, DES is free from any statistical or mathematical weakness.'



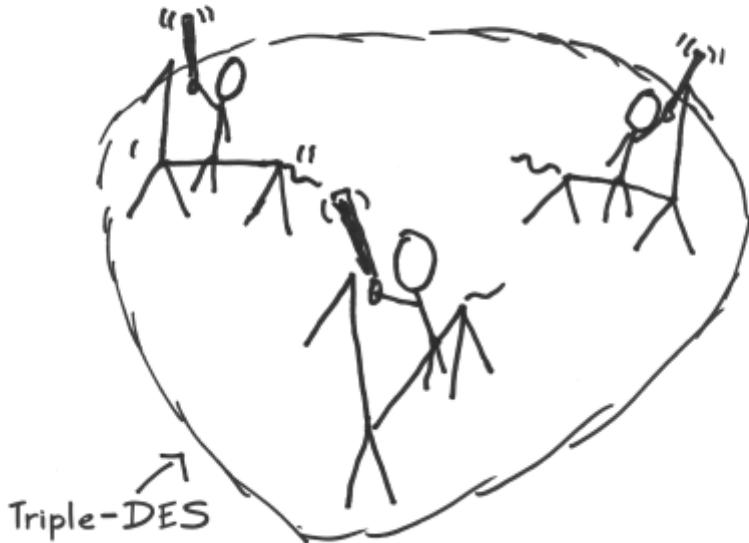
Check out that Feistel network!



Over the years, many attackers challenged DES. He was defeated in several battles.



The only way to stop the attacks was to use DES 3 times in row to form 'Triple-DES.' This worked, but it was awfully slow.



Another decree went out\*...

We need something at least as strong as Triple-DES, but it has to be fast and flexible.

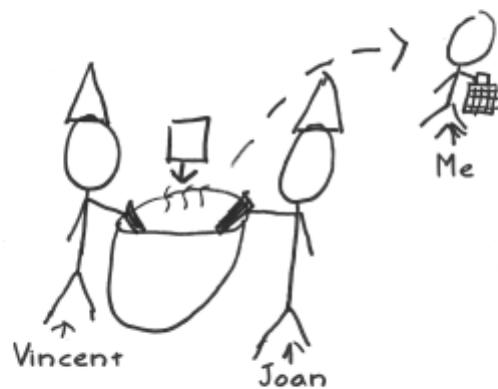


\* ~ early 1997

This call rallied the crypto wizards  
to develop something better.

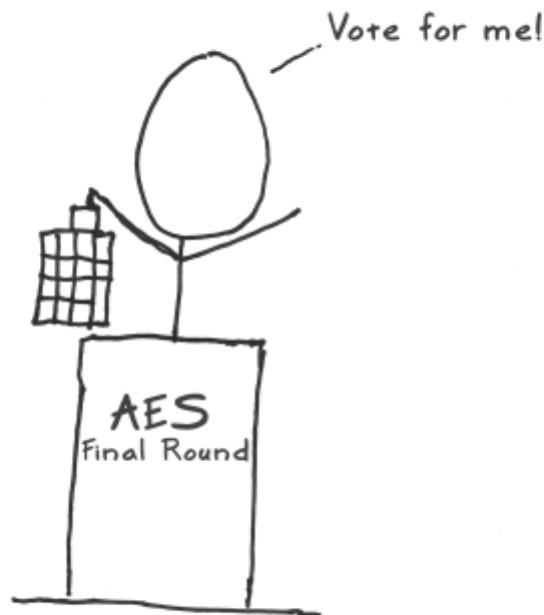


My creators, Vincent Rijmen and Joan Daemen, were among these crypto wizards. They combined their last names to give me my birth name: Rijndael.\*



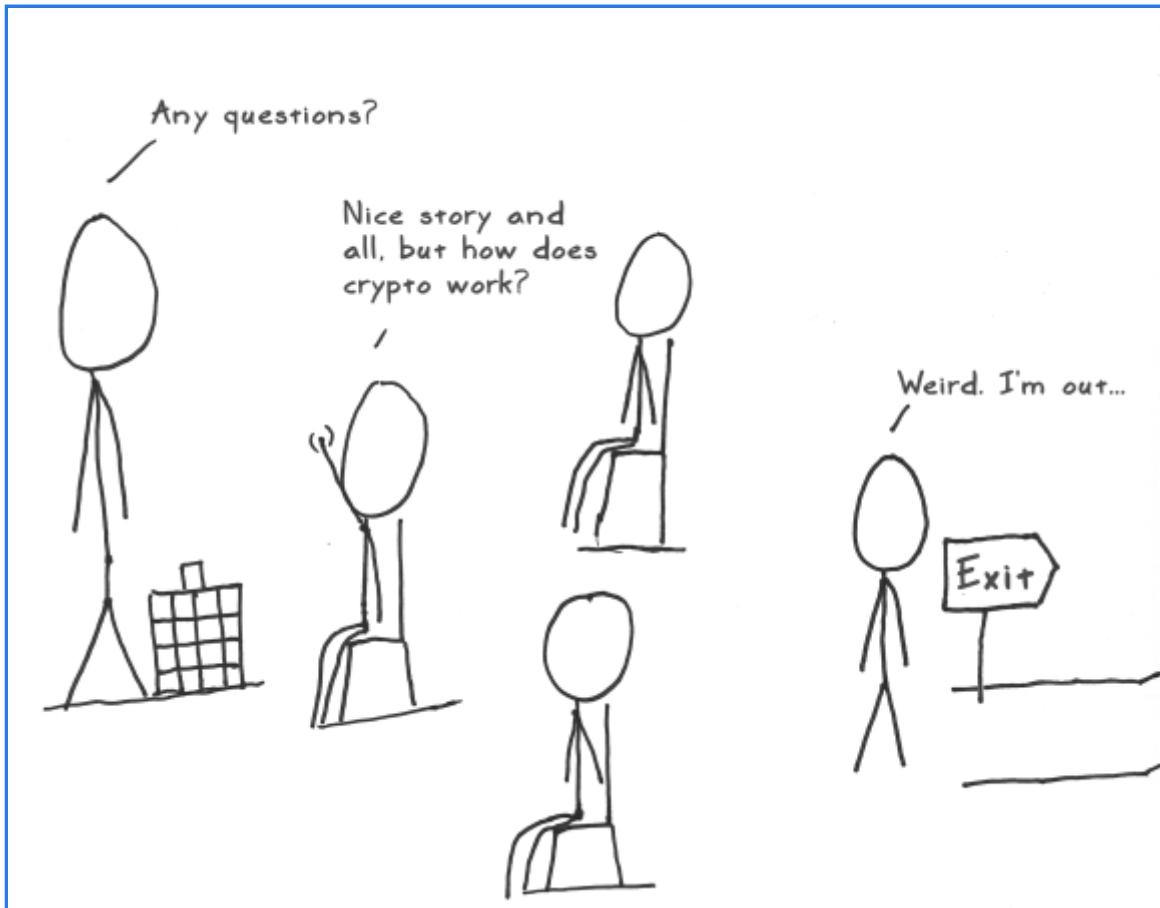
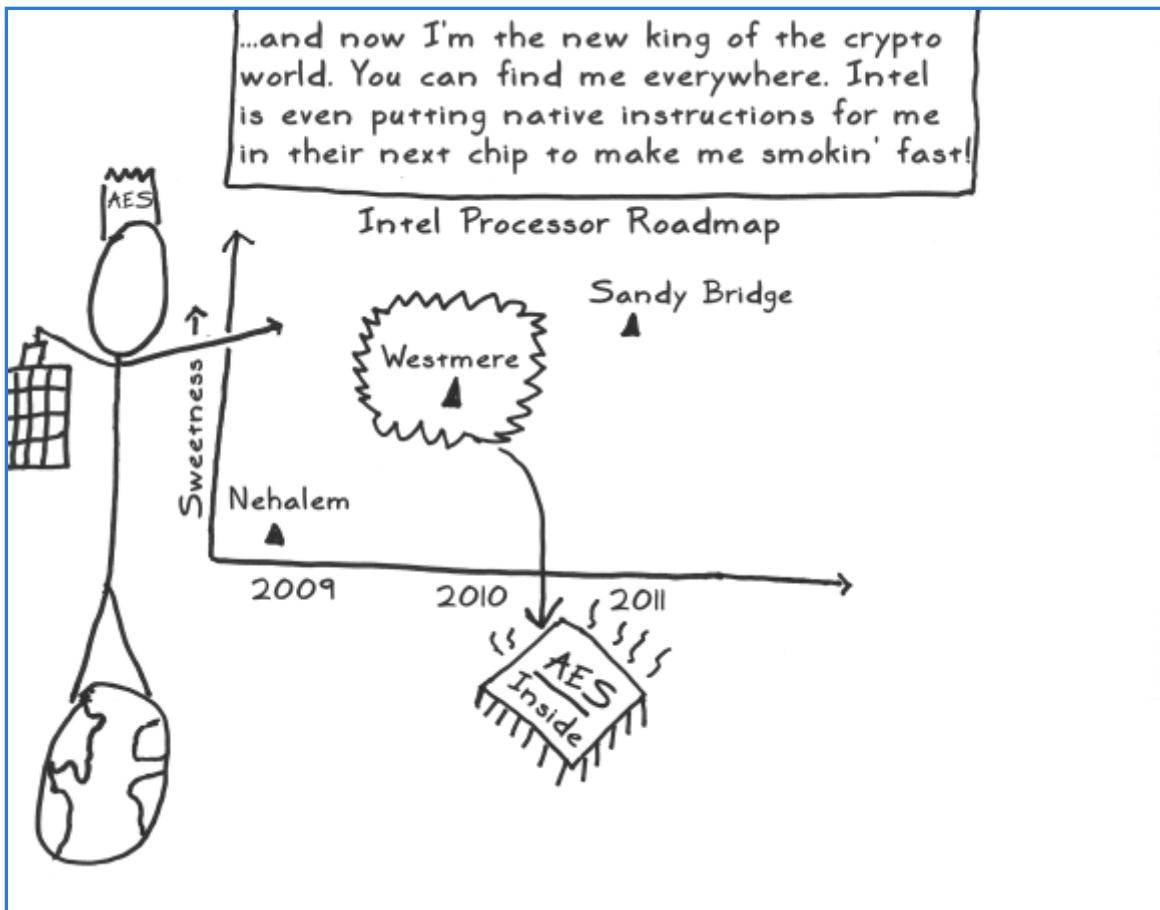
\* That's pronounced 'Rhine Dahl' for the non-Belgians out there.

Everyone got together to vote and...



I won!!

	Rijndael	Serpent	Twofish	MARS	RC6
General Security	2	3	3	3	2
Implementation Difficulty	3	3	2	1	1
Software Performance	3	1	1	2	2
Smart Card Performance	3	3	2	1	1
Hardware Performance	3	3	2	1	2
Design Features	2	1	3	2	1
Total	16	14	13	10	9



# Act 2: Crypto Basics

Great question! You only need to know 3 big ideas to understand crypto.



