



Institut et hôpital neurologiques de Montréal
Montreal Neurological Institute and Hospital

MCIN MCGILL CENTRE
for INTEGRATIVE
NEUROSCIENCE



Looking Inside the Black Box

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McGill Centre for Integrative Neuroscience

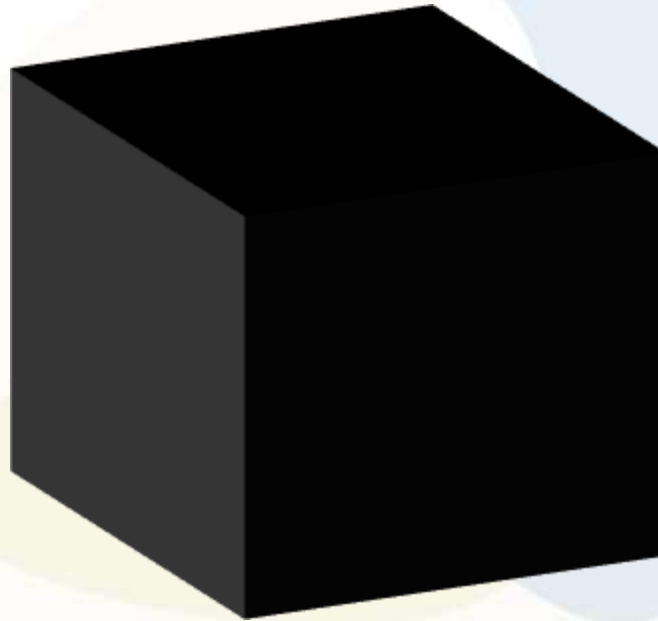


Centre universitaire
de santé McGill



McGill University
Health Centre

Danger!

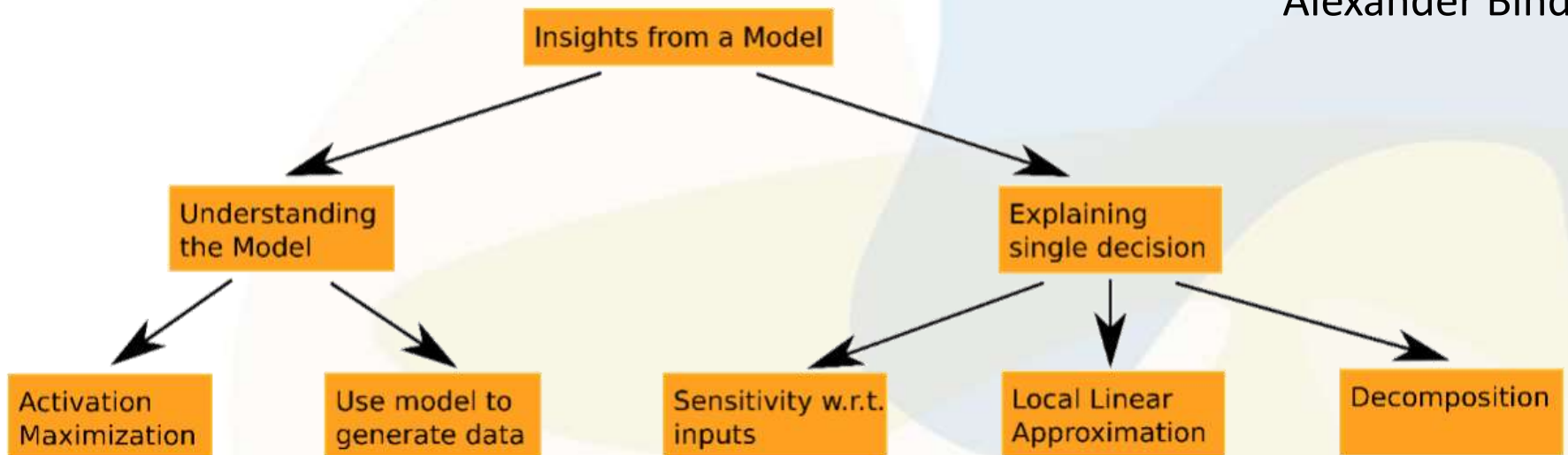


**If you gaze long into an abyss,
the abyss also gazes into you.**

Interpretability



Alexander Binder

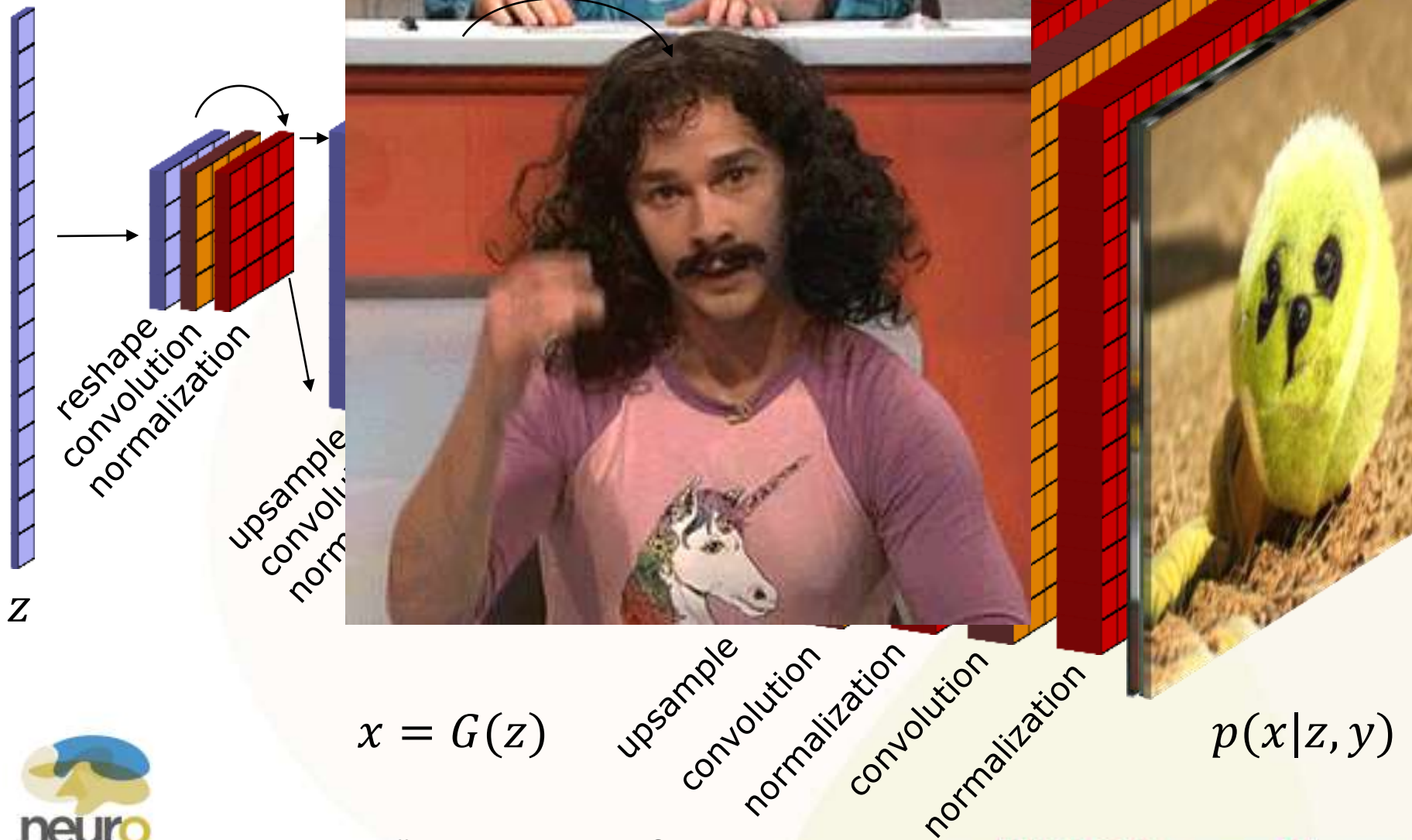


Ask GPT-2

Q: How can we interpret the predictions of deep neural networks?

A: Deep learning is not perfect (and there's nothing stopping us from improving the algorithm), but the current state in the marketplace implies that machine learning is being more widely adopted than it has in the past. If you think about it - how important is it to get a computer to do all the computations, while leaving the user and content completely unaware of what's going on? This is probably exactly the goal of deep learning!

