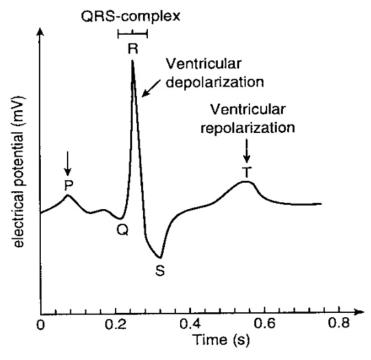
E40M Bode Plots, dB

Reading

- Reader
 - 7.1-7.2 Bode Plots

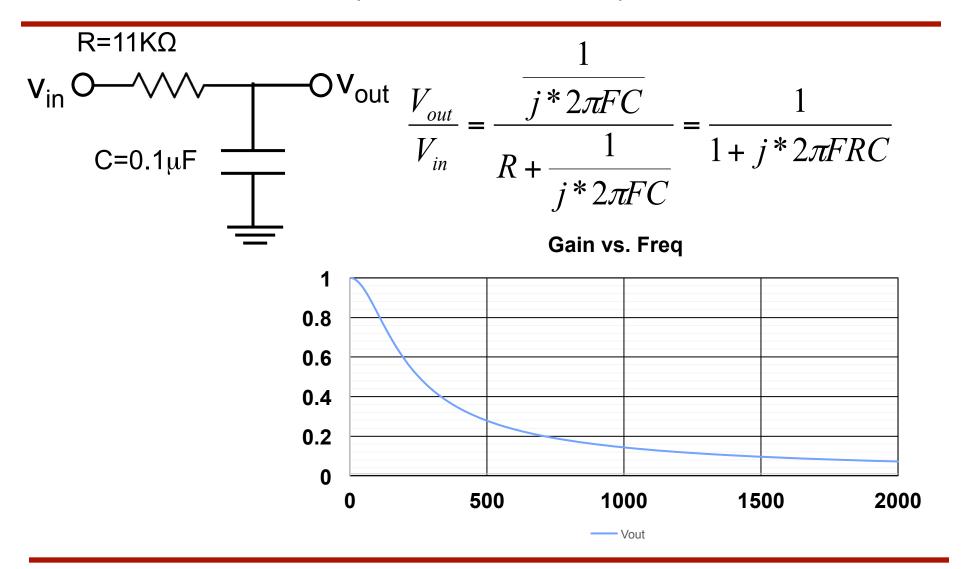
EKG Lab

- Concepts
 - Amplifiers
 - Impedance
 - Noise
 - Safety
 - Filters
- Components
 - Capacitors
 - Inductors
 - Instrumentation and Operational Amplifiers

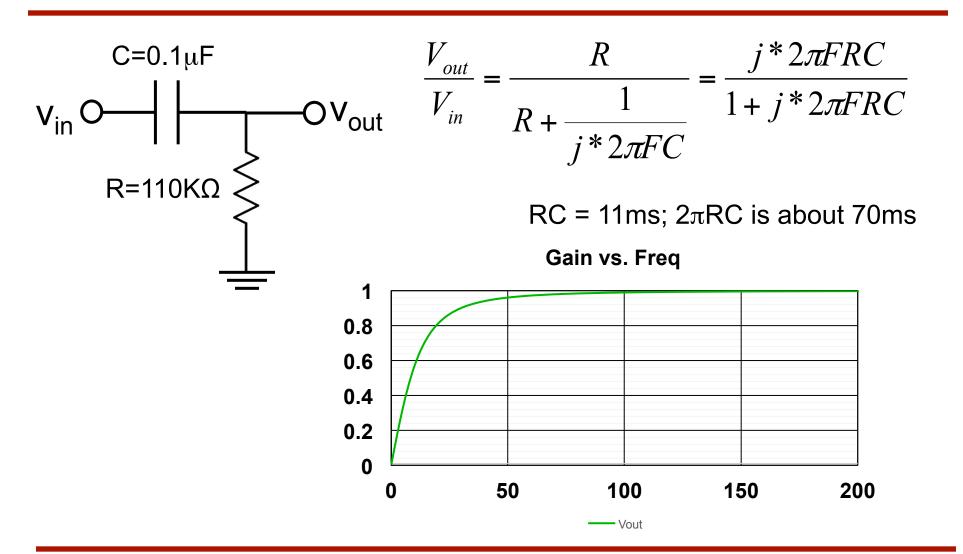


In this project we will build an electrocardiagram (ECG or EKG). This is a noninvasive device that measures the electrical activity of the heart using electrodes placed on the skin.

