

Week 4: NumPy and Pandas

Numerical Computing and Data Manipulation

Dr. Eyuphan Koc

Bogazici University

Fall 2025

Based on "Python Data Science Handbook" by Jake VanderPlas
Chapter 2: Introduction to NumPy
Chapter 3: Data Manipulation with Pandas (Sections 3.0-3.6)
<https://github.com/jakevdp/PythonDataScienceHandbook>

NumPy Topics (Sections 1-9)

- ➊ Introduction to NumPy
- ➋ Array Fundamentals
- ➌ Array Operations & Ufuncs
- ➍ Aggregations & Statistics
- ➎ Broadcasting
- ➏ Boolean Operations
- ➐ Advanced Indexing
- ➑ Sorting
- ➒ Structured Data

Pandas Topics (Sections 10-16)

- ➓ Introduction to Pandas
- ➑ Pandas Core Objects
- ➒ Data Indexing & Selection
- ➓ Operations in Pandas
- ➑ Handling Missing Data
- ➒ Hierarchical Indexing
- ➓ Combining Datasets
- ➑ Summary & Next Steps

What is NumPy?

NumPy = Numerical Python

- Fundamental package for scientific computing in Python
- Provides fast, efficient multi-dimensional arrays
- Foundation for Pandas, SciPy, Matplotlib, and more
- Written in C - blazing fast performance

Why NumPy?

- Efficient operations on large datasets
- Vectorized computations (no loops!)
- Broadcasting for operations on different shapes
- Essential for data science and scientific computing
- Foundation for the entire PyData ecosystem

[TOGETHER] Speed Comparison: Lists vs NumPy

Python Lists

- Flexible but slow
- Type checking at every operation
- Overhead for each element

```
1 # Python list: slow
2 import time
3 L = list(range(1000000))
4 start = time.time()
5 result = [x**2 for x in L]
6 print(f"Time: {time.time()-start:.4f}s")
7 # Time: ~0.15s
```

NumPy Arrays

- Fixed type - no checking
- Contiguous memory block
- Vectorized C operations

```
1 # NumPy array: fast!
2 import numpy as np
3 A = np.arange(1000000)
4 start = time.time()
5 result = A**2
6 print(f"Time: {time.time()-start:.4f}s")
7 # Time: ~0.002s (75x faster!)
```

Key Takeaway

NumPy is 10-100x faster for numerical operations! Essential for large engineering datasets.

Installing and Importing NumPy

Installation

```
1 # Using pip
2 pip install numpy
3
4 # Using conda (recommended for data science)
5 conda install numpy
```

Standard Import Convention

```
1 import numpy as np # ALWAYS use this convention!
2
3 # Check version
4 print(np.__version__) # e.g., '1.24.3'
```

Why np?

Universal convention in data science community - makes code readable to everyone

Creating Your First NumPy Arrays

```
1 import numpy as np
2
3 # From Python list - 1D array
4 my_list = [1, 2, 3, 4, 5]
5 arr = np.array(my_list)
6 print(arr) # [1 2 3 4 5]
7
8 # 2D array (matrix)
9 matrix = np.array([[1, 2, 3],
10                    [4, 5, 6],
11                    [7, 8, 9]])
12 print(matrix)
13 # [[1 2 3]
14 #  [4 5 6]
15 #  [7 8 9]]
16
17 # Unlike lists, all elements must be same type!
18 mixed = np.array([1, 2.5, 3]) # Will convert to float
19 print(mixed.dtype) # dtype('float64')
```

Creating Arrays: Common Methods

```
1 import numpy as np
2
3 # Zeros - initialize array
4 zeros = np.zeros(10) # [0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]
5 zeros_matrix = np.zeros((3, 3)) # 3x3 matrix of zeros
6
7 # Ones
8 ones = np.ones(5) # [1. 1. 1. 1. 1.]
9 fives = np.ones(5) * 5 # [5. 5. 5. 5. 5.]
10
11 # Sequential values
12 seq = np.arange(0, 11, 2) # [0 2 4 6 8 10] (start, stop, step)
13
14 # Evenly spaced values
15 linear = np.linspace(0, 1, 5) # [0. 0.25 0.5 0.75 1.] (start, stop, count)
16
17 # Random values
18 random_vals = np.random.random(5) # 5 random values between 0 and 1
19 random_ints = np.random.randint(0, 10, size=5) # 5 random integers 0-9
20
21 # Identity matrix
22 I = np.eye(3) # [[1. 0. 0.], [0. 1. 0.], [0. 0. 1.]]
```

Array Attributes: Understanding Your Data

```
1 import numpy as np
2 np.random.seed(0) # for reproducibility
3
4 # Create arrays of different dimensions
5 x1 = np.random.randint(10, size=6) # 1D array
6 x2 = np.random.randint(10, size=(3, 4)) # 2D array
7 x3 = np.random.randint(10, size=(3, 4, 5)) # 3D array
8
9 print("x3 ndim: ", x3.ndim) # 3
10 print("x3 shape:", x3.shape) # (3, 4, 5)
11 print("x3 size: ", x3.size) # 60
12
13 print("dtype:", x3.dtype) # int64
14 print("itemsize:", x3.itemsize, "bytes") # 8 bytes
15 print("nbytes:", x3.nbytes, "bytes") # 480 bytes
```

Key Attributes

- **ndim**: number of dimensions
- **shape**: size of each dimension
- **size**: total number of elements
- **dtype**: data type of elements

Data Types in NumPy

Common Data Types

- int32, int64: Integers
- float32, float64: Floats
- complex128: Complex numbers
- bool: True/False

```
1 # Specify dtype at creation
2 arr = np.array([1, 2, 3],
3                 dtype=np.float32)
4
5 # Convert dtype
6 arr_float64 = arr.astype(np.float64)
7
8 print(arr.dtype)           # float32
9 print(arr_float64.dtype)   # float64
```

Why It Matters

- Memory: float32 uses half the space
- Precision: float64 for high accuracy
- Speed: Smaller types = faster processing

```
1 # Memory comparison
2 a32 = np.ones(1000000, dtype=np.float32)
3 a64 = np.ones(1000000, dtype=np.float64)
4
5 print(f"32-bit: {a32.nbytes/1e6} MB")
6 # 4.0 MB
7 print(f"64-bit: {a64.nbytes/1e6} MB")
8 # 8.0 MB
```

Indexing and Slicing: Accessing Array Elements

```
1 import numpy as np
2
3 # 1D array - similar to Python lists
4 x = np.arange(10) # [0 1 2 3 4 5 6 7 8 9]
5 print(x[0])       # 0 (first element)
6 print(x[-1])      # 9 (last element)
7 print(x[4:7])      # [4 5 6] (slice from index 4 to 6)
8 print(x[::2])      # [0 2 4 6 8] (every 2nd element)
9 print(x[::-1])     # [9 8 7 6 5 4 3 2 1 0] (reverse)
10
11 # 2D array - row, column indexing
12 x2 = np.array([[12, 5, 2, 4],
13               [7, 6, 8, 8],
14               [1, 6, 7, 7]])
15
16 print(x2[0, 0])    # 12 (element at row 0, col 0)
17 print(x2[2, -1])   # 7 (element at row 2, last column)
18 print(x2[0, :])    # [12 5 2 4] (first row)
19 print(x2[:, 1])    # [5 6 6] (second column)
20 print(x2[:2, :2])  # [[12 5], [ 7 6]] (2x2 subarray)
```

[TOGETHER] Array Views vs Copies

```
1 import numpy as np
2
3 # Original array
4 original = np.array([1, 2, 3, 4, 5])
5
6 # SLICING creates a VIEW (not a copy!)
7 view = original[1:4]
8 view[0] = 999
9 print(original) # [1 999 3 4 5] <-- Original changed!
10
11 # To create independent copy, use .copy()
12 original = np.array([1, 2, 3, 4, 5])
13 independent = original[1:4].copy()
14 independent[0] = 999
15 print(original) # [1 2 3 4 5] <-- Original unchanged
16 print(independent) # [999 3 4]
```

Critical for Engineering!