GANs



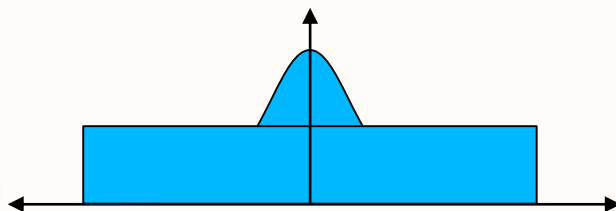
$$x = G(z)$$

$$p(x|z, y)$$

BigGAN



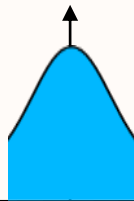
$p(z)$



BigGAN



$p(z)$



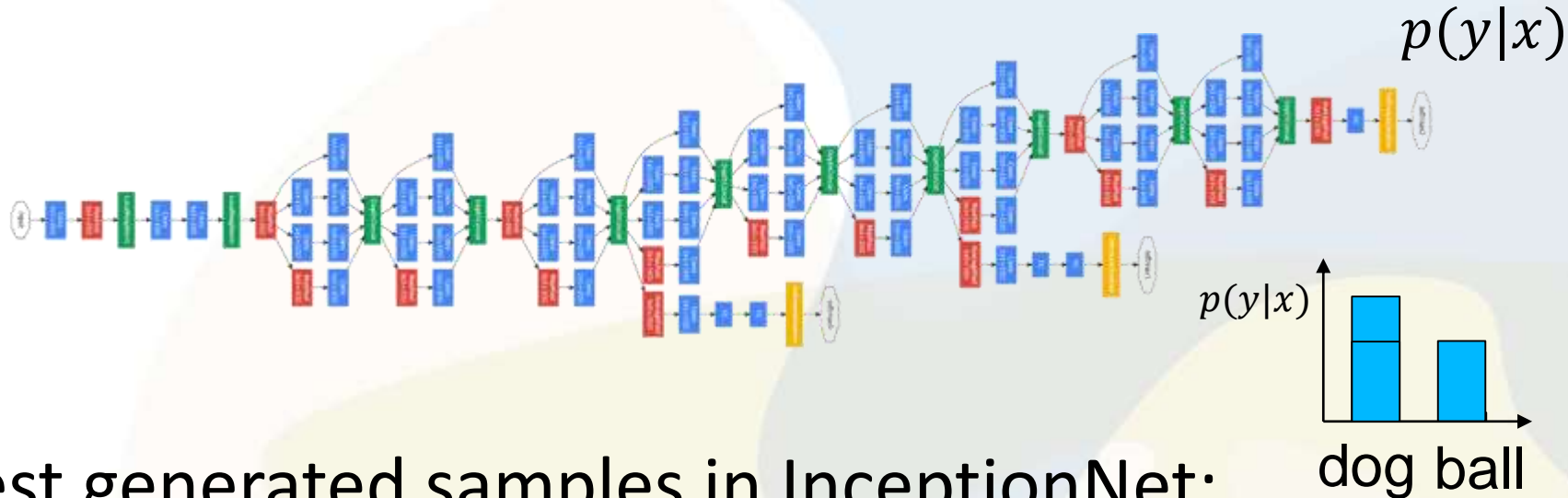
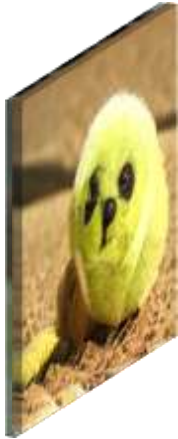
Truncation Trick



colab.research.google.com/github/tensorflow/hub/blob/master/examples/colab/biggan_generation_with_tf_hub.ipynb

Inception Score

$$x = G(z)$$



Test generated samples in InceptionNet:

- Low entropy in $p(y|x)$
- High entropy in $\int p(y|x = G(z))dz = p(y)$

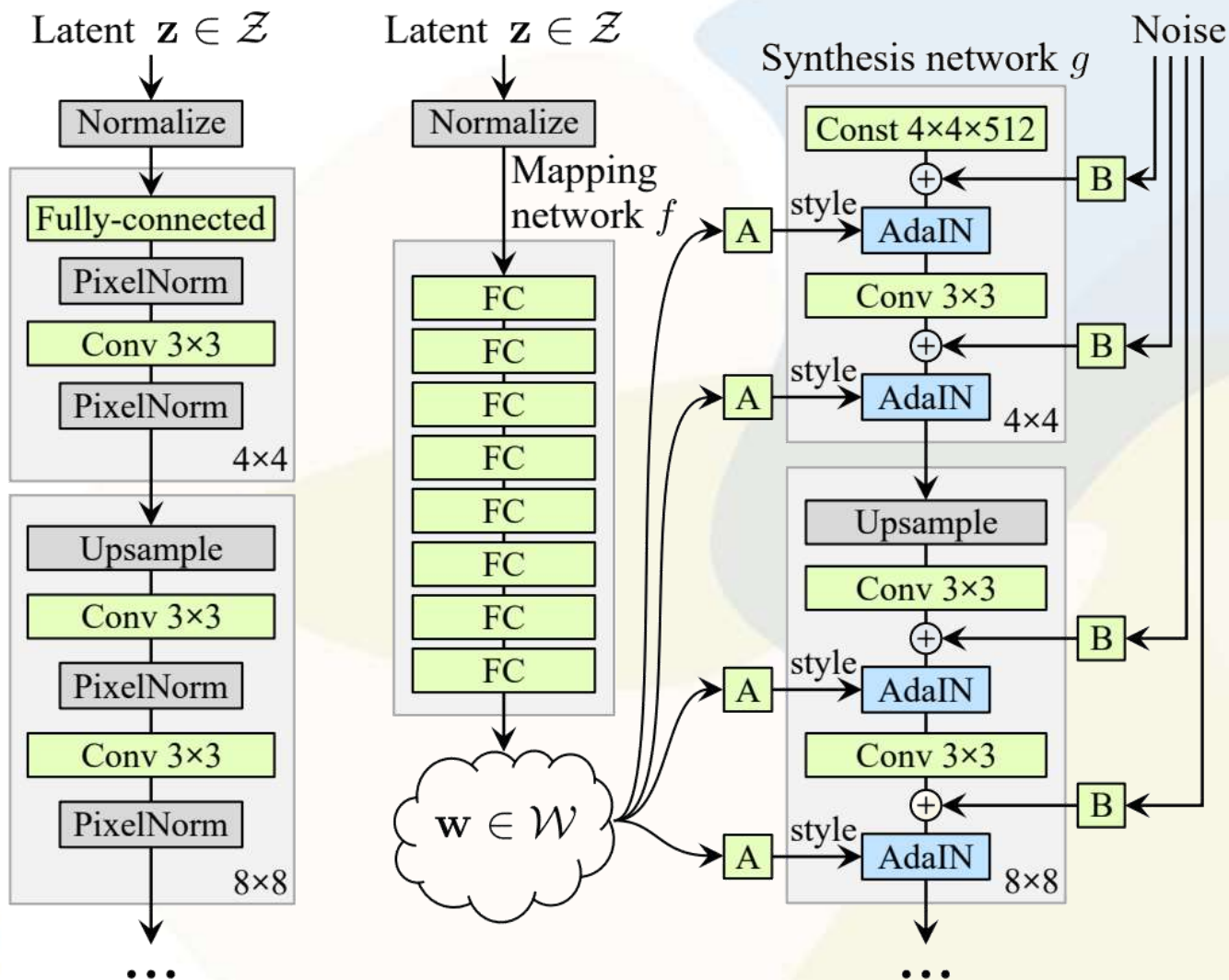
$$IS(x) = e^{\mathbb{E}_x KL(p(y|x) || p(y))}$$