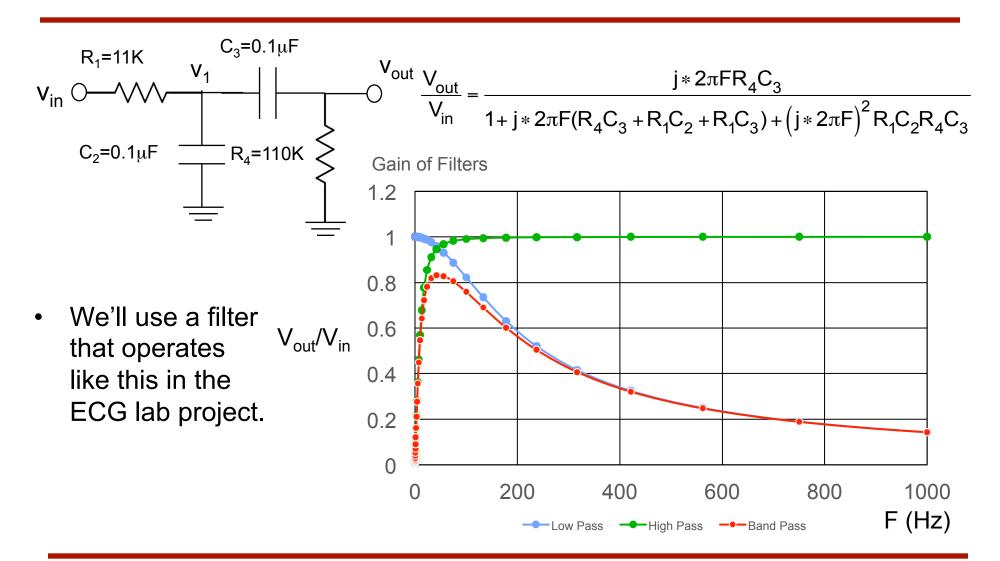
Analyzing RC Circuits Using Impedance – Review (Low Pass Filter)



Analyzing RC Circuits Using Impedance – Review (High Pass Filter)



Analyzing RC Circuits Using Impedance – Review (Band Pass Filter)

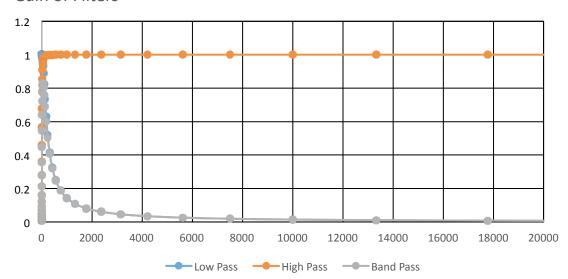


BODE PLOTS

Our Plots Are Not Very Good

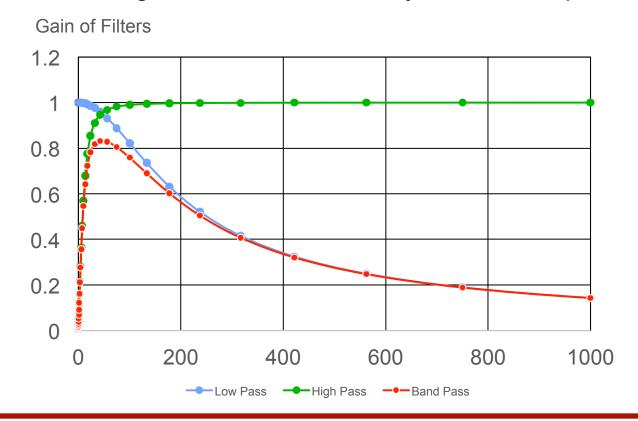
- Most of the plot is for the "high frequency"
 - Your ear is very interested in each octave (2x) in freq
 - If you plot the full audio spectrum (20-20kHz)
 - 50% of the plot will be from 10-20kHz
 - And that is only one octave of ten!
 - You won't be able to see the first five octaves!

