```
* Some other definitions
#define _inline(f...) f() __attribute__((always inline)); f
#define foreach(it, b, e) for (typeof(b) it = (b); it != (e); it++)
\#define foreach(x...) foreach(x)
#define all(v) (v).begin(), (v).end()
#define rall(v) (v).rbegin(), (v).rend()
* Field with barriers
#include <list>
#include <set>
const int TAM = 2000;
typedef pair<point, point> segment;
typedef pair<int, int> barrier;
struct field {
 int n, m;
 point v[TAM];
 barrier b[TAM];
 list<int> e[TAM];
 field(): n(0), m(0) {}
 void clear() {
    for (int i = 0; i < n; i++) e[i].clear();
    n = m = 0;
 int ccw(int a, int b, int c) { return ::ccw(v[a], v[b], v[c]); }
 void make barrier(int i, int j) {
    e[i].push back(m); e[j].push back(m);
    b[m++] = barrier(i, j);
 }
 //Removes the degenerate cases
 void normalize() {
    set<segment> T; set<point> U;
    for (int i = 0; i < n; i++) make barrier(i, i);
    for (int i = 0; i < m; i++) {
     point p = v[b[i].first], q = v[b[i].second];
      set<point> S;
     S.insert(p); S.insert(q);
      for (int j = 0; j < m; j++) {
       point r = v[b[j].first], s = v[b[j].second];
       if (r == p || r == q || s == p || s == q) continue;
       if (cmp((q - p) % (s - r)) == 0) {
         if (between(p, r, q)) S.insert(r);
         if (between(p, s, q)) S.insert(s);
        } else if (seg intersect(p, q, r, s)) {
          S.insert(line intersect(p, q, r, s));
      foreach (st, all(S)) {
        if (st != S.begin()) T.insert(segment(p, *st));
```

```
U.insert(p = *st);
       }
     }
     clear();
     foreach (it, all(U)) v[n++] = *it;
     foreach (it, all(T)) {
       int i = lower bound(v, v+n, it->first) - v;
       int j = lower bound(v, v+n, it->second) - v;
       make barrier(i, j);
     }
  //Poggi-Moreira-Fleischman-Cavalcante Algorithm
  //Determine the graph with all edges in an eventual minimum path
  void pmfc(graph& G) {
     int sel[TAM][2], active[TAM];
     for (int i = 0; i < n; i++) {
       vector< pair<double, int> > T;
       foreach (it, all(e[i])) {
         int j = b[*it].first + b[*it].second - i;
         T.push back(make pair(arg(v[i] - v[i]), i));
       }
       sort(all(T));
       if (T.empty()) T.push back(make pair(0, i));
       active[i] = 0;
       int p = T.size();
       for (int j = 0; j < p; j++) {
         sel[i][0] = T[j].second; sel[i][1] = T[(j+1) % p].second;
         if (ccw(sel[i][0], sel[i][1], i) <= 0) {
           active[i] = 1; break;
       }
     }
     G.init(n);
     for (int i = 0; i < n; i++) for (int j = 0; j < i; j++) {
       if (!active[i] || !active[j]) continue;
       if (ccw(i, j, sel[i][0]) * ccw(i, j, sel[i][1]) == -1 || \
           ccw(i, j, sel[j][0]) * ccw(i, j, sel[j][1]) == -1)
         continue:
       for (int k = 0; k < m; k++) {
         int org = b[k].first, dest = b[k].second;
         if (org == i||org == j||dest == i||dest == j) continue;
         if (seg intersect(v[i], v[j], v[org], v[dest])) goto PROX;
       G.aresta(i, j, 1, abs(v[j] - v[i]));
PROX:
     }
  }
};
* Arbitrary precision arithmetics
#include <sstream>
