

Course 2: Supervised Learning



IMT Atlantique
Bretagne-Pays de la Loire
École Mines-Télécom

2025-10-09

Course 2: Supervised Learning

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Summary

Last session

- AI definition
- Applications & Open Issues
- Deep learning
- Foundation models

Today's session

- Learning from labeled examples
- Challenges of supervised learning

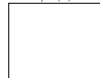
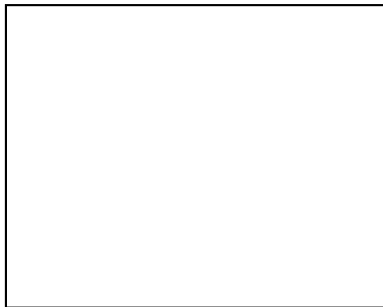
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- 2 Applications & Open Issues
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- Learning from labeled examples
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└ Notations

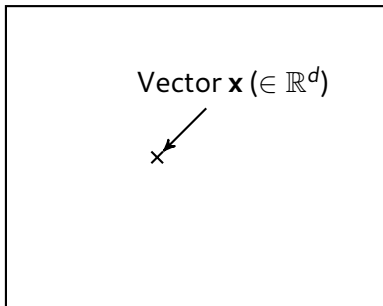
Vector space (\mathbb{R}^d)Vector space (\mathbb{R}^d)

We denote a vector space of real values in dimension d . We will consider vectors x in this space, and the set \mathcal{X} of all such vectors.

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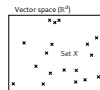


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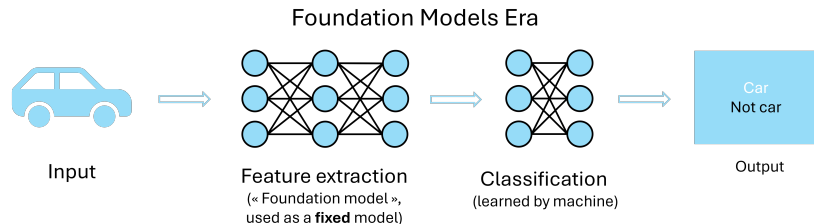
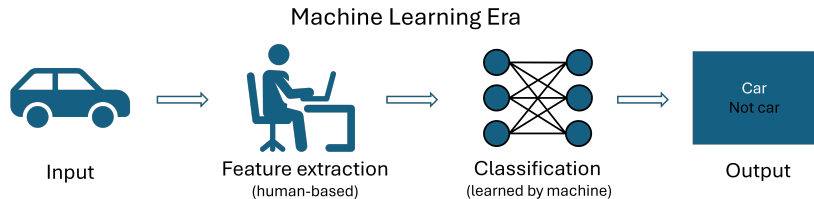


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What is the vector x ? (1/2)

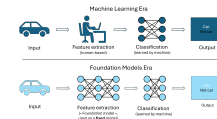


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What is the vector x ? (2/2)

Traditional Machine Learning

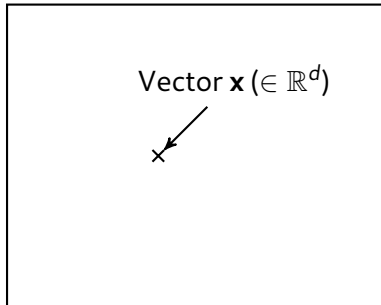
x is the data, or a small transformation of the data
Ex: images, or edges in the image

The era of Foundation models

x is the projection of data in an **embedding space**

- Advantage: richer semantically than the original image
- Disadvantage: Not interpretable nor easily understandable

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Embeddings are vectors in the latent space, i.e. the input vectors (image, text, ...) that have been mapped in a lower dimensional space by a function $f: R^d \rightarrow R^l$. Embeddings are usually richer semantically and easier to manipulate for a downstream task (e.g. classification). See also Lab 1 for more examples.