Gain of Filters



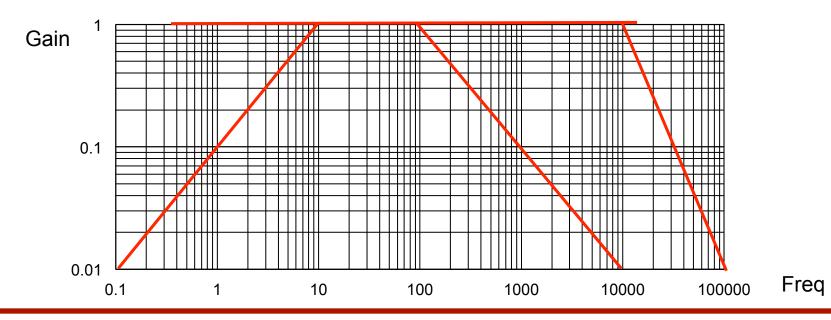
More Plot Issues

- The plots usually are proportional to:
 - Constant, or F or F⁻¹ or F² or F⁻²
 - It would be great if these were easy to see on a plot

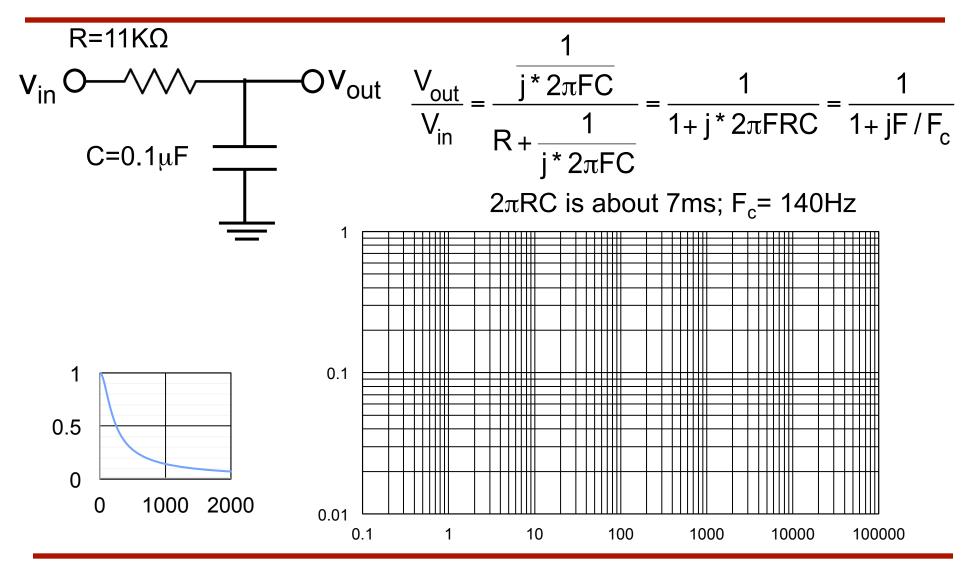


There is an Easy Way to Fix Both Issues

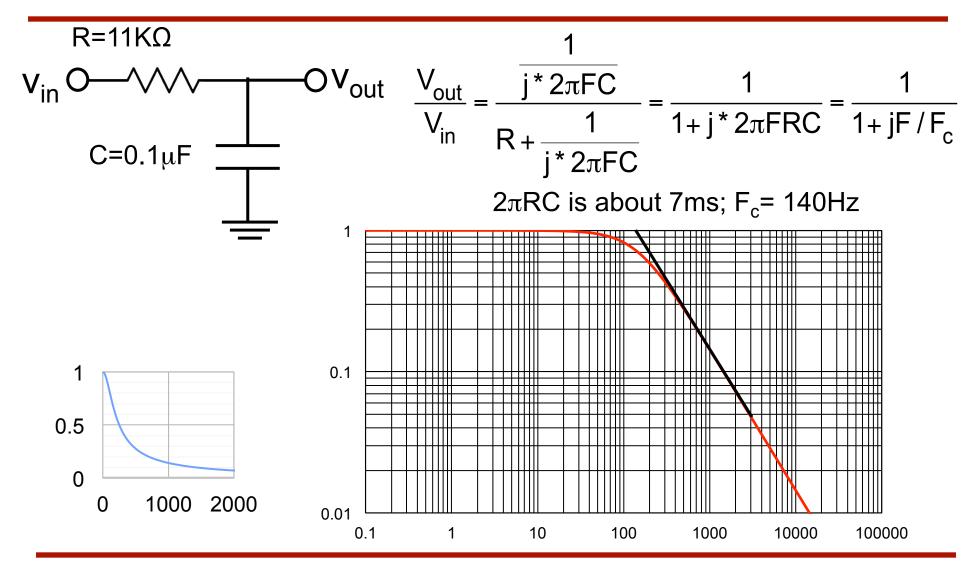
- Use a log-log plot
 - That is plot the log(Gain) vs log(F)
 - Usually labeled with Gain and F
 - But the spacing between numbers is their log
- Any power of F is a straight line log(Fⁿ) = n* log(F)
 So the slope of the line is the power of F



