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1 Introduction

A social network consists of a set of objects connected to each other by social relations. The best way to model social networks is using graphs: the objects (entities) are represented as nodes and the connections as edges between two different nodes (see Figure 1). The most common example we can take is the World Wide Web (WWW) where we have web pages as nodes connected by hyperlinks, the edges.

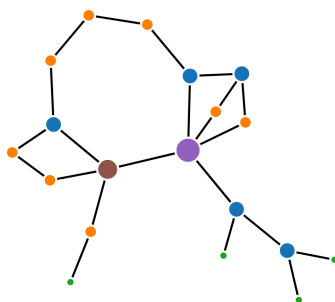


Figure 1. Example of social network graph

The goal of this project is to create a social network of computational science authors belonging to Swiss institutions and corporations, and then analyze the relative graph, represented by an adjacency matrix. I want to find the relations between authors of the same or different institutions and belonging to the same or to different research scenarios: how they interact with each other and if they are strictly related to the institution or cooperate throughout Switzerland. The result will provide also a ranking of the authors and the institutions to see which are the most influential in the computational science research.

The first step is retrieving all the necessary information for the construction of the social network, i.e., names of the authors and relationships between each other. I crawled the 2015, 2016 and 2017 PASC Conferences and different SIAM conferences of several years, selecting the topics relevant to us (e.g. Optimization, Parallel Computing,...). The PASC conferences are interdisciplinary and bring together researchers across the areas of computational science, high-performance computing, and various domain sciences.

The second step is the information analysis to find out relations between institutions and between members belonging to the same or different institutes. With PageRank algorithm we obtain a ranking of all the conference participants; it is an algorithm used by Google Search to rank websites in their search engine results, but it can be applied to any social network.

In this project I use the algorithm to measure the importance of the institution members considering the number and quality of their collaborations and to find out the relevant universities for computational science researches.

I also analyze the institutions connectivity matrices and their structure: looking at the cliques present in the matrices, we can for example detect the different research areas of the institutions and the connection between them. Cliques are dense sub matrices which represent a group of authors that are closely connected with each other.

The results will provide an interesting picture of the different research scenarios in Switzerland and how they interact with each other.

2 Information Retrieval

Information retrieval is the process of extracting, starting from an information need, the relevant information from a collection of resources. In this project, the necessary information are the names of the institutions members and the collaborations between them.

Firstly I try to use Mendeley API but it allows only to take 100 results per query and if you run the same query more times it returns always the same information. Additionally it does not return all the information needed i.e., not all authors have a specified institution and only few papers were available.

After this first unproductive attempt to use Mendeley API, I decide to extract the information from some online conferences' programs; the idea is that if two authors made a conference together, then they are connected in my social network.

I crawl the conferences' programs and I construct a parser to extract the information from the HTML pages and to organize the data.

2.1 Crawling

A web crawler is an Internet bot that browses the World Wide Web, typically for the purpose of web indexing of search engines. In this project the goal is not indexing web pages but save the information contained in the HTML to parse them and construct the social network.

The web pages that I decide to crawl are the online programs of 2015, 2016 and 2017 PASC conferences and of SIAM conferences with arguments concerning computational science i.e., Optimization, Parallel Computing, Computational Science & Engineering, Imaging Science, Uncertainty Quantification, Linear Algebra in Signals, Systems & Control, Data Mining and Analysis of Partial Differential Equations.

I use Apache Nutch, a highly extensible and scalable open source web crawler, allowing the user to crawl a lot of web pages with few command lines. It starts with a list of URLs to visit, called the seeds; I create this list including all the links to the computational science conferences web pages previously mentioned.

As the crawler visits the URLs, it identifies all the hyperlinks in the page and adds them to the list of URLs to visit; in my case I crawl only the pages in the starting seed ignoring all the internal links. The crawler copies and saves the information as it goes and stores in a repository each page as a distinct file.

Thanks to Apache Nutch I manage to create a text file with the HTML of all the saved conference pages. Obtained this file, the next step is studying the structure of the page and how to extract the information needed. Where we can find the information in the page, if they are in some particular tag, as we can extract them. The parser is responsible for these tasks.

2.2 Parsing

A parser is a program that receives data as input and breaks it up into smaller elements that can then be used for different purposes. In this project, the parser reads the text file created after the crawling and extracts from it the information about Swiss institutions and their members. The data obtained is used to create the social network ready to be analyzed.