Fréchet Inception Distance

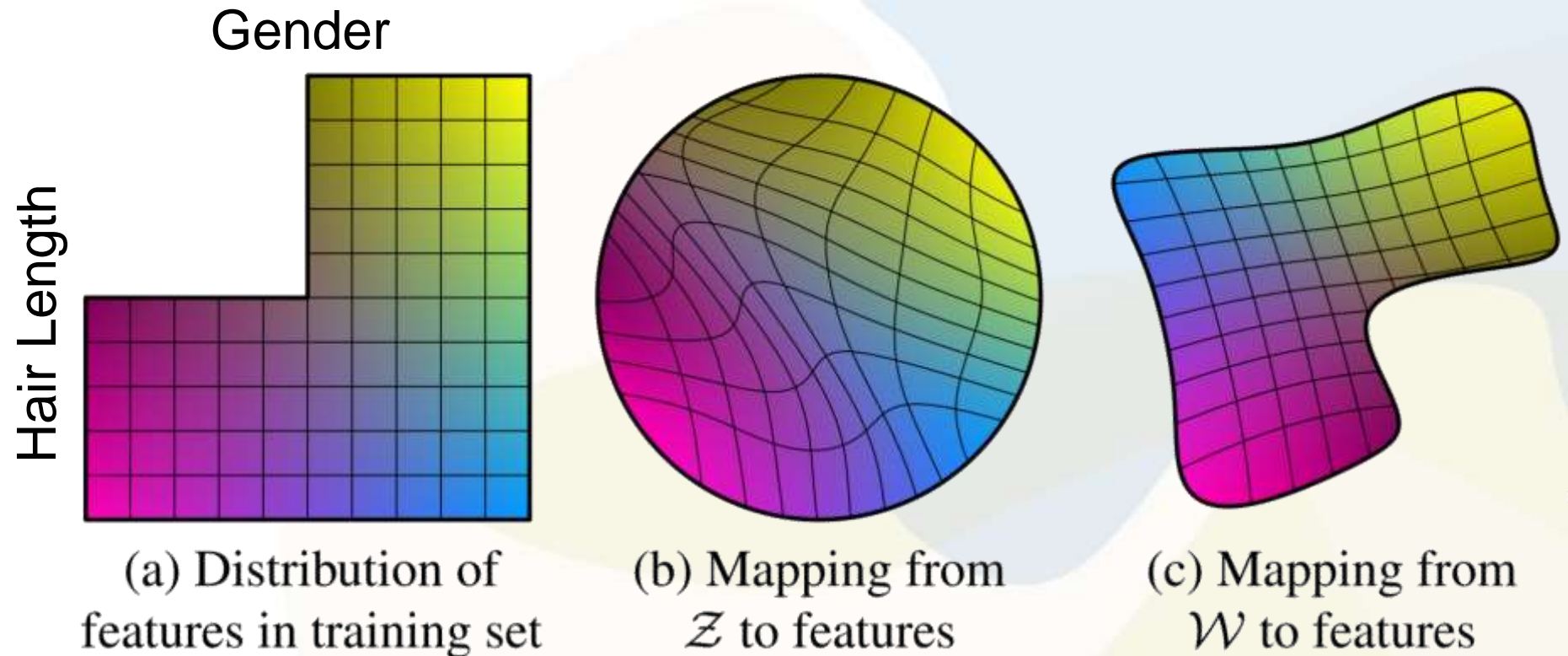


$$FID(x) = (\mu_r - \mu_g)^2 + Tr\left(\Sigma_r + \Sigma_g - 2\sqrt{\Sigma_r \Sigma_g}\right)$$