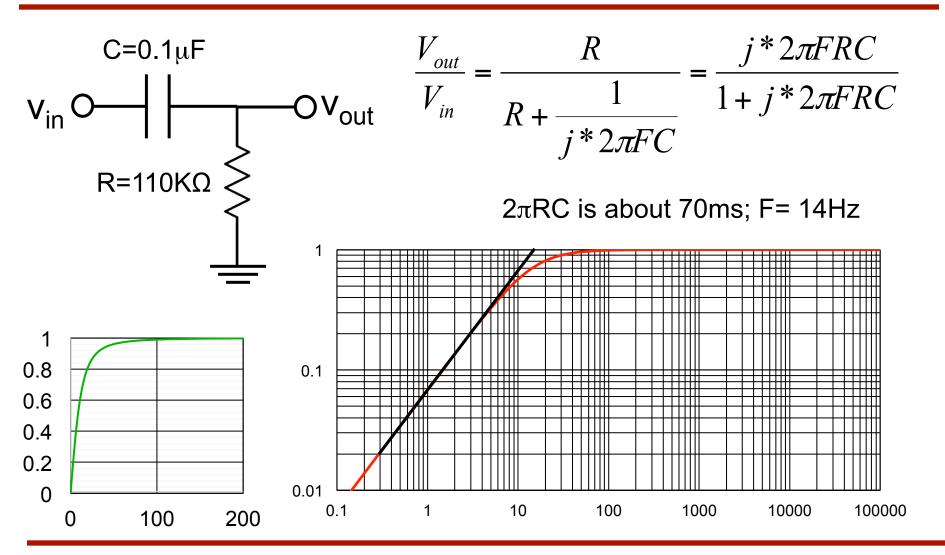
Example - Low Pass Filter



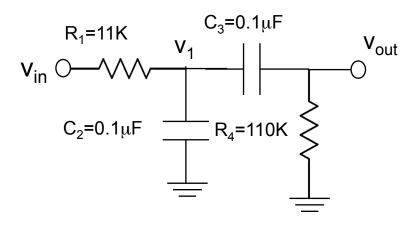
Low Pass

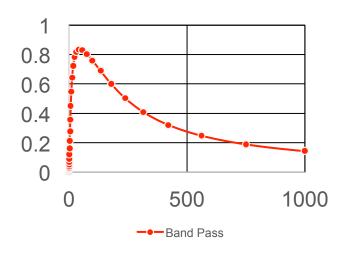


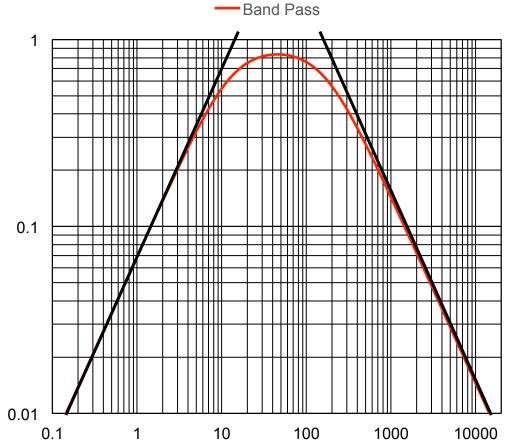
High-Pass



Band Pass - Combining the Low and High Pass







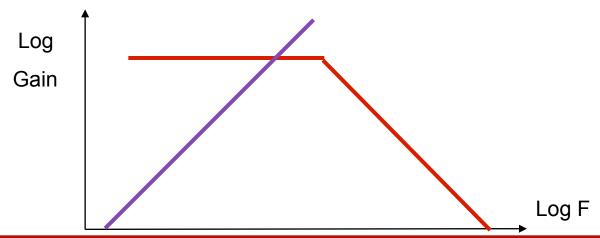
One More Trick With Log-Log Plots

Remember:

$$log(A*B) = log(A) + log(B)$$
, and $log(A/B) = lob(A) - log(B)$

• So:
$$\frac{V_{out}}{V_{in}} = \frac{j * 2\pi FRC}{1 + j * 2\pi FRC}$$

- Can add two lines
 - One slope +1