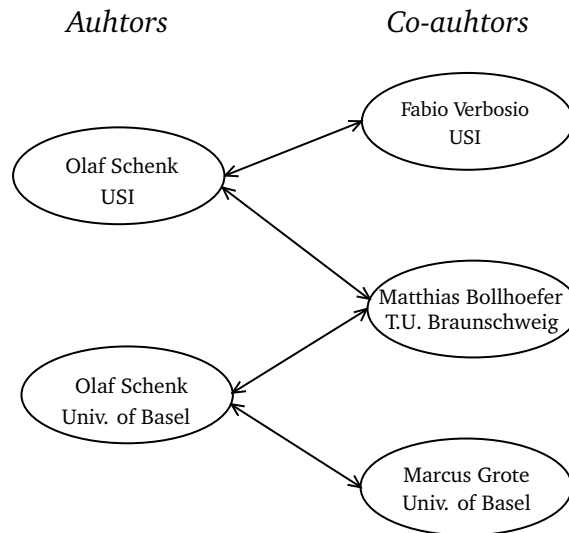


Figure 2. Example of author with two different universities and different coauthors

In this project I personally write a parser, using Python programming language, to extract the information from the conferences HTML pages. The parser goes through the structure of the page and extracts only the useful information. Clearly, different page structures require different parser, then I write two of them because the SIAM conferences and the PASC have different structures.

The parser extracts only the lines of the pages which contain the names of the authors, their institutions and nationality; the institutions members that present a work together at a conference appear in group in the page so I keep them together to later extract the relations. Thanks to the nation expressed in the program I can differentiate the Swiss authors from the rest of the the world.

Once that the desired lines are collected, I take the groups one after the other, and I extract name, institution, nation and coauthors for each member. With all this information I manage to construct a social network and its corresponding adjacency matrix.

In case a single author belongs to two distinct institutions I decide to include two different entries because I'm interest in institutions collaborations: so the same author can have some coauthors with one university and completely different coauthors with the other one. We can see an example in Figure 2 where professor Olaf Schenk is affiliated to two different universities (Università della Svizzera Italiana and Univerisity of Basel) and collaborates with Matthias Bollhoefer from both institutions but he works with Fabio Verbosio only from USI and with Marcus Grote only from the University of Basel.

I make two different databases, one for Switzerland and one for the whole world. The first one contains only Swiss authors and their collaborations with members of the same nation, while in the second there are also authors other nations and their collaborations are extended to all over the world. For each author I save the name, the university, the nation, a list of his coauthors and I assign to each of them a unique index.

From this data set I easily create the adjacency matrix and thanks to the indexes I can switch between the matrix and the database; from the graph I can read the index and go in the database to see to which author it corresponds.

3 The PageRank Algorithm

PageRank is an algorithm used by Google Search to rank websites in their search engine results. It was developed by Larry Page and Sergey Brin (the Google founders) in 1996 as part of their research project at Stanford University.

PageRank is used, together with other algorithms, to measure the importance of web pages and sort them by popularity in the results; it can be used on any graph to compute the importance of each node by its PageRank value. Larry Page and Sergey Brin algorithm works by counting the number and quality of links to a page, to compute a value which represents its importance: more popular a page is, more likely it receives links from other websites and even more likely from important websites.

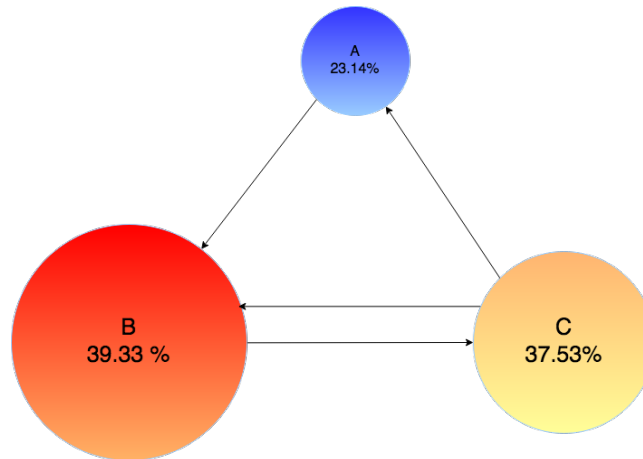


Figure 3. PageRank example

As we can see in Figure 3, node C has higher PageRank than A even if it has the same number of inner links; this is because the only inner link of C is from the most important node of the graph, B, so it is considered to be more important than the inner link on node A.