const int DIG = 4;
const int BASE = 10000; // BASE**3 < 2**51 --> BASE = 10^DIG
```

```
const int TAM = 2048;
struct bigint {
  int v[TAM], n;
  bigint(int x = 0): n(1) {
    memset(v, 0, sizeof(v));
    v[n++] = x; fix();
  bigint(char *s): n(1) {
    memset(v, 0, sizeof(v));
    int sign = 1;
    while (*s && !isdigit(*s)) if (*s++ == '-') sign *= -1;
    char *t = strdup(s), *p = t + strlen(t);
    while (p > t) {
      *p = 0; p = max(t, p - DIG);
      sscanf(p, "%d", &v[n]);
      v[n++] *= sign;
    }
    free(t); fix();
  bigint& fix(int m = 0) {
    n = max(m, n);
    int sign = 0;
    for (int i = 1, e = 0; i \le n \mid \mid e \& (n = i); i++) {
      v[i] += e; e = v[i] / BASE; v[i] %= BASE;
      if (v[i]) sign = (v[i] > 0) ? 1 : -1;
    for (int i = n - 1; i > 0; i - -)
      if (v[i] * sign < 0) \{ v[i] += sign * BASE; v[i+1] -= sign; \}
    while (n && !v[n]) n--;
    return *this;
  int cmp(const bigint& x = 0) const {
    int i = max(n, x.n), t = 0;
    while (1) if ((t = ::cmp(v[i], x.v[i])) || i-- == 0) return t;
  bool operator < (const bigint& x) const { return cmp(x) < 0; }
  bool operator ==(const bigint& x) const { return cmp(x) == 0; }
  bool operator !=(const bigint& x) const { return cmp(x) != 0; }
  operator string() const {
    ostringstream s; s << v[n];
    for (int i = n - 1; i > 0; i - -) {
      s.width(DIG); s.fill('0'); s << abs(v[i]);
    }
    return s.str();
  friend ostream& operator <<(ostream& o, const bigint& x) {</pre>
    return o << (string) x;</pre>
  }
   bigint& operator +=(const bigint& x) {
     for (int i = 1; i \le x.n; i++) v[i] += x.v[i];
     return fix(x.n);
   bigint operator +(const bigint& x) { return bigint(*this) += x; }
   bigint& operator -=(const bigint& x) {
```

```
for (int i = 1; i <= x.n; i++) v[i] -= x.v[i];</pre>
     return fix(x.n);
   bigint operator -(const bigint& x) { return bigint(*this) -= x; }
   bigint operator -() { bigint r = 0; return r -= *this; }
   void ams(const bigint& x, int m, int b) {//*this+=(x * m)<<b;}
     for (int i = 1, e = 0; (i \le x.n \mid \mid e) && (n = i + b); i++) {
       v[i+b] += x.v[i] * m + e; e = v[i+b] / BASE; v[i+b] %= BASE;
     }
   bigint operator *(const bigint& x) const {
     bigint r;
     for (int i = 1; i \le n; i++) r.ams(x, v[i], i-1);
     return r:
   bigint& operator *=(const bigint& x) {return *this = *this * x;}
   // cmp(x / y) == cmp(x) * cmp(y); cmp(x % y) == cmp(x);
   bigint div(const bigint& x) {
     if (x == 0) return 0;
     bigint q; q.n = max(n - x.n + 1, 0);
     int d = x.v[x.n] * BASE + x.v[x.n-1];
     for (int i = q.n; i > 0; i--) {
       int j = x.n + i - 1;
       q.v[i] = int((v[j] * double(BASE) + v[j-1]) / d);
       ams(x, -q.v[i], i-1);
       if (i == 1 || j == 1) break;
       v[i-1] += BASE * v[i]; v[i] = 0;
     fix(x.n); return q.fix();
   bigint& operator /=(const bigint& x) { return *this = div(x); }
   bigint& operator %=(const bigint& x) { div(x); return *this; }
   bigint operator /(const bigint& x) {return bigint(*this).div(x);}
   bigint operator %(const bigint& x) {return bigint(*this) %= x;}
