Contents

1 Introduction

A social network consists of a set of objects connected to each other by social relations. The best way to model social networks is using graphs (see Figure 1): the objects (entities) are represented as nodes and the connections as edges between two different nodes. The most common example we can take is the World Wide Web (WWW) where we have web pages as nodes connected by hyperlinks, the edges.
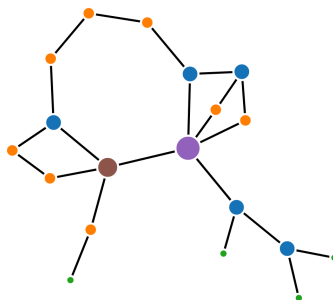
Figure 1. Example of social network graph

The goal of this project is to create a social network of computational science authors belonging to Swiss institutions and then analyze the relative graph.

I want to find the relations between authors of the same or different institutions and belonging to the same or to different research scenarios: how they interact with each other and if they are strictly related to the institution or cooperate throughout Switzerland. The result will provide also a ranking of the authors and the institutions to see which are the most influential in the computational science research.

The first step is retrieving all the necessary information for the construction of the social network, i.e., names of the authors and relationships between each other. I crawled the 2015, 2016 and 2017 PASC Conferences and different SIAM conferences of several years, selecting the topics relevant to us (e.g. Optimization, Parallel Computing,...). The PASC conferences are interdisciplinary and bring together researchers across the areas of computational science, high-performance computing, and various domain sciences,

The second step is the information analysis to find out relations between institutions and between members belonging to the same institution. With PageRank algorithm we obtain a "ranking" of all conferences' participants. PageRank is an algorithm used by Google Search to rank websites in their search engine results, but it can be applied to any social network. In this project I use the algorithm to measure the importance of institutions' members considering the number and quality of their collaborations. I use graph partitioning techniques to invert the process and obtain the institutions from members collaborations: it is reasonable to assume that members of the same institution collaborate more between each other than with other institutions' representatives.

I also analyze the institutions' connectivity matrices and their structure: looking at the cliques present in the matrices we can for example detect the different research areas of the institutions and the connection between them. Cliques are dense sub matrices which represent a group of authors that are closely connected with each other.

The results will provide an interesting picture of the different research scenarios in Switzerland and how they interact with each other.

2 Information Retrieval

Information retrieval is the process of extracting, starting from an information need, the relevant information from a collection of resources. In this project the necessary information are the names of the institutions' members and the collaborations between them.

After the first useless attempt to use Mendeley API, I decide to extract the information from some online conferences' programs; the idea is that if two authors made a conference together, in my social network it turns out that they have collaboration.

I crawl the conferences' programs and I construct a parser to extract the information from the html pages and to organize the data.

2.1 Crawling

A web crawler is an Internet bot that browses the World Wide Web, typically for the purpose of web indexing of search engines. In this project the goal is not indexing web pages but save the information contained in the html to parse them and construct the social network.

The web pages that I decide to crawl are the online programs of 2015, 2016 and 2017 PASC conferences and of SIAM conferences with arguments concerning computational science, i.e. Optimization, Parallel Computing, Computational Science & Engineering, Imaging Science, Uncertainty Quantification, Linear Algebra in Signals, Systems & Control, Data Mining, Analysis of Partial Differential Equations.

I use Apache Nutch that is a highly extensible and scalable open source web crawler and it allow you to crawl a lot of web pages with few command lines. It starts with a list of URLs to visit, called the seeds; I create this list putting there all the links to the computational science web pages previously selected.
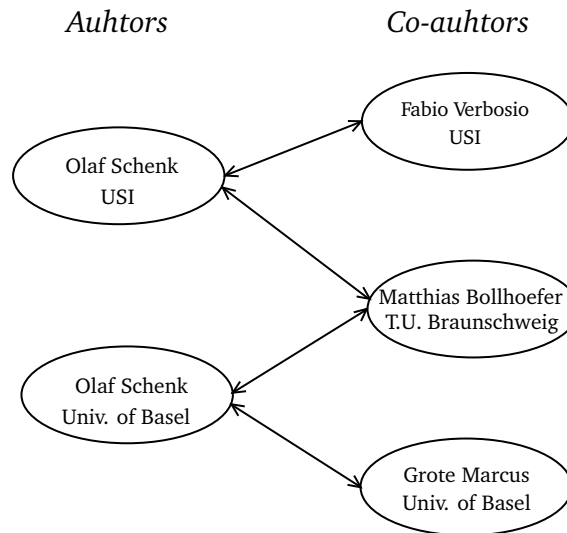
As the crawler visits the URLs, it identifies all the hyperlinks in the page and adds them to the list of URLs to visit; in my case I crawl only the pages in the starting seed ignoring all the internal links. The crawler copies and saves the information as it goes and stores each page in a distinct file in a repository.

