

Design And Analysis Of Algorithms-Assignment 4

Group-2

ADITYA RAJ(IIT2017005)
MOHIT PAHUJA(IIT2017007)

MAYANK MRINAL(IIT2017006)
ARASHPREET SINGH (IIT2017008)

Abstract—This document is complete design and analysis of algorithm of finding an optimal way if you can reach a given number x from 0 when you move i steps.

I. INTRODUCTION

In this problem we have to find an optimal way to reach at point x from 0 by moving i distance in i^{th} step. For example 3 takes 2 steps (0, 1) (1, 3) and 4 takes 3 steps (0, -1), (-1, 1) (1, 4). So we are finding both minimum number of moves and the path. For this we have design only one algorithm .

This report further contains::

- II. Algorithm Design.
- III. Algorithm Analysis
- IV. Experimental Study.
- V. Conclusions.
- VI. References.

II. ALGORITHM DESIGN

A. Algorithm 1

Idea is to move in one direction as long as possible, this will give minimum moves. Starting at 0 first move takes us to 1, second move takes us to 3 (1+2) position, third move takes us to 6 (1+2+3) position, and so on; So for finding target we keep on adding moves until we find the n th move such that $1+2+3+\dots+n \geq \text{target}$. Now if sum ($1+2+3+\dots+n$) is equal to target the our job is done, i.e we'll need n moves to reach target. Now next case where sum is greater than target. Find the difference by how much we are ahead, i.e $\text{sum} - \text{target}$. Let the difference be $d = \text{sum} - \text{target}$.

If we take the i -th move backward then the new sum will become $(\text{sum} - 2i)$, i.e $1+2+3+\dots-x+x+1+\dots+n$. Now if $\text{sum} - 2i = \text{target}$ then our job is done. Since, $\text{sum} - \text{target} = 2i$, i.e difference should be even as we will get an integer i flipping which will give the answer. So following cases arise.

Case1 : Difference is even then answer is n , (because we will always get a move flipping which will lead to target).

Case2 : Difference is odd, then we take one more step, i.e add $n+1$ to sum and now again take the difference. If difference is even the $n+1$ is the answer else we would have to take one more move and this will certainly make the difference even then answer will be $n+2$.

Explanation : Since difference is odd. Target is either odd or even. case 1: n is even ($1+2+3+\dots+n$) then adding $n+1$ makes the difference even. case 2: n is odd then adding $n+1$ doesn't makes difference even so we would have to take one more move, so $n+2$.

Algorithm 1

```
printv(vector v)
for i=0,i<v.size,i++
v[i]

main()
cin<-target
sum<-0
i<-1
ctr<-0
while sum<= target do
    sum<sum+i
    if sum==target then
        ctr<-1
        i++
    else
end
if ctr==0 then
    s<-0
    i<-1
    while sum<= target do
        s<s+i
        i++
        if s<= target then
            v.push_back(s)
        else
            i<-c
        end
    end
    out<-no. of moves: v.size
    printv(v)
    return 0
end
end if
=0
```

```

while abs(sum-target)%2!=0 do
    sum ← sum+i
    i++
end
rev ← (sum-target)>>1
sum ← 0
step ← 1

while sum!=target do
    if step!=rev then
        sum<sum+step
    else
        end
        sum←sum- step
        v.push_back(sum)
        step++
    end
    cout<no. of moves: v.size
    printv(v)
    return 0

```

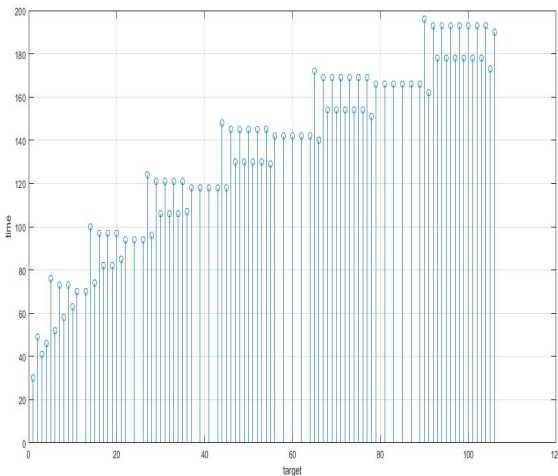
III. ALGORITHM ANALYSIS

A. Time Complexity

- We have calculated the time consumed in each step in terms of number of computations, as given in the above pseudo code.
- Thus for general value of x let say n , the time complexity is going to be in order of $2n$.
- The best case, worst case and average case time complexity will be same i.e. $O(n)$.

B. Space Complexity

- Since the number of memory location depends on the the variable x since we are storing the path in vector. In worst case the size of the requirement will be $O(x)$.



Thus the graph depicts, our calculation, that is the algorithm takes polynomial of order n .

IV. EXPERIMENTAL STUDY

The graph depicts that the plot between the target i.e. n and time which comes out to be approximately in the order of $2n$.

The integrated Development environment of C++ is used for processing the algorithm and graphical analysis is done using MATLAB stem function.

V. CONCLUSIONS

In this document we conclude that our algorithm has a polynomial time complexity with order of $2n$ for all the cases i.e. best, worst and average case. The space complexity is also of the order n (where n is the size of target number.) Therefore both time and space complexity is $O(n)$.

VI. REFERENCES

1. <https://www.geeksforgeeks.org/find-minimum-moves-reach-target-infinite-line/>
2. [CLR96] Thomas H. Cormen, Charles E. Leiserson, and Ronald L Rivest. Introduction to algorithms. The MIT press, 2nd edition, 1996.
3. [DW96] Nell Dale and Henry M. Walker. Abstract data types: specifications, implementations, and applications. D. C. Heath and Company, Lexington, MA, USA, 1996.