   bigint pow(int x) {
     if (x < 0) return (*this == 1 || *this == -1) ? pow(-x) : 0;
     bigint r = 1:
     for (int i = 0; i < x; i++) r *= *this;
     return r;
   bigint root(int x) {
     if (cmp() == 0 \mid | cmp() < 0 \&\& x % 2 == 0) return 0;
     if (*this == 1 || x == 1) return *this;
     if (cmp() < 0) return -(-*this).root(x);
     bigint a = 1, d = *this;
     while (d != 1) {
       bigint b = a + (d /= 2);
       if (cmp(b.pow(x)) >= 0) \{ d += 1; a = b; \}
     }
     return a;
   }
};
```

```
B00KCASE
int main () {
 int runs; cin>>runs;
 while (runs--) {
   int N;
   cin>>N;
   vector<pair<int,int> > b(N);
   for (int i=0; i<N; i++)</pre>
     cin>>b[i].first>>b[i].second;
   sort(b.begin(),b.end(),greater<pair<int,int> >());
   vector<int> h(N),t(N),tsum(N+1);
   for (int i=0; i<N; i++) {
     h[i]=b[i].first;
     t[i]=b[i].second;
     tsum[i+1]=tsum[i]+t[i];
   }
   vector<vector<int> > H(tsum[N]+1, vector<int>(tsum[N]+1, INF));
   H[0][0]=0;
   for (int i=0; i<N; i++)
     for (int T1=tsum[i+1]; T1>=0; T1--)
       for (int T2=tsum[i+1]; T2>=0; T2--) {
        if (T1> t[i]) H[T1][T2] <?= H[T1-t[i]][T2];</pre>
        if (T1==t[i]) H[T1][T2] <?= H[T1-t[i]][T2] + h[i];</pre>
        if (T2> t[i]) H[T1][T2] <?= H[T1][T2-t[i]];</pre>
        if (T2==t[i]) H[T1][T2] <?= H[T1][T2-t[i]] + h[i];</pre>
       }
   int res = INT MAX;
   for (int T1=1; T1<=tsum[N]; T1++)</pre>
     for (int T2=1; T2<=tsum[N]; T2++)
       res <?= (T1 >? T2 >? (tsum[N]-T1-T2)) * (h[0]+H[T1][T2]);
   cout << res << endl;</pre>
 }
}
* VASE COLLECTOR
long long v[36]; int bitcnt[1<<18];
int countbits(long long a) {return bitcnt[a>>18]+bitcnt[a&0x3FFFF];}
int check(int n, int cur, int sel, long long mask) {
 if (countbits(mask)<n) return 0;</pre>
 if (sel==n) return 1;
 if (sel+36-cur<n) return 0;</pre>
 return check(n,cur+1,sel,mask) || check(n,cur+1,sel+1,mask&v[cur]);
}
```

```
int main() {
  for(int i=0;i<(1<<18);i++) {
       int cnt=0;
       for(int j=0; j<18; j++)
         if ((1<<j)&i) cnt++;
       bitcnt[i]=cnt;
  }
 int N;
 cin >> N;
 while (N--) {
       int m;
       cin >> m;
       for(int i=0; i<36; i++) v[i]=0;
       for(int i=0;i<m;i++) {
         int x,y;
         cin >> x >> y;
         v[y-1] = (1LL << (x-1));
       }
       int n;
       for(n=2;n*n<=m && check(n,0,0,(1LL<<36)-1);n++);</pre>
       cout << n-1 << endl;
  return 0;
}
* Transversing a maze (Ro and Bot Meet - ACM 2117)
* Transversing a maze using left or right hand rule. In this
                                                                *
                                                                *
* code the maze nxm is represented as an int M[n][m] matrix in
* which each cell is a bit mask indicating if the path in some
                                                                *
* direction is open or not. We have:
               The one bit in the mask indicates that a direction
               is open. Ro transverses the maze using the left
               hand rule and Bot using the right hand rule.