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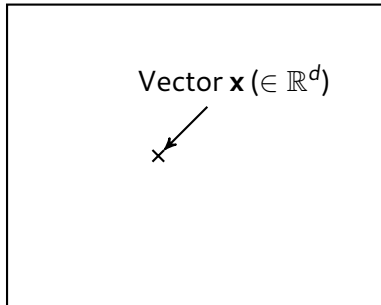
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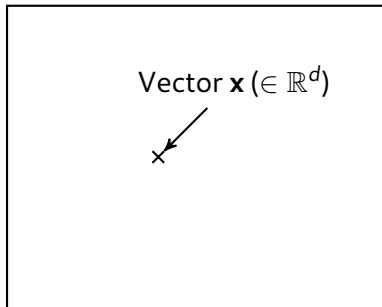
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In this class, we will illustrate the concepts using images... **BUT in the lab, you will use embedding spaces (the future is probably there)**

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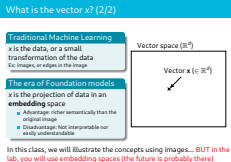


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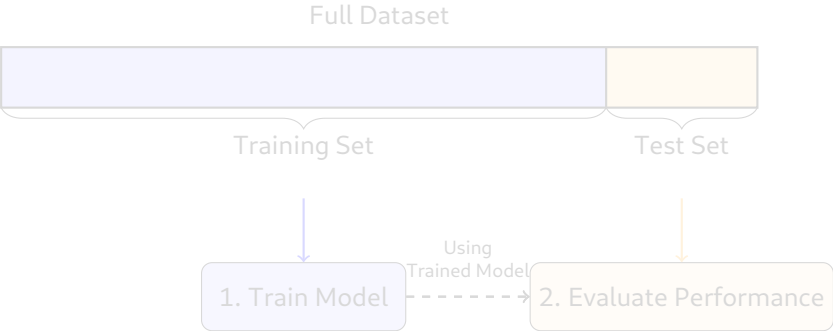
Learning: Training and Test sets

The Training Set

Data used by the model to **learn** from examples.

The Test Set

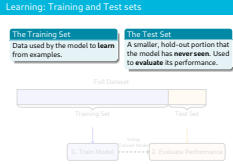
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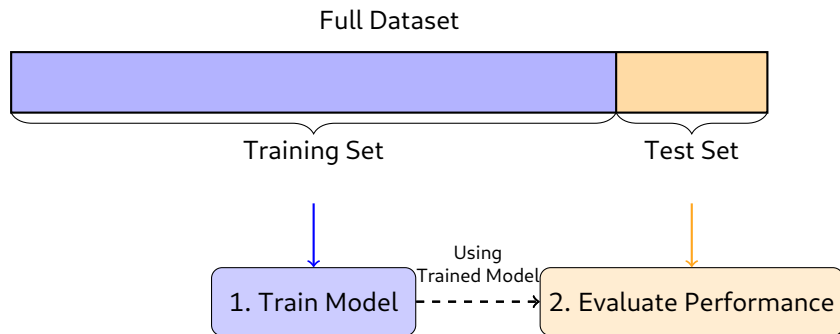
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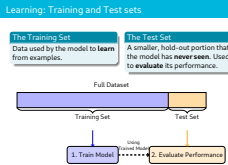
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Learning: Training and Test sets