### Big Idea #1: Confusion

It's a good idea to obscure the relationship between your real message and your 'encrypted' message. An example of this 'confusion' is the trusty ol' Caesar Cipher:

Plaintext: ATTACK AT DAWN
↓ ↓ ↓ ↓ ↓ ↓
Ciphertext: DWWDFTN DW GDZQ
A + 3 letters = D



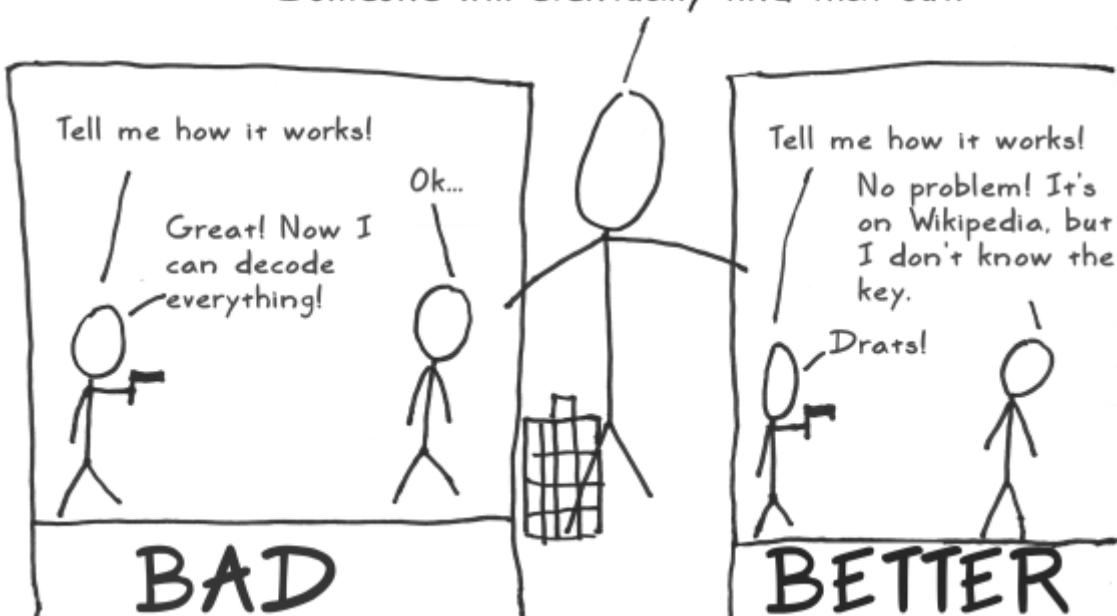
## Big Idea #2: Diffusion

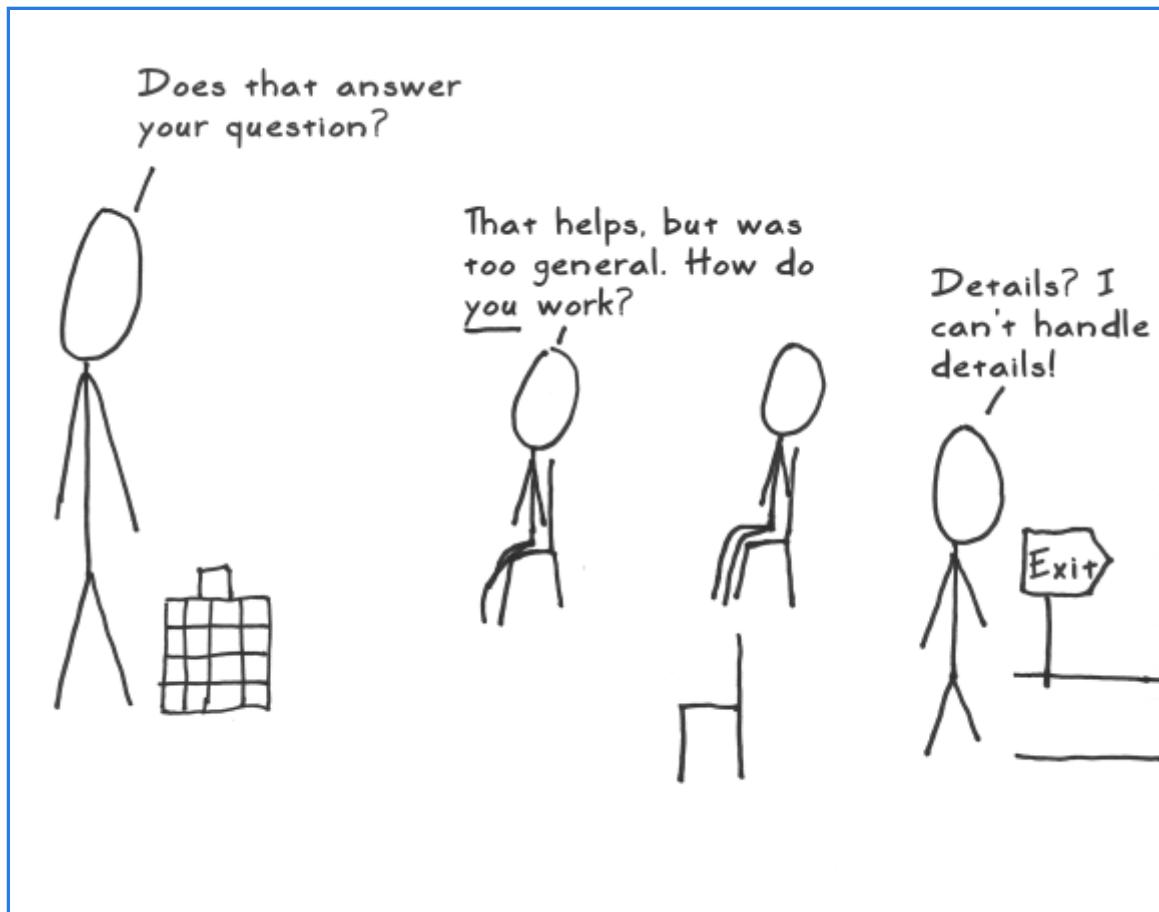
It's also a good idea to spread out the message. An example of this 'diffusion' is a simple column transposition:



## Big Idea #3: Secrecy Only in the Key

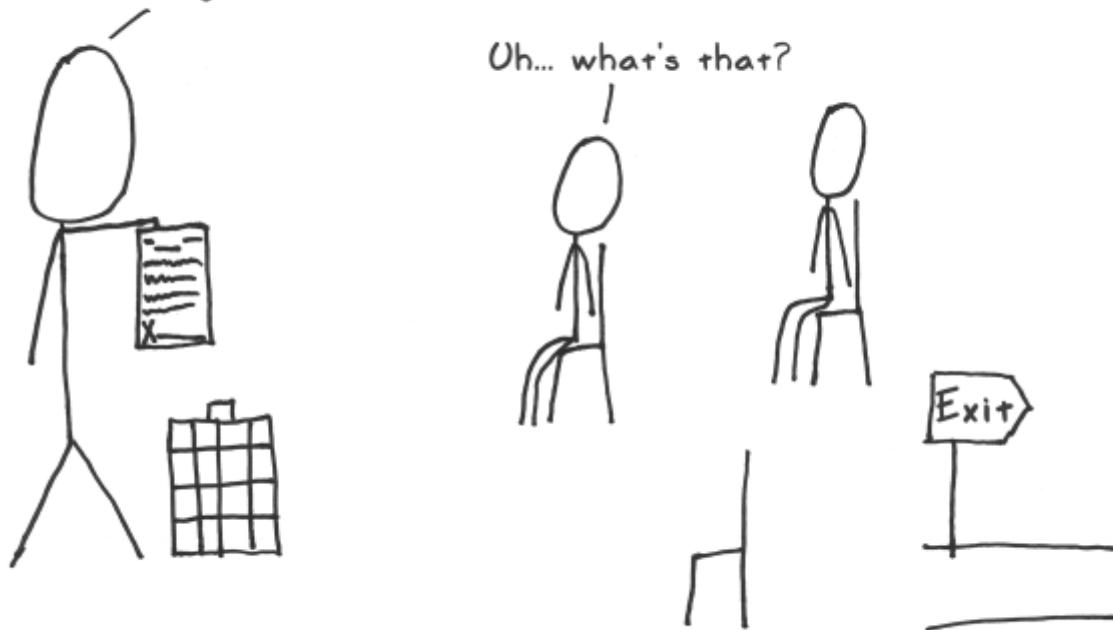
After thousands of years, we learned that it's a bad idea to assume that no one knows how your method works. Someone will eventually find that out.





## Act 3: Details

I'd be happy to tell you  
how I work, but you have  
to sign this first.



## Foot-Shooting Prevention Agreement

I, \_\_\_\_\_, promise that once  
Your Name

I see how simple AES really is, I will  
not implement it in production code  
even though it would be really fun.

This agreement shall be in effect  
until the undersigned creates a  
meaningful interpretive dance that  
compares and contrasts cache-based,  
timing, and other side channel attacks  
and their countermeasures.

\ /



Signature

Date

I take your data and load it  
into this 4x4 square.\*



### ATTACK AT DAWN!

A	C	T	W
T	K		N
T		D	!
A	A	A	O I ↵

Padding at the  
end since it  
wasn't exactly  
16 bytes.

\* This is the 'state matrix' that I carry with me at all times.

The initial round has me xor each input byte with the corresponding byte of the first round key.



A	C	T	W	S				12	63	74	77
T	K	N		O	I	B	K	1b	7a	62	05
T	D	!		M	2	I	E	19	12	0d	64
A	A	A	O	E	8	T	Y	04	79	15	58

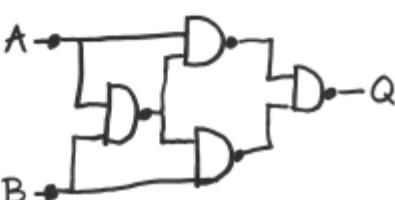
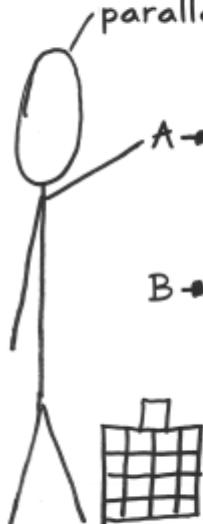


=



### A Tribute to XOR

There's a simple reason why I use xor to apply the key and in other spots: it's fast and cheap – a quick bit flipper. It uses minimal hardware and can be done in parallel since no pesky 'carry' bits are needed.



AES  $\oplus$

## Key Expansion: Part 1

I need lots of keys for use in later rounds. I derive all of them from the initial key using a simple mixing technique that's really fast. Despite its critics,\* it's good enough.



S			
O	I	B	K
M	2	I	E
E	8	T	Y

Initial Key

e1	c1	e1	c1
21	10	52	19
86	b4	fd	b8
f2	ca	9e	c7

#1

...

ae	a6	a0	d4
97	d8	a6	c5
4d	7d	7a	d9
ef	ed	05	06

#9

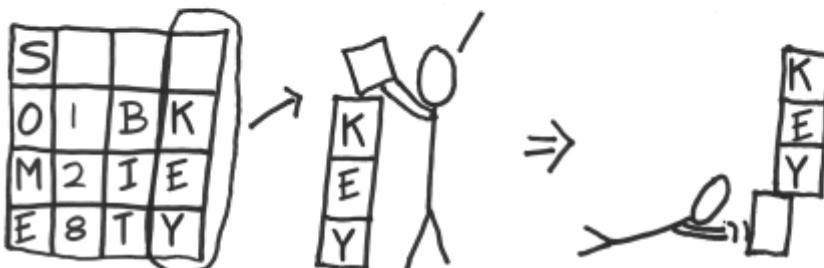
3e	98	38	ec
a2	7a	dc	19
22	5f	25	fc
a7	4a	4f	49

#10

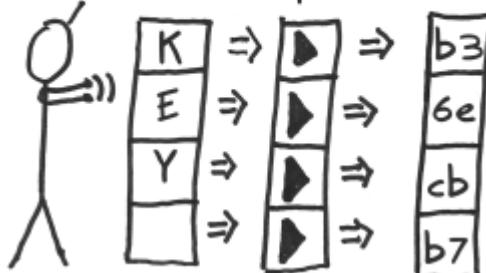
- By far, most complaints against AES's design focus on this simplicity.

## Key Expansion: Part 2a

- I take the last column of the previous round key and move the top byte to the bottom:

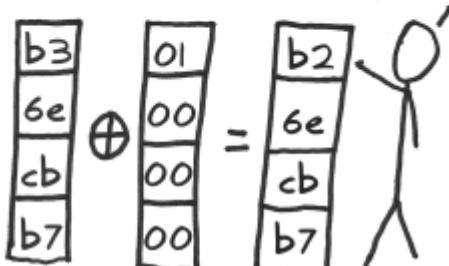


- Next, I run each byte through a substitution box that will map it to something else:

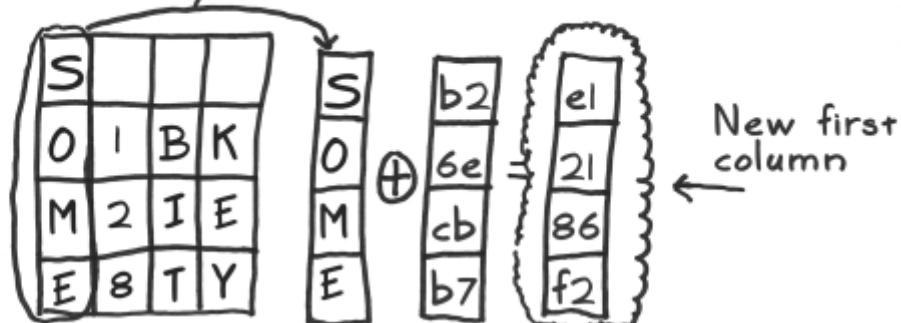


## Key Expansion: Part 2b

- ③ I then xor the column with a 'round constant' that is different for each round.