Thanks to Apache Nutch I manage to create a text file with the html of all the saved conferences' pages. Obtained this file ,the next step is studying the structure of the page and how to extract the information needed: where are the information I need? Are they in a particular html tag? How we can extract them? Is here that the parser do its job.

2.2 Parsing

A parser is a program that receives some data as input and breaks it up into smaller elements that can then be used for different purposes. In this project the parser read the text file created after the crawling, extracting from the text the information about Swiss institutions and their members. The data obtained is used to create the social network ready to be analyzed.

In this project I personally write a parser, using Python programming language, to extract the information from the conferences' html pages. The parser go through the structure of the page and extract only the pieces where there are useful information; clearly different page structures require different parser. I write two of them because all the SIAM conferences have the same structure but the PASC ones are different.

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Figure 2. Example of author with two different universities and different coauthors

The parser extract only the lines of the pages which contain the names of the authors, their institutions and nationality; the institutions' members that make a conference together appear in group in the page so I keep them together to later get the relations. Thanks to the nation expressed in the program I can differentiate the Swiss authors from the ones from all over the world.

Obtained the desired lines I take the groups, one after the other, and I extract name, institution, nation and coauthors for each member. With all this information I manage to construct a social network and its adjacency matrix.

I run into some problems like an author with two different institution and I decide to consider it as two different authors because I'm interest in institutions collaborations: so the same author can have some coauthors with one university and completely different coauthors with the other one. We can see an example in Figure 2 where professor Olaf Schenk has two different universities, Università della Svizzera Italiana and Univerisity of Basel: he collaborates with Matthias Bolhoefer with both institutions but he works with Fabio Verbosio only in USI and with Grote Marcus only in the University of Basel.

3 The PageRank Algorithm

PageRank is an algorithm used by Google Search to rank websites in their search engine results; it was developed by Larry Page and Sergey Brin (the Google's founders) in 1996 as part of their research project at Stanford University.

PageRank is used, together with other algorithms, to measure the importance of web pages and sort them by popularity in the result; it can be used in any graph to compute the importance of each node with its PageRank value. Larry Page and Sergey Brin algorithm works by counting the number and quality of links to a page to compute a value which represents its importance; more popular a page is, more likely it receives links from other websites and more likely from important websites.

As we can see in Fig ure 3, node C has higher PageRank than A even if it has the same
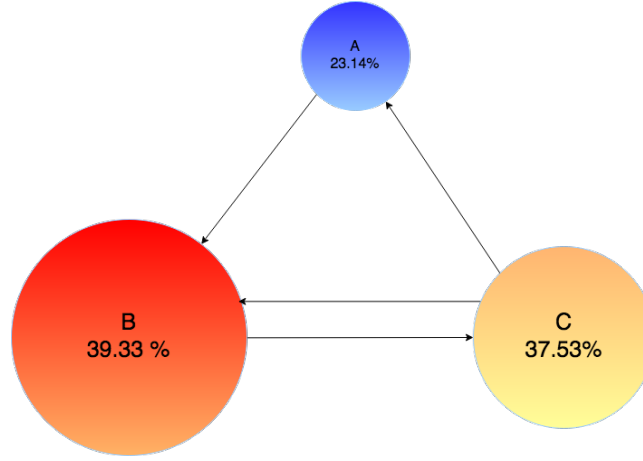
Figure 3. PageRank example

number of inner links; this is because the only inner link of C is from the most important node of the graph B so it is considered to be more important than the inner link of node A.

While surfing websites, going from one page to another I want to avoid problems with pages without outer links so I introduce two different methods to choose the next page. The surfer can:

- randomly choose an outgoing link from the page,

- choose a random page from the network.