Supervised learning

Definition
Given a training set, composed of:
■ **x**: inputs (raw signals or feature vectors (e.g. embeddings))
■ **y**: labels (annotated by humans)
Learn:
■ a function $f()$ such that $\hat{y} \approx f(x)$
⇒ $f()$ is **learned** by the Machine Learning algorithm
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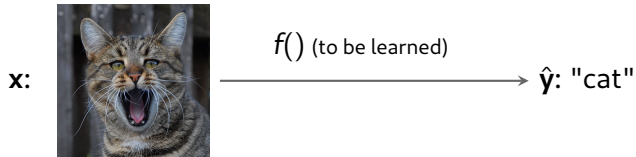
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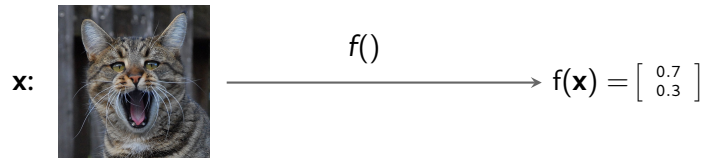
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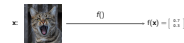
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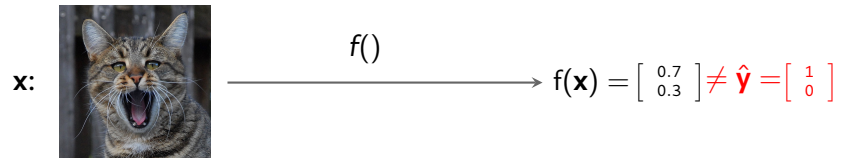
\mathbf{x} :  $\xrightarrow{f() \text{ (to be learned)}}$ $\hat{\mathbf{y}}$: "cat"



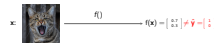
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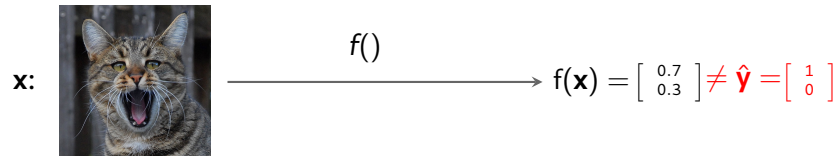
Supervised learning: in practice





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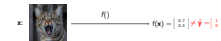
Loss

- Here, labels are encoded as one-hot vectors,
- We compute a **loss** $\mathcal{L}(f(\mathbf{x}), \hat{\mathbf{y}})$
- Training consist in minimizing the loss!

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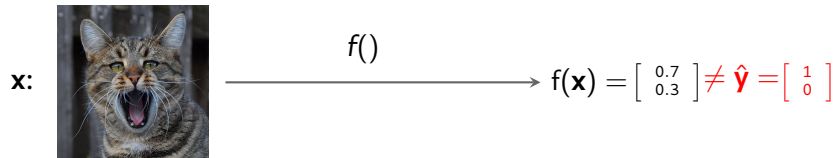
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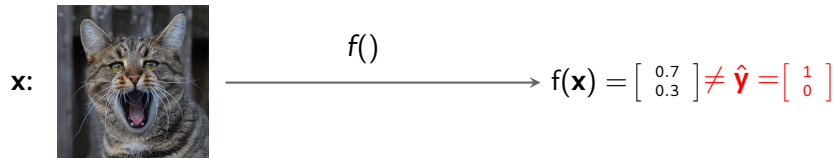
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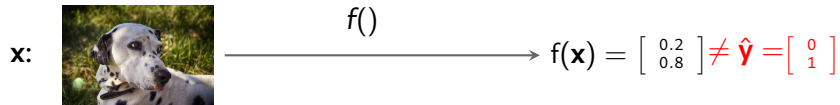
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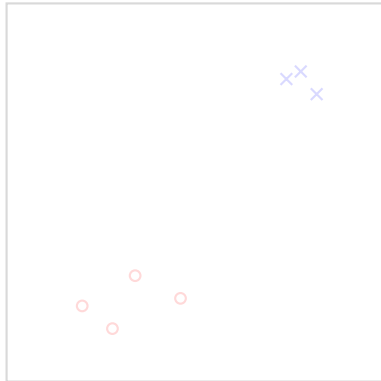
Supervised learning

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Supervised learning

Examples

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- **Regression** (\hat{y} is scalar)
- Tons of applications:
 - Pattern recognition,
 - Prediction...