          1
       2
#define between(i,a,b) ( (a \le i) \& (i \le b) )
#define in maze(i,j) ((0 \le i) \& \& (i \le n) \& \& (0 \le j) \& \& (j \le m))
int getValue( char c ) {
 if (c >= 'A' \&\& c <= 'F') return (c - 'A') + 10;
 else if ( c >= 'a' && c <= 'f' ) return ( c - 'a' ) + 10;
 else return ( c - '0' );
}
int M[50][50]; int diri[4] = \{-1,0,1,0\}; int dirj[4] = \{0,1,0,-1\};
int main() {
 int n,m, maze=1;
 char ch[10];
 int roi, roj, rod, boti, botj, botd;
 while (scanf("%d %d", &n, &m), n || m)
```

```
rep(i,n) rep(j,m) {
     scanf("%s", ch);
     M[i][j] = getValue(ch[0]);
   roi = roj = 0; rod = (M[0][0] & (1<<3)) ? 1 : 2;
   boti = n-1; botj = m-1; botd = (M[n-1][m-1] \& (1 << 1)) ? 3 : 0;
   bool found = false;
   while (in maze(roi,roj) && in maze(boti,botj))
     if ((roi == boti) && (roj == botj)) {found = true; break;}
     rod = (rod+3)%4; botd = (botd+1)%4;
     while (!(M[roi][roi] & (1<<rod))) rod = (rod + 1)%4;</pre>
     while (!(M[boti][botj] & (1<<botd))) botd = (botd + 3)%4;</pre>
     roi += diri[rod]; roj += dirj[rod];
     boti += diri[botd]; botj += dirj[botd];
   }
   printf("Maze %d: The robots ", maze++);
   if (found) printf("meet in row %d, column %d.\n\n", roi+1,
   else printf("do not meet.\n\n");
 }
}
* EURO EFFICIENCE - minimize coins used ( including change )
#define between(x,a,b) ( (a < x) \& \& (x < b) )
#define p rep(i,n) for (int i=1; i<=n; i++)
int main() {
 int testcases, sum, c, s, d[101]; bool finished;
 scanf("%d", &testcases);
 while(testcases - -){
   s = 1; finished = false;
   p rep(i, 100) d[i] = INF;
   rep(i,6) \{ scanf("%d", &c); d[c] = 1; \} // coin values
   while (!finished) {
     finished = true; ++s;
     p rep(i, 100) {
       if (d[i] == INF) finished = false;
       p rep(j, 100) if (d[i]+d[j] == s)
         if (i+j <= 100) d[i+j] <?= s;
         if (i-j > 0) d[i-j] <?= s;
         if (j-i > 0) d[j-i] <?= s;
       }
     }
   }
   s = sum = 0;
   p rep(i, 100) {
     s >?= d[i]; sum += d[i];
   printf("%4.2f %d\n", ((float)sum) / 100., s);
  }
```

```
}
* STABLE MARRIAGE - match m men to n woman in a stable and monogamic*
* fashion. L[i][ ] is the list of women in order of decreasing
* preference of man i and R[j][i] is how attractive man i to woman
* j, so, if R[j][i1] > R[j][i2] then woman j prefers man i1 to i2.
* L2R[i] contains man i's mate and R2L[j] contains the mate of woman*
* j or -1 if she is unmated. Condition: n>=m. Complexity O(m^2)
int m, n; int L[MAXM][MAXW], R[MAXW][MAXM];
int L2R[MAXM], R2L[MAXW]; int p[MAXM];
void stableMarriage() {
 static int p[MAXM];//man's preferences
 rep(j,n) R2L[j] = -1; rep(k,128) p[k] = 0;
 rep(i,m) {//for each man
   int man = i;
   while ( man >= 0 )
     int wom;
     while( 1 ) {//proposes women
      wom = L[man][p[man]++];
      if( R2L[wom] < 0 || R[wom][man] > R[wom][R2L[wom]] ) break;
     int hubby = R2L[wom]; //old husband from the woman
     R2L[L2R[man] = wom] = man;
     man = hubby; //remarry dumped husband
   }
 }
}
* SET RECONSTRUCTION FROM PAIRWISE SUM: Given a multiset S of
 integers, reconstructs the multiset V such that S is the multiset *
* of pairwise sums of V.Returns true if successful and false if
* confused.
