

### TFY4195 H2020 - Assignment 3: to be handed in Oct8, 2020

**A3-1.** An electromagnetic wave is travelling in air/vacuum, specified by the following function:

$$\vec{E} = (-6\hat{x} + 3\sqrt{5}\hat{y}) \cos \left[ \frac{1}{3}(\sqrt{5}x + 2y) \cdot \pi \cdot 10^7 - 9.42 \cdot 10^{15}t \right] \cdot 10^2 \quad \left[ \frac{V}{m} \right]$$

The unit of length is [m] and time [s].

Find,

- the electric ( $E_0$ ) and magnetic ( $B_0$ ) field amplitudes,
- their directions (as unit vectors),
- the direction of propagation,
- the wavelength ( $\lambda$ ), propagation number ( $k$ ) and frequency ( $\nu$ ),
- the speed,
- the irradiance (in  $W/m^2$ ).

Draw a scheme that shows the directions of  $E_0$ ,  $B_0$  and  $k$  (vector) in an  $xyz$  coordinate system.

**A3-2.** Analyze the polarization state of the following electromagnetic waves by plotting the electric field trace over a period  $[0, 2\pi]$  for  $\omega t$  (for example at  $z = 0$ ).

- $\vec{E} = E_0 \cos \left( kz - \omega t + \frac{\pi}{4} \right) \cdot \hat{x} + E_0 \cos \left( kz - \omega t - \frac{\pi}{4} \right) \cdot \hat{y}$
- $\vec{E} = E_0 \cos \left( kz - \omega t + \frac{\pi}{4} \right) \cdot \hat{x} + 2E_0 \sin(kz - \omega t) \cdot \hat{y}$
- $\vec{E} = \frac{1}{2}E_0 \cos(kz - \omega t) \cdot \hat{x} + E_0 \sin \left( kz - \omega t - \frac{\pi}{2} \right) \cdot \hat{y}$