We assume that the surfer follows the first option with probability p (typically $p = 0.85$) and the second with probability $1 - p$. This theoretical random walk is known as a Markov chain or Markov process.

The probability that an infinite random surfer visits a specific website is called its PageRank; a page will have high rank if other pages with high rank link to it.

3.1 How to compute PageRank values

To apply PageRank, from a graph of n nodes we construct a n-by-n connectivity matrix G such that

$$g_{ij} = 1 \quad \text{if and only if nodes } i \text{ and } j \text{ are connected.}$$

The number of non-zeros in G is the total number of connections in the graph.

The row r_i represents the number of inner-links of page i, while column c_i the number of outer-links. So we can define:

- In-degree of page i: $\quad r_i = \sum_{j=1}^{n} g_{ij}$

- Out-degree of page i: $\quad c_i = \sum_{j=1}^{n} g_{ji}$

Let p be the probability that the surfer follows a link and $1 - p$ the probability that it chooses a random page, then $\delta = \frac{1-p}{n}$ is the probability that a particular random page is chosen.

We construct a transition probability matrix A where all elements are positive, smaller than one and sums of columns are equal to one; column j represents the probabilities to go from page j to all other pages. So we set

$$a_{ij} = \begin{cases} \frac{pg_{ij}}{c_j} + \delta & \text{if } c_j \neq 0 \\ \frac{1}{n} & \text{if } c_j = 0 \end{cases}$$

In other words, if page j has no outer links, it means that column j of A present a uniform probability $\frac{1}{n}$ in all its elements. Since matrix A is a transition matrix of a Markov chian, all its eigenvalues are real, between 0 and 1, and 1 is an eigenvalue itself.

We can now compute PageRank values by solving the problem.

$$A x = x$$

It is a particular eigenvalue problem because usually they are of the form $A x = \lambda x$. Finding the solution of eigensystems is complicated and doesn't exist direct methods; the process has to be iterative such as the power or Jacobi methods.

In our specific problem we have $\lambda = 1$ so the power method seems to be the most effective. It computes the eigenvector relative to the greatest eigenvalue and it is our problem since A is a matrix of a Markov chain.

The transition matrix A can be written as

$$A = pGD + ez^T,$$

where D is a diagonal matrix with the reciprocals of the out-degrees, i.e.,

$$d_{jj} = \begin{cases} \frac{1}{n} & \text{if } c_j \neq 0 \\ 0 & \text{if } c_j = 0 \end{cases},$$

z is the vector formed by

$$z_j = \begin{cases} \delta & \text{if } c_j \neq 0 \\ \frac{1}{n} & \text{if } c_j = 0 \end{cases},$$

and e is the vector of length n with all ones.

We can write the linear system

$$(I - A)x = 0$$

as

$$(I - pGD)x = \gamma e$$

where $\gamma = z^T x$. To conclude, since the value of the scalar γ depends on the unknown x, we impose the condition $\gamma = 1$, then solve

$$(I - pGD)x = e$$

and then rescale the solution so that $\sum_{i=1}^{n} x_i = 1$.

Algorithm 1 (PageRank)

 1: **procedure** PAGERANK

 2: $U \leftarrow$ list of *authors*

 3: $G \leftarrow$ adjacency matrix

 4: $p \leftarrow$ dumping factor

 5: $G \leftarrow G - \text{diag}(G)$ (remove self collaborations)

 6: $c \leftarrow \text{sum}(G,1)$ $r \leftarrow \text{sum}(G,2)$ (Compute out-degree and in-degree of each node)

 7: $D \leftarrow$ Diagonal matrix with reciprocals of out-degrees

 8: $(I - pGD)x = e$

 9: $x \leftarrow x / sum(x)$ (normalize the result x)

10: $x \leftarrow$ sort x in descending order

11: **return** x
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4   The Graph Partitioning Algorithm

Graph partitioning consists in dividing a graph $G = (V, E)$[1] cutting the smaller number of edges and obtaining sub-graphs with specific properties. For example k-way partitioning divides the graph G into k smaller components.