StyleGAN



StyleGAN



StyleGAN



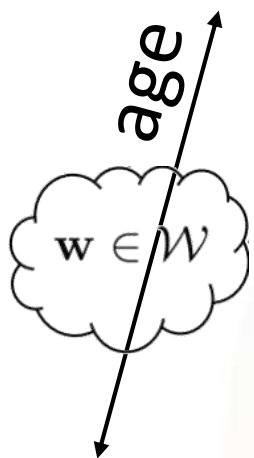
StyleGAN



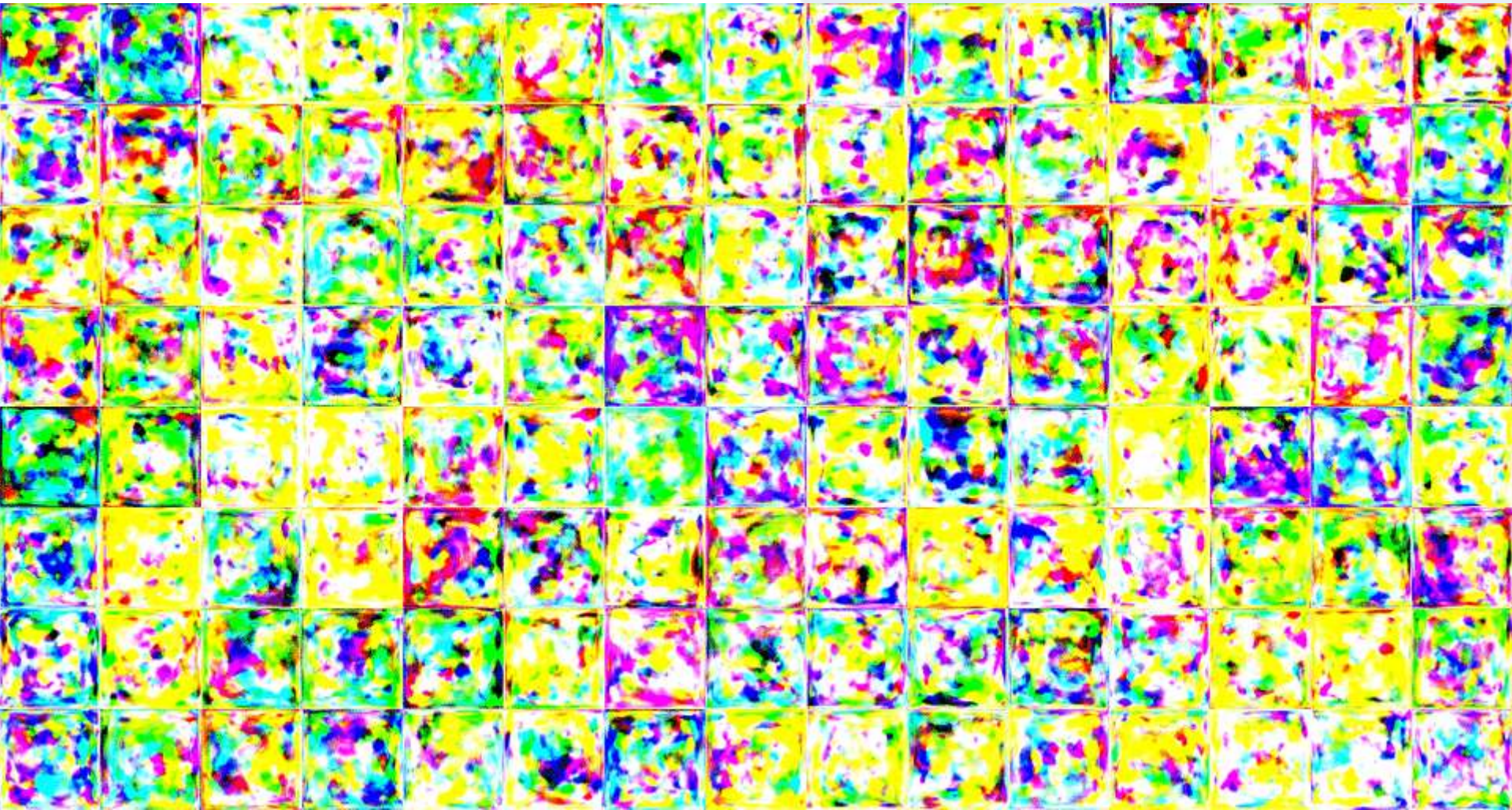
StyleGAN



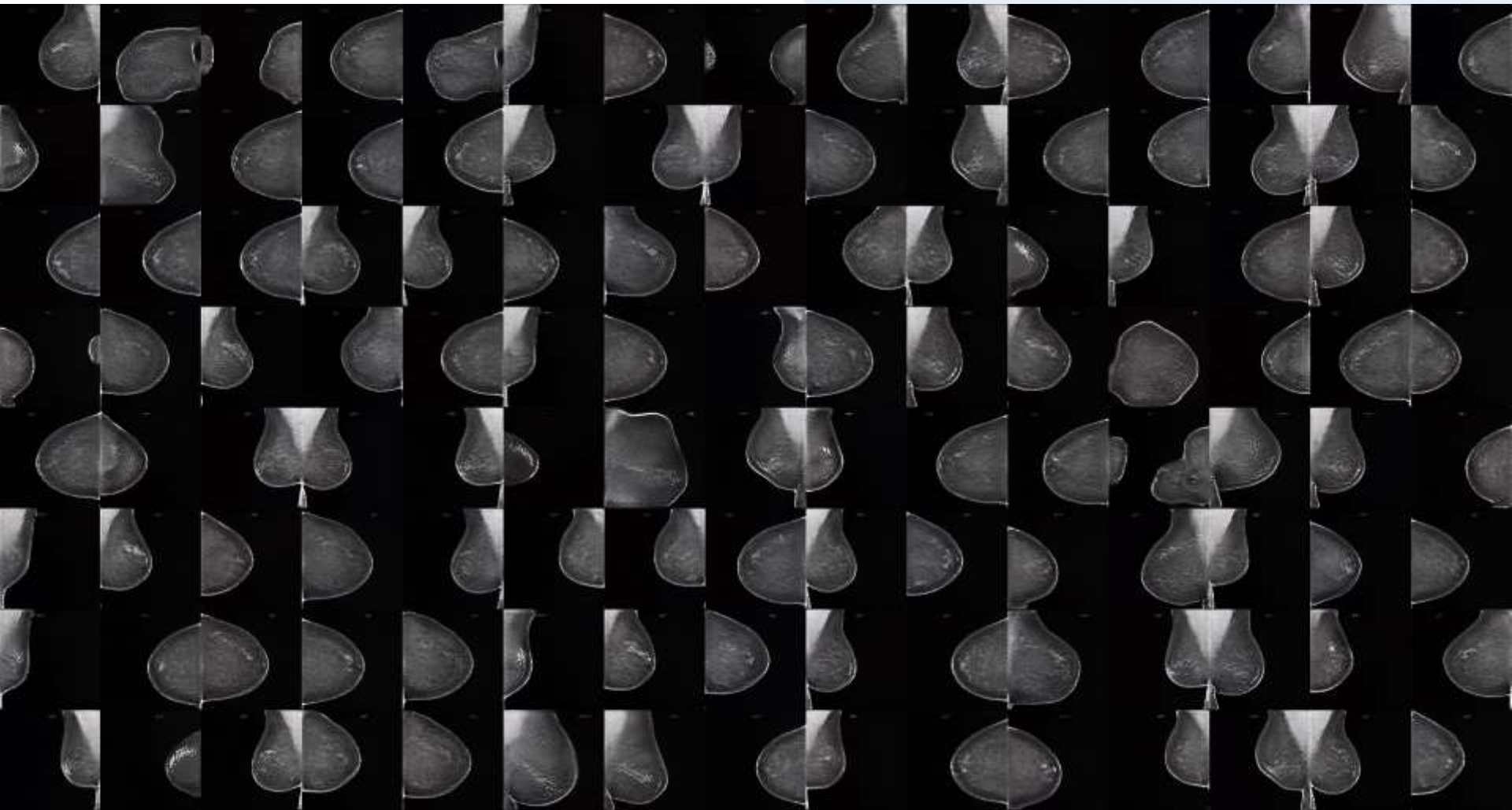
StyleGAN



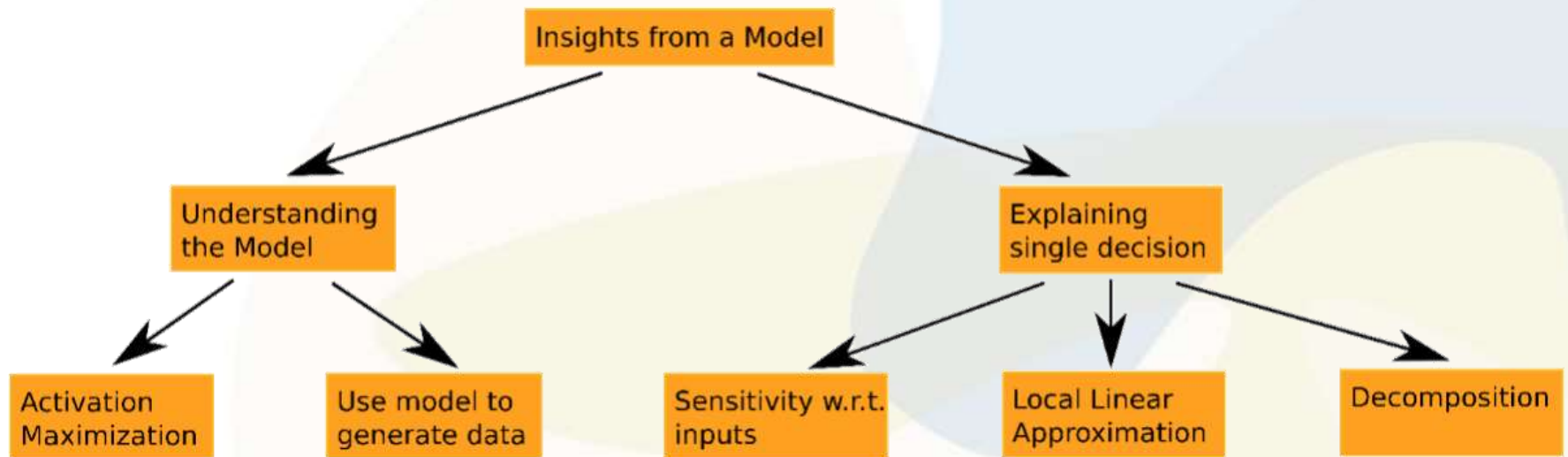
StyleGAN



StyleGAN



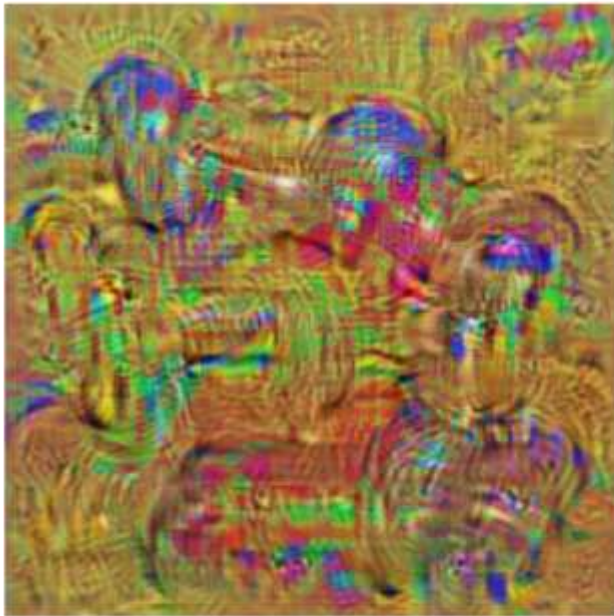
Interpretability



BigGAN
StyleGAN

Class Appearance Models

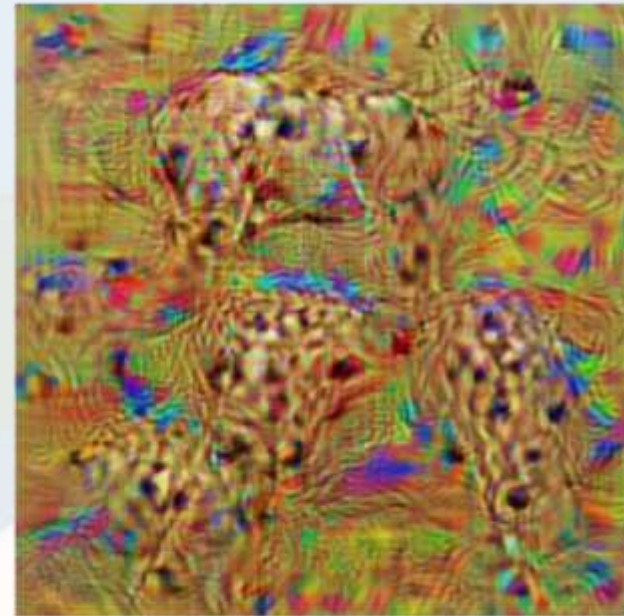
$$\operatorname{argmax}_x p(y = c|x) - \lambda ||x||_2^2$$