Views save memory but can cause bugs. Always use `.copy()` when you need independent data.

Reshaping Arrays

```
1 import numpy as np
2
3 # 1D to 2D
4 loads = np.arange(12)
5 print(loads) # [ 0  1  2  3  4  5  6  7  8  9 10 11]
6
7 # Reshape to 3x4 matrix
8 matrix = loads.reshape(3, 4)
9 print(matrix)
10 # [[ 0  1  2  3]
11 #   [ 4  5  6  7]
12 #   [ 8  9 10 11]]
13
14 # Reshape to 4x3 matrix
15 matrix2 = loads.reshape(4, 3)
16 print(matrix2)
17 # [[ 0  1  2]
18 #   [ 3  4  5]
19 #   [ 6  7  8]
20 #   [ 9 10 11]]
21
22 # Use -1 to auto-calculate one dimension
23 matrix3 = loads.reshape(2, -1) # 2 rows, auto-calculate columns
24 print(matrix3.shape) # (2, 6)
25
26 # Flatten back to 1D
27 flat = matrix.flatten() # or .ravel() for view
28 print(flat) # [ 0  1  2  3  4  5  6  7  8  9 10 11]
```

Concatenating and Splitting Arrays

```
1 import numpy as np
2
3 # Concatenate 1D arrays
4 dead_load = np.array([10, 15, 20])
5 live_load = np.array([5, 8, 10])
6 total_load = np.concatenate([dead_load, live_load])
7 print(total_load) # [10 15 20  5  8 10]
8
9 # Stack vertically (vstack)
10 loads = np.vstack([dead_load, live_load])
11 print(loads)
12 # [[10 15 20]
13 #  [ 5  8 10]]
14
15 # Stack horizontally (hstack)
16 loads = np.hstack([dead_load, live_load])
17 print(loads) # [10 15 20  5  8 10]
18
19 # Split array
20 split_loads = np.split(total_load, [3]) # Split at index 3
21 print(split_loads[0]) # [10 15 20]
22 print(split_loads[1]) # [ 5  8 10]
```

Vectorized Arithmetic: No Loops Needed!

```
1 import numpy as np
2
3 # Create arrays
4 x = np.arange(4)
5 print("x =", x) # [0 1 2 3]
6
7 # Element-wise operations (vectorized - FAST!)
8 print("x + 5 =", x + 5) # [5 6 7 8]
9 print("x - 5 =", x - 5) # [-5 -4 -3 -2]
10 print("x * 2 =", x * 2) # [0 2 4 6]
11 print("x / 2 =", x / 2) # [0. 0.5 1. 1.5]
12 print("x ** 2 =", x ** 2) # [0 1 4 9]
13
14 # Multiple arrays
15 a = np.array([1, 2, 3, 4])
16 b = np.array([4, 3, 2, 1])
17 print("a + b =", a + b) # [5 5 5 5]
18 print("a * b =", a * b) # [4 6 6 4]
19
20 # Compare to Python list (requires loop!)
21 # result = [x**2 for x in my_list] # Slow!
```

Universal Functions (ufuncs): Fast Operations

```
1 import numpy as np
2
3 # Trigonometric functions
4 theta = np.linspace(0, np.pi, 3)
5 print("sin(theta) =", np.sin(theta))
6 print("cos(theta) =", np.cos(theta))
7 print("tan(theta) =", np.tan(theta))
8
9 # Exponential and logarithmic
10 x = [1, 2, 3]
11 print("e^x =", np.exp(x))          # [2.718  7.389 20.086]
12 print("2^x =", np.exp2(x))         # [2.  4.  8.]
13 print("log(x) =", np.log(x))       # [0.  0.693  1.099]
14
15 # Absolute value
16 x = np.array([-2, -1, 0, 1, 2])
17 print("abs(x) =", np.abs(x))       # [2  1  0  1  2]
18
19 # All much faster than Python loops!
```

[EXPLORE] Example: Computation on Arrays

```
1 import numpy as np
2
3 # Compute values of sin(x) for many values
4 x = np.linspace(0, np.pi, 3)
5 print("x      =", x)
6 # [0.          1.57079633  3.14159265]
7
8 print("sin(x) =", np.sin(x))
9 # [0.0000000e+00  1.0000000e+00  1.2246468e-16]
10
11 # Compute a more complex operation
12 x = np.arange(5)
13 y = np.empty(5)
14 for i in range(5):
15     y[i] = x[i] ** 2
16 print(y) # [ 0.  1.  4.  9. 16.]
17
18 # Much better with vectorization:
19 x = np.arange(5)
20 y = x ** 2
21 print(y) # [ 0  1  4  9 16]
```


Basic Aggregations: Summarizing Data

```
1 import numpy as np
2
3 # Random data
4 L = np.random.random(100)
5
6 # Summary statistics
7 print(np.sum(L))      # Sum of all values
8 print(np.min(L))      # Minimum value
9 print(np.max(L))      # Maximum value
10 print(np.mean(L))     # Mean
11 print(np.std(L))      # Standard deviation
12 print(np.var(L))      # Variance
13
14 # These also work as array methods:
15 print(L.sum())
16 print(L.min())
17 print(L.max())
18 print(L.mean())
19 print(L.std())
20
21 # Percentiles
22 print(np.percentile(L, 25)) # 1st quartile
23 print(np.median(L))        # 50th percentile
24 print(np.percentile(L, 75)) # 3rd quartile
```

Multi-Dimensional Aggregations: The axis Parameter

```
1 import numpy as np
2
3 # 2D array example
4 M = np.random.random((3, 4))
5 print(M)
6
7 # Aggregate along different axes
8 print("Shape:", M.shape) # (3, 4)
9
10 # Sum all values
11 print(M.sum())
12
13 # Sum along axis 0 (collapse rows -> result has shape (4,))
14 print(M.sum(axis=0))
15
16 # Sum along axis 1 (collapse columns -> result has shape (3,))
17 print(M.sum(axis=1))
18
19 # Works with other functions too:
20 print(M.min(axis=0)) # Min of each column
21 print(M.max(axis=1)) # Max of each row
```

More Aggregation Functions

```
1 import numpy as np
2
3 data = np.array([10, 15, 20, 25, 30, 35, 40])
4
5 # Basic stats
6 print(f"Sum: {np.sum(data)}")           # 175
7 print(f"Product: {np.prod(data)}")      # 3.15e9
8 print(f"Mean: {np.mean(data)}")        # 25.0
9 print(f"Std: {np.std(data)}")           # 10.0
10 print(f"Variance: {np.var(data)}")      # 100.0
11
12 # Min/Max
13 print(f"Min: {np.min(data)}")           # 10
14 print(f"Max: {np.max(data)}")           # 40
15 print(f"Argmin: {np.argmin(data)}")     # 0 (index of min)
16 print(f"Argmax: {np.argmax(data)}")     # 6 (index of max)
17
18 # Cumulative operations
19 cumsum = np.cumsum(data) # [10 25 45 70 100 135 175]
20 cumprod = np.cumprod(data[:4]) # [10 150 3000 75000]
21
22 # Boolean operations
23 print(f"Any > 50: {np.any(data > 50)}") # False
24 print(f"All > 5: {np.all(data > 5)}")   # True
```

