Assignment #4

Due 9 February 2010

1. Find the exact values in each case:

(a)
$$\sin^{-1}(-1/2)$$

(b)
$$\sin^{-1}(\sin(20\pi/3))$$

(c)
$$\tan(\tan^{-1}(16))$$

(d)
$$\cos\left(\sin^{-1}(.3) + \cos^{-1}(.2)\right)$$

2. Evaluate
$$\lim_{x \to +\infty} e^{-2x} \sinh(x)$$
.

3. Evaluate the following integrals:

(a)
$$\int \frac{e^x}{\sqrt{1 - e^{2x}}} dx$$

(b)
$$\int_0^3 \frac{1}{9+x^2}$$

4. Let
$$y = \tan^{-1}(x) + \ln\left(\sqrt{\frac{x-1}{x+1}}\right)$$
. Show that $y' = \frac{2x^2}{x^4 - 1}$.

5. Show that $\frac{1 + \tanh(x)}{1 - \tanh(x)} = e^{2x}.$