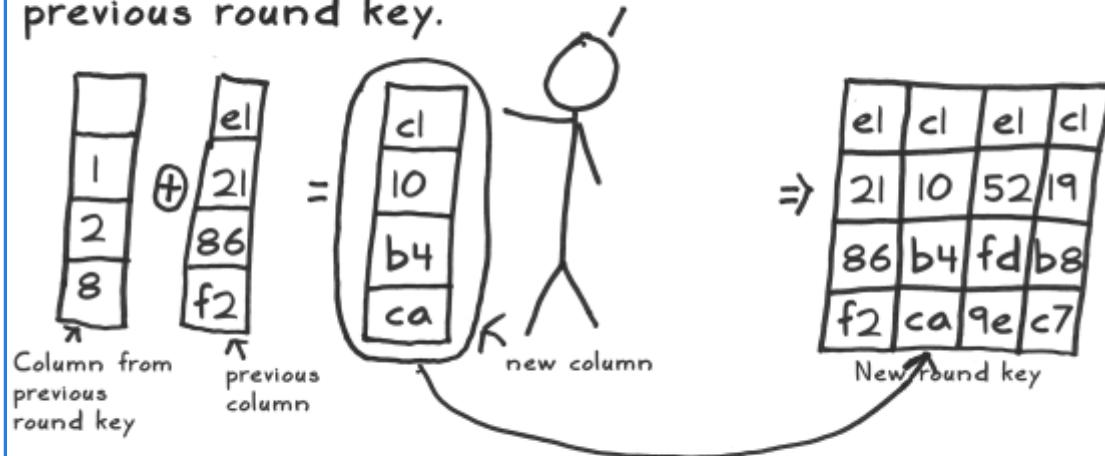


- ④ Finally, I xor it with the first column of the previous round key:



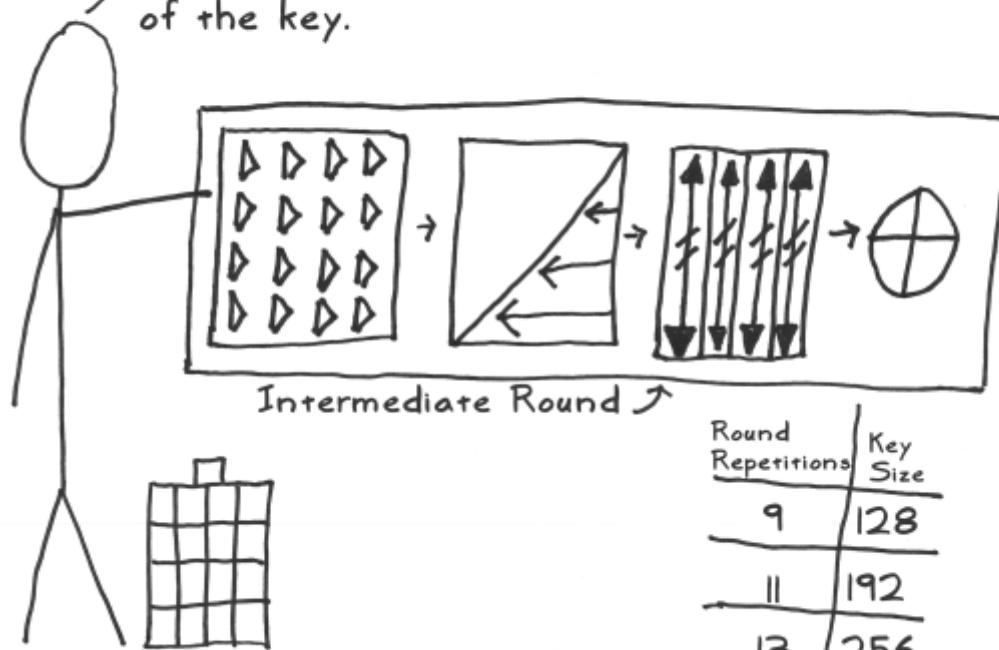
## Key Expansion: Part 3

The other columns are super-easy.\* I just xor the previous column with the same column of the previous round key.



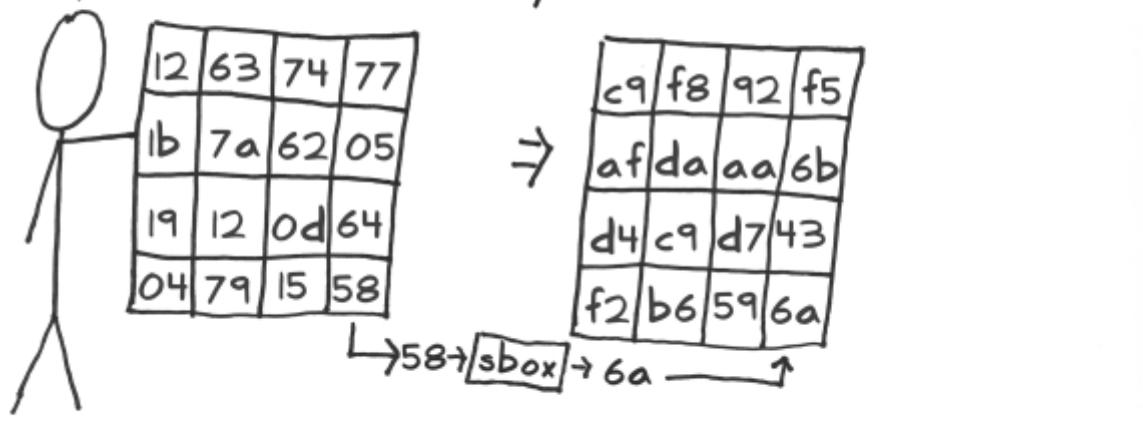
\* Note that 256 bit keys are slightly more complicated.

Next, I start the intermediate rounds. A round is just a series of steps I repeat several times. The number of repetitions depends on the size of the key.



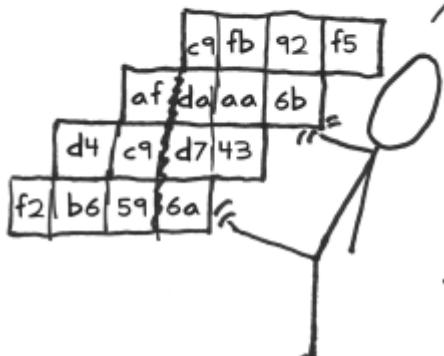
### Applying Confusion: Substitute Bytes

I use confusion (Big Idea #1) to obscure the relationship of each byte. I put each byte into a substitution box (sbox), which will map it to a different byte:

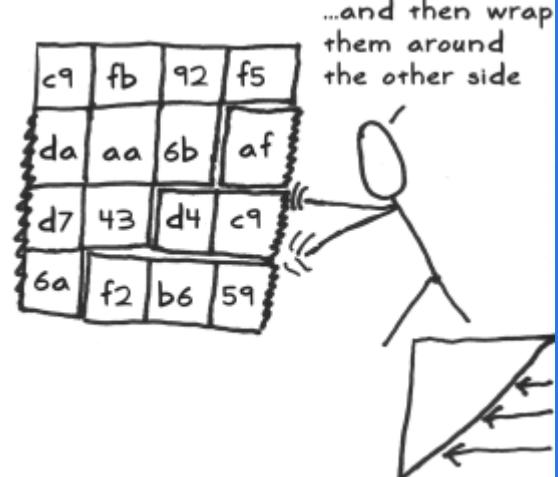


## Applying Diffusion, Part 1: Shift Rows

Next I shift the rows to the left



Hiiiii yaah!



...and then wrap them around the other side

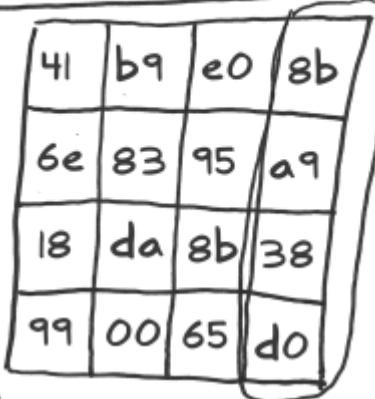


Denotes  
permutation

## Applying Diffusion, Part 2: Mix Columns



I take each column and mix up the bits in it.



## Applying Key Secrecy: Add Round Key



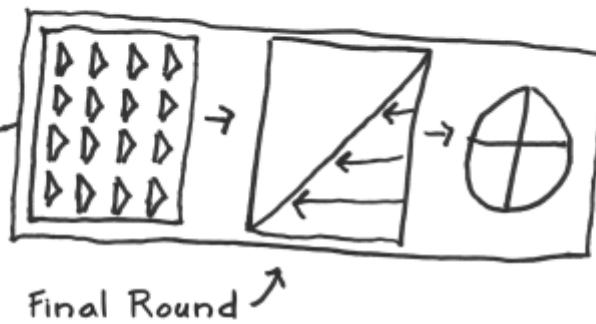
At the end of each round, I apply the next round key with an xor:

$$\begin{array}{|c|c|c|c|} \hline & 41 & b9 & e0 & 8b \\ \hline & 6e & 83 & 95 & a9 \\ \hline & 18 & da & 8b & 38 \\ \hline & 99 & 00 & 65 & d0 \\ \hline \end{array} \oplus \begin{array}{|c|c|c|c|} \hline & e1 & c1 & e1 & c1 \\ \hline & 21 & 10 & 52 & 19 \\ \hline & 86 & b4 & fd & b8 \\ \hline & f2 & ca & 9e & c7 \\ \hline \end{array} = \begin{array}{|c|c|c|c|} \hline & a0 & 78 & 01 & 4a \\ \hline & 4f & 93 & c7 & b0 \\ \hline & 9e & 6e & 76 & 80 \\ \hline & 6b & ca & fb & 17 \\ \hline \end{array}$$

$d0 \oplus c7 = 17$



In the final round, I skip the "Mix Columns" step since it wouldn't increase security\* and would just slow things down:

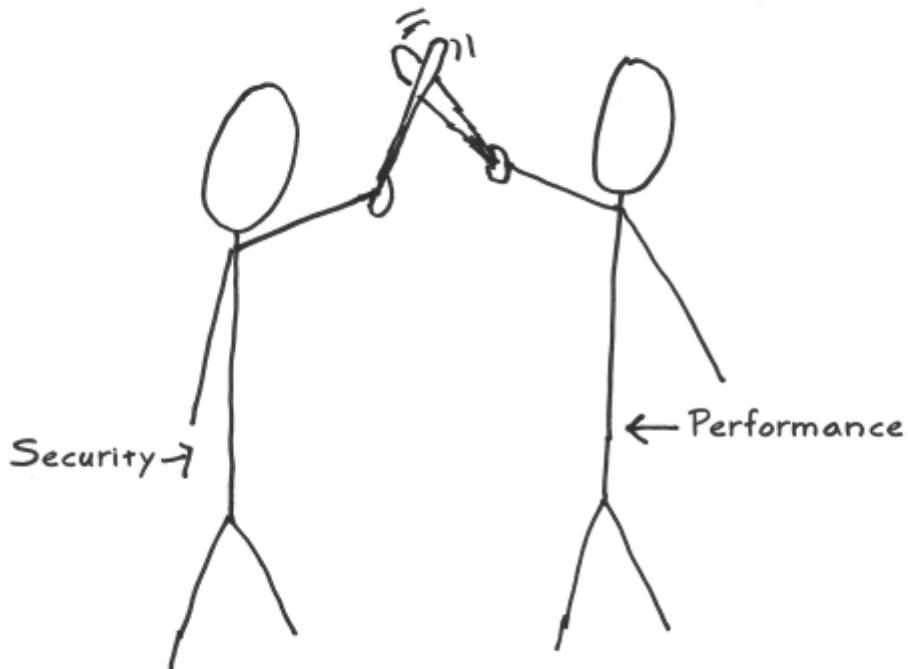


\*The diffusion it would provide wouldn't go to the next round.