#include <set>
bool pairsums( int *ans, multiset< int > &seq ) {
   int N = seq.size();
   if( N < 3 ) return false;</pre>
     typeof( seq.end() ) it = seq.begin();
   int a = *it++, b = *it++, i = 2;
   for( ; i * ( i - 1 ) < 2 * N && it != seq.end(); i++, ++it ) {</pre>
      // assume seq[i] = ans[1] + ans[2]
      ans[0] = a + b - *it;
      if( ans[0] & 1 ) continue;
       ans[0] >>= 1;
      // try ans[0] as a possible least element
      multiset< int > seq2 = seq;
       int j = 1;
```

```
while( seq2.size() ) {
          ans[j] = *seq2.begin() - ans[0];
          for( int k = 0; k < j; k++ ) {
               typeof( seq2.end() ) jt=seq2.find(ans[k]+ans[j]);
              if( jt == seq2.end() ) goto HERE;
              seq2.erase( jt );
          j++;
       }
       HERE:;
       if( j * ( j - 1 ) < 2 * N ) continue;</pre>
       // it worked! [modify this to deal with multiple answers]
       return true;
   }
   return false;
}
* POWER MOD: Computes b^p \mod m. Wants b >= 0, p >= 0, m >= 1.
int powmod( long long b, int p, int m )
   long long r = 1;
   for( int i = ( 1 << 30 ); i; i >>= 1 )
   //for( long long i = (1LL \ll 62); i; i \gg 1)//for big powers
   {
       r *= r; r %= m;
       if( p & i ) { r *= b; r %= m; }
   return ( int )r;
}
* ROMAN NUMERALS
string fill( char c, int n ) { string s; while( n-- ) s += c; return
s; }
string toRoman( int n ) {
if( n < 4 ) return fill( 'i', n );
if( n < 6 ) return fill( 'i', 5 - n ) + "v";</pre>
if( n < 9 ) return string( "v" ) + fill( 'i'</pre>
if( n < 11 ) return fill( 'i', 10 - n ) + "x";</pre>
if( n < 40 ) return fill( 'x', n / 10 ) + toRoman( n % 10 );</pre>
if( n < 60 ) return fill( 'x', 5 - n / 10 ) + 'l' + toRoman( n % 10
if( n < 90 ) return string( "l" ) + fill( 'x', n / 10 - 5 ) +</pre>
toRoman(n % 10);
if( n < 110 ) return fill( 'x', 10 - n / 10 ) + "c" + toRoman( n %</pre>
10):
if( n < 400 ) return fill( 'c', n / 100 ) + toRoman( n % 100 );</pre>
if( n < 600 ) return fill( 'c', 5 - n / 100 ) + 'd' + toRoman( n %
100);
if( n < 900 ) return string( "d" ) + fill( 'c', n / 100 - 5 ) +</pre>
```

```
toRoman(n % 100);
if( n < 1100 ) return fill( 'c', 10 - n / 100 ) + "m" + toRoman( n</pre>
% 100 );
if( n < 4000 ) return fill( 'm', n / 1000 ) + toRoman( n % 1000 );</pre>
return "?";
}
* Hungarian Algorithm
#define SIZE (2*MAX+1)
int mat[SIZE][SIZE]; /* Weighted Matrix */
int matchedWith[SIZE];
int level[SIZE]; int parent[SIZE]; int N;
int weight[SIZE]; /* Weight/Label of each Node */
int S[SIZE]; /* Set of vertices of X/U in Hungarian Tree */
           /* Vertices in Y/V and in the current Matching */
int T[SIZE]:
void init(void) { rep(i,SIZE) memset(mat[i],0,sizeof(int)*SIZE); }
int augmentPath(int u) {
 int v,w,last; int q[SIZE+1],head,tail;
 memset(level, 0, sizeof(int)*(2*N+1));
 memset(parent, 0, sizeof(int)*(2*N+1));