[TOGETHER] Example: Analyzing Multi-Dimensional Data

```
1 import numpy as np
2
3 # Precipitation data: 12 months x 5 years
4 precip_data = np.array([
5     [3.2, 2.8, 3.5, 2.9, 3.1], # January
6     [2.5, 2.9, 2.3, 2.7, 2.6], # February
7     [3.8, 4.1, 3.6, 4.0, 3.9], # March
8     # ... (more months)
9 ])
10
11 # Analysis
12 mean_per_month = np.mean(precip_data, axis=1)
13 mean_per_year = np.mean(precip_data, axis=0)
14 overall_mean = np.mean(precip_data)
15 overall_std = np.std(precip_data)
16
17 # Find extremes
18 max_precip = np.max(precip_data)
19 min_precip = np.min(precip_data)
20
21 print(f"Overall mean: {overall_mean:.2f}")
22 print(f"Std deviation: {overall_std:.2f}")
23 print(f"Range: {min_precip:.2f} - {max_precip:.2f}")
```

Broadcasting: Operating on Different Shapes

What is Broadcasting?

Broadcasting allows NumPy to perform operations on arrays of different shapes without explicitly replicating data.

Broadcasting Rules

- 1 If arrays have different dimensions, pad smaller shape with 1s on the left
- 2 If shapes don't match in a dimension, stretch dimension with size 1
- 3 If sizes disagree and neither is 1, raise error

Why It Matters

No loops needed! Operations are fast and memory-efficient. Essential for data science operations on large datasets.

Broadcasting Examples

```
1 import numpy as np
2
3 # Scalar + Array (broadcasts scalar to all elements)
4 a = np.array([0, 1, 2])
5 a + 5 # array([5, 6, 7])
6
7 # 1D + 1D
8 a = np.ones((3, 3))
9 b = np.arange(3)
10 a + b
11 # array([[1., 2., 3.],
12 #        [1., 2., 3.],
13 #        [1., 2., 3.]])
14
15 # Broadcasting with higher dimensions
16 a = np.arange(3).reshape((3, 1))
17 b = np.arange(3)
18 print(a + b)
19 # [[0 1 2]
20 #   [1 2 3]
21 #   [2 3 4]]
```

Broadcasting in 2D: Centering Data

```
1 import numpy as np
2
3 # Data matrix (10 observations x 3 features)
4 X = np.random.random((10, 3))
5
6 # Compute mean of each column (feature)
7 Xmean = X.mean(axis=0)
8
9 # Center the data (subtract mean from each column)
10 X_centered = X - Xmean
11
12 # Verify mean is now ~0 for each feature
13 print(X_centered.mean(axis=0))
14 # [~0. ~0. ~0.]
15
16 # This works because Xmean has shape (3,) which broadcasts
17 # to match X's shape (10, 3) by replicating across rows
```

[EXPLORE] Broadcasting: Plotting Functions

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 # Create a 2D grid using broadcasting
5 x = np.linspace(0, 5, 50)
6 y = np.linspace(0, 5, 50)[: , np.newaxis]
7
8 # Broadcasting: x is (50,), y is (50,1)
9 # Result z is (50, 50)
10 z = np.sin(x) ** 10 + np.cos(10 + y * x) * np.cos(x)
11
12 plt.imshow(z, origin='lower', extent=[0, 5, 0, 5],
13           cmap='viridis')
14 plt.colorbar()
15 plt.title('Broadcasting Example')
16 plt.show()
17
18 # This creates a 2D function from 1D arrays!
```


Comparison Operators: Element-wise Comparisons

```
1 import numpy as np
2
3 # Data array
4 x = np.array([1, 2, 3, 4, 5])
5
6 # Comparison operators return boolean arrays
7 print(x < 3)
8 # [ True  True False False False]
9
10 print(x > 3)
11 # [False False False  True  True]
12
13 print(x == 3)
14 # [False False  True False False]
15
16 # Multiple comparisons (use & and |, not 'and' and 'or')
17 print((x > 1) & (x < 5))
18 # [False  True  True  True False]
19
20 # Count how many satisfy condition
21 print(np.sum(x > 2)) # 3 (True=1, False=0)
22
23 # Percentage
24 print(np.mean(x > 2)) # 0.6 (60%)
```

Boolean Indexing: Filtering Data

```
1 import numpy as np
2
3 # Data array
4 x = np.array([1, 2, 3, 4, 5])
5
6 # Create boolean mask
7 mask = x < 3
8 print(mask)
9 # [ True  True False False False]
10
11 # Use mask to filter data
12 print(x[mask]) # [1 2]
13
14 # Can use directly without creating variable
15 print(x[x < 3]) # [1 2]
16
17 # More complex example with 2D
18 np.random.seed(0)
19 X = np.random.randint(10, size=(3, 4))
20 print(X)
21 # [[5 0 3 3]
22 #   [7 9 3 5]
23 #   [2 4 7 6]]
24
25 print(X[X < 5]) # [0 3 3 3 2 4] (flattened)
```

Boolean Operators: Combining Conditions

```
1 import numpy as np
2
3 # Example: Rainy days analysis
4 rainfall_inches = np.array([0.2, 0.5, 0.0, 1.2, 0.8, 0.0, 0.3])
5
6 # Multiple criteria with & (AND) and | (OR)
7 print((rainfall_inches > 0) & (rainfall_inches < 1))
8 # [ True  True False False  True False  True]
9
10 print((rainfall_inches <= 0) | (rainfall_inches >= 1))
11 # [False False  True  True False  True False]
12
13 # Use np.sum() to count matches
14 print(np.sum((rainfall_inches > 0) & (rainfall_inches < 1))) # 4
15
16 # IMPORTANT: Use & and | for arrays, not 'and' and 'or'!
17 # Also: always use parentheses around conditions
18
19 # Boolean operators
20 print(~(rainfall_inches > 0.5)) # NOT
21 # [ True False  True False False  True  True]
```

[TOGETHER] Example: Analyzing Weather Data

```
1 import numpy as np
2
3 # Weather data
4 np.random.seed(1)
5 rainfall = np.random.random(365) * 2 # inches per day
6
7 # Analysis
8 rainy_days = np.sum(rainfall > 0.5)
9 dry_days = np.sum(rainfall < 0.1)
10 median_precip = np.median(rainfall)
11 mean_precip = np.mean(rainfall)
12
13 print(f"Rainy days (>0.5 in): {rainy_days}")
14 print(f"Dry days (<0.1 in): {dry_days}")
15 print(f"Median: {median_precip:.2f} in")
16 print(f"Mean: {mean_precip:.2f} in")
17
18 # Get all rainy day amounts
19 rainy = rainfall[rainfall > 0.5]
20 print(f"Average rainfall on rainy days: {rainy.mean():.2f} in")
```

Fancy Indexing: Using Arrays as Indices