...and that's it. Each round I do makes the bits more confused and diffused. It also has the key impact them. The more rounds, the merrier!

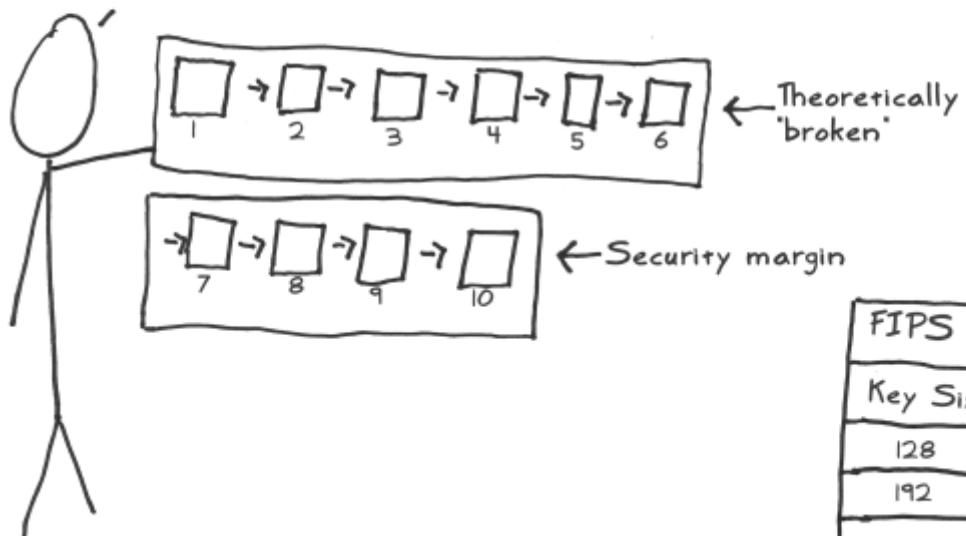


Determining the number of rounds always involves several tradeoffs.



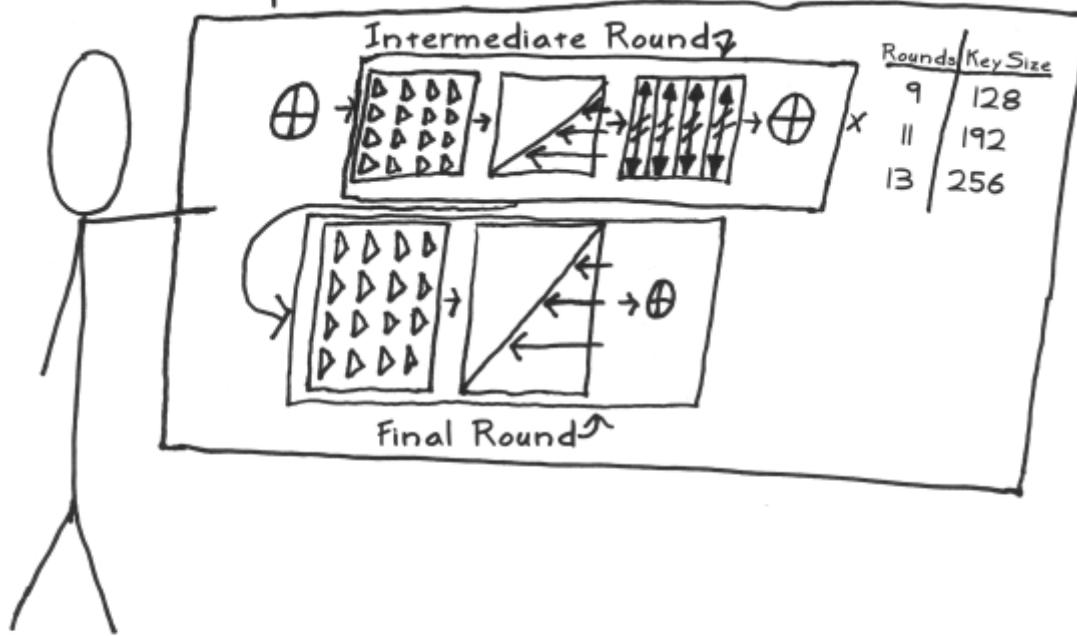
"Security always comes at a cost to performance" - Vincent Rijmen

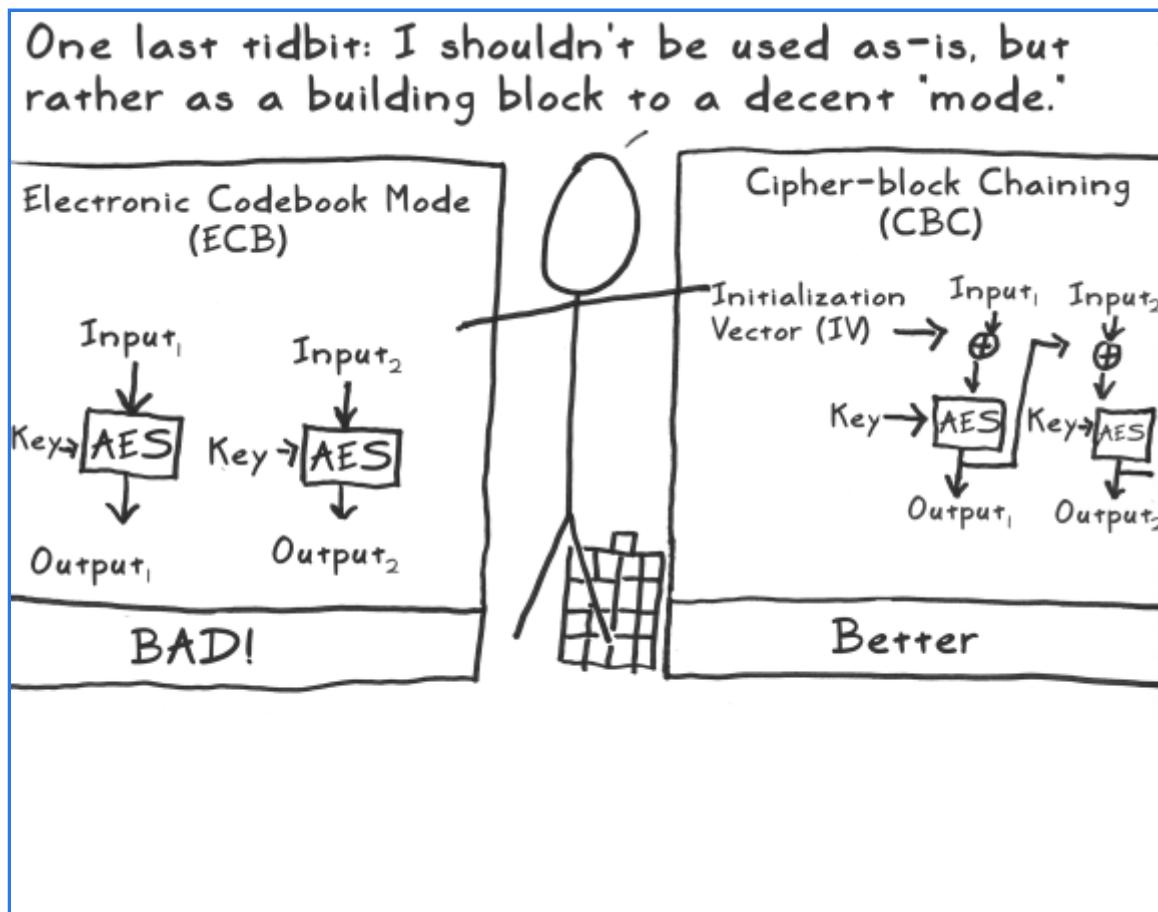
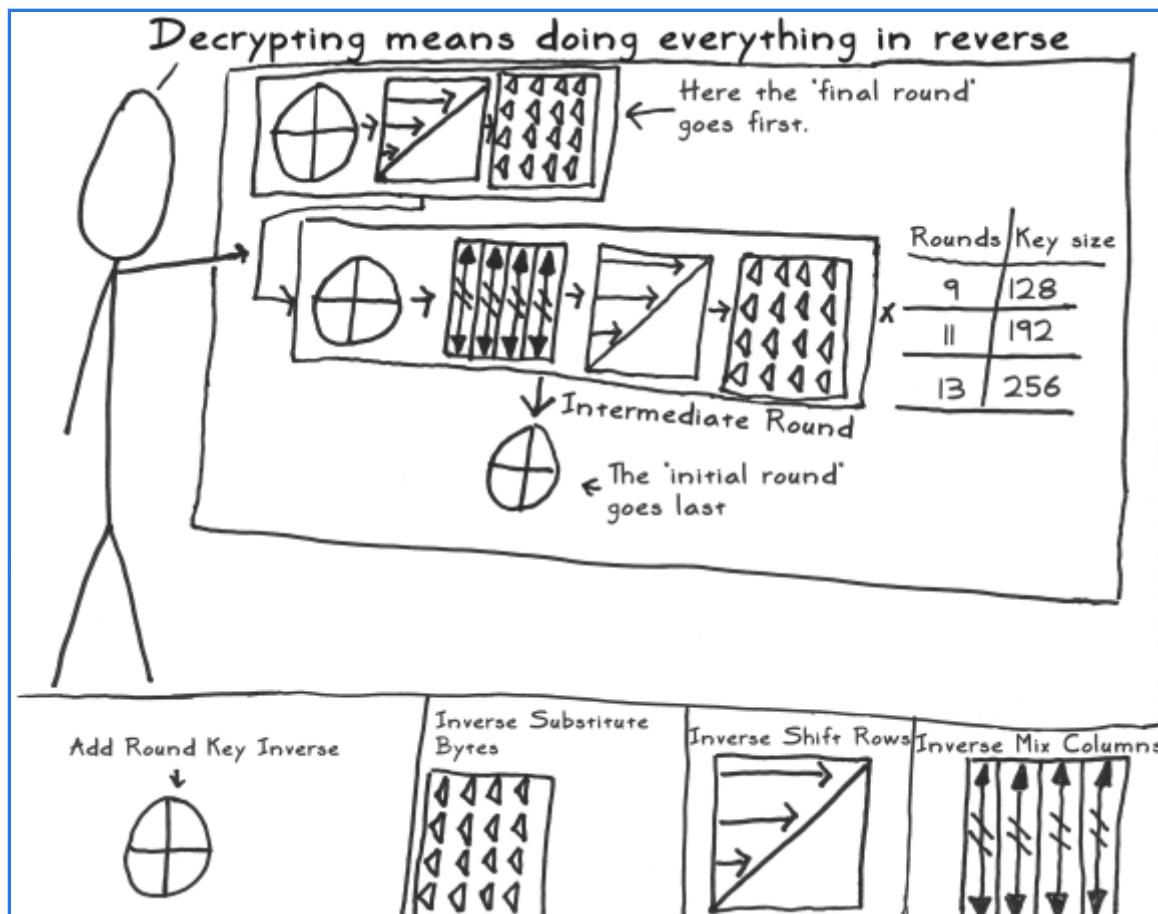
When I was being developed, a clever guy was able to find a shortcut path through 6 rounds. That's not good! If you look carefully, you'll see that each bit of a round's output depends on every bit from two rounds ago. To increase this diffusion 'avalanche,' I added 4 extra rounds. This is my 'security margin.'



FIPS 197 Spec	
Key Size	Rounds
128	10
192	12
256	14

So in pictures, we have this:





Make sense? Did that answer your question?



Almost...except you just waved your hands and used weird analogies. What really happens?