 A partitioning algorithm is said to be efficient if it divides a given graph into smaller components with about the same size, cutting as few edges as possible. A valid and fast method is the coordinate bisection, which simply chooses a partitioning plane perpendicular to one of the coordinate axes but spectral algorithm is more efficient. It finds a partition based on the eigenvalues and eigenvectors of the Laplacian matrix of the graph and doesn't need the nodal coordinates.

 As we can see in Figure 4 sometimes coordinate and spectral partitioning behave similarly but usually the second one is more effective.

4.1   How to apply spectral graph partitioning

To apply graph partitioning we need the adjacency matrix A of the graph, which is symmetric since the graph is considered to be undirected, and the Laplacian matrix L constructed such that:

$$L_{ij} = \begin{cases} d_i & if \ \ i = j \\ -1 & if \ \ i \neq j \ and \ (i,j) \in E \\ 0 & \text{otherwise} \end{cases}$$

where d_i is the vertex degree of node $i \in V$. The relation between A and L is

$$L = D - A$$

where D is the diagonal matrix having the d_i's on the diagonal. Since L is symmetric and positive semidefinite by construction, all its eigenvalues are real and nonnegative. The first eigenvalue is always zero and, in the general case, the multiplicity of the the first eigenvalue corresponds to the number of connected components of the graph.

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[1] A graph G with vertexes V and edges E.
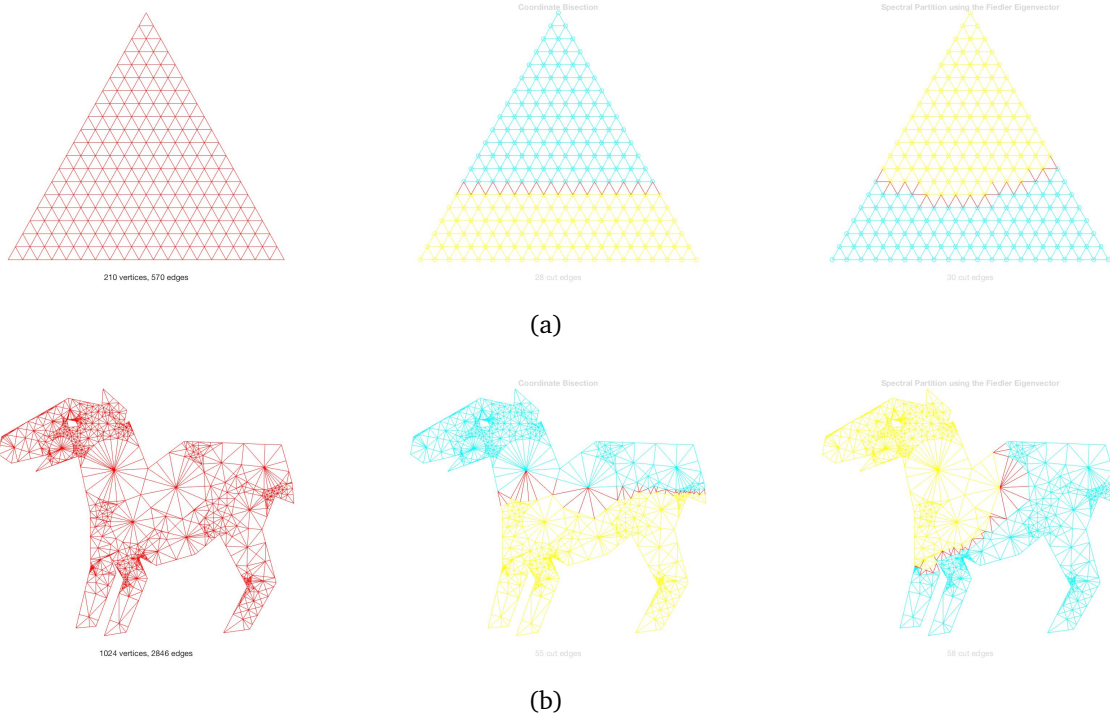
Figure 4. In both (a) and (b) we have the graph at the left, the coordinate bisection in the middle and the spectral partition on the right