```
1 import numpy as np
2
3 # Simple array
4 x = np.array([51, 92, 14, 71, 60, 20, 82, 86, 74, 74])
5
6 # Select specific elements by index
7 ind = [3, 7, 4]
8 print(x[ind]) # [71 86 60]
9
10 # 2D indexing
11 X = np.arange(12).reshape((3, 4))
12 print(X)
13 # [[ 0  1  2  3]
14 #   [ 4  5  6  7]
15 #   [ 8  9 10 11]]
16
17 # Select specific rows and columns
18 row = np.array([0, 1, 2])
19 col = np.array([2, 1, 3])
20 print(X[row, col]) # [ 2  5 11]
21
22 # Select a subset of rows
23 print(X[[0, 2]])
24 # [[ 0  1  2  3]
25 #   [ 8  9 10 11]]
```

Modifying Values with Fancy Indexing

```
1 import numpy as np
2
3 # Start with array of zeros
4 x = np.zeros(10)
5 print(x)  # [0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]
6
7 # Set specific indices
8 ind = [0, 3, 5]
9 x[ind] = 99
10 print(x)  # [99.  0.  0. 99.  0. 99.  0.  0.  0.  0.]
11
12 # Increment specific values
13 x[ind] += 1
14 print(x)  # [100.   0.   0. 100.   0. 100.   0.   0.   0.   0.]
15
16 # Repeated indices - behavior is subtle!
17 x = np.zeros(5)
18 i = [0, 0, 0]
19 x[i] += 1
20 print(x)  # [1. 0. 0. 0. 0.] - only incremented once!
```

Combined Indexing: Mix and Match

```
1 import numpy as np
2
3 # 2D array
4 X = np.arange(12).reshape((3, 4))
5 print(X)
6 # [[ 0  1  2  3]
7 #   [ 4  5  6  7]
8 #   [ 8  9 10 11]]
9
10 # Fancy indexing + slicing
11 # Select rows 0 and 2, columns 1 and 3
12 result = X[[0, 2]][:, [1, 3]]
13 print(result)
14 # [[ 1  3]
15 #   [ 9 11]]
16
17 # Boolean mask + fancy indexing
18 mask = X[:, 1] > 5
19 print(mask) # [False False  True]
20 print(X[mask])
21 # [[ 8  9 10 11]]
```

Sorting Arrays

```
1 import numpy as np
2
3 # Unsorted array
4 x = np.array([2, 1, 4, 3, 5])
5
6 # Sort (returns new sorted array)
7 print(np.sort(x)) # [1 2 3 4 5]
8
9 # argsort: returns indices that would sort the array
10 i = np.argsort(x)
11 print(i) # [1 0 3 2 4]
12 print(x[i]) # [1 2 3 4 5]
13
14 # Sort in descending order
15 print(x[np.argsort(x)[::-1]]) # [5 4 3 2 1]
16
17 # Sort 2D array along axis
18 np.random.seed(42)
19 X = np.random.randint(0, 10, (4, 6))
20 print(X)
21
22 # Sort each column
23 print(np.sort(X, axis=0))
24
25 # Sort each row
26 print(np.sort(X, axis=1))
```


Practical Sorting: Finding Top N Elements

```
1 import numpy as np
2
3 # Array of values
4 x = np.array([7, 2, 3, 1, 6, 5, 4])
5
6 # Partition: smallest 3 on left, rest on right
7 print(np.partition(x, 3))
8 # [2 1 3 4 6 5 7] (3 smallest values on left, not sorted)
9
10 # Get indices for partition
11 i = np.argpartition(x, 3)
12 print(x[i])
13 # [2 1 3 4 6 5 7]
14
15 # Find top K values efficiently
16 # Partition so K largest are on the right
17 K = 3
18 partitioned = np.partition(x, -K)
19 print(partitioned[-K:]) # [5 6 7] (not necessarily sorted)
20
21 # For sorted top K, use argsort
22 top_k_sorted = x[np.argsort(x)[-K:]]
23 print(top_k_sorted) # [5 6 7]
```

Structured Arrays: Mixing Data Types

```
1 import numpy as np
2
3 # Create structured array for person data
4 data = np.zeros(4, dtype={
5     'names': ('name', 'age', 'weight'),
6     'formats': ('U10', 'i4', 'f8')
7 })
8
9 # Fill data
10 data['name'] = ['Alice', 'Bob', 'Cathy', 'Doug']
11 data['age'] = [25, 45, 37, 19]
12 data['weight'] = [55.0, 85.5, 68.0, 61.5]
13
14 print(data)
15 # [('Alice', 25, 55. ) ('Bob', 45, 85.5)
16 #  ('Cathy', 37, 68. ) ('Doug', 19, 61.5)]
17
18 # Access by field name
19 print(data['name']) # ['Alice' 'Bob' 'Cathy' 'Doug']
20 print(data['age'])  # [25 45 37 19]
21
22 # Filter
23 print(data[data['age'] < 30]['name']) # ['Alice' 'Doug']
```

Note

For complex data, Pandas DataFrames are usually better! Let's learn about them now.

From NumPy to Pandas: The Next Step

What is Pandas?

- Built on top of NumPy
- Provides DataFrame: labeled, 2D data structure
- Like Excel or SQL tables, but in Python
- Industry standard for data manipulation
- Essential for real-world data analysis

Why Pandas After NumPy?

- NumPy: Fast arrays, but no labels or structure
- Pandas: Labels + missing data + heterogeneous types
- Access data by name, not just index position
- Built-in tools for reading CSV, Excel, SQL
- Better for messy, real-world data

Installing and Importing Pandas

Installation

```
1 # Using pip
2 pip install pandas
3
4 # Using conda (recommended for data science)
5 conda install pandas
```

Standard Import Convention

```
1 import pandas as pd # ALWAYS use this convention!
2 import numpy as np  # Often used together
3
4 # Check version
5 print(pd.__version__) # e.g., '2.0.0'
```

Universal Convention

Like NumPy's `np`, always import Pandas as `pd`. This is the universal standard!

NumPy vs Pandas: A Quick Comparison

NumPy Array

- Access by integer index
- No column names
- Homogeneous types
- Fast but minimal structure

```
1 # NumPy array
2 data = np.array([[1, 2, 3],
3                  [4, 5, 6]])
4 print(data[0, 1]) # 2
5 # Which column is this? Must remember!
```

Pandas DataFrame

- Access by label or index
- Named columns and rows
- Mixed types allowed
- More features, slight overhead

```
1 # Pandas DataFrame
2 df = pd.DataFrame([[1, 2, 3],
3                    [4, 5, 6]],
4                    columns=['A', 'B', 'C'])
5 print(df['B'][0]) # 2
6 # Clear what column 'B' means!
```

The Pandas Ecosystem

Core Data Structures

- **Series:** 1D labeled array (like a column)
- **DataFrame:** 2D labeled table (like a spreadsheet)
- **Index:** Row and column labels

Common Use Cases

- Loading and cleaning CSV/Excel data
- Time series analysis (stock prices, weather)
- Database-style operations (join, merge, group)
- Handling missing data
- Statistical analysis and visualization
- Data preprocessing for machine learning

Learning Path

Master NumPy first (✓), then Pandas builds naturally on top!

The Pandas Series: 1D Labeled Array

```
1 import pandas as pd
2 import numpy as np
3
4 # Create Series from list
5 data = pd.Series([0.25, 0.5, 0.75, 1.0])
6 print(data)
7 # 0    0.25
8 # 1    0.50
9 # 2    0.75
10 # 3    1.00
11 # dtype: float64
12
13 # Access values and index
14 print(data.values) # array([0.25, 0.5 , 0.75, 1.  ])
15 print(data.index)  # RangeIndex(start=0, stop=4, step=1)
16
17 # Access like array
18 print(data[1])      # 0.5
19 print(data[1:3])    # Series with indices 1, 2
```

Series with Custom Index