 - One flat and then slope -1



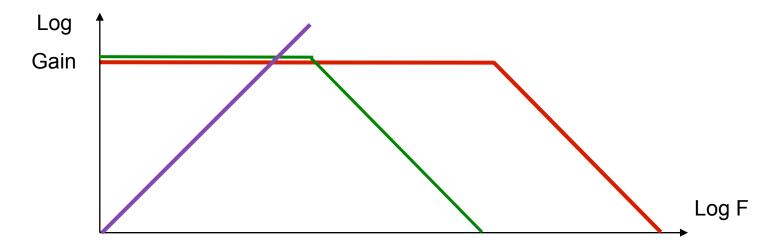
Log-Log Plot Tricks, cont'd

Our bandpass filter earlier had a gain function of the form

$$\frac{V_{out}}{V_{in}} = \frac{j*2\pi FR_2C_2}{1+j*2\pi F(R_1C_1 + R_2C_2) + \left(j*2\pi F\right)^2R_1C_1R_2C_2}$$

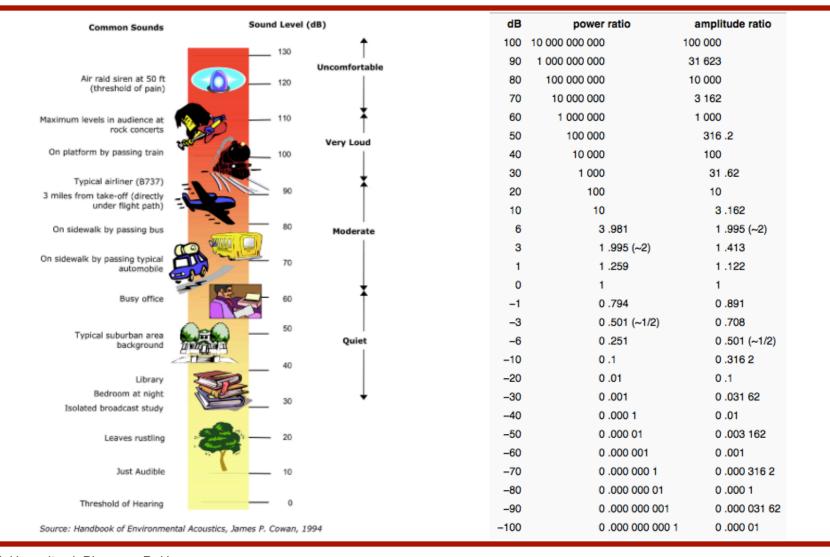
 If we can factor the polynomial, then we can add lines as on the last slide

$$\frac{V_{out}}{V_{in}} = \frac{j * 2\pi FR_2C_2}{\left(1 + j * 2\pi FR_1C_1\right) * \left(1 + j * 2\pi FR_2C_2\right)}$$