The eigenvalues of L are ordered as follows:

$$0 = \lambda_1 = \ldots = \lambda_m < \lambda_{m+1} \leq \ldots \lambda_n$$

The eigenvector corresponding to the first eigenvalue λ_1 is the vector of all ones and it does not provide information about the graph structure; the second lowest eigenvector, instead, called "Fiedler eigenvector", is used by spectral partitioning to return the smaller sub-graphs. Dividing the nodes of graph G according to the median s of the Fiedler vector $v = (v_1, v_2, ..., v_n)$ gives two partitions V_1 and V_2 such that

$$\begin{cases} v_i \in V_1 & \text{if} \quad v_i \leq s \\ v_i \in V_2 & \text{if} \quad v_i > s \end{cases} \quad .$$

Such a partition is called the Fiedler cut and leads to two parts of G with nearly equal number of vertexes, minimizing the number of cut edges.

Fiedler theorem said that if the graph G is connected, L the Laplacian matrix, N_+ and N_- a partitioning such that

$$x(i) = +1 \qquad \text{if } v_i \text{ in } N_+$$

$$x(i) = -1 \qquad \text{if } v_i \text{ in } N_-$$

Then the number of edges cut is:

$$\#\text{edge\_cut} = \frac{1}{4} x^T L x$$

This problem of minimizing the number of cut edges is NP-hard and can be written as a constrained minimization problem:

$$\min_z f(z) = \frac{1}{4} z^T L z \qquad \text{subject to} \qquad \begin{cases} z^T z = n & \text{z is a real vector} \\ z^T e = 0 & \text{with } e = [1, 1, ..., 1]^T \end{cases}$$


Algorithm 2 (Graph Partitioning)

1: **procedure** GRAPH PARTITIONING
2:     $G \leftarrow$ (V,E)
3:     compute Fiedler vector of $L = D$ - A
4:     Sort the vector values
5:     Put first half of the nodes in V_1 and second half in V_2
6:     $E_1 \leftarrow$ edges with both nodes in V_1
7:     $E_2 \leftarrow$ edges with both nodes in V_2
8: **return** $G1 =$ (V1,E1) and $G2 =$ (V2,E2)

4.2   K-way Partitioning

K-way partitioning of a graph G of n nodes, consists in a division of its nodes in k disjoint subset, all with size nearly $\frac{n}{k}$ (see Figure 5).
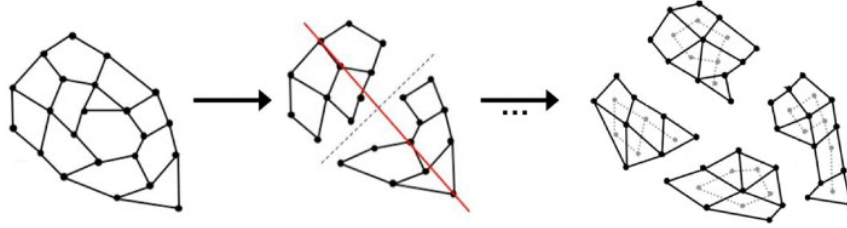
Figure 5. Example of k-way graph partitioning

We consider only the simple case where we want to divide the graph in k partitions and k is a power of two. The idea is just to apply the spectral partitioning $\frac{k}{2}$ times recursively to each of the partitions obtained. The method is presented in Algorithm 3.

5   Numerical analysis

After retrieving all the necessary information and organizing the data in adjacency matrix, I applied PageRank and Graph Partitioning algorithms, obtaining the following results. Since the Swiss authors' names obtained are only 422, I decide to extend the research to the institutions from all over the word, reaching 16425 names.

I first construct the adjacency matrix of the authors and their corresponding universities; for the universities I also build a weighted matrix which keep the number of collaborations between each university. We can see the matrices obtained in figure 6 and 7

The sparsity of the Swiss author adjacency matrix is 0.0085 instead the one of world author matrix is $2.4312 * 10^{-04}$.
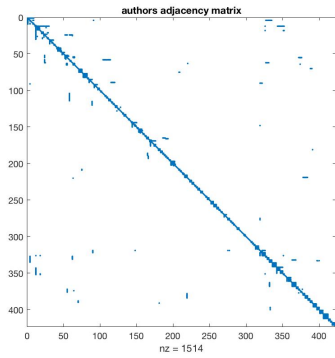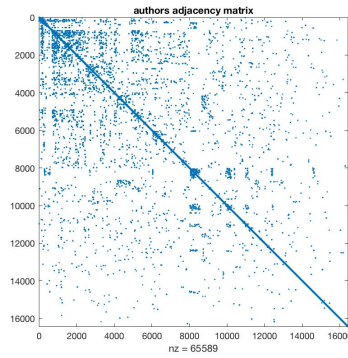