dumbbell



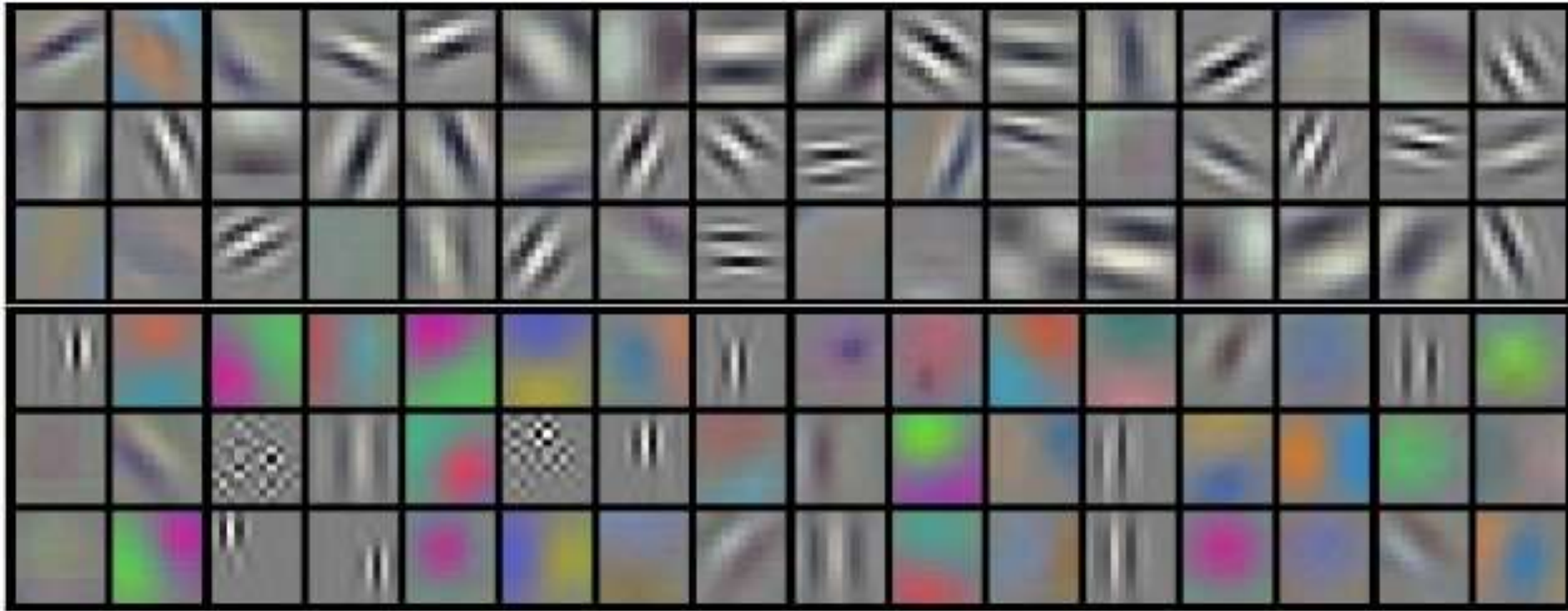
cup



dalmatian

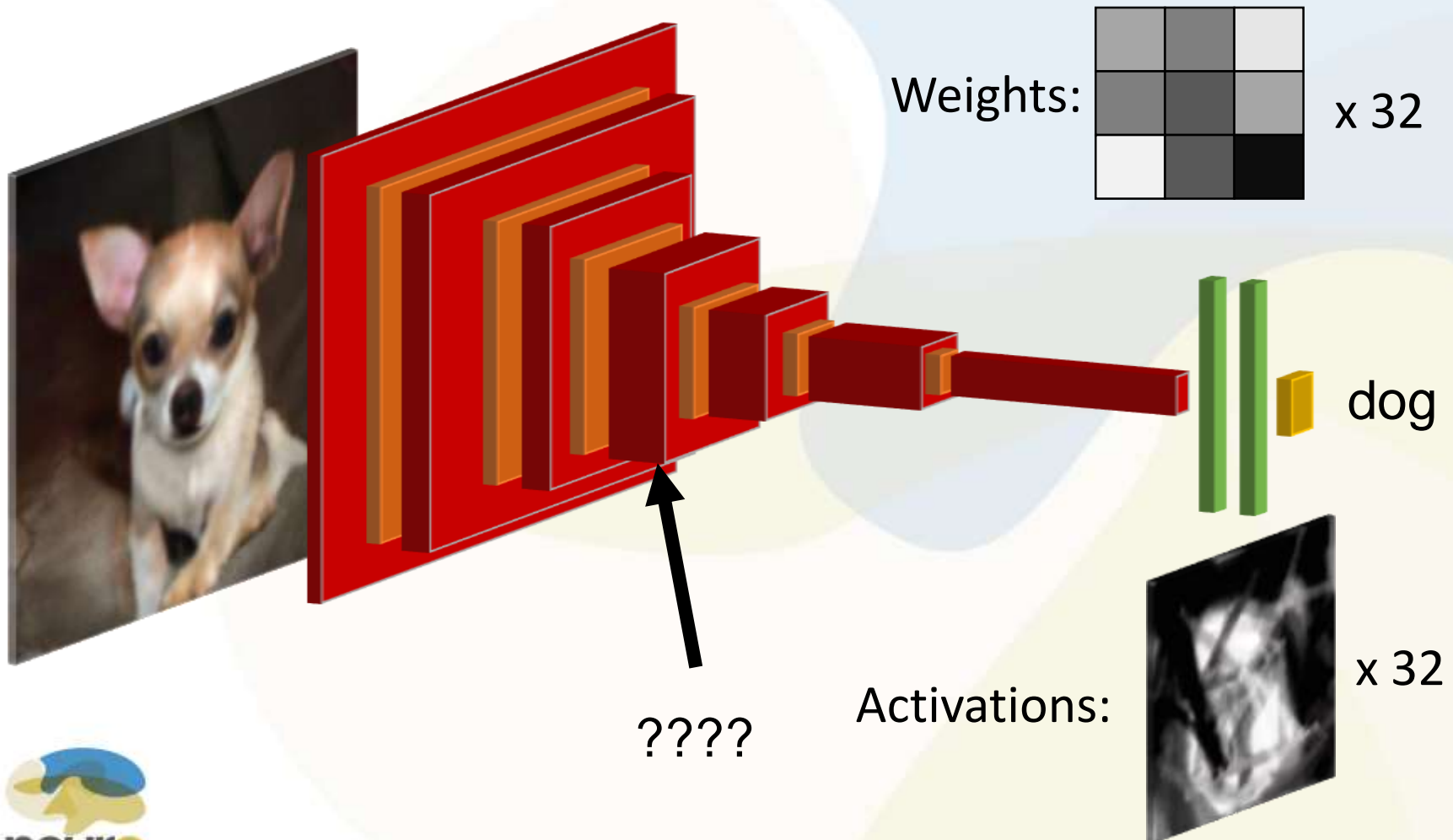


Visualizing Filters

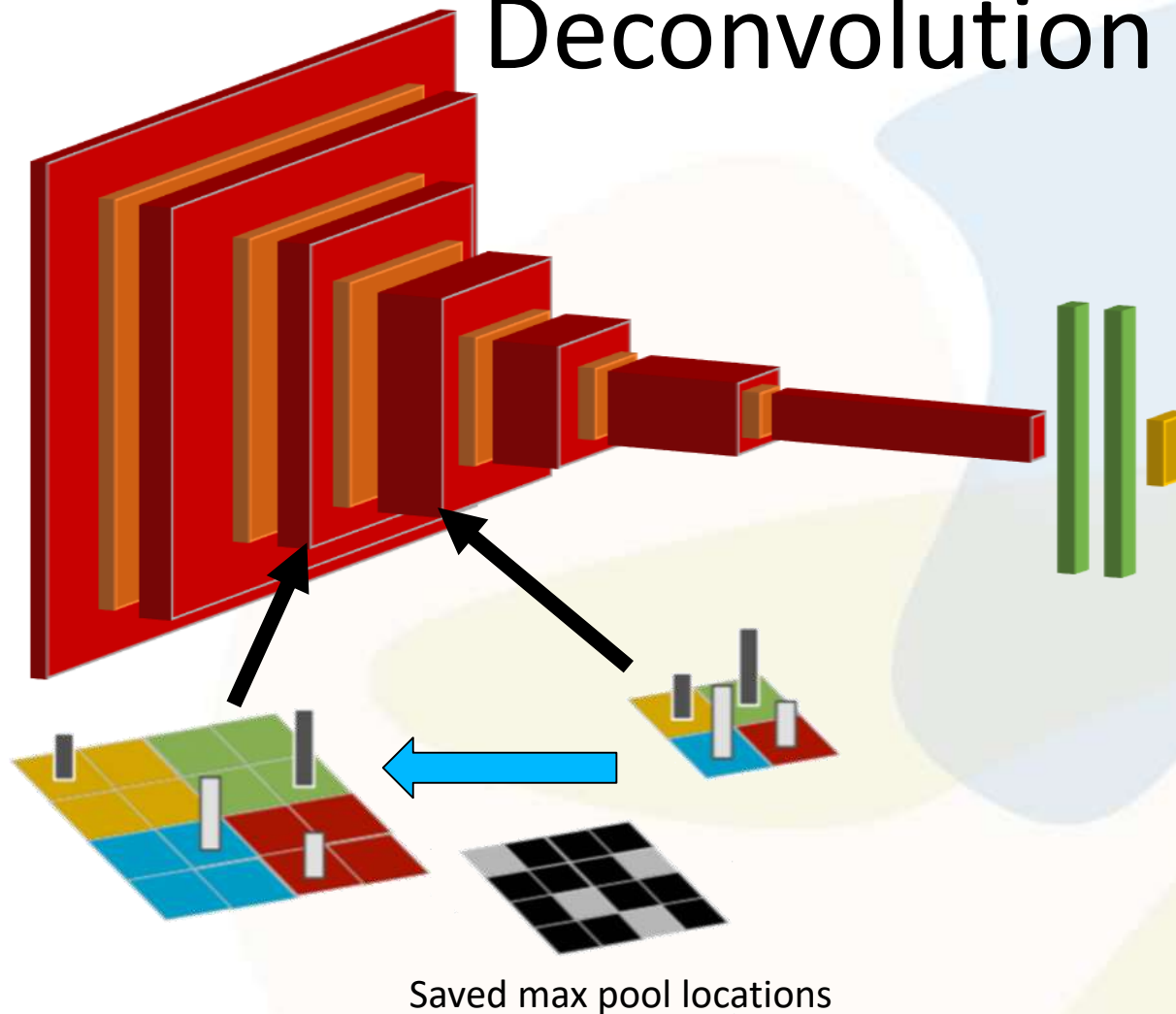


Filter weights for layer 1 of AlexNet

Visualizing Filters



Deconvolution



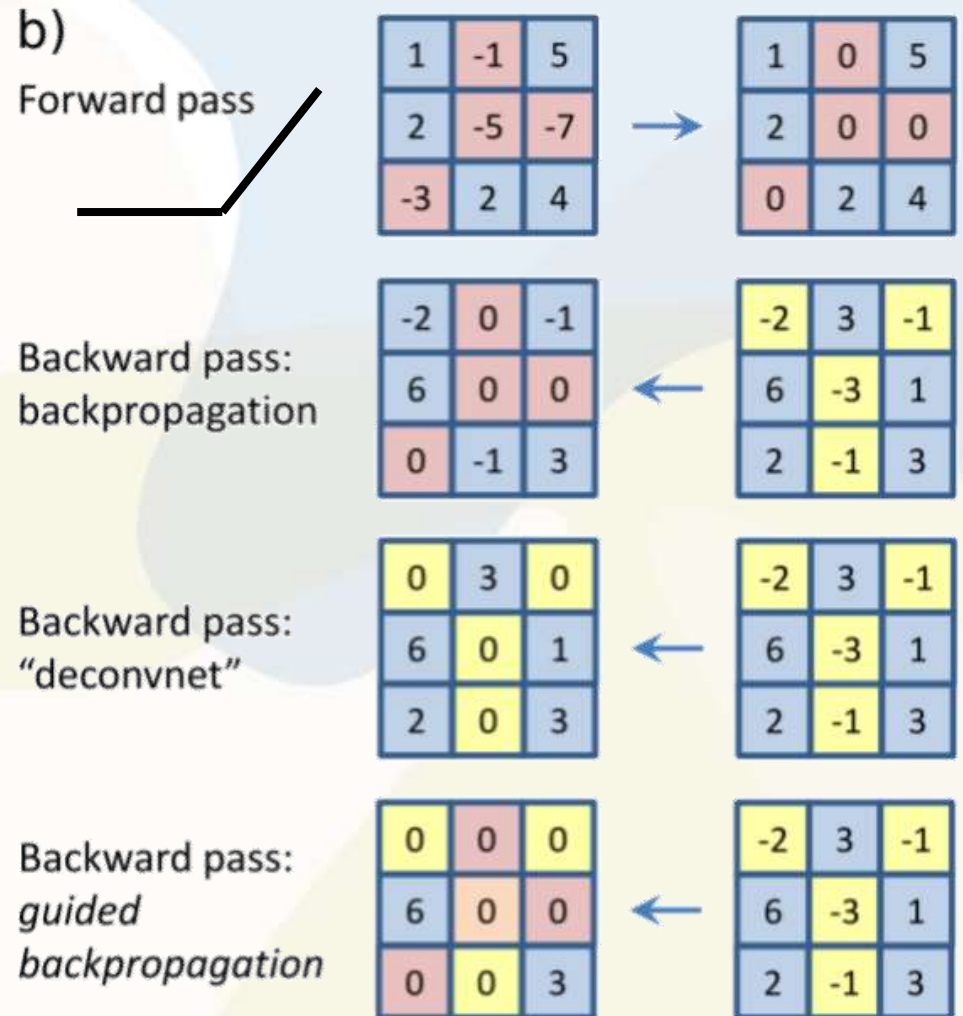
What input x
does this filter
respond to?

Deconvolution



Guided Backprop

- Deconvolution fails without max pooling!