```
1 import pandas as pd
2
3 # Series with string index (like a dictionary!)
4 data = pd.Series([0.25, 0.5, 0.75, 1.0],
5                  index=['a', 'b', 'c', 'd'])
6 print(data)
7 # a    0.25
8 # b    0.50
9 # c    0.75
10 # d    1.00
11
12 # Access by label
13 print(data['b']) # 0.5
14
15 # Can use non-contiguous indices
16 data = pd.Series([0.25, 0.5, 0.75, 1.0],
17                  index=[2, 5, 3, 7])
18 print(data[5]) # 0.5
```


Series from Dictionary

```
1 import pandas as pd
2
3 # Create Series from dictionary
4 population_dict = {
5     'California': 38332521,
6     'Texas': 26448193,
7     'New York': 19651127,
8     'Florida': 19552860,
9     'Illinois': 12882135
10 }
11 population = pd.Series(population_dict)
12 print(population)
13 # California      38332521
14 # Florida         19552860
15 # Illinois        12882135
16 # New York        19651127
17 # Texas           26448193
18
19 # Dictionary-style access
20 print(population['California']) # 38332521
21
22 # Array-style slicing
23 print(population['California':'Illinois'])
```

The DataFrame: 2D Labeled Data Structure

```
1 import pandas as pd
2
3 # Create DataFrame from dictionary of Series
4 area_dict = {'California': 423967, 'Texas': 695662,
5              'New York': 141297, 'Florida': 170312,
6              'Illinois': 149995}
7 area = pd.Series(area_dict)
8
9 states = pd.DataFrame({'population': population,
10                       'area': area})
11 print(states)
12 #           area  population
13 # California  423967    38332521
14 # Florida    170312    19552860
15 # Illinois   149995    12882135
16 # New York   141297    19651127
17 # Texas      695662    26448193
18
19 print(states.index)    # State names
20 print(states.columns)  # ['area', 'population']
```

[TOGETHER] Creating DataFrames: Multiple Ways

```
1 import pandas as pd
2 import numpy as np
3
4 # From dictionary of lists
5 df1 = pd.DataFrame({'A': [1, 2, 3],
6                     'B': [4, 5, 6]})
7
8 # From list of dictionaries
9 df2 = pd.DataFrame([{'a': 1, 'b': 2},
10                    {'a': 3, 'b': 4, 'c': 5}])
11 print(df2)
12 #      a  b   c
13 # 0  1.0  2  NaN
14 # 1  3.0  4  5.0
15
16 # From NumPy array
17 df3 = pd.DataFrame(np.random.rand(3, 2),
18                    columns=['foo', 'bar'],
19                    index=['a', 'b', 'c'])
20
21 # Add new column
22 states['density'] = states['population'] / states['area']
```

DataFrame as Dictionary of Series

```
1 import pandas as pd
2
3 # Access column (returns Series)
4 print(states['area'])
5 # California    423967
6 # Florida       170312
7 # ...
8
9 # Also works with attribute-style access
10 print(states.area) # Same as states['area']
11
12 # Check if they're the same object
13 print(states.area is states['area']) # True
14
15 # Add new column
16 states['density'] = states['population'] / states['area']
17 print(states)
18 #           area  population    density
19 # California  423967    38332521    90.413926
20 # Florida     170312    19552860   114.806121
21 # ...
```

The Index Object

```
1 import pandas as pd
2
3 # Create Index
4 ind = pd.Index([2, 3, 5, 7, 11])
5 print(ind) # Index([2, 3, 5, 7, 11], dtype='int64')
6
7 # Index as immutable array
8 print(ind[1]) # 3
9 print(ind[:2]) # Index([2, 5, 11])
10
11 # Index attributes (like NumPy arrays)
12 print(ind.size, ind.shape, ind.ndim, ind.dtype)
13 # 5 (5,) 1 int64
14
15 # Indices are IMMUTABLE
16 # ind[1] = 0 # This will raise TypeError!
17
18 # Index as ordered set
19 indA = pd.Index([1, 3, 5, 7, 9])
20 indB = pd.Index([2, 3, 5, 7, 11])
21 print(indA & indB) # Intersection: [3, 5, 7]
22 print(indA | indB) # Union: [1, 2, 3, 5, 7, 9, 11]
```

Key Takeaways: Pandas Objects

Series

- 1D labeled array = generalized NumPy array
- Also like a specialized dictionary
- Has both `values` (array) and `index` (labels)

DataFrame

- 2D labeled data structure = table with named columns
- Like a dictionary of Series (all sharing same index)
- Has `index` (rows), `columns`, and `values`
- Can contain heterogeneous types

Index

- Immutable array for row/column labels
- Supports set operations (union, intersection)
- Shared between Series/DataFrame for alignment

Series Indexing: Dictionary and Array Style

```
1 import pandas as pd
2
3 data = pd.Series([0.25, 0.5, 0.75, 1.0],
4                  index=['a', 'b', 'c', 'd'])
5
6 # Dictionary-style indexing
7 print(data['b']) # 0.5
8 print('a' in data) # True
9
10 # Array-style slicing
11 print(data['a':'c']) # Includes 'c'! (explicit index)
12 # a    0.25
13 # b    0.50
14 # c    0.75
15
16 print(data[0:2]) # Excludes index 2 (implicit index)
17 # a    0.25
18 # b    0.50
19
20 # Masking
21 print(data[(data > 0.3) & (data < 0.8)])
22 # Fancy indexing
23 print(data[['a', 'c']])
```

The Indexers: loc, iloc, and ix

Confusion with Integer Indices

When Series has integer index, `data[1]` uses explicit index, but `data[1:3]` uses implicit. This can be confusing!

```
1 data = pd.Series(['a', 'b', 'c'], index=[1, 3, 5])
2
3 # loc: ALWAYS uses explicit index
4 print(data.loc[1])      # 'a'
5 print(data.loc[1:3])    # Indices 1, 3 (both included!)
6
7 # iloc: ALWAYS uses implicit Python-style index
8 print(data.iloc[1])     # 'b' (position 1)
9 print(data.iloc[1:3])   # Positions 1, 2 (excludes 3)
```

Best Practice

Always use `loc` and `iloc` explicitly! Makes code clearer and prevents bugs.

DataFrame Indexing: Columns Come First

```
1 import pandas as pd
2
3 area = pd.Series({'California': 423967, 'Texas': 695662,
4                  'New York': 141297, 'Florida': 170312})
5 pop = pd.Series({'California': 38332521, 'Texas': 26448193,
6                 'New York': 19651127, 'Florida': 19552860})
7 data = pd.DataFrame({'area':area, 'pop':pop})
8
9 # Access column (returns Series)
10 print(data['area']) # Column 'area'
11
12 # Attribute-style access (if name doesn't conflict)
13 print(data.area) # Same as data['area']
14
15 # Add new column
16 data['density'] = data['pop'] / data['area']
17
18 # Slicing accesses ROWS (different from columns!)
19 print(data['Florida':'New York']) # Rows Florida to New York
```

[TOGETHER] DataFrame: loc and iloc