dB

Use of Logarithmic Scales to Represent Wide Ranges



dB

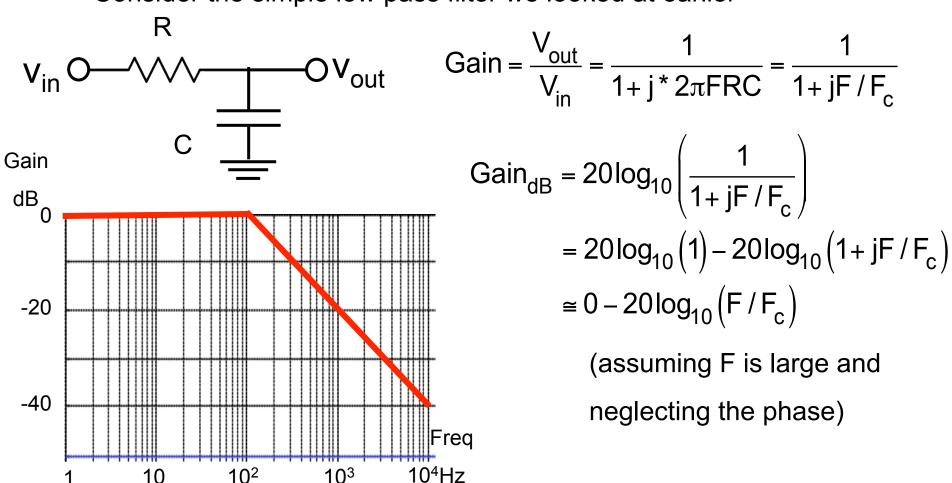
- In many places you will see the symbol dB
 - This is decibel
 - It is a logarithmic measure of power gain
 - dB = 10 * log (Power_{out}/Power_{in})
- It is logarithmic so
 - 10dB is a 10x change in power
 - 20dB is a 100x change in power
 - 3dB is a 2x change in power
- Since power is proportional to V²
 - A 10x change in voltage is a 100x change in power
 - This is a 20dB change
 - 6dB is a 2x change in voltage

Plotting Gain vs. Frequency

- Want to plot log(gain) vs. log(frequency)
- dB is already log of the gain
 - So the plots look semilog
 - Log of frequency in the x direction
 - dB in the y direction
 - But this is the log-log plot that we want
- Please remember that dB measures power
 - 10x in voltage = 20dB

Plotting dB vs. Frequency

Consider the simple low pass filter we looked at earlier



FYI – Hendrik Bode

Hendrik Wade Bode



Hendrik Wade Bode

Born December 24, 1905

Madison, Wisconsin

June 21, 1982 (aged 76) Cambridge, Massachusetts

Residence Cambridge, Massachusetts

Nationality American

Died

Fields Control Systems, Physics,

Mathematics, Telecommunications

Institutions Ohio State University

Bell Laboratories Harvard University

Alma mater Ohio State University

Columbia University

Known for Bode plot, Control theory,

Telecommunications

Notable awards Richard E. Bellman Control Heritage Award (1979)

Rufus Oldenburger Medal (1975)

President's Certificate of Merit Edison Medal (1969)

Ernest Orlando Lawrence Award

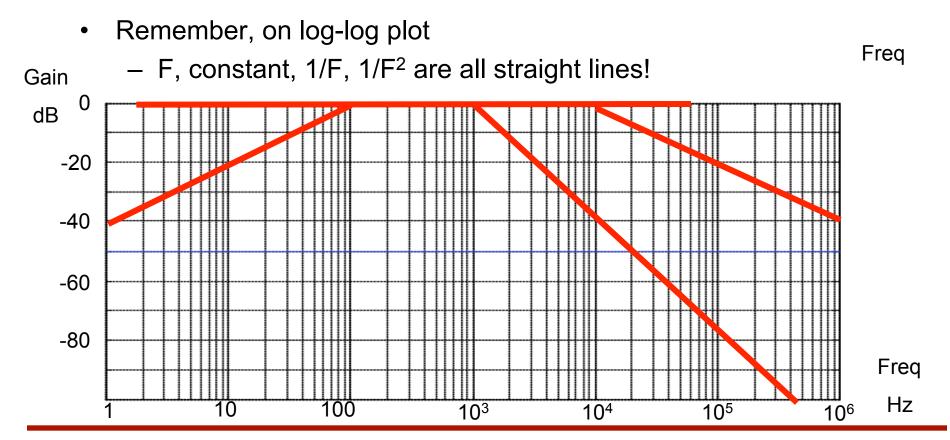
(1960)