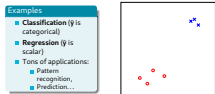


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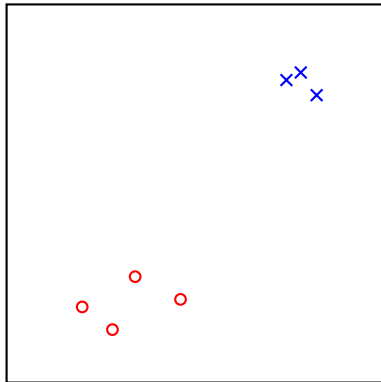


- We insist here one more time on the fact that learning is not memorizing. An expert is needed to provide the labels, that is why it is "supervised".
- Few examples of regression tasks (predicting the price of a product in the stock market, the age of a person based on his/her face, ...) and classification tasks (recognizing apples versus oranges).
- When the plot appears, say that for example if we have the points labeled in blue and the points labeled in red, a simple function could be learnt by just dividing the space in two regions.



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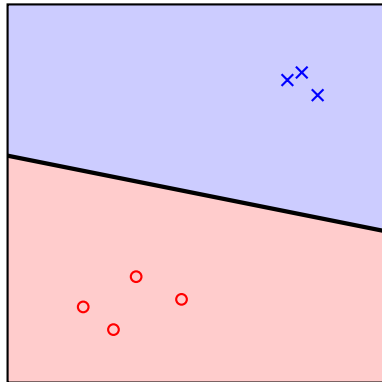
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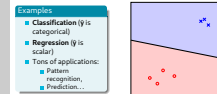
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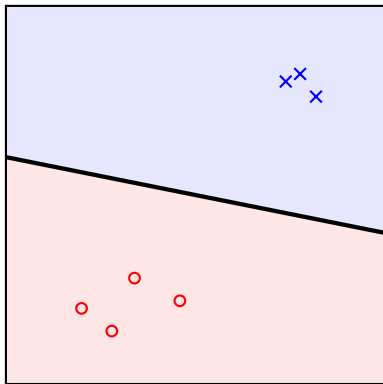
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An ill-defined problem

- An infinity of potential solutions, one must be the "best one" but is unreachable,
- \Rightarrow requires **priors or constraints**.



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└ Challenges of supervised learning (1/6)

The point here is simply illustrate the fact that the solution is not unique. One way to find a solution that could be "better" than another one is to use prior knowledge or constraints of the problem at hand.

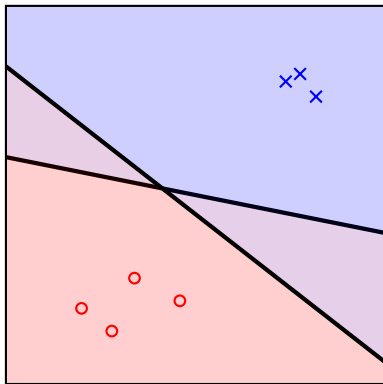
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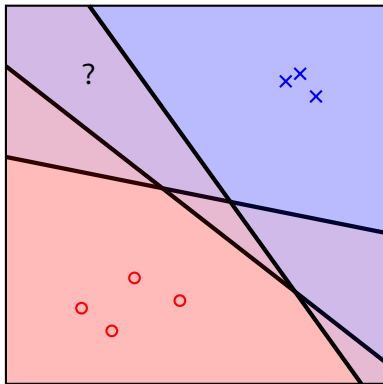
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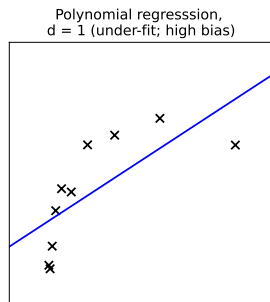
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Bias/variance trade-off

A **simple** solution that almost matches is better than a complex one that fully matches!