```
1 import pandas as pd
2
3 # iloc: Python-style integer indexing
4 print(data.iloc[:3, :2]) # First 3 rows, first 2 columns
5 #
6 #   area  pop
7 # California  423967  38332521
8 # Florida    170312  19552860
9 # Illinois   149995  12882135
10
11 # loc: Label-based indexing
12 print(data.loc[:'Florida', :'pop']) # Up to Florida, up to pop
13 #
14 #   area  pop
15 # California  423967  38332521
16 # Florida    170312  19552860
17
18 # Mixing both styles
19 print(data.loc[data.density > 100, ['pop', 'density']])
20 #
21 #   pop  density
22 # Florida    19552860  114.806121
23 # New York   19651127  139.076746
```

Boolean Masking in DataFrames

```
1 import pandas as pd
2
3 # Boolean mask on rows
4 high_density = data.density > 100
5 print(data[high_density])
6 #           area      pop      density
7 # Florida    170312  19552860  114.806121
8 # New York   141297  19651127  139.076746
9
10 # Combine with loc for specific columns
11 print(data.loc[high_density, ['pop', 'density']])
12
13 # Boolean operations
14 # Use & (AND), | (OR), ~ (NOT), not 'and', 'or', 'not'!
15 mask = (data['density'] > 50) & (data['density'] < 120)
16 print(data[mask])
17
18 # Fancy indexing: select specific rows and columns
19 print(data.loc[['California', 'Texas'], ['pop', 'area']])
```

Indexing Conventions: Summary

Series Indexing

- `data[key]`: Dictionary-style access by explicit index
- `data[i:j]`: Array-style slicing by implicit index
- `data.loc[key]`: Explicit indexing
- `data.iloc[i]`: Implicit integer indexing

DataFrame Indexing

- `data['col']`: Access column
- `data.iloc[i, j]`: Integer row/column indexing
- `data.loc[label, col]`: Label-based row/column indexing
- `data[mask]`: Boolean masking on rows

Key Rule

Columns are primary in DataFrames! `data['col']` gets column, not row.

Ufuncs: Index Preservation

```
1 import pandas as pd
2 import numpy as np
3
4 rng = np.random.RandomState(42)
5 ser = pd.Series(rng.randint(0, 10, 4))
6 print(ser)
7 # 0      6
8 # 1      3
9 # 2      7
10 # 3      4
11
12 # NumPy ufuncs preserve index!
13 print(np.exp(ser))
14 # 0      403.428793
15 # 1      20.085537
16 # 2     1096.633158
17 # 3      54.598150
18
19 # Works with DataFrames too
20 df = pd.DataFrame(rng.randint(0, 10, (3, 4)),
21                   columns=['A', 'B', 'C', 'D'])
22 print(np.sin(df * np.pi / 4)) # Preserves row/column labels!
```

[TOGETHER] Index Alignment in Operations

```
1 import pandas as pd
2
3 # Top 3 states by area
4 area = pd.Series({'Alaska': 1723337, 'Texas': 695662,
5                  'California': 423967})
6 # Top 3 states by population
7 population = pd.Series({'California': 38332521, 'Texas': 26448193,
8                        'New York': 19651127})
9
10 # Division aligns indices automatically!
11 density = population / area
12 print(density)
13 # Alaska          NaN    (no population data)
14 # California      90.413926
15 # New York        NaN    (no area data)
16 # Texas           38.018740
17
18 # Result contains UNION of indices
19 # Missing values filled with NaN
```

Index Alignment: Controlling Missing Values

```
1 import pandas as pd
2
3 A = pd.Series([2, 4, 6], index=[0, 1, 2])
4 B = pd.Series([1, 3, 5], index=[1, 2, 3])
5
6 # Default: union of indices, fill with NaN
7 print(A + B)
8 # 0      NaN
9 # 1      5.0
10 # 2      9.0
11 # 3      NaN
12
13 # Use .add() method with fill_value
14 print(A.add(B, fill_value=0))
15 # 0      2.0  (2 + 0)
16 # 1      5.0  (4 + 1)
17 # 2      9.0  (6 + 3)
18 # 3      5.0  (0 + 5)
```

Python Operator	Pandas Method
+	add()
-	sub(), subtract()
*	mul(), multiply()
/	truediv(), div(), divide()
//	floordiv()
%	mod()
**	pow()

Why Use Methods?

Methods allow you to specify `fill_value` for missing data and control alignment behavior.

Operations Between DataFrame and Series

```
1 import pandas as pd
2 import numpy as np
3
4 # Create DataFrame
5 A = np.array([[3, 8, 2, 4],
6               [2, 6, 4, 8],
7               [6, 1, 3, 8]])
8 df = pd.DataFrame(A, columns=list('QRST'))
9
10 # Subtract first row (broadcasts row-wise by default)
11 print(df - df.iloc[0])
12 #      Q  R  S  T
13 # 0  0  0  0  0
14 # 1 -1 -2  2  4
15 # 2  3 -7  1  4
16
17 # For column-wise, specify axis
18 print(df.subtract(df['R'], axis=0))
19 #      Q  R  S  T
20 # 0 -5  0 -6 -4
21 # 1 -4  0 -2  2
22 # 2  5  0  2  7
```

Key Advantages of Pandas Operations

Automatic Index Alignment

- Operations automatically align on matching indices
- No need to manually match row/column labels
- Prevents errors from misaligned data

Index Preservation

- Labels are maintained through operations
- Results keep meaningful row/column names
- Data context is never lost

Compare to NumPy

NumPy arrays lose label information. Pandas keeps everything organized and labeled!

The Problem

Real-world data is rarely clean! Missing values are common in:

- Sensor data (equipment failures)
- Survey responses (unanswered questions)
- Database joins (unmatched records)
- Data entry errors

Pandas Approach: Two Sentinels

- **None**: Python object for missing data
- **NaN**: IEEE floating-point "Not a Number"
- Pandas treats them (nearly) interchangeably

None vs NaN

```
1 import numpy as np
2 import pandas as pd
3
4 # None: Python object (slow, object dtype)
5 vals1 = np.array([1, None, 3, 4])
6 print(vals1.dtype) # object
7 # Operations are slow! Uses Python loops, not C
8
9 # NaN: Floating-point (fast, native type)
10 vals2 = np.array([1, np.nan, 3, 4])
11 print(vals2.dtype) # float64
12 # Fast! Uses compiled C code
13
14 # NaN is "contagious"
15 print(1 + np.nan) # nan
16 print(0 * np.nan) # nan
17
18 # Pandas converts between them automatically
19 print(pd.Series([1, np.nan, 2, None]))
20 # 0    1.0
21 # 1    NaN
22 # 2    2.0
23 # 3    NaN
```

Detecting Missing Data

```
1 import pandas as pd
2 import numpy as np
3
4 data = pd.Series([1, np.nan, 'hello', None])
5
6 # isnull(): returns Boolean mask
7 print(data.isnull())
8 # 0      False
9 # 1       True
10 # 2      False
11 # 3       True
12
13 # notnull(): opposite of isnull()
14 print(data.notnull())
15 # 0       True
16 # 1      False
17 # 2       True
18 # 3      False
19
20 # Use Boolean indexing to filter
21 print(data[data.notnull()])
22 # 0      1
23 # 2    hello
```

[TOGETHER] Dropping Missing Data