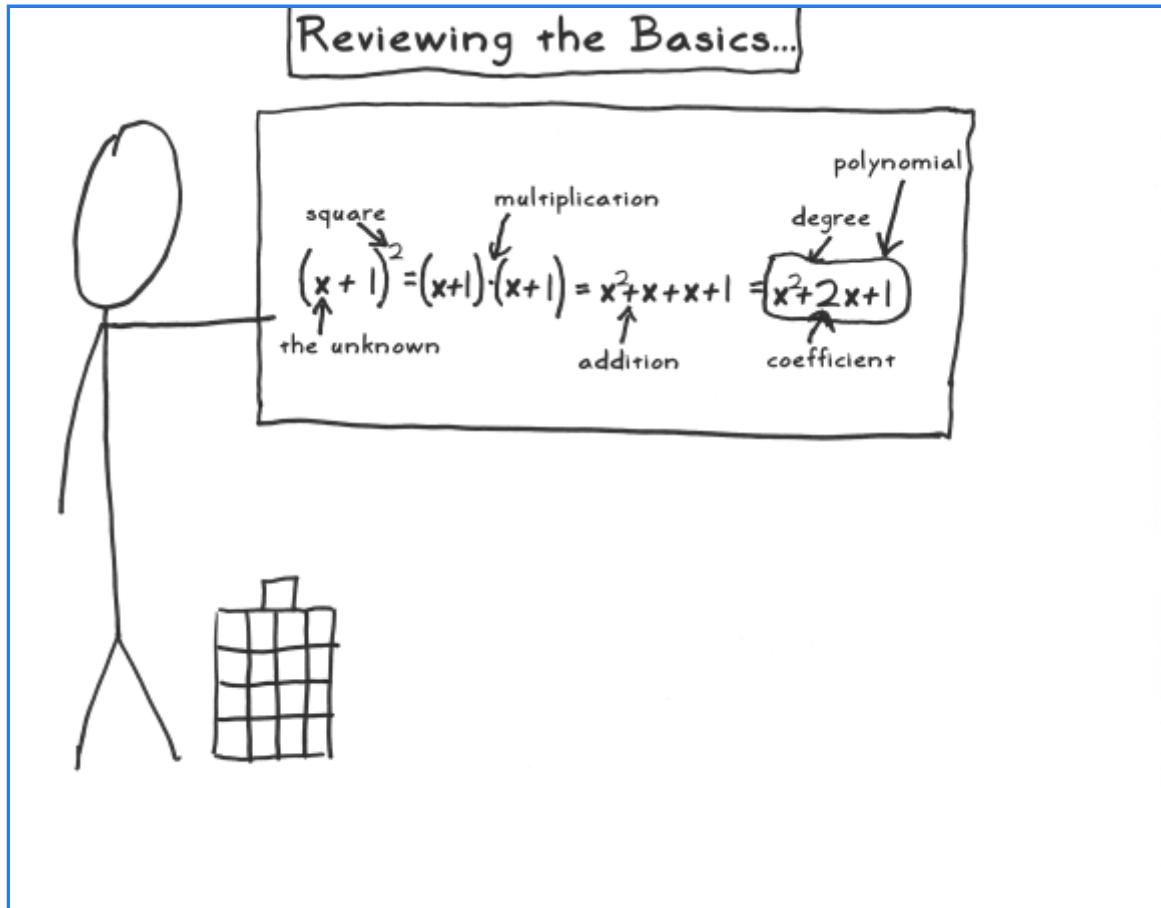
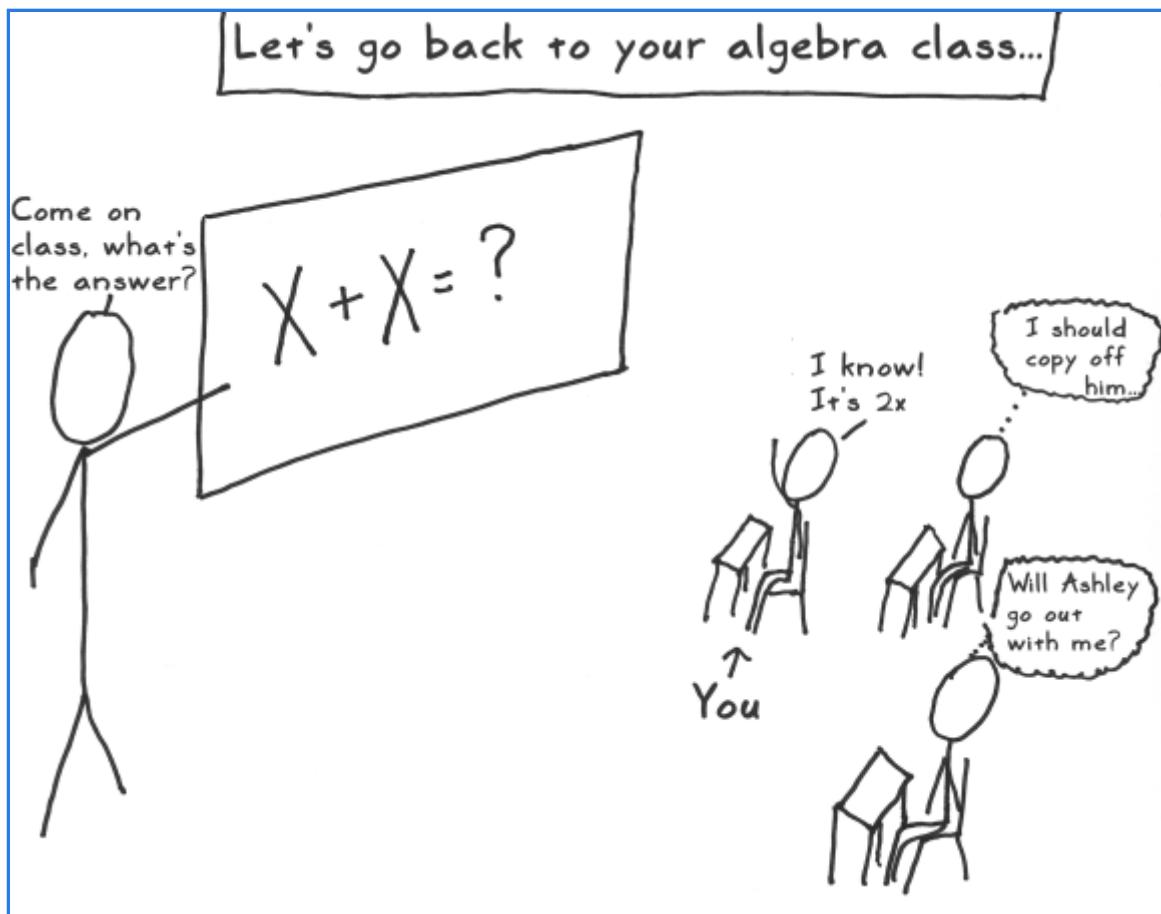
Another great question! It's not hard, but... it involves a little... math.



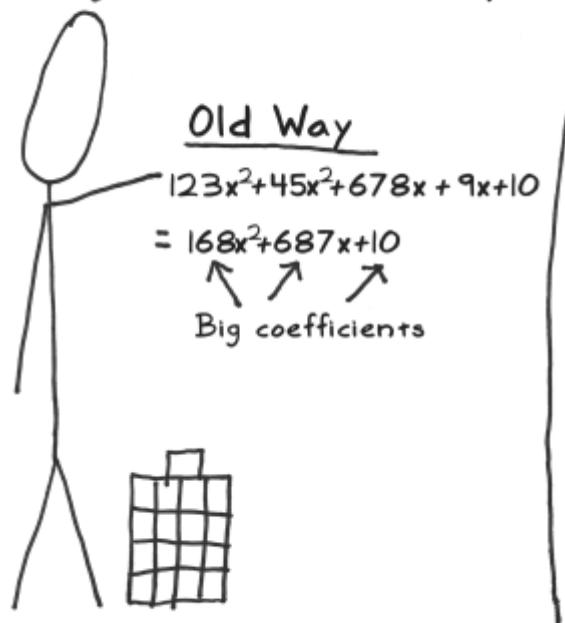
I'm game.  
Bring it on!!



## Act 4: Math!



We'll change things slightly. In the old way, coefficients could get as big as we wanted. In the new way, they can only be 0 or 1:



New Way

$$\begin{aligned} & x^2 \oplus x^2 \oplus x^2 \oplus x \oplus 1 \\ & = x^2 \oplus 1 \quad \text{The 'new' add*} \\ & \qquad \qquad \qquad \uparrow \uparrow \\ & \qquad \qquad \qquad \text{Small coefficients} \\ & x^2 \oplus x^2 \oplus x^2 = (x^2 \oplus x^2) \oplus x^2 \\ & = 0 \oplus x^2 \\ & = x^2 \end{aligned}$$

\*Nifty Fact: In the new way, addition is the same as subtraction (e.g.  $x \oplus x = x - x = 0$ )

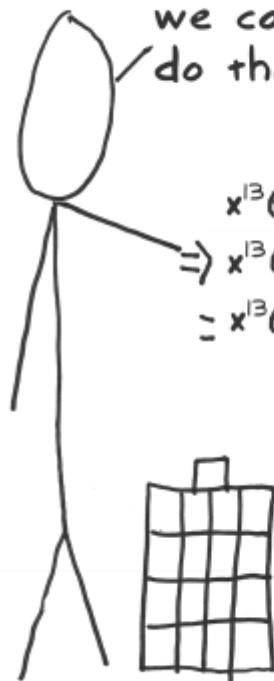
Remember how multiplication could make things grow fast?

$$\begin{aligned} & (x^7 + x^5 + x^3 + x) \cdot (x^6 + x^4 + x^2 + 1) \\ & = x^{7+6} + x^{7+4} + x^{7+2} + x^{7+0} + x^{5+6} + x^{5+4} + x^{5+2} + x^{5+0} \\ & \quad + x^{3+6} + x^{3+4} + x^{3+2} + x^{3+0} + x^{1+6} + x^{1+4} + x^{1+2} + x^{1+0} \\ & = x^{13} + x^{11} + x^9 + x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x^7 + x^5 + x^3 + x \\ & = x^{13} + x^{11} + x^{10} + x^9 + x^8 + x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x \\ & = x^{13} + 2x^{11} + 3x^9 + 4x^7 + 3x^5 + 2x^3 + x \end{aligned}$$

Big and yucky!

With the 'new' addition, things are simpler, but the  $x^{13}$  is still too big. Let's make it so we can't go bigger than  $x^7$ . How can we do that?

$$\begin{aligned} & x^{13} \oplus 2x^{11} \oplus 3x^9 \oplus 4x^7 \oplus 3x^5 \oplus 2x^3 \oplus x \\ \Rightarrow & x^{13} \oplus 0x^{11} \oplus x^9 \oplus 0x^7 \oplus x^5 \oplus 0x^3 \oplus x \\ = & x^{13} \oplus x^9 \oplus x^5 \oplus x \end{aligned}$$



We use our friend, "clock math," to do this. Just add things up and do long division. Keep a close watch on the remainder:

$$4 \text{ o'clock} + 10 \text{ hours} = 2 \text{ o'clock}$$

$$\Rightarrow \text{ (4)} \quad + 10 \text{ hours} = \text{ (2)}$$

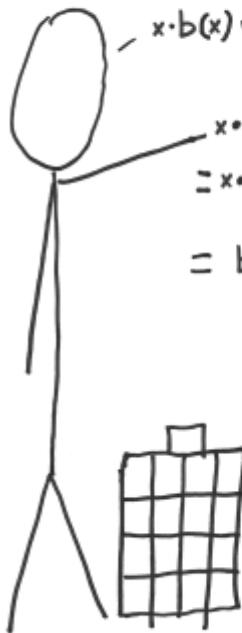
$$\Rightarrow 4 \quad + 10 = 14$$

$$\Rightarrow 12 \overline{)14} \quad \begin{matrix} 1 \\ R(2) \\ 2 \end{matrix}$$



\*This is also known as 'modular addition.' Math geeks call this a 'group.' AES uses a special group called a 'finite field.'