While surfing websites, going from one page to another, I want to avoid problems with pages without outer links so I introduce two different methods to choose the next page. The surfer can:

- randomly choose an outgoing link from the page, or
- choose a random page from the network.

We assume that the surfer follows the first option with probability p (typically $p = 0.85$) and the second with probability $1 - p$. This theoretical random walk is known as a Markov chain or Markov process.

The probability that an infinite random surfer visits a specific website is called its PageRank; a page will have high rank if other pages with high rank link to it.

3.1 How to compute PageRank values

To apply PageRank, from a graph of n nodes we construct a n -by- n connectivity matrix G such that

$$g_{ij} = 1 \quad \text{if and only if nodes } i \text{ and } j \text{ are connected.}$$

The number of non-zeros in G is the total number of connections in the graph.

The scalar r_i represents the number of inner-links of page i , while column c_i the number of outer-links. So we can define:

- In-degree of page i : $r_i = \sum_{j=1}^n g_{ij}$
- Out-degree of page i : $c_i = \sum_{j=1}^n g_{ji}$

Since the collaboration is a symmetric relation, my graph is undirected, hence the number of inner-links is equal to the number of outer-links.

Let p be the probability that the surfer follows a link and $1-p$ the probability that it chooses a random page, then $\delta = \frac{1-p}{n}$ is the probability that a particular random page is chosen.

We construct a transition probability matrix A where all the elements are positive and smaller than one, and the sum of each column is equal to one; this last property is due to the fact that column j represents the probabilities to go from page j to all other pages. So, we set

$$a_{ij} = \begin{cases} \frac{pg_{ij}}{c_j} + \delta & \text{if } c_j \neq 0 \\ \frac{1}{n} & \text{if } c_j = 0 \end{cases}.$$

In other words, if page j has no outer links, it means that column j of A present a uniform probability $\frac{1}{n}$ in all its elements. Since matrix A is a transition matrix of a Markov chain, all its eigenvalues are real, between 0 and 1, and 1 is an eigenvalue itself

$$0 \leq \lambda_1 \leq \lambda_2 \leq \dots \leq \lambda_n = 1.$$

We can now compute PageRank values by solving the problem

$$Ax = x.$$

This is a particular eigenvalue problem because usually they are of the form $Ax = \lambda x$. In our specific problem, in fact, we have $\lambda = 1$ so we compute the eigenvector relative to the greatest eigenvalue which is 1, as just mentioned.

The transition matrix A can be written as

$$A = pGD + ez^T,$$

where D is a diagonal matrix with the reciprocals of the out-degrees, i.e.,

$$d_{jj} = \begin{cases} \frac{1}{n} & \text{if } c_j \neq 0 \\ 0 & \text{if } c_j = 0 \end{cases},$$

z is the vector formed by

$$z_j = \begin{cases} \delta & \text{if } c_j \neq 0 \\ \frac{1}{n} & \text{if } c_j = 0 \end{cases},$$

and e is the vector of length n with all ones.

We can write the linear system

$$(I - A)x = 0$$

as

$$(I - pGD)x = \gamma e$$

where $\gamma = z^\top x$. To conclude, since the value of the scalar γ depends on the unknown x , we impose the condition $\gamma = 1$, then solve

$$(I - pGD)x = e$$

and then rescale the solution so that $\sum_{i=1}^n x_i = 1$.

Algorithm 1 (PageRank)

```

1: procedure PAGERANK
2:    $U \leftarrow$  list of authors
3:    $G \leftarrow$  adjacency matrix
4:    $p \leftarrow$  dumping factor
5:    $G \leftarrow G - \text{diag}(G)$  (remove self collaborations)
6:    $c \leftarrow \text{sum}(G,1)$   $r \leftarrow \text{sum}(G,2)$  (Compute out-degree and in-degree of each node)
7:    $D \leftarrow$  Diagonal matrix with reciprocals of out-degrees
8:   Solve  $(I - pGD)x = e$ 
9:    $x \leftarrow x / \text{sum}(x)$  (normalize the result  $x$ )
10:   $x \leftarrow$  sort  $x$  in descending order
11: return  $x$ 

```

4 Numerical analysis

After retrieving all the necessary information and organizing the data in adjacency matrices, I applied PageRank and Graph Partitioning algorithms, obtaining the following results. Since the Swiss author names obtained are only 422, I decide to extend the research to the institutions from all over the world, reaching 16425 names. So the analysis is done in parallel for both Swiss collaborations and authors from all over the world.