```
1 import pandas as pd
2 import numpy as np
3
4 # Series: dropna() removes NaN values
5 data = pd.Series([1, np.nan, 2, None, 3])
6 print(data.dropna())
7 # 0      1.0
8 # 2      2.0
9 # 4      3.0
10
11 # DataFrame: more options!
12 df = pd.DataFrame([[1,      np.nan, 2],
13                    [2,      3,      5],
14                    [np.nan, 4,      6]])
15
16 # Drop rows with ANY NaN
17 print(df.dropna()) # Only row 1 remains
18
19 # Drop columns with ANY NaN
20 print(df.dropna(axis='columns')) # Only column 2 remains
21
22 # Drop only if ALL values are NaN
23 print(df.dropna(how='all'))
```

Filling Missing Data

```
1 import pandas as pd
2 import numpy as np
3
4 data = pd.Series([1, np.nan, 2, None, 3], index=list('abcde'))
5
6 # Fill with constant value
7 print(data.fillna(0))
8 # a      1.0
9 # b      0.0  <- filled
10 # c      2.0
11 # d      0.0  <- filled
12 # e      3.0
13
14 # Forward fill: propagate previous value
15 print(data.fillna(method='ffill'))
16 # b      1.0  <- filled with 'a'
17 # d      2.0  <- filled with 'c'
18
19 # Back fill: propagate next value
20 print(data.fillna(method='bfill'))
21 # b      2.0  <- filled with 'c'
22 # d      3.0  <- filled with 'e'
```

DataFrame: Filling with axis Parameter

```
1 import pandas as pd
2 import numpy as np
3
4 df = pd.DataFrame([[1,    np.nan, 2],
5                    [2,    3,    5],
6                    [np.nan, 4,    6]])
7
8 # Forward fill along columns (row-wise)
9 print(df.fillna(method='ffill', axis=1))
10 #      0      1      2
11 # 0  1.0  1.0  2.0
12 # 1  2.0  3.0  5.0
13 # 2  NaN  4.0  6.0  <- No previous value in row
14
15 # Forward fill along rows (column-wise)
16 print(df.fillna(method='ffill', axis=0))
17 #      0      1      2
18 # 0  1.0  NaN  2
19 # 1  2.0  3.0  5
20 # 2  2.0  4.0  6  <- Filled from row 1
```


Missing Data: Summary

Detection

- `isnull()`: Boolean mask of missing values
- `notnull()`: Boolean mask of valid values
- Use for filtering or counting: `data[data.notnull()]`

Removal

- `dropna()`: Remove NaN values
- Series: drops NaN entries
- DataFrame: drops rows or columns (specify axis)
- Control with `how='all'` or `thresh=n`

Filling

- `fillna(value)`: Replace with constant
- `fillna(method='ffill')`: Forward fill
- `fillna(method='bfill')`: Backward fill
- Specify axis for direction in DataFrame

The Challenge

Often need to work with data indexed by more than one or two keys:

- Data by (state, year)
- Measurements by (subject, visit, test)
- Stock prices by (date, ticker)

Solution: MultiIndex

- Multiple index levels within a single index
- Store higher-dimensional data in 1D Series or 2D DataFrame
- More flexible than Panel (3D) or Panel4D (4D)
- Efficient and intuitive for complex data

Creating a MultiIndex Series

```
1 import pandas as pd
2
3 # State population data for multiple years
4 index = pd.MultiIndex.from_tuples([
5     ('California', 2000), ('California', 2010),
6     ('New York', 2000), ('New York', 2010),
7     ('Texas', 2000), ('Texas', 2010)
8 ])
9 populations = [33871648, 37253956, 18976457,
10               19378102, 20851820, 25145561]
11 pop = pd.Series(populations, index=index)
12 print(pop)
13 # (California, 2000)    33871648
14 # (California, 2010)    37253956
15 # (New York, 2000)      18976457
16 # (New York, 2010)      19378102
17 # (Texas, 2000)         20851820
18 # (Texas, 2010)         25145561
19
20 # Name the index levels
21 pop.index.names = ['state', 'year']
```

[TOGETHER] Indexing with MultiIndex

```
1 import pandas as pd
2
3 # Access all data for year 2010
4 print(pop[:, 2010])
5 # state
6 # California      37253956
7 # New York        19378102
8 # Texas           25145561
9
10 # Access all data for California
11 print(pop['California'])
12 # year
13 # 2000      33871648
14 # 2010      37253956
15
16 # Access specific element
17 print(pop['California', 2010]) # 37253956
18
19 # Slicing works too!
20 print(pop['California':'New York'])
```

MultiIndex DataFrames

```
1 import pandas as pd
2
3 # Add another column to our MultiIndex data
4 pop_df = pd.DataFrame({
5     'total': pop,
6     'under18': [9267089, 9284094, 4687374,
7                 4318033, 5906301, 6879014]
8 })
9 print(pop_df)
10 #
11 # state      year
12 # California 2000 33871648 9267089
13 #           2010 37253956 9284094
14 # New York   2000 18976457 4687374
15 #           2010 19378102 4318033
16 # Texas      2000 20851820 5906301
17 #           2010 25145561 6879014
18
19 # Calculate fraction under 18
20 f_u18 = pop_df['under18'] / pop_df['total']
21 print(f_u18.unstack()) # Convert to regular DataFrame
```

Creating MultiIndex: Multiple Methods

```
1 import pandas as pd
2
3 # From arrays
4 pd.MultiIndex.from_arrays([
5     ['a', 'a', 'b', 'b'],
6     [1, 2, 1, 2]
7 ])
8
9 # From tuples
10 pd.MultiIndex.from_tuples([
11     ('a', 1), ('a', 2), ('b', 1), ('b', 2)
12 ])
13
14 # From product (Cartesian product)
15 pd.MultiIndex.from_product([
16     ['a', 'b'], # Level 0
17     [1, 2]      # Level 1
18 ])
19
20 # All create the same MultiIndex!
21 # MultiIndex(levels=[['a', 'b'], [1, 2]],
22 #             codes=[[0, 0, 1, 1], [0, 1, 0, 1]])
```

Stack and Unstack

```
1 import pandas as pd
2
3 # Unstack: convert MultiIndex to regular DataFrame
4 print(pop.unstack())
5 # year          2000      2010
6 # state
7 # California  33871648  37253956
8 # New York   18976457  19378102
9 # Texas      20851820  25145561
10
11 # Stack: convert back to MultiIndex Series
12 print(pop.unstack().stack())
13 # state      year
14 # California 2000      33871648
15 #           2010      37253956
16 # New York   2000      18976457
17 #           2010      19378102
18 # Texas      2000      20851820
19 #           2010      25145561
20
21 # Can specify level to unstack
22 print(pop.unstack(level=0)) # Unstack states instead
```

MultIndex: Key Concepts

Why Use MultiIndex?

- Represent higher-dimensional data compactly
- More flexible than Panel/Panel4D
- Efficient for sparse multi-dimensional data
- Intuitive slicing and indexing

Key Operations

- `MultiIndex.from_tuples()`, `from_arrays()`, `from_product()`
- `pop['California']`: Partial indexing
- `pop[:, 2010]`: Slicing on second level
- `unstack()`: `MultiIndex` \rightarrow `DataFrame`
- `stack()`: `DataFrame` \rightarrow `MultiIndex`

Important

MultiIndex must be sorted for partial slicing! Use `sort_index()` if needed.

Why Combine Data?

Common Scenarios

- Combining data from multiple sensors/sources
- Appending new observations to existing dataset
- Merging different measurements of same subjects
- Concatenating time series data from different periods

Pandas Tools

- **pd.concat()**: General concatenation
- **df.append()**: Quick row append (less efficient)
- **pd.merge()** and **pd.join()**: Database-style joins (next lecture!)

Simple Concatenation with pd.concat()