We can do 'clock' math with polynomials. Instead of dividing by 12, my creators told me to use  $m(x) = x^8 \oplus x^4 \oplus x^3 \oplus x \oplus 1$ . Let's say we wanted to multiply  $x \cdot b(x)$  where  $b(x)$  has coefficients  $b_7 \dots b_0$ :



$$x \cdot b(x) \\ = x \cdot (b_7x^7 \oplus b_6x^6 \oplus b_5x^5 \oplus b_4x^4 \oplus b_3x^3 \oplus b_2x^2 \oplus b_1x \oplus b_0)$$

$$= b_7x^8 \oplus b_6x^7 \oplus b_5x^6 \oplus b_4x^5 \oplus b_3x^4 \oplus b_2x^3 \oplus b_1x^2 \oplus b_0x$$

Eek!  $x^8$  is too big. We must make it smaller.

\*Remember that each  $b_n$  (e.g.  $b_7$ ) is either 0 or 1.

We divide it by  $m(x) = x^8 \oplus x^4 \oplus x^3 \oplus x \oplus 1$  and take the remainder:

$$\begin{array}{r} b_7 \\ \hline x^8 \oplus x^4 \oplus x^3 \oplus x \oplus 1 | b_7x^8 \oplus b_6x^7 \oplus b_5x^6 \oplus b_4x^5 \oplus b_3x^4 \oplus b_2x^3 \oplus b_1x^2 \oplus b_0x \\ \oplus \quad b_7x^8 \\ \hline b_6x^7 \oplus b_5x^6 \oplus b_4x^5 \oplus (b_3 \oplus b_7)x^4 \oplus (b_2 \oplus b_7)x^3 \\ \qquad \qquad \qquad \qquad \qquad \qquad \qquad \oplus b_1x^2 \oplus (b_0 \oplus b_7)x \oplus b_7 \end{array}$$

Remainder

$$\rightarrow b_6x^7 \oplus b_5x^6 \oplus b_4x^5 \oplus b_3x^4 \oplus b_2x^3 \oplus b_1x^2 \oplus b_0x \\ \qquad \qquad \qquad \qquad \qquad \qquad \qquad \oplus b_7 \cdot (x^4 \oplus x^3 \oplus x \oplus 1)$$

Note how the b's are shifted left by 1 spot.

This is just  $b_7$  multiplied by a small polynomial.

Now we're ready for the hardest blast from the past: logarithms. After logarithms, everything else is cake! Logarithms let us turn multiplication into addition:



$$\log(x \cdot y) = \log(x) + \log(y)$$

$$\text{So... } \log(10 \cdot 100) = \log(10^1) + \log(10^2) \\ = 2 + 1 = 3$$

In reverse:

$$\begin{aligned} \log^{-1}(1) &= 10^1 = 10 \\ \log^{-1}(2) &= 10^2 = 100 \\ \log^{-1}(3) &= 10^3 = 1,000 \end{aligned}$$

$$\Rightarrow 10 \cdot 100 = 1,000$$

We can use logarithms in our new world. Instead of using 10 as the base, we can use the simple polynomial of  $x \oplus 1$  and watch the magic unravel.\*



$$(x \oplus 1)^1 = x \oplus 1$$

$$(x \oplus 1)^2 = (x \oplus 1)(x \oplus 1) = x^2 \oplus x \oplus x \oplus 1 = x^2 \oplus 1$$

$$(x \oplus 1)^3 = (x \oplus 1)^2 \cdot (x \oplus 1) = x^3 \oplus x^2 \oplus x \oplus 1$$

So...

$$\log_{x \oplus 1}(x \oplus 1) = 1, \log_{x \oplus 1}(x^2 \oplus 1) = 2, \log_{x \oplus 1}(x^3 \oplus x^2 \oplus x \oplus 1) = 3$$



\*If you keep multiplying by  $(x \oplus 1)$  and then take the remainder after dividing by  $m(x)$ , you'll see that you generate all possible polynomials below  $x^8$ . This is very important!

Why bother with all of this math?\* Encryption deals with bits and bytes, right? Well, there's one last connection: a 7<sup>th</sup> degree polynomial can be represented in exactly 1 byte since the new way uses only 0 or 1 for coefficients:



$$\begin{aligned}
 & x^4 \oplus x^3 \oplus x \oplus 1 \\
 = & 0x^7 \oplus 0x^6 \oplus 0x^5 \oplus 1x^4 \oplus 1x^3 \oplus 0x^2 \oplus 1x \oplus 1 \\
 = & \underbrace{0 \quad 0 \quad 0}_{\downarrow} \quad \underbrace{1}_{\downarrow} \quad \underbrace{1 \quad 0 \quad 1}_{\downarrow} \quad \underbrace{1}_{\downarrow} \\
 & 1011_2 = 11_{10} = b_{16} \leftarrow \text{hexadecimal} \\
 = & \mathbf{b} \leftarrow \text{A single byte!}
 \end{aligned}$$

\*Although we'll work with bytes from now on, the math makes sure everything works out.

With bytes, polynomial addition becomes a simple xor. We can use our logarithm skills to make a table for speedy multiplication.\*

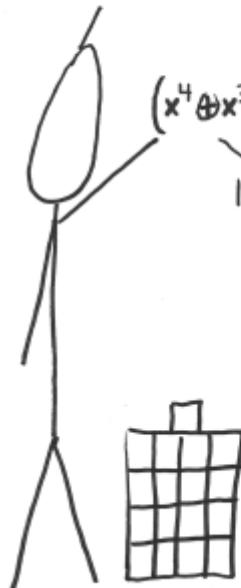


$$\begin{aligned}
 & (x^4 \oplus x^3 \oplus x \oplus 1) \oplus (x^7 \oplus x^5 \oplus x^3 \oplus x) \\
 = & \mathbf{b} \quad \oplus \quad aa \quad \leftarrow \text{byte xor} \\
 = & b1 \\
 = & x^7 \oplus x^5 \oplus x^4 \oplus 1
 \end{aligned}$$
  

$$\begin{aligned}
 & (x^4 \oplus x^3 \oplus x \oplus 1) \cdot (x^7 \oplus x^5 \oplus x^3 \oplus x) \\
 = & \mathbf{b} \quad \cdot \quad aa \quad \text{logarithm table lookup} \\
 \Rightarrow & \log(\mathbf{b}) + \log(aa) = c8 + 1f = e7 \\
 & \qquad \qquad \qquad \text{inverse table lookup} \\
 \Rightarrow & \log^{-1}(e7) = 8c \Rightarrow \mathbf{b} \cdot aa \\
 = & x^7 \oplus x^3 \oplus x^2
 \end{aligned}$$

\*We can create the table as we keep multiplying by  $(x \oplus 1)$ .

Since we know how to multiply, we can find the 'inverse' polynomial byte for each byte. This is the byte that will undo/invert the polynomial back to 1. There are only 255\* of them, so we can use brute force to find them:



$$(x^4 \oplus x^3 \oplus x \oplus 1) \cdot ? = 1$$

$$1b \cdot cc = 1$$

found using a brute force for-loop

\*There are only 255 instead of 256 because 0 has no inverse.

Now we can understand the mysterious s-box. It takes a byte 'a' and applies two functions. The first is 'g' which just finds the byte inverse. The second is 'f' which intentionally makes the math uglier to foil attackers.



$$g(a) = a^{-1}$$

$$f(a) = \begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 0 \\ 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 \end{bmatrix} \cdot \begin{bmatrix} a_7 \\ a_6 \\ a_5 \\ a_4 \\ a_3 \\ a_2 \\ a_1 \\ a_0 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$\text{sbox}[a] = f(g(a))$$

$$\text{sbox}[58] = f(g(58))$$

$$\text{sbox}[58] = f(18) = 6a$$

$$58 \cdot 18 = 01$$

We can also understand those crazy round constants in the key expansion. I get them by starting with '1' and then keep multiplying by 'x':

01
00
00
00

02
00
00
00

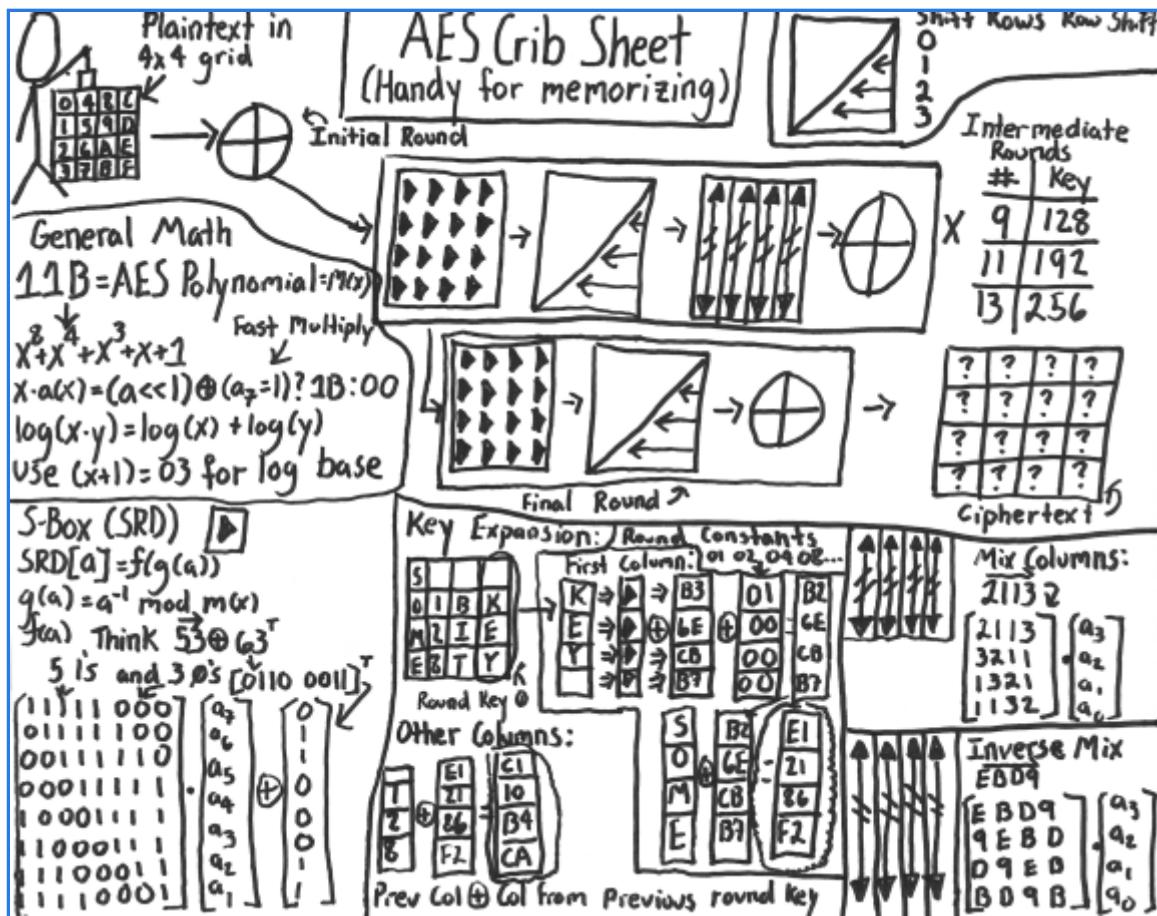


01	02	04	08	10	20	40	80	1b	36
00000000	00	000000	000000	000000	000000	000000	000000	000000	000000
00000000	00	000000	000000	000000	000000	000000	000000	000000	000000
00000000	00	000000	000000	000000	000000	000000	000000	000000	000000