- Guided backprop changes how **ReLU** is handled

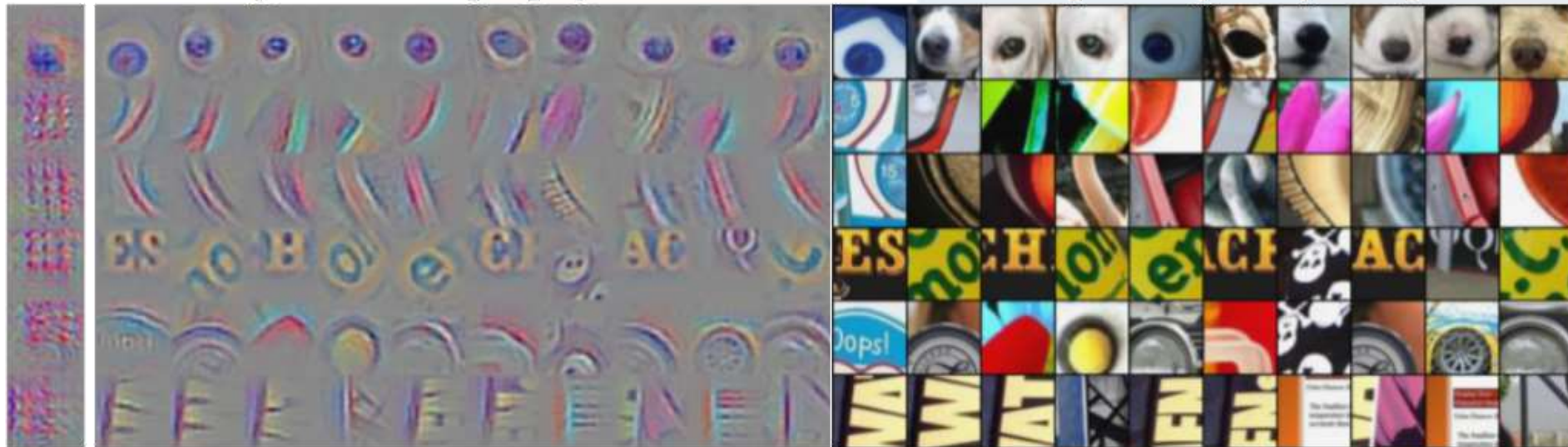


Guided Backprop

deconv

guided backpropagation

corresponding image crops



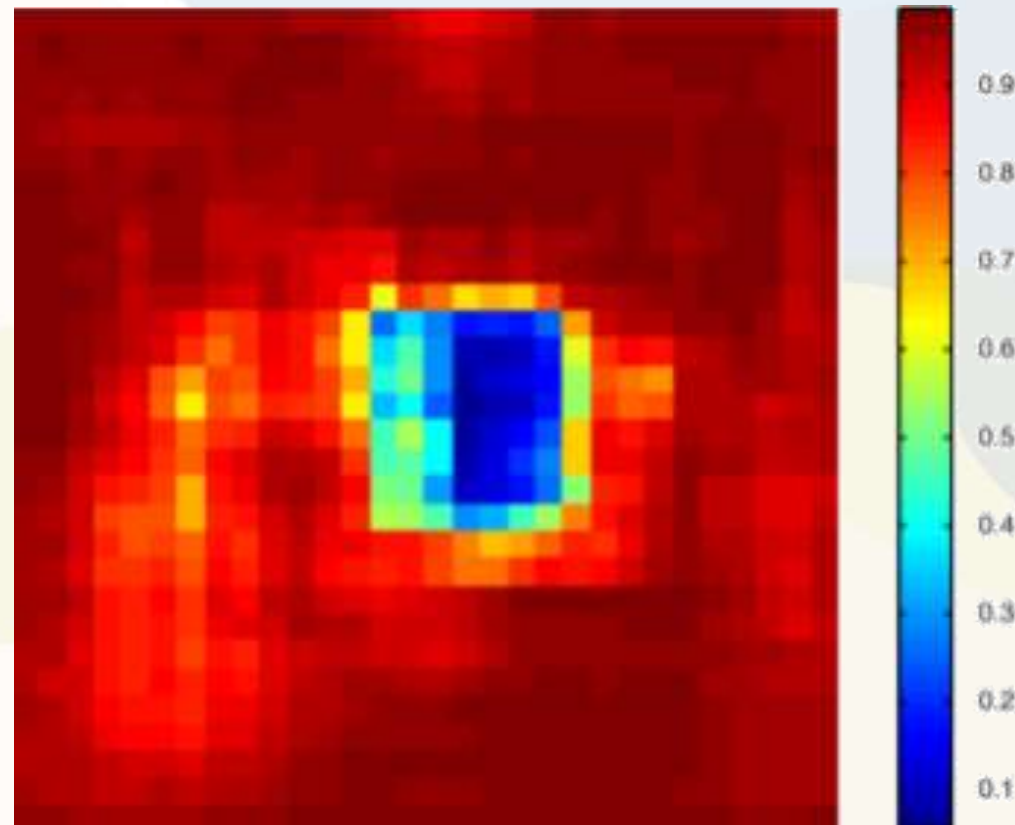
Input Importance



Occlusion Testing



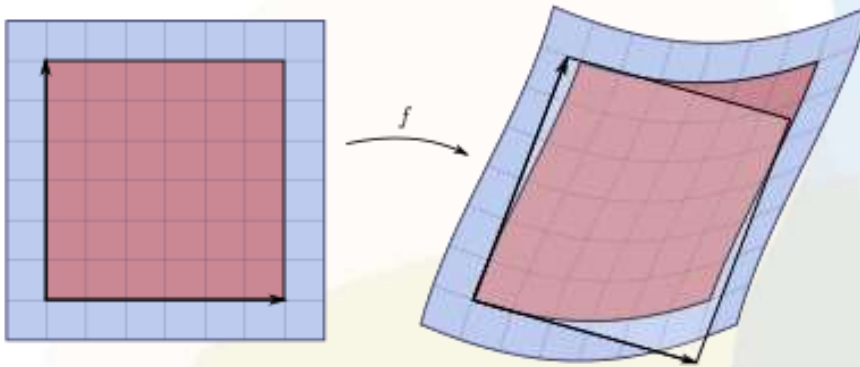
x



$p(y=pomeranian / x)$ when occluded

Saliency

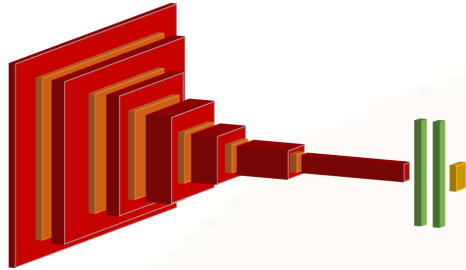
- Jacobian:



$$J = \begin{bmatrix} \frac{\partial \hat{y}_1}{\partial x_1} & \dots & \frac{\partial \hat{y}_1}{\partial x_k} \\ \dots & \dots & \dots \\ \frac{\partial \hat{y}_m}{\partial x_1} & \dots & \frac{\partial \hat{y}_m}{\partial x_k} \end{bmatrix}$$

- Best linear approximation for non-linear mapping $p(y|x)$ near \mathbf{x}

Backprop

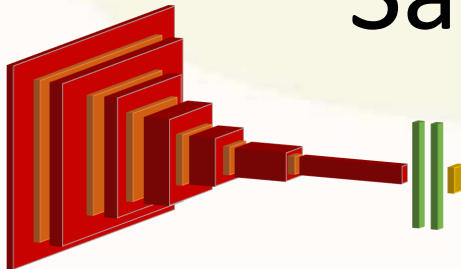


$$\hat{y} = p(y|x) \rightarrow L(y, \hat{y})$$



$$\nabla_{\theta} L(y, \hat{y}) = \left[\frac{\partial L}{\partial w_1}, \frac{\partial L}{\partial w_2}, \dots, \frac{\partial L}{\partial w_n} \right]^T$$

Saliency

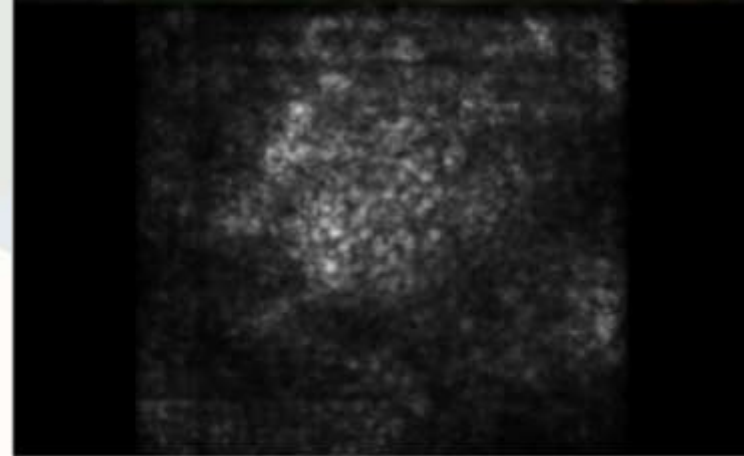
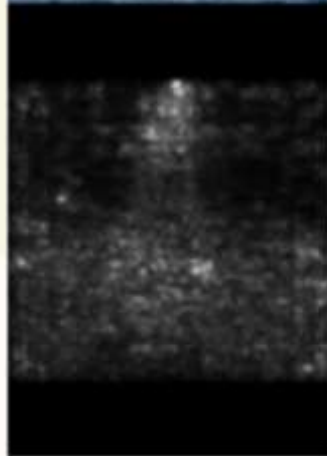
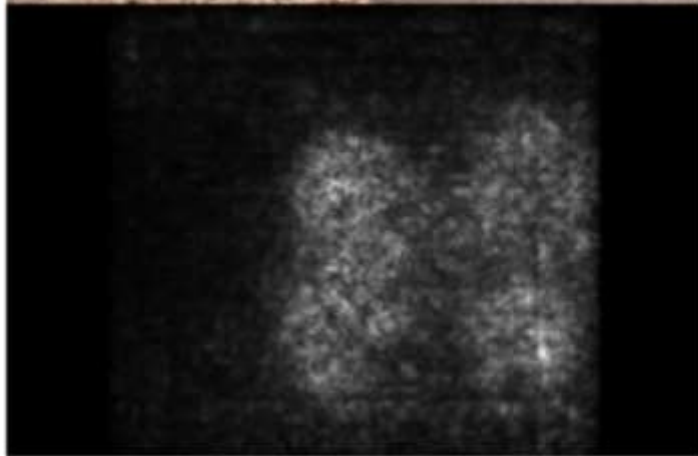


\hat{y}

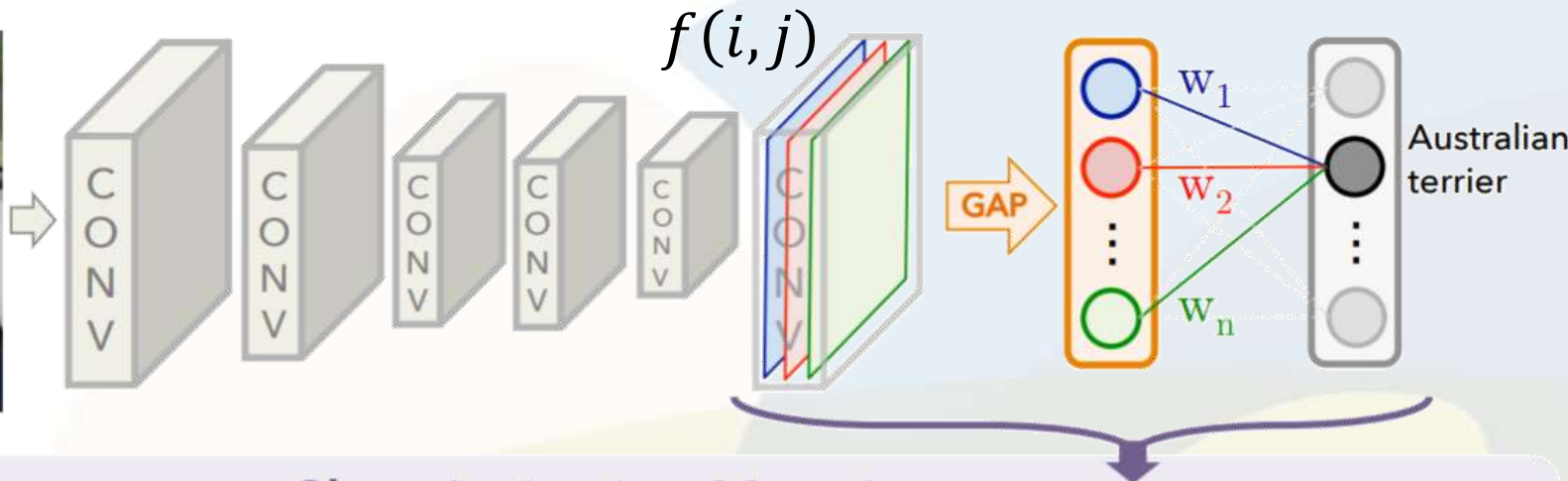


$$\begin{bmatrix} \frac{\partial \hat{y}_1}{\partial x_1} & \dots & \frac{\partial \hat{y}_1}{\partial x_k} \\ \dots & \dots & \dots \\ \frac{\partial \hat{y}_m}{\partial x_1} & \dots & \frac{\partial \hat{y}_m}{\partial x_k} \end{bmatrix}$$