```
1 import pandas as pd
2
3 # Concatenate Series
4 ser1 = pd.Series(['A', 'B', 'C'], index=[1, 2, 3])
5 ser2 = pd.Series(['D', 'E', 'F'], index=[4, 5, 6])
6 print(pd.concat([ser1, ser2]))
7 # 1      A
8 # 2      B
9 # 3      C
10 # 4      D
11 # 5      E
12 # 6      F
13
14 # Concatenate DataFrames (row-wise by default)
15 df1 = pd.DataFrame({'A': ['A1', 'A2'], 'B': ['B1', 'B2']})
16 df2 = pd.DataFrame({'A': ['A3', 'A4'], 'B': ['B3', 'B4']})
17 print(pd.concat([df1, df2]))
18 #      A      B
19 # 0  A1  B1
20 # 1  A2  B2
21 # 0  A3  B3   <- Index repeated!
22 # 1  A4  B4
```

Concatenation Along Different Axes

```
1 import pandas as pd
2
3 df1 = pd.DataFrame({'A': ['A0', 'A1'],
4                     'B': ['B0', 'B1']})
5 df2 = pd.DataFrame({'C': ['C0', 'C1'],
6                     'D': ['D0', 'D1']})
7
8 # Concatenate along columns (axis=1)
9 print(pd.concat([df1, df2], axis=1))
10 #      A      B      C      D
11 # 0  A0    B0    C0    D0
12 # 1  A1    B1    C1    D1
13
14 # Concatenate along rows (axis=0, default)
15 print(pd.concat([df1, df2], axis=0))
16 #      A      B      C      D
17 # 0  A0    B0    NaN    NaN
18 # 1  A1    B1    NaN    NaN
19 # 0  NaN    NaN    C0    D0
20 # 1  NaN    NaN    C1    D1
```

[TOGETHER] Handling Duplicate Indices

```
1 import pandas as pd
2
3 df1 = pd.DataFrame({'A': ['A0', 'A1'], 'B': ['B0', 'B1']})
4 df2 = pd.DataFrame({'A': ['A2', 'A3'], 'B': ['B2', 'B3']})
5
6 # Option 1: Ignore old index, create new one
7 print(pd.concat([df1, df2], ignore_index=True))
8 #      A  B
9 # 0  A0 B0
10 # 1  A1 B1
11 # 2  A2 B2
12 # 3  A3 B3
13
14 # Option 2: Add hierarchical index with keys
15 print(pd.concat([df1, df2], keys=['x', 'y']))
16 #      A  B
17 # x 0  A0 B0
18 #   1  A1 B1
19 # y 0  A2 B2
20 #   1  A3 B3
21
22 # Option 3: Verify integrity (raise error if duplicates)
23 # pd.concat([df1, df2], verify_integrity=True) # Raises error!
```

Concatenation with Joins

```
1 import pandas as pd
2
3 df1 = pd.DataFrame({'A': ['A0', 'A1', 'A2'],
4                     'B': ['B0', 'B1', 'B2']})
5 df2 = pd.DataFrame({'B': ['B3', 'B4', 'B5'],
6                     'C': ['C3', 'C4', 'C5']})
7
8 # Default: outer join (union of columns)
9 print(pd.concat([df1, df2]))
10 #      A    B    C
11 # 0   A0   B0  NaN
12 # 1   A1   B1  NaN
13 # 2   A2   B2  NaN
14 # 0  NaN   B3   C3
15 # 1  NaN   B4   C4
16 # 2  NaN   B5   C5
17
18 # Inner join: intersection of columns
19 print(pd.concat([df1, df2], join='inner'))
20 #      B
21 # 0   B0
22 # 1   B1
23 # 2   B2
24 # 0   B3
25 # 1   B4
26 # 2   B5
```

The append() Method

```
1 import pandas as pd
2
3 df1 = pd.DataFrame({'A': ['A1', 'A2'], 'B': ['B1', 'B2']})
4 df2 = pd.DataFrame({'A': ['A3', 'A4'], 'B': ['B3', 'B4']})
5
6 # append() is shorthand for pd.concat([df1, df2])
7 print(df1.append(df2))
8 #      A    B
9 # 0  A1  B1
10 # 1  A2  B2
11 # 0  A3  B3
12 # 1  A4  B4
```

Important Note

- append() does NOT modify original DataFrame
- It creates a new DataFrame (like all Pandas operations)
- Less efficient than pd.concat() for multiple appends
- For many appends: collect in list, then use pd.concat() once

Combining Data: Summary

pd.concat()

- General-purpose concatenation
- Works on Series and DataFrame
- `axis=0`: concatenate rows (default)
- `axis=1`: concatenate columns
- `join='outer'` (default) or `join='inner'`
- `ignore_index=True`: reset index
- `keys=['x', 'y']`: add hierarchical index

append()

- Shorthand for row concatenation
- Returns new DataFrame (doesn't modify original)
- Less efficient for multiple operations

Coming Soon

`pd.merge()` and `pd.join()` for database-style joins (inner, outer, left, right)

Array Fundamentals

- Creating and manipulating arrays
- Indexing, slicing, reshaping
- Data types and memory
- Broadcasting rules

Operations

- Vectorized arithmetic
- Universal functions (ufuncs)
- Mathematical operations
- Boolean operations

Data Analysis

- Aggregations and statistics
- Boolean masking
- Fancy indexing
- Sorting and searching

Why NumPy?

- 10-100x faster than Python lists
- Foundation for all scientific Python
- Memory efficient
- Integrates with C/Fortran code

Core Structures

- Series: 1D labeled arrays
- DataFrame: 2D labeled tables
- Index: Row and column labels
- MultiIndex: Hierarchical indices

Data Selection

- loc/iloc indexing
- Boolean masking
- Fancy indexing
- Slicing and filtering

Operations

- Index alignment
- Missing data handling
- Concatenation and append
- Element-wise operations

Why Pandas?

- Named rows and columns
- Built-in missing data support
- Built on NumPy (fast!)
- Industry standard for data analysis

NumPy Ecosystem: What's Built on Top

Scientific Computing Stack

- **SciPy**: Scientific algorithms (optimization, integration, linear algebra)
- **Pandas**: Structured data analysis (DataFrames) - **NEXT WEEK!**
- **Matplotlib**: Visualization and plotting
- **scikit-learn**: Machine learning
- **TensorFlow/PyTorch**: Deep learning

Domain-Specific Libraries

- **Astropy**: Astronomy and astrophysics
- **Biopython**: Bioinformatics
- **QuantLib**: Financial modeling
- All built on NumPy's fast array operations!

Advanced Pandas Topics

Building on this week's foundation:

- Merge and Join: Database-style data combination
- GroupBy: Split-apply-combine operations
- Pivot Tables: Excel-style data summarization
- Time Series: Working with dates and times
- Reading/Writing Data: CSV, Excel, SQL, JSON
- String Operations: Text processing in Pandas

Introduction to Matplotlib

- Basic plotting with matplotlib
- Line plots, scatter plots, histograms
- Customizing plots (labels, legends, styles)
- Integration with Pandas DataFrames
- Creating publication-quality figures

Thank You!

Questions?

Dr. Eyuphan Koc
eyuphan.koc@bogazici.edu.tr