- Bode (1905 –1982) spent most of his career at Bell Labs.
- He worked on control system theory and electronic filters and during WW II he worked on using radar information to direct antiaircraft guns to try to intercept enemy aircraft and missiles like the German V2 missile.
- But today he's best remembered for inventing Bode plots used to describe the frequency behavior of linear systems.

(Wikipedia)

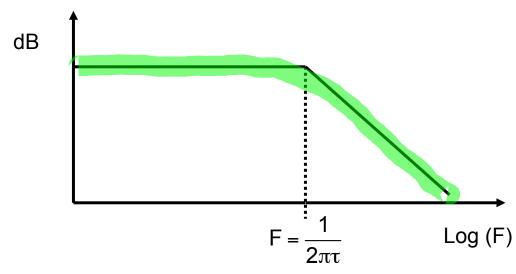
Plotting the Output

- We use a Bode Plot to plot the transfer function of a circuit
 - Remember that this is the log of gain vs. log of frequency



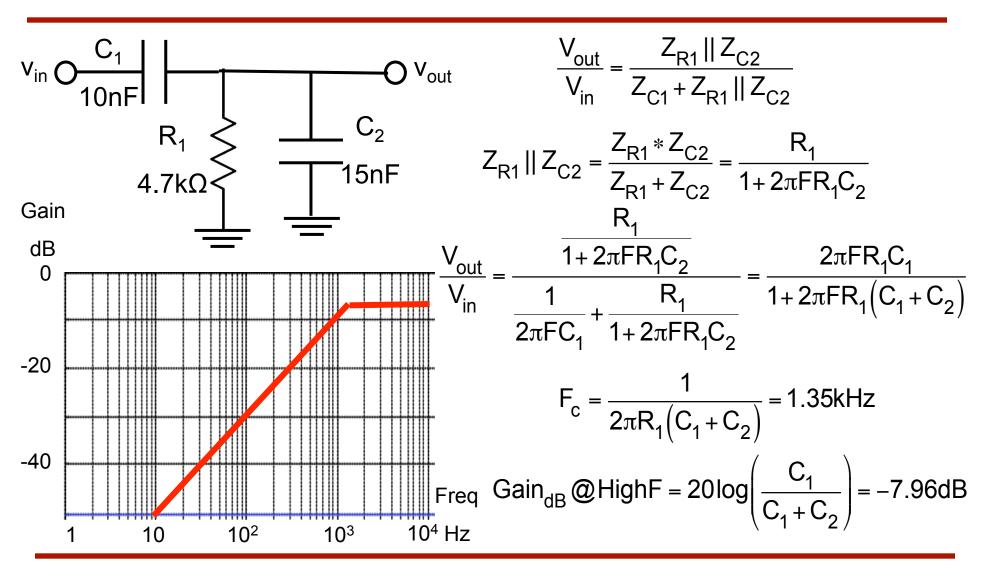
Circuit Bode Plots

- These are generally easy to draw
 - Know the slopes at different frequency ranges
 - Plot those straight lines
 - These lines will intercept at the F where the terms are equal i.e. F = 1/2πτ = 1/2πRC