- Bias: Error from **erroneous assumptions in the learning algorithm**.
- Variance: Error from **sensitivity to small fluctuations** in the training set.



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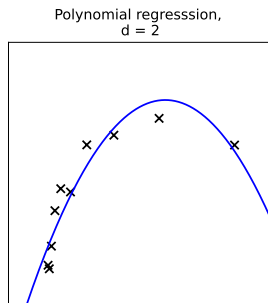


Here, the goal is to show what happens when trying to learn a polynomial function, with a polynomial regression of degree d (i.e. fitting points with a polynomial of degree d). If the regression model is a polynomial of degree 1, it is not able to fit the points. If we take a polynomial of degree 2, it is able to fit the points, but not in a very good way. If we take a polynomial of degree 6, it fits the points very well, but it is not a good estimator, as it is not able to generalize to other points. This is the overfitting problem. Hence, a high bias indicates erroneous assumptions in the learning algorithm, and a high variance indicates that the algorithm is very sensitive to particularities in training data.

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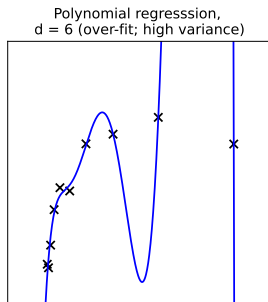


Here, the goal is to show what happens when trying to learn a polynomial function, with a polynomial regression of degree d (i.e. fitting points with a polynomial of degree d). If the regression model is a polynomial of degree 1, it is not able to fit the points. If we take a polynomial of degree 2, it is able to fit the points, but not in a very good way. If we take a polynomial of degree 6, it fits the points very well, but it is not a good estimator, as it is not able to generalize to other points. This is the overfitting problem. Hence, a high bias indicates erroneous assumptions in the learning algorithm, and a high variance indicates that the algorithm is very sensitive to particularities in training data.

Bias/variance trade-off

A **simple** solution that almost matches is better than a complex one that fully matches!

- Bias: Error from **erroneous assumptions in the learning algorithm**.
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Challenges of supervised learning (2/6)

Bias/variance trade-off

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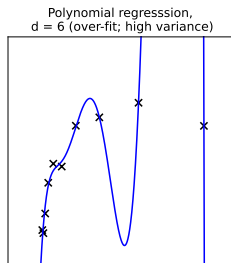
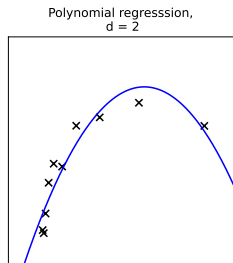
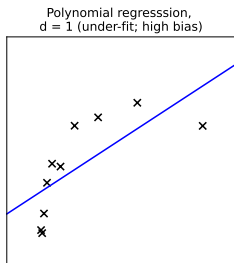
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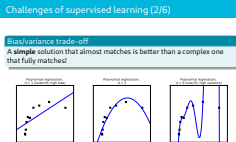
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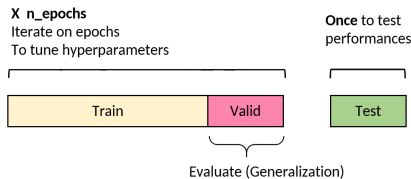
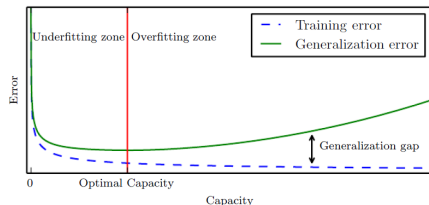
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Overfitting

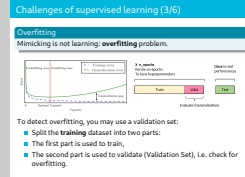
Mimicking is not learning: **overfitting** problem.



To detect overfitting, you may use a validation set:

- Split the **training** dataset into two parts:
- The first part is used to train,
- The second part is used to validate (Validation Set), i.e. check for overfitting.