Algorithm 3 (k-way Partitioning)

1: **procedure** K-WAY PARTITIONING
2: $\quad G \leftarrow (V,E)$
3: $\quad k \leftarrow$ number of desired partitions
4: $\quad$ Apply spectral partitioning on G and find G_1 and G_2
5: *loop*:
6: $\quad$ **if** $\frac{k}{2} > 1$ **then**
7: $\quad\quad$ Recursive partition on G_1 with $\frac{k}{2}$
8: $\quad\quad$ Recursive partition on G_2 with $\frac{k}{2}$
9: $\quad\quad k \leftarrow \frac{k}{2}$
10: $\quad$ **goto** *loop*
11: **return** $G_1 = (V_1, E_1) \dots G_K = (V_K, E_K)$


(a)

(b)

Figure 6. (a) is the Swiss authors' adjacency matrix and (b) is the one of the world authors

The universities that collaborate more in Switzerland are the École polytechnique fédérale de Lausanne and the ETH Zürich which correspond to the indexes 7 and 8 in the matrix. In the weighted matrix we can observe that these two universities collaborate both internally in the university but also with other institutions: for example ETH Zürich has 19 collaboration with Università della Svizzera italiana.

5.1   PageRank – forse (inclusi in R.analysis)

## 5.2   Graph Partitioning – forse (inclusi in R.analysis)
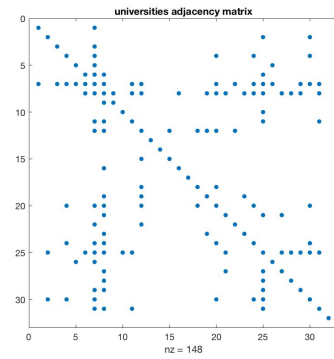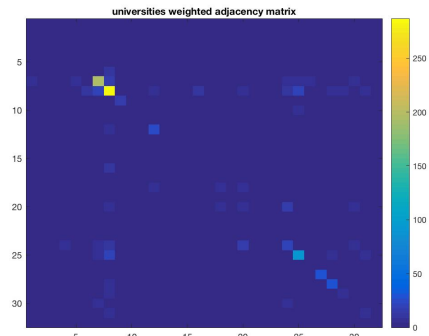
Figure 7. (a) is the Swiss university adjacency matrix, (b) is the universities weighted graph

6 Bibliography Temporary

- https://en.wikipedia.org/wiki/PageRank

- Assignment1 1 Course Numerical Computing 2107/2018

- Assignment2 1 Course Numerical Computing 2107/2018

- "https://am.vsb.cz/export/sites/am/cs/theses/kabelikova_ing.pdf"

- https://en.wikipedia.org/wiki/Graph_partition

(a)
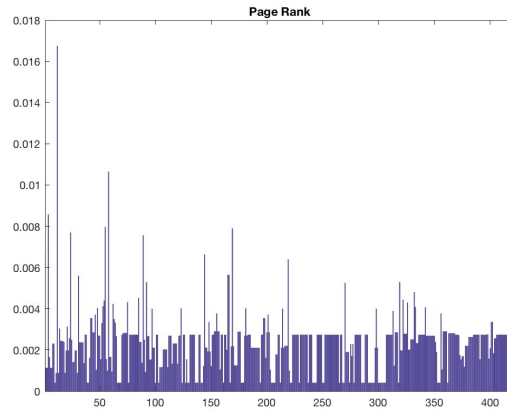
Index	Pagerank	In_degree	Out_degree	Name	University
12	0.016757	30	30	'Rolf Krause'	'USI'
58	0.010648	12	12	'Christoph Schwab'	'ETHZ'
4	0.0085765	14	14	'Simone Deparis'	'EPFL'
55	0.0079721	12	12	'Costas Bekas'	'IBM'
169	0.0078995	8	8	'Bruno Sudret'	'ETHZ'
24	0.0076977	12	12	'Peter Arbenz'	'ETHZ'
89	0.0075607	7	7	'Fabio Nobile'	'EPFL'
1	0.0067923	8	8	'Alfio Quarteroni'	'EPFL'
144	0.0066262	7	7	'Olaf Schenk'	'USI'
219	0.0063917	10	10	'Torsten Hoefler'	'ETHZ'