I first construct the adjacency matrices of the authors and their corresponding institutions; for the organizations I also build a weighted matrix which keeps stored the number of collaborations between them. I consider that each author collaborates with himself so the diagonal of the matrix will contain ones. We can see in Figure 4 the authors matrices, while in Figure 5 the one of the Swiss institutions.

The sparsity of a matrix is the number of zero-valued elements divided by the total number of elements; the Swiss authors adjacency matrix has sparsity equal to $8.5 \cdot 10^{-3}$ instead the one of the world authors matrix is $2.4 \cdot 10^{-4}$.

In Figure 5(b) (lets call this matrix U) we can see the matrix representing the weighted collaborations between Swiss universities: as we can see in the bar at the right, blue corresponds to no collaboration and while increasing the number of collaborations the color changes to yellow. The institutions which collaborate more in Switzerland are École Polytechnique Fédérale de Lausanne and ETH Zürich which correspond to the 7th and 8th columns/rows in the matrix. These two universities collaborate both internally in the university (see the yellow squares

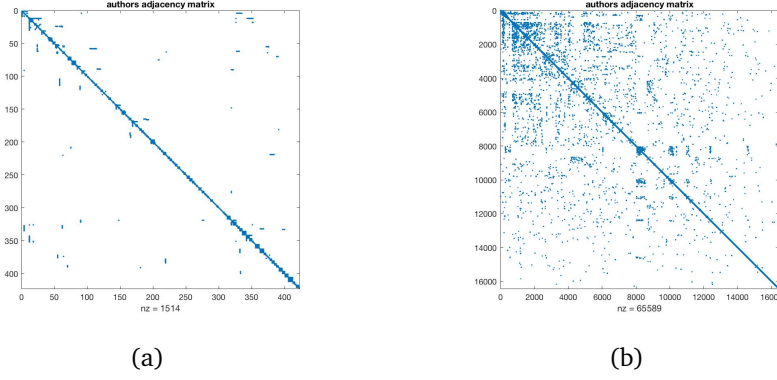


Figure 4. (a) is the Swiss authors' adjacency matrix and (b) is the one of the world authors

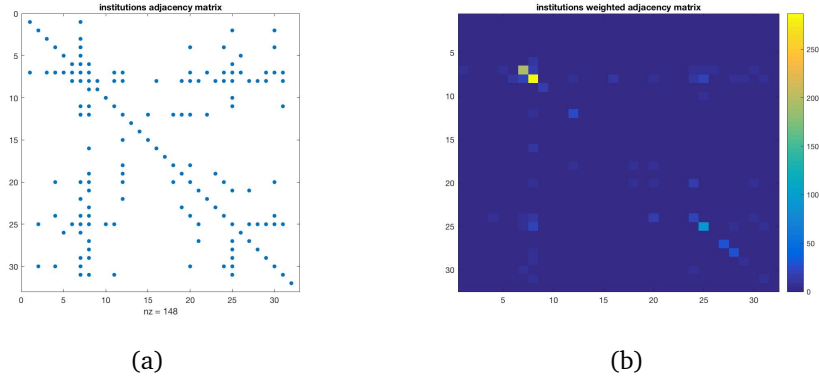


Figure 5. (a) is the Swiss institutions adjacency matrix, (b) is the organizations weighted graph

of $U_{7,7}$ and $U_{8,8}$ entries of the matrix U) but also with other institutions (see the 7th and 8th columns/rows of U where we have a lot of light-blue squares): for example ETH Zürich has 19 collaboration with Università della Svizzera italiana (25th column). We can see that most of the light-blue squares appear in the diagonal of the matrix; it means that institutions' members usually works with authors of the same organization instead of ones from a different institution.

Add something to say why do we apply the cuthill, come influenza i metodi numerici

I applied the Cuthill-McKee algorithm to the two authors matrices: it permutes a sparse matrix that has a symmetric sparsity pattern into a band matrix form with a small bandwidth. A band matrix is a sparse matrix whose non-zero elements are confined to a diagonal band; if the bandwidth of a symmetric matrix A is n , it means that

$$A_{ij} = 0 \text{ if } |j - i| > n$$

This means that all the non zero elements are put as near as possible to the diagonal of the matrix, as we can see in Figure 6.