Saliency



Class Activation Mapping

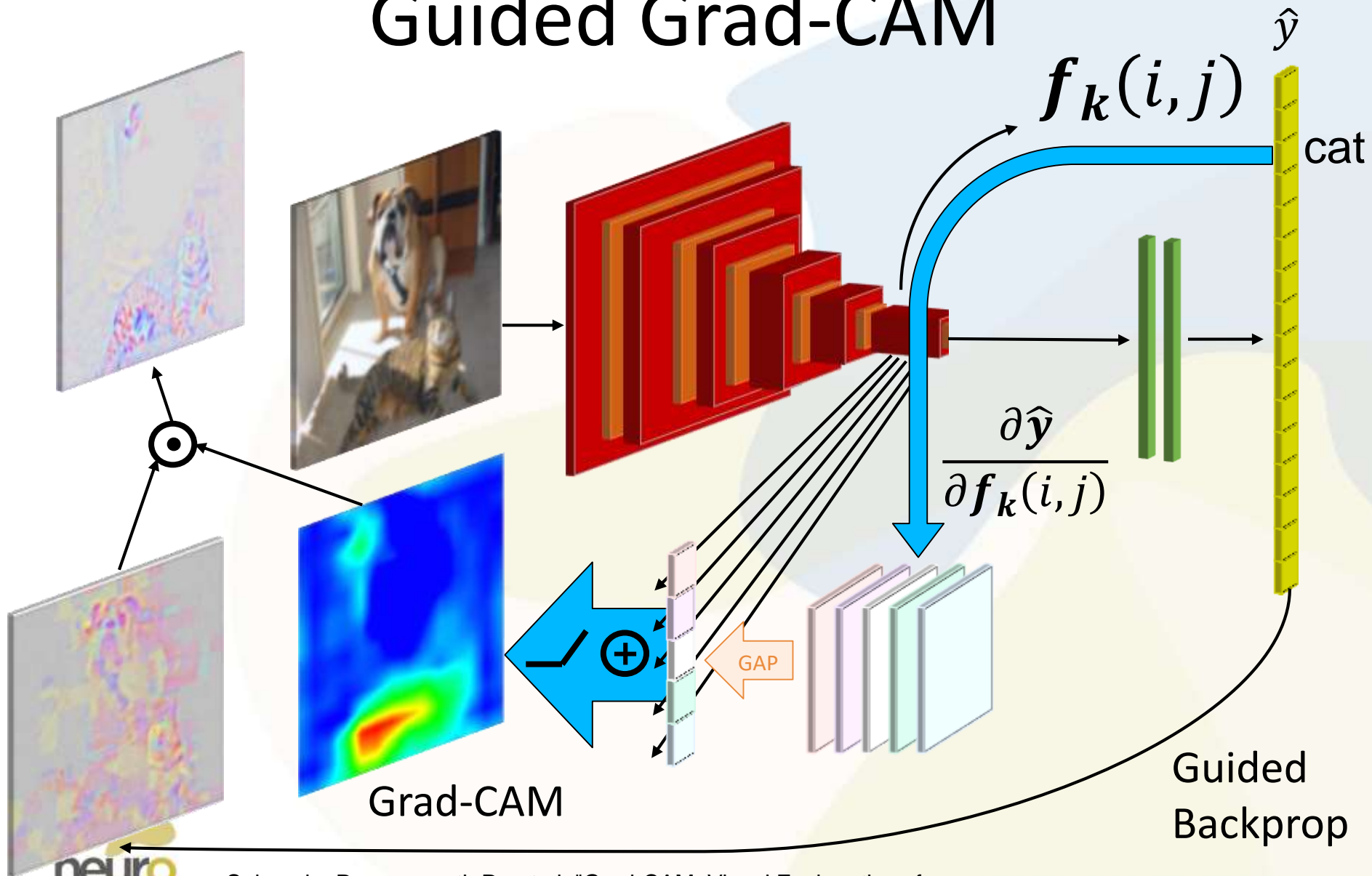


Class Activation Mapping

$$w_1 * f_1(i, j) + w_2 * f_2(i, j) + \dots + w_n * f_n(i, j) = F^k$$

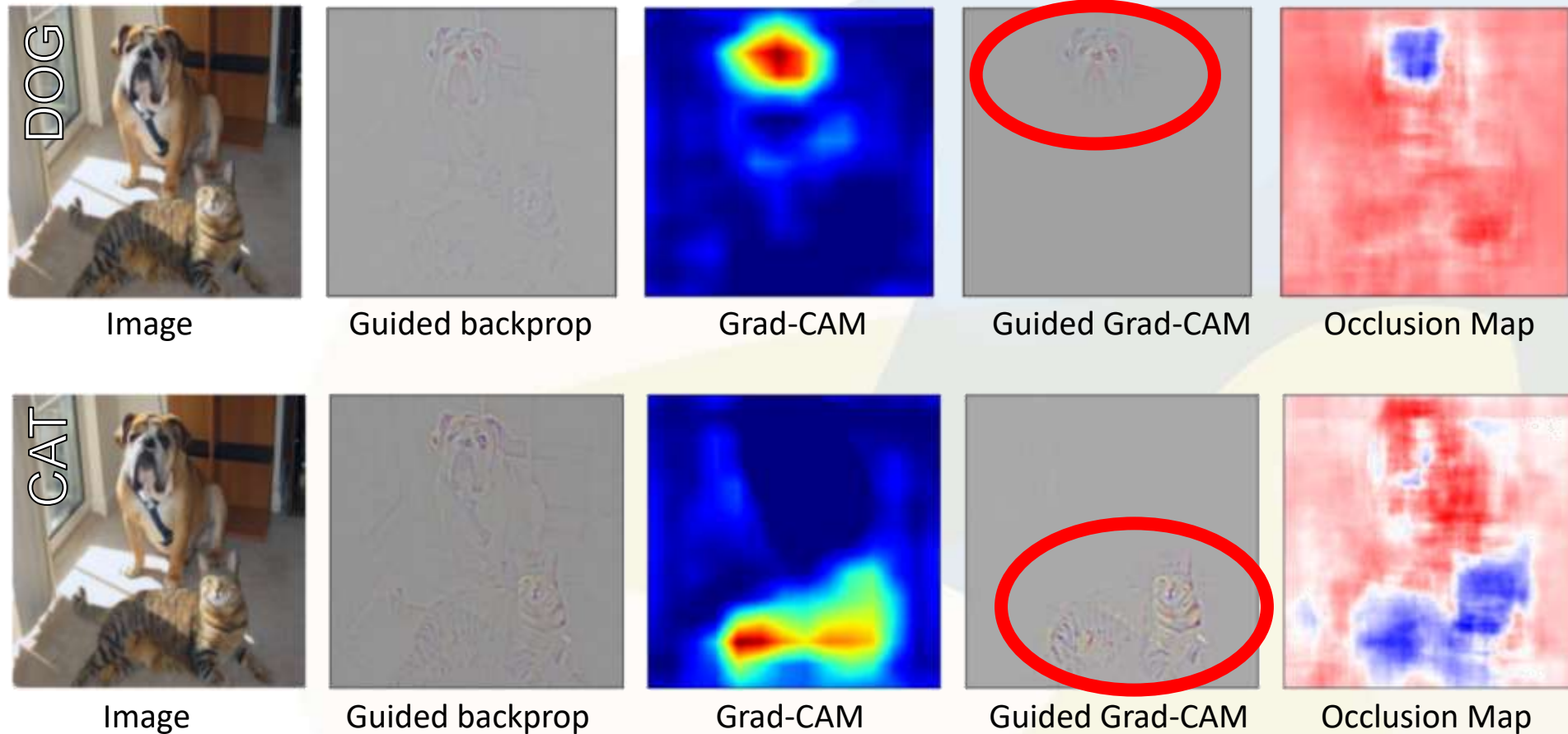
Class Activation Map (Australian terrier)

Guided Grad-CAM

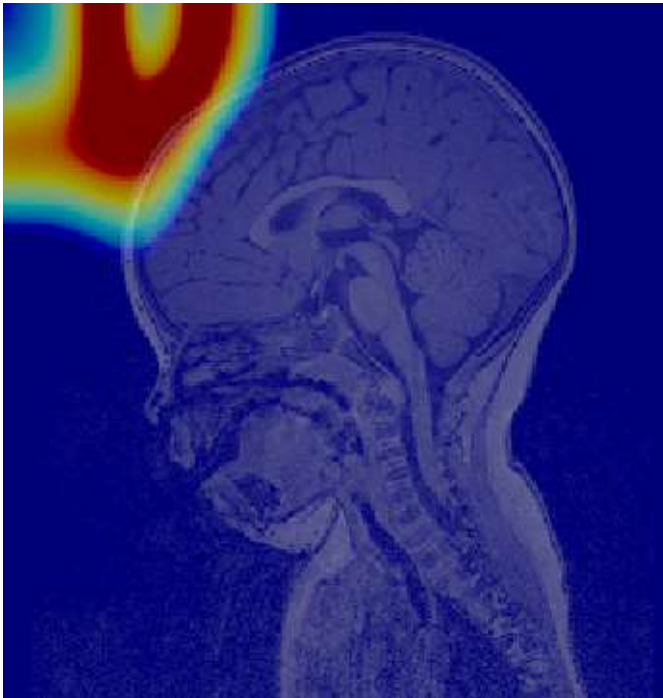


Selvaraju, Ramprasaath R., et al. "Grad-CAM: Visual Explanations from Deep Networks via Gradient-Based Localization." *ICCV*. 2017.