Challenges of supervised learning (3/6)



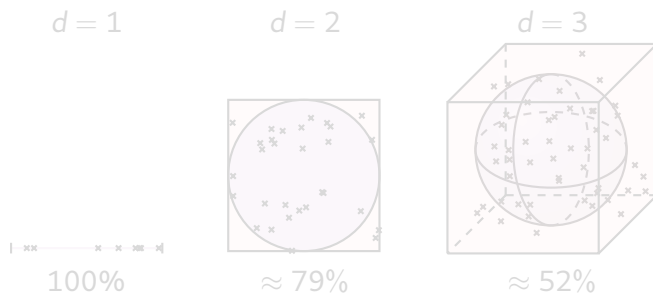
Here, learning curves are presented, with the goal to illustrate overfitting. The diagram on the left shows the error (in regression or classification). The X axis is illustrative, it doesn't correspond to something specific (although one could imagine it to correspond to order of a polynomial, epochs of training a neural net, ...) but it illustrates the situations of underfitting and overfitting.

To go further: Cross-validation ([https://en.wikipedia.org/wiki/Cross-validation_\(statistics\)](https://en.wikipedia.org/wiki/Cross-validation_(statistics))).

Challenges of supervised learning (4/6)

Curse of dimensionality

- Geometry is not intuitive in **high dimension**,
- Efficient methods in 2D are not necessarily still valid.

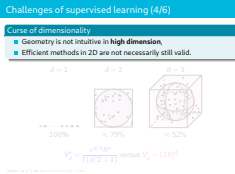


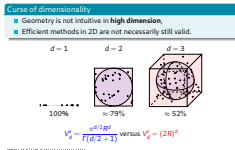
$$V_d^s = \frac{\pi^{d/2} R^d}{\Gamma(d/2 + 1)} \text{ versus } V_d^c = (2R)^d$$

see <https://youtu.be/dZrGXYty3qc?t=533>

Challenges of supervised learning (4/6)

The point here is to show that when the dimension increases, the space tends to be more and more "empty". V_d^s is the volume of the hypersphere, and V_d^c is the volume of the hypercube. The crosses in the different figures are generated by each coordinates following a uniform distribution $\mathcal{U}(0, R)$ (so on average they have a value of $R/2$). When d increases, the ratio between the hypersphere and the hypercube becomes smaller and smaller, so that the majority of the volume of the hypercube lies in the corners, this means that the majority of crosses will be equally far from the center of the hypersphere (for instance a nearest neighbors algorithm would not work at all!). The intuitions we have easily in 2D are not valid anymore, so we can imagine why it is difficult to build good classifiers in high dimensions.



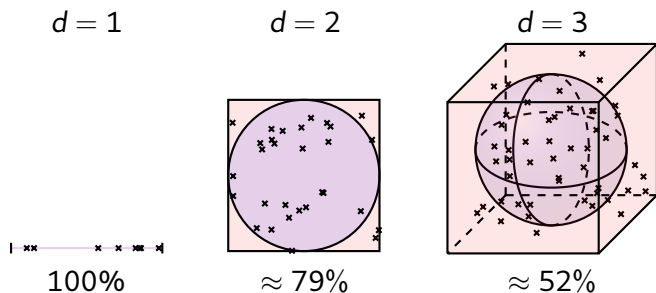


Challenges of supervised learning (4/6)

Challenges of supervised learning (4/6)

Curse of dimensionality

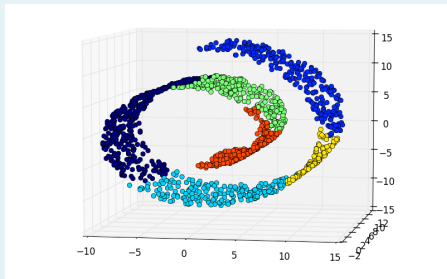
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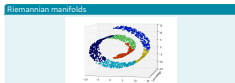
Riemannian manifolds



The natural space of data may not always be suited to represent data!
⇒ Part of the reason why embeddings are richer semantically.