For the matrix of Swiss authors in 6(a) the bandwidth is 48, instead the one of the authors from all the world 6(b) has a bandwidth of 1210.

We can notice that in both figures the number of non-zero elements, written below the graph, doesn't change; in fact, the reverse Cuthill-McKee ordering consists only in rows and columns permutations and don't change any entry of the matrix.

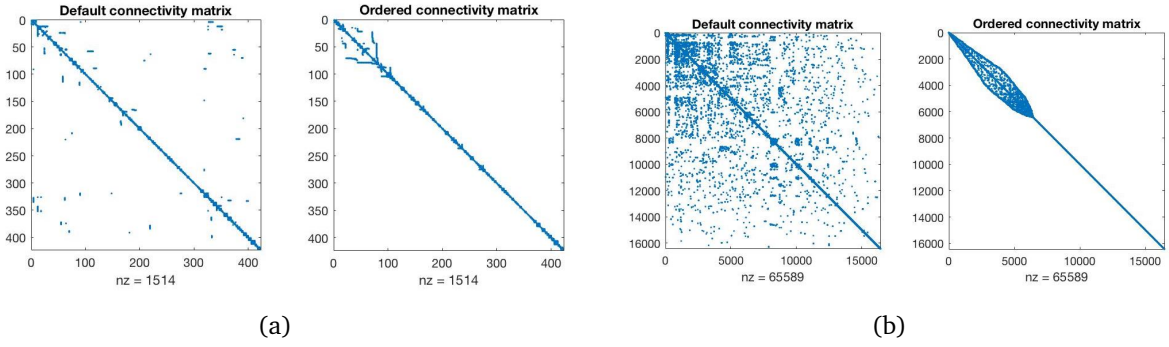


Figure 6. The Reverse Cuthill McKee ordering for only Switzerland in (a) and for the authors of all the world in (b)

4.1 PageRank

Applying the PageRank algorithm I obtain a sorted list of authors and in Figure ?? we can see all the 422 Swiss authors with their corresponding PageRank value.

In Table ?? we can see the first 10 most “popular” authors sorted by the algorithm; we can see that the *In_degree* column, which correspond to the number of collaboration, it is not sorted because PageRank takes into account also the quality of the collaborations. For example the third author *Simone Deparis* has more collaborations than the second *Christoph Schwab*. To see it better we can compare this table with the one in Figure ?? containing the first 10 authors sorted only by degree-centrality (i.e., number of collaborations). The most collaborative author is still *Rolf Krause* because it has 30 associations but from the second we can already see some differences.

Index	PageRank	Degree Centrality	Name	Institution
12	0.016757	30	Rolf Krause	USI
58	0.010648	12	Christoph Schwab	ETHZ
4	0.0085765	14	Simone Deparis	EPFL
55	0.0079721	12	Costas Bekas	IBM
169	0.0078995	8	Bruno Sudret	ETHZ
24	0.0076977	12	Peter Arbenz	ETHZ
89	0.0075607	7	Fabio Nobile	EPFL
1	0.0067923	8	Alfio Quarteroni	EPFL
144	0.0066262	7	Olaf Schenk	USI
219	0.0063917	10	Torsten Hoefer	ETHZ

Table 1. First ten Swiss authors sorted by PageRank

Index	Degree Centrality	Name
12	30	Rolf Krause
4	14	Simone Deparis
24	12	Peter Arbenz
55	12	Costas Bekas
58	12	Christoph Schwab
219	10	Torsten Hoefer
332	10	Nicolas Salamin
319	9	Michael Afanasiev
1	8	Alfio Quarteroni
169	8	Bruno Sudret

Table 2. First ten Swiss authors sorted by degree centrality

I have also applied the PageRank algorithm to the universities’ adjacency matrix obtaining the results in Figure 8.

We can observe that the most present universities in the area of computational science are École Polytechnique Fédérale de Lausanne, ETH Zürich and Università della Svizzera italiana. Here the universities sorted by PageRank corresponds to the sorting by number of collaborations (*In_degree* column).

About what concerning world information we can better see the difference between PageRank and degree centrality sorting in Figure ??; the Swiss *Rolf Krause*, member of USI, has the 7th PageRank value with only 38 collaborations but does not appear in the first ten positions of the degree centrality list.