First 10 round constants

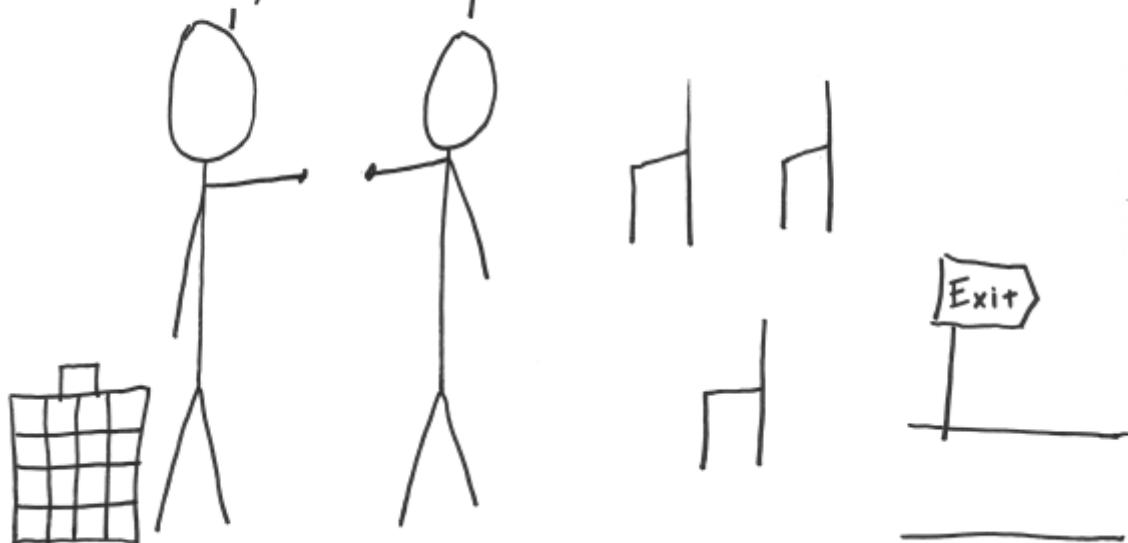
Mix Columns is the hardest. I treat each column as a polynomial. I then use our new multiply method to multiply it by a specially crafted polynomial and then take the remainder after dividing by  $x^4 + 1$ . This all simplifies to a matrix multiply:

$$\begin{aligned}
 & \text{Matrix } \rightarrow \begin{array}{|c|c|c|c|} \hline & a_3 & a_2 & a_1 & a_0 \\ \hline \end{array} \quad b(x) = c(x) \cdot a(x) \bmod x^4 + 1 \\
 & = (03x^3 + 01x^2 + 01x + 02) \cdot (a_3x^3 + a_2x^2 + a_1x + a_0) \bmod x^4 + 1 \\
 & \quad \text{special polynomial} \qquad \qquad \qquad \text{the column} \\
 & = x^4 + 1 \quad \frac{03a_3 \cdot x^2 + (3a_2 + a_3)x + (3a_1 + a_2 + a_3)}{03a_3x^6 + 03a_2x^5 + 03a_1x^4 + 03a_0x^3 + 01a_3x^5 + 01a_2x^4 + 01a_1x^3 + 01a_0x^2} \\
 & \quad + 01a_3x^4 + 01a_2x^3 + 01a_1x^2 + 01a_0x + 02a_3x^3 + 02a_2x^2 + 02a_1x + 02a_0 \\
 & \oplus \frac{03a_3x^6 + 03a_3x^2}{3a_2x^5 + 3a_1x^4 + 3a_0x^3 + a_3x^5 + a_2x^4 + a_1x^3 + a_0x^2 + a_3x^4 + a_2x^3 + a_1x^2 + a_0x + 2a_3x^3} \\
 & \oplus \frac{3a_2x^5 + a_3x^5 + 3a_2x + a_3x}{3a_1x^4 + 3a_0x^3 + a_2x^4 + a_1x^3 + a_0x^2 + a_3x^4 + a_2x^3 + a_1x^2 + a_0x + 2a_3x^3} \\
 & \oplus \frac{3a_1x^4 + 3a_0x^3 + a_2x^4 + a_1x^3 + a_0x^2 + a_3x^4 + a_2x^3 + a_1x^2 + a_0x + 2a_3x^3}{(3a_3 + a_2 + a_1 + a_0)x^4 + (3a_3 + a_2 + a_1 + a_0)} \\
 & \oplus \frac{(2a_3 + a_2 + a_1 + a_0)x^3 + (3a_3 + 2a_2 + a_1 + a_0)x^2}{\begin{bmatrix} 2 & 1 & 1 & 3 \\ 3 & 2 & 1 & 1 \\ 1 & 3 & 2 & 1 \\ 1 & 1 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} a_3 \\ a_2 \\ a_1 \\ a_0 \end{bmatrix}} = \begin{bmatrix} b_3 \\ b_2 \\ b_1 \\ b_0 \end{bmatrix}
 \end{aligned}$$

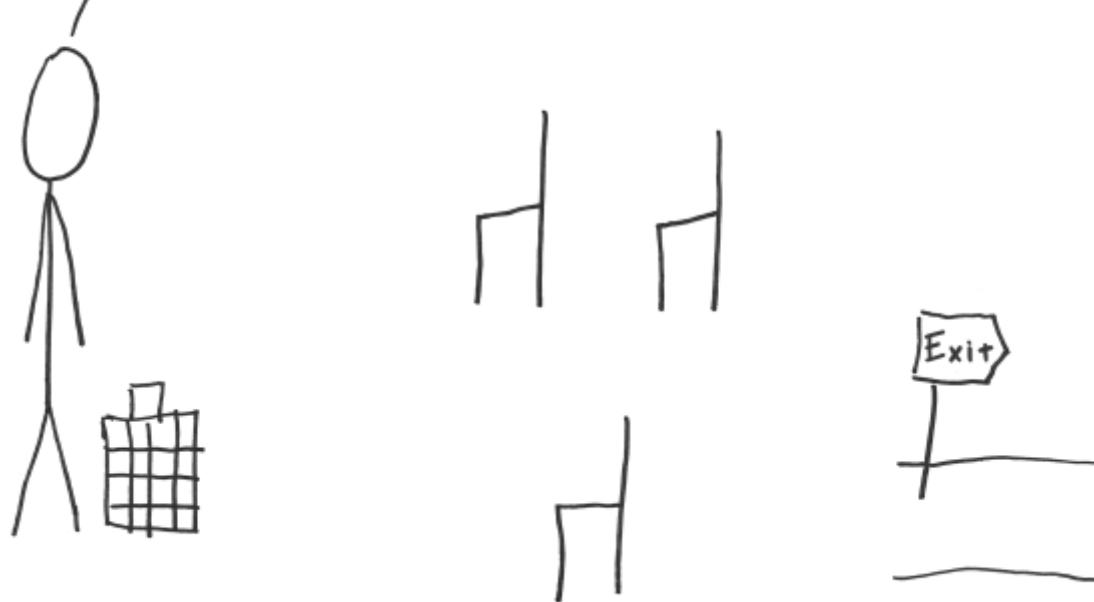


Whoa... I think I get it now. It's relatively simple once you grok the pieces. Thanks for explaining it. I gotta go now.

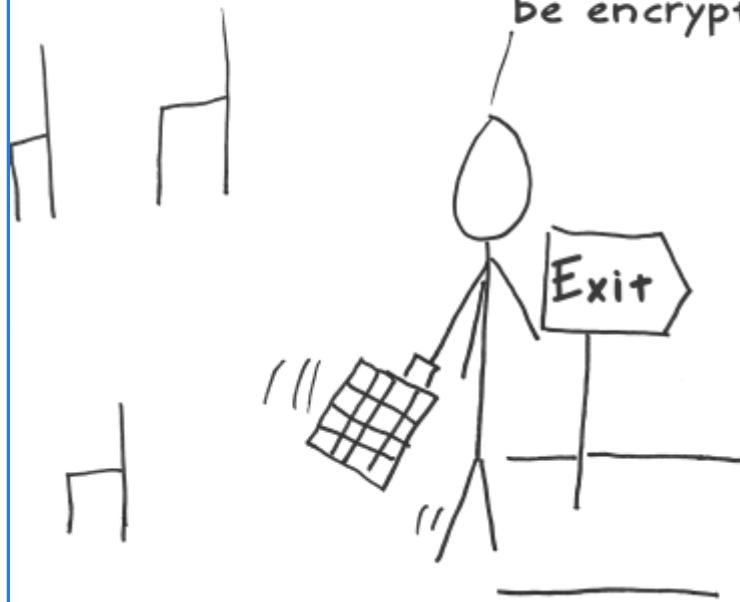
My pleasure.  
Come back anytime!

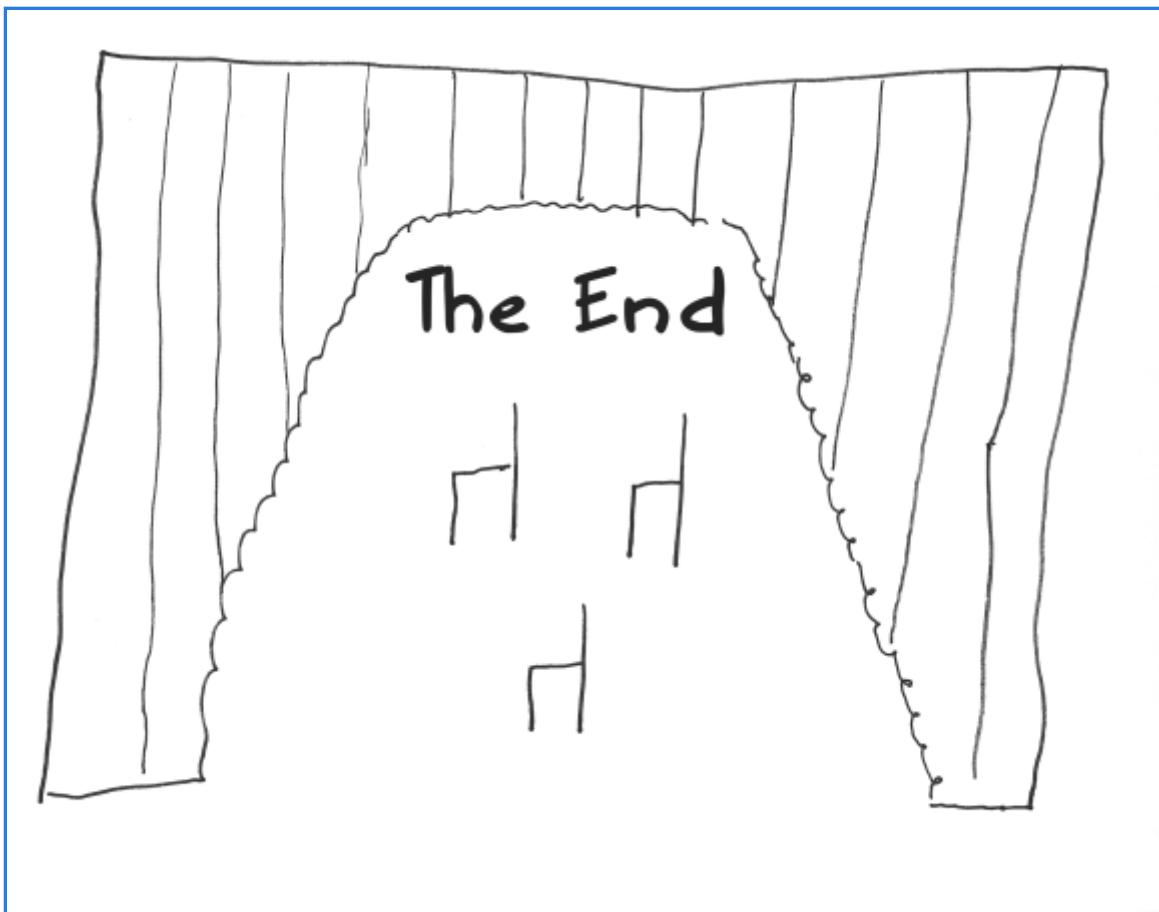


But there's so much more to talk about: my resistance to linear and differential cryptanalysis, my Wide Trail Strategy, impractical related-key attacks, and... so much more... but no one is left.



Oh well... there's some boring router traffic that needs to be encrypted. Gotta go!

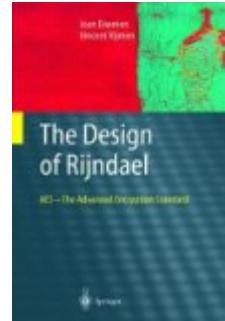




## Epilogue

I created a heavily-commented AES/Rijndael implementation to go along with this post and [put it on GitHub](#). In keeping with the Foot-Shooting Prevention Agreement, it shouldn't be used for production code, but it should be helpful in seeing exactly where all the numbers came from in this play. Several resources were useful in creating this:

- [The Design of Rijndael](#) is *the* book on the subject, written by the Rijndael creators. It was helpful in understanding specifics, especially the math (although some parts were beyond me). It's also where I got the math notation and graphical representation in the left and right corners of the scenes describing the layers ([SubBytes](#), [ShiftRows](#), [MixColumns](#), and [AddRoundKey](#)).
- The [FIPS-197](#) specification formally defines AES and provides a good overview.
- [The Puzzle Palace](#), especially [chapter 9](#), was helpful while creating Act 1. For more on how the NSA modified DES, see [this](#).
- More on Intel's (and now AMD) inclusion of native AES instructions can be found [here](#) and in detail [here](#). - Other helpful resources include [Wikipedia](#), [Sam Trenholme's AES math series](#), and [this animation](#).