 head = 0; tail = 1; q[1] = u; level[u] = 1; last = 0;
 while((head!=tail) && !last) {
   head++; v = q[head];
   if(level[v]%2) {
     for(w=N+1; w<=2*N; w++) {
       if(!level[w] && (mat[v][w]==weight[v]+weight[w])) {
         if(!matchedWith[w]) {
           parent[w] = v;
           last
                    = w;
           break:
         }
         else if(matchedWith[w]!=v)/* Unmatched Edge(v,w) */
           parent[w] = v; level[w] = level[v]+1; q[++tail] = w;
         }
       }
     }
   }
   else
   {
             = matchedWith[v];/* Matching partner of v */
     parent[w] = v;
                       /* Engue matched Edge (v,w) */
     q[++tail] = w;
     level[w] = level[v]+1;
   }
 }
 if(last) {
```

```
for(w=last; w; w=parent[parent[w]]) {
      matchedWith[w]
                          = parent[w];
      matchedWith[parent[w]]
    }
    return 1;
  }
  else
  {
    for(v=1; v<=N; v++)
    {
      if(level[v]) S[v] = 1;
      if(level[N+v]) T[N+v] = 1;
    }
    return 0;
  }
}
void optimalMatching(void) {
  int i,j,max,slack,u,v;
  int nMatch,eps;
  memset(matchedWith, 0, sizeof(int)*(2*N+1));
  for(i=1;i<=N;i++) {
    max = 0;
    for(j=N+1;j<=2*N;j++) if(mat[i][j] > max) max = mat[i][j];
    weight[i] = max; weight[i+N] = 0;
  }
  nMatch = 0:
 while(1) {
    memset(S,0,sizeof(int)*(2*N+1));
    memset(T, 0, sizeof(int)*(2*N+1));
    for(i=1;i<=N;i++) {
      if(!matchedWith[i]) {
        if(augmentPath(i)) nMatch++;
      }
    }
    if(nMatch == N) break;
    eps = INF;
    for(i=1;i<=N;i++) if(S[i]) for(j=N+1;j<=2*N;j++) if(!T[j]){
      slack = weight[i]+weight[j]-mat[i][j];
      if(slack < eps) eps = slack;</pre>
    for(i=1;i<=N;i++) {
      if(S[i]) weight[i]
                           -= eps;
      if(T[i+N]) weight[i+N] += eps;
    }
  }
  return ;
}
void main(void)
//usage
N = \dots; init();
for(i=1;i<=N;i++) for(j=N+1;j<=2*N;j++)
        scanf("%d",&mat[i][j]);
```

```
optimalMatching();
answer in matchedWith[i] i=1...N
* Perimeter of the union of rectangles
double union perimeter(vector<rect>& R) {
 int n = R.size(); if (n == 0) return 0;
 vector< pair<double, int> > E;
 int m = 0;
 for (int i = 0; i < n; i++) {
   E.push back(make pair(R[i].x1, i));
   E.push back(make pair(R[i].x2, ~i));
   y[m++] = R[i].y1;
   y[m++] = R[i].y2;
 sort(all(E)); sort(y, y + m); m = unique(y, y + m, cmp eq) - y;
 double last = E[0].first, r = 0, dy = 0;
 segtree T(0, m-1);
 for (int i = 0; i < 2*n; i++) {
   int k = E[i].second; bool in = (k \ge 0); if (!in) k = \sim k;
   double dx = E[i].first - last;
   r += dx * T.a;
   int a = lower_bound(y, y + m, R[k].y1, cmp_lt) - y;
   int b = lower_bound(y, y + m, R[k].y2, cmp_lt) - y;
   if (in) T.insert(a, b);
   else T.erase(a, b);
   r += fabs(dy - T.len);
   dy = T.len;
   last += dx;
 }
 return r;
}
```