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└ Challenges of supervised learning (5/6)



The natural space of data may not always be suited to represent data!
⇒ Part of the reason why embeddings are richer semantically.

Top part : the point here is to show an example of a dataset in 3D, which is actually much simpler because it is 1D. A nice example to explain the swiss roll is to explain how to roll the cake to make it !

Challenges of supervised learning (6/6)

Computation time

Example on ImageNet, simply going through all images:

- $n = 10.000.000$, $d \approx 1.000.000$,
- $\approx 10^{13}$ elementary operations,
- $\approx 2h45$ on a modern processor.

Scalability

- Finding the best solution to a problem would be feasible with unlimited computation time,
- But searching through the space of possible functions is often **untractable**,
- Solutions must be computationally reasonable, which is the true challenge today.

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Course 2: Supervised Learning

└ Challenges of supervised learning (6/6)

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Challenges of supervised learning (6/6)

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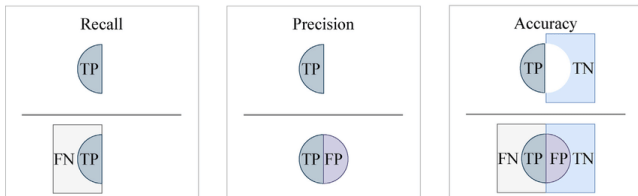
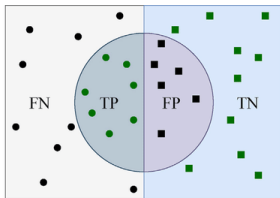
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Accuracy, Precision and Recall

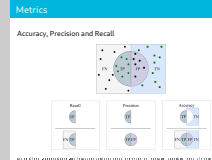


https://www.researchgate.net/publication/346129022_Overview_of_Machine_Learning_Part_1/figures

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Course 2: Supervised Learning

Metrics



n.b. The picture is relative to a one class problem.

Accuracy: fraction of correctly classified instances over all instances (can be misleading for imbalanced classes)

Recall: fraction of positive (correctly retrieved) instances among relevant items

Precision: fraction of positive (correctly retrieved) instances among the retrieved instances
The confusion matrix is useful to visualize the results of a supervised learning algorithm. It compares the instances of the ground truth (actual class) and the predicted class. The diagonal elements indicate the instances that are correctly predicted and the off diagonal elements the instances that are misclassified.

Metrics

A useful tool: the confusion matrix

		Ground truth		
		+	-	
Predicted	+	True positive (TP)	False positive (FP)	Precision = $TP / (TP + FP)$
	-	False negative (FN)	True negative (TN)	Recall = $TP / (TP + FN)$
				Accuracy = $(TP + TN) / (TP + FP + TN + FN)$

Source: https://www.researchgate.net/publication/334840641_A_cloud_detection_algorithm_for_satellite_imagery_based_on_deep_learning/figures?lo=1

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Lab Session 2 and presentation in Session 3

Lab Supervised Learning

- Basics of machine learning using sklearn (including new definitions / concepts)
- Tests on the modality chosen in Lab 1 (text, vision or audio), based on the same foundation model than in Lab 1.

Project 1 (P1)

Odd binome number must choose one supervised learning method among those available (see Lab 2). You will present

- A description of the theory behind both methods,
- Basic tests on toy datasets and on your modality.

During Session 3 you will have 7 minutes to present.

Careful, **7min is very short!**

Your presentation should be **educational** and addressed to the rest of the class.

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Course 2: Supervised Learning

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└ Lab Session 2 and assignments for Session 3

List of Supervised Learning Methods

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- Support Vector Machines (SVM)
- Decision Trees
- Random Forest classifiers
- Logistic Regression
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