In Figure ?? we can see the first 10 universities with higher PageRank value: in the computational science area the most important are the University of California and the Massachusetts

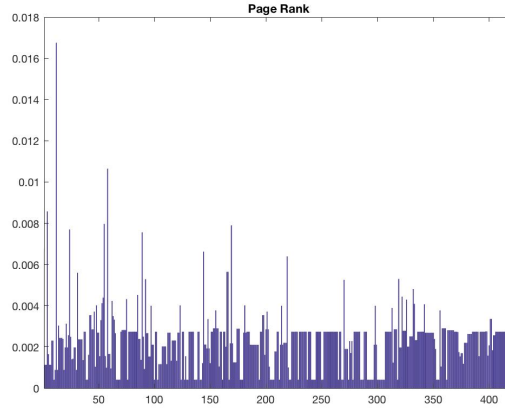
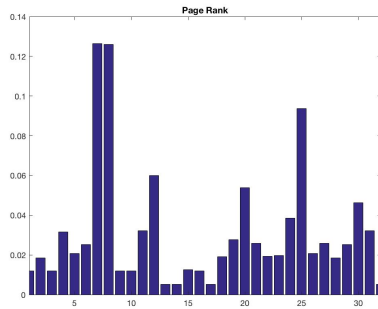
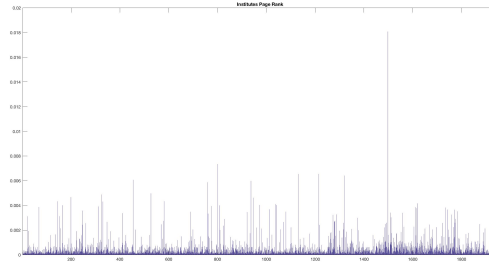


Figure 7. Bar graph of Swiss authors PageRank values



(a)



(b)

Figure 8. ?? is a bar graph of PageRank values, ?? are the first 15 universities with higher PageRank value

Index	PageRank	D.Centrality	Institution
7	0.12632	16	EPFL
8	0.12601	16	ETHZ
25	0.09368	12	USI
12	0.059924	7	IBM
20	0.053813	7	SIB
30	0.046199	6	University of Geneva
24	0.038438	5	UNIL
11	0.032109	4	HES-SO Valais-Wallais
31	0.032109	4	University of Neuchatel
4	0.031569	4	CHUV

Table 3. First ten Swiss institutions sorted by PageRank

Index	PageRank	D.Centrality	Institution
1498	0.018077	256	University of California
801	0.0073476	114	Massachusetts Institute of Technology
1215	0.0065502	101	Stanford University
1132	0.0065372	103	Sandia National Laboratories
1319	0.0064138	97	The University of Texas at Austin
454	0.0060685	92	Georgia Institute of Technology
937	0.0059833	96	New York University-NYU
760	0.0058694	87	Lawrence Berkeley National Laboratory
527	0.0049737	80	IBM
326	0.0048789	69	EPFL

Table 4. First ten institutions sorted by PageRank

Index	PageRank	D.Centrality	Name	Institution
1343	0.00066775	47	Youssef M. Marzouk	Massachusetts Institute of Technology
3794	0.00064672	42	Andrea L. Bertozzi	University of California
2719	0.00055678	42	Stanley J. Osher	University of California
115	0.00052919	49	Omar Ghattas	The University of Texas at Austin
2478	0.00052283	23	Stefan Ulbrich	Technical University Darmstadt
2333	0.0005056	33	Gianluca Iaccarino	Stanford University
25	0.00049204	38	Rolf Krause	USI
758	0.00047899	52	Xiaoye Sherry Li	Lawrence Berkeley National Laboratory
701	0.00047145	51	Eric Phipps	Sandia National Laboratories
773	0.00045236	41	James W. Demmel	University of California

Table 5. First ten authors sorted by PageRank

Index	Degree Centrality	Name
715	52	Mark S. Shephard
758	52	Xiaoye Sherry Li
701	51	Eric Phipps
115	49	Omar Ghattas
1343	47	Youssef M. Marzouk
188	44	Siva Rajamanickam
189	43	Erik G. Boman
957	43	Lois Curfman McInnes
784	42	Emmanuel Agullo
2719	42	Stanley J. Osher

Table 6. First ten authors sorted by degree centrality

Institute of Technology. At ranking 10th we can find the Swiss institution, École Polytechnique

Fédérale de Lausanne, which was in the first position in the Swiss list.

5 Bibliography **Temporary**

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6 Conclusions

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