Please leave a comment if you notice something that can be better explained.

**Update #1:** Several scenes were updated to fix some errors mentioned in the comments.

**Update #2:** By request, I've created a slide show presentation of this play in both [PowerPoint](#) and [PDF](#) formats. I've licensed them under the [Creative Commons Attribution License](#) so that you can use them as you see fit. If you're teaching a class, consider giving extra credit to any student giving a worthy interpretive dance rendition in accordance with the Foot-Shooting Prevention Agreement.

241 Comments    Moserware

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**Anonymous** • 7 years ago

Should be be in the preface of CS cryptography textbooks! Terrific

2 ⤵ | ⤴ • Reply • Share ↗



**Gidz Paul** • a month ago

Awesome.. :o

^ | ⤴ • Reply • Share ↗



**Walter Zambotti** • 2 months ago

Very nice. Did I miss where in the presentation you display the final encrypted text???

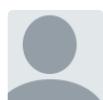
^ | ⤴ • Reply • Share ↗



**netdeamon** • 6 months ago

Cool !!! Keep it up!

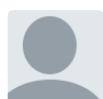
^ | ⤴ • Reply • Share ↗



**Felipe S Mattos** • 8 months ago

this is rocksome! very nice work!

^ | ⤴ • Reply • Share ↗



**assignment writing** • 8 months ago

It's actually a good work that you have shared which covers up some topics about that kind of subject that was being tackled in school for those students who studies in the field of engineering. Through this, they can learn something that they will going to use as their guide.

^ | ⤴ • Reply • Share ↗



**Benjamin Barenblat** • a year ago

A minor error in part 2, scene 11: entry 6 of the right block should read 'ff' not 'fo'. This



A minor error in act 5, scene 11: entry  $a_{01}$  of the right block should read 10, not 10. (This has already been corrected in scenes 12 and 13.)

[^](#) [v](#) • Reply • Share



**Adam M. Erickson** • 3 years ago

This should be in CS and ISM textbooks. A+ Moser.

[^](#) [v](#) • Reply • Share



**Kevin** • 3 years ago

Thanks man!! :)

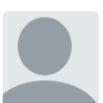
[^](#) [v](#) • Reply • Share



**Raymond Starkey** • 3 years ago

**Talent, talent, talent, talent.** Art - must try harder.

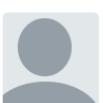
[^](#) [v](#) • Reply • Share



**Theuns Alberts** • 3 years ago

Brilliantly explained! And thanks for the effort with the accompanied code.

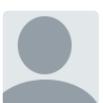
[^](#) [v](#) • Reply • Share



**Todd** • 3 years ago

Awesome. But where is the part where the NSA builds in a back door to circumvent all the cryptology?

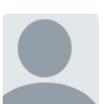
[^](#) [v](#) • Reply • Share



**Anonymous** • 3 years ago

was fun.....gr8.....learning it and signng the letter....

[^](#) [v](#) • Reply • Share



**Anonymous** • 4 years ago

Can't figure out if ALL these have any relation at all with this one:

"The key to this encryption rule is given by two numbers  $n$  and  $r$ . The number  $n$  is chosen in a very particular way:  $n$  is the product of two primes  $p$  and  $q$ , where  $n$  is the product of two primes  $p$  and  $q$ . To encrypt  $x$  we just compute:  $y = x^r \pmod{n}$ .

The decryption then works via a simple formula, analogous to the encryption: we compute  $y^s \pmod{n}$ .

Suppose we choose  $n = p * q = 29 * 37 = 1073$ . Let's take  $r = 25$  with this choice of  $n$  and  $r$ , the choice  $s = 121$  is an appropriate decryption key...

The decryption illustrated on the previous page is possible because  $r$  and  $s$  have a very special relationship. With  $p = 29$ , and  $q = 37$ , we compute:

$m = (p-1) * (q-1) = 1008$  and then we have chosen  $r$  and  $s$  so that:

$r * s = 25 * 121 = 3025 = 1 \pmod{m}$ ..."

Link: [http://web.math.princeton.edu/...](http://web.math.princeton.edu/)

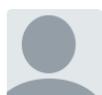
[^](#) [v](#) • Reply • Share

[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**Cường Đặng Đình** • 4 years ago

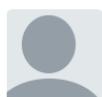
thanks very much!!!!!!

[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**Trung Le** • 4 years ago

That was a really good work you have done! Helped me a ton to understand AES in a visual way. Keep it up!

[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**KF** • 4 years ago

Thank you for your awesome job... really let me understand much. This is fun too. Appreciate it very much.

[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**Jeff Moser** • 4 years ago

Thanks everyone for the kind feedback!

**Anonymous:** For details about being resistant to cryptanalysis, I recommend reading [the book](#) but it's quite a bit more complicated than this comic. Perhaps try [the Wikipedia page](#). Regarding modes, [Wikipedia's page on it](#) is pretty good.[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**Charulatha Jain** • 4 years ago

Its an awesome presentation and quite helpful for beginners to understand the concepts.

Thank you for the awesome presentation.

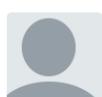
[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**Anonymous** • 4 years ago

This is one of the most superb explanations of AES I've ever seen. So easy to understand, it's brilliant. But I'd love to know more about the resistance to cryptanalysis, I understand what it is but I have no idea how AES resists it. Plus I'd like to know more about the various "modes" you touched on!

In summary: encore!

[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**durdave** • 4 years ago

Great! But I'm still left with the question "Will Ashley go out with me?" Maybe if I get a Ferrari?

[^](#) [|](#) [v](#) [• Reply](#) [• Share](#) [›](#)**Anonymous** • 4 years ago

Superb. Keep it up Brother.

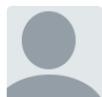
^ | v · Reply · Share >



**Anonymous** · 4 years ago

Amazing would be an understatement!

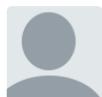
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**naveregnide** · 5 years ago

Hey! Just stopping by to say that this lovely comic really helped me understand AES a lot more. Such a great sense of humour used in it too! Thanks!

^ | v · Reply · Share >



**Jeff Moser** · 5 years ago

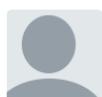
Thanks everyone for the kind feedback over the years.

Special thanks to [txipxi](#) for the Spanish translation.

**Vincent:** For details on how all S-Box values are calculated, follow along with [the S-Box demonstration section](#) my example program and the [f\(x\)](#) and [g\(x\)](#) section as well. For even more details, see how [I implemented f and g](#). Note specifically how "f" is a multiply then an add/xor. Each bit of the result of the multiply is obtained through 8 boolean multiplies/ands.

Hope that helps!

^ | v · Reply · Share >

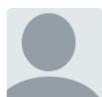


**Vincent** · 5 years ago

Hi Jeff, is it possible to show your working on  $f(\{18\})=\{6a\}$ ? I have been trying to work out the rotational matrix part but still getting the answer wrong. Did you sum up all the 8 rows of multiplication before you XOR with  $\{63\}$ ?

Is it possible can anyone show the working for multiple inverse for  $\{58\}$  is  $\{18\}$ ?

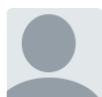
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**Krishnaprasad** · 5 years ago

This is great.. lot of effort to explain, very easy to understand!! awesome..

^ | v · Reply · Share >



**Anonymous** · 5 years ago

Wonderful! Great work!

Makes understanding AES a lot of fun!

Genius!

^ | v · Reply · Share >



**txipxi** · 5 years ago

Awesome!!!

My humble contribution to your great work, a Spanish translation:

<http://www.slideshare.net/txip...>

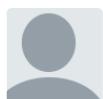
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**The Grey Man** · 5 years ago

WOW. Thanks for the excellent, amusing and visual run down on AES.

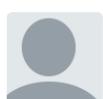
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**SherryL** · 5 years ago

Wow, it's great to explain the AES this way. I've tried much to understand AES before I found this. BRAVO! Thanks!

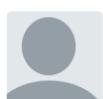
^ | v · Reply · Share ·



**Anonymous** · 5 years ago

I would like to read more like this..it was a fun way of learning for an adult.

^ | v · Reply · Share ·



**Anonymous** · 5 years ago

Thanks for this.

^ | v · Reply · Share ·

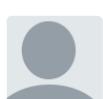


**Jeff Moser** · 5 years ago

**20 box:** It's a decent book if you want a very academic overview of AES. It was a bit *too* academic for my tastes and was one of the reasons why I created this post.

If you're looking for a more hands-on/pragmatic understanding of AES, I'd recommend you just read and understand the source code that I included with this post.

^ | v · Reply · Share ·



**20 box** · 5 years ago

Is that book you recommended is good? I am considering buying it here in India but it is too costly a book for Indian standards and is not available on local markets.. so have to buy it from amazon or something.. but too costly..

Just want to know if it is worth \$100 or not? as it would be the price for me including shipping...

^ | v · Reply · Share ·



**Sandoval** · 5 years ago

wow!

99.9% of comp professionals never can talk in simple English; BUT you've just proved that you are the 0.1%!

^ | v · Reply · Share ·



&lt;Martani/&gt; Fakhrou • 6 years ago

Totally awesome,

this is gonna help me in my crypto exam tomorrow :D

^ | v · Reply · Share ›

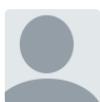


arun • 6 years ago

hey man..a very well explained..good job..

well m also working on AES and m really a bad prograamer..My work is with Equivalent Inverse Cipher have you worked on it...got nay code of it????It's really urgent.....pls

^ | v · Reply · Share ›



Viviana • 6 years ago

Thanks a LOT for this explanation!

I nearly had given up trying to understand AES when I found that..!

^ | v · Reply · Share ›



Anonymous • 6 years ago

After reading this I am not sure if I successfully crypt-ed or decrypt-ed my knowledge about AES.

But really is awesome! Thank u!

^ | v · Reply · Share ›

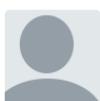


John A • 6 years ago

Great article on AES! AltDrive online backup uses AES-256 encryption in CTR (EAX) mode.

It's super secure, inexpensive, and full featured.

^ | v · Reply · Share ›



Anonymous • 6 years ago

thanks for explanation!

^ | v · Reply · Share ›



H.V. • 6 years ago

That really is a great way to understand the AES! Thanks a lot!

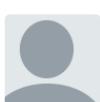
^ | v · Reply · Share ›



Anonymous • 6 years ago

thank you so much for the comic. Actually I didn't plan to go into AES for my script, but after reading through the play I'll be well prepared for any question (in the last resort I would just recommend them to read through your story themselves ;-))

^ | v · Reply · Share ›



Anonymous • 6 years ago

Awesome great job, thanks for taking the time to share :)

^ | v · Reply · Share ›



**David's Holla Atchya! Blog** • 6 years ago

I was the 11,000 profile visitor. As a mathematician, that's pretty special for me. Thanks for the explanation, Jeff.

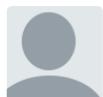
^ | v · Reply · Share ›



**JR** • 6 years ago

A very impressive work. Thanx a lot.

^ | v · Reply · Share ›



**Adam** • 6 years ago

Very good work!

^ | v · Reply · Share ›



**Krishnaprabhu Balakrishnan** • 6 years ago

No one will be able to explain Encryption (a complex subject for most of us) in such a simple manner.

Thanks and appreciate the effort to put this together.

Krishnaprabhu Balakrishnan

^ | v · Reply · Share ›



**Shivashankar B** • 7 years ago

very good... even a layman can understand this stuff... its a really a very good explanation that i ever come across thank you

^ | v · Reply · Share ›