(b)

**Figure 8.** (a) is a bar graph of PageRank values, (b) are the first 15 people with higher PageRank value

(a)
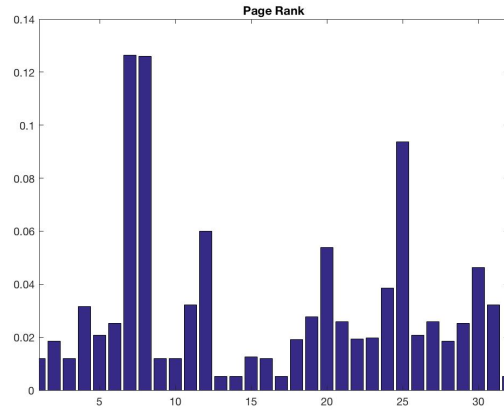
| Index	Pagerank	In_degree	Out_degree	University
7	0.12632	16	16	'EPFL'
8	0.12601	16	16	'ETHZ'
25	0.09368	12	12	'USI'
12	0.059924	7	7	'IBM'
20	0.053813	7	7	'SIB'
30	0.046199	6	6	'University of Geneva'
24	0.038438	5	5	'UNIL'
11	0.032109	4	4	'HES–SO Valais–Wallis'
31	0.032109	4	4	'University of Neuchatel'
4	0.031569	4	4	'CHUV'

(b)

Figure 9. (a) is a bar graph of PageRank values, (b) are the first 15 universities with higher PageRank value
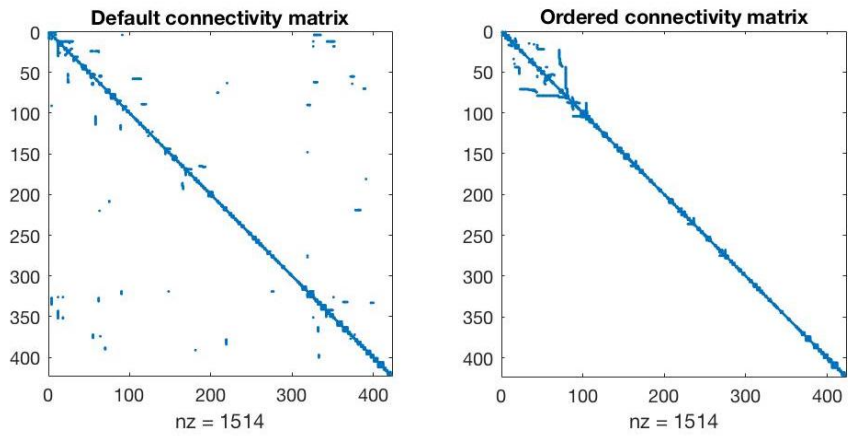
Figure 10. The Reverse Cuthill McKee ordering

13

Index	Authors	Degree_Centrality
12	'Rolf Krause'	30
4	'Simone Deparis'	14
24	'Peter Arbenz'	12
55	'Costas Bekas'	12
58	'Christoph Schwab'	12
219	'Torsten Hoefler'	10
332	'Nicolas Salamin'	10
319	'Michael Afanasiev'	9
1	'Alfio Quarteroni'	8
169	'Bruno Sudret'	8

Figure 11. Degree Centrality
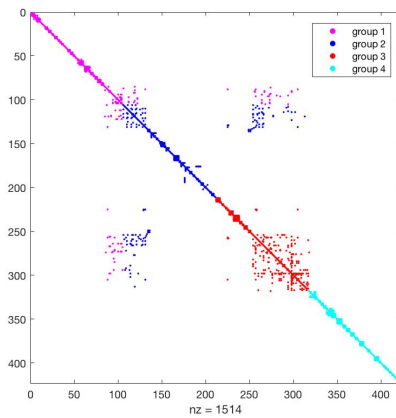
Figure 12. The graph partitioning algortihm