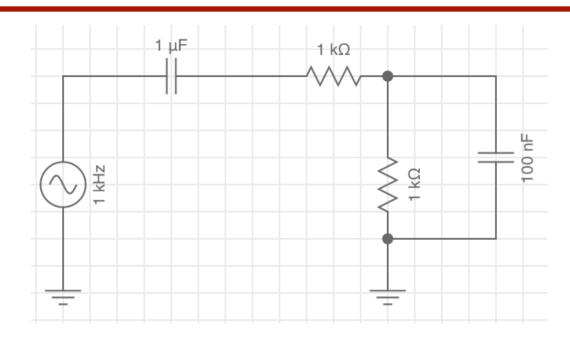


Actual curve will be close to the straight lines

Example



EveryCircuit - Frequency Resonse

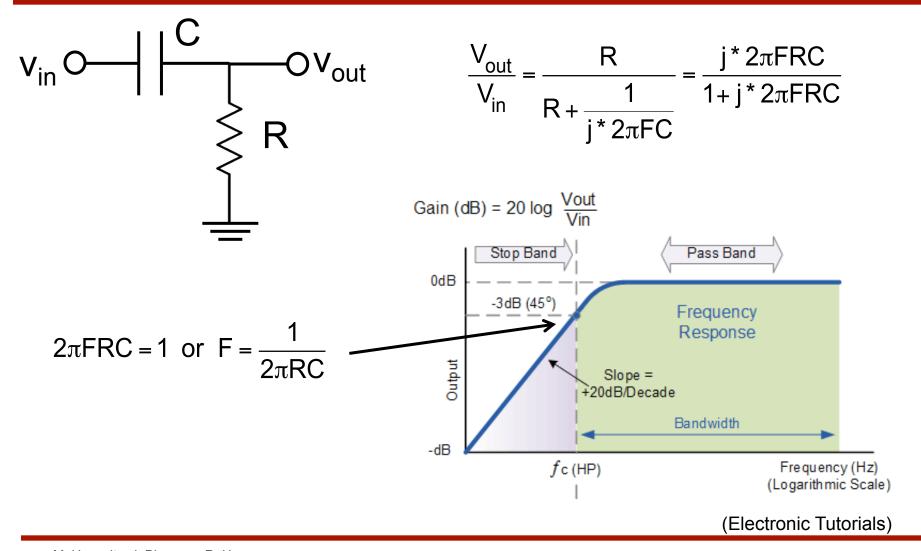


- EveryCircuit can be used to calculate and plot Bode plots for circuits. We'll demo this in class.
- This is very useful for checking answers to HW problems or for developing understanding about circuit frequency response.

Bonus Section (Not on HW, Exams) See Class Reader For Details

WHAT DOES (1 + j*x) REALLY MEAN?

An Example - High Pass RC Filter Bonus Material - See Class Reader For Details



3dB? Bonus Material - See Class Reader For Details

- Notice that when the two terms are the same, $F = 1/2\pi RC$
 - The overall gain is -3dB
 - This might seem right since -3dB is ½, BUT
 - This is the power ratio!
 - The voltage ratio is only $1/\sqrt{2}$!
- What is going on?
- To understand, we'll need to think about what (1 + j*x) means

Adding Sine and Cosine Waveforms Bonus Material - See Class Reader For Details

- 1 + j*x means the waveform is the sum of
 - A sinewave with amplitude 1
 - With a cosine wave with amplitude "x"
- The good news is that this always results in a sinusoidal waveform
 - With some phase shift between a sin and cos (+90°)
 - So we can write

$$A\sin(2\pi Ft + \phi) = \sin(2\pi Ft) + x * \cos(2\pi Ft)$$

And we want to find A and φ

The Trick Bonus Material - See Class Reader For Details

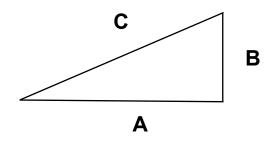
$$C * sin(2\pi Ft + \phi) = A * sin(2\pi Ft) + B * cos(2\pi Ft)$$

- This equation is always true so
 - At t = 0, the sine term is zero

$$C * sin(\phi) = B$$

- At t = 1/(4F), the cosine term is zero, so

$$C * cos(\phi) = A$$



So the amplitude of the resulting sine wave is

$$\sqrt{A^2 + B^2}$$

Learning Objectives For Today

- Understand how to create Bode plots for RC circuits
 - You plot two straight lines that intercept at $F=1/2\pi RC$
- (Bonus Section) Understand what an amplitude of (1+ j*2πRCF) means
 - The result is a sum of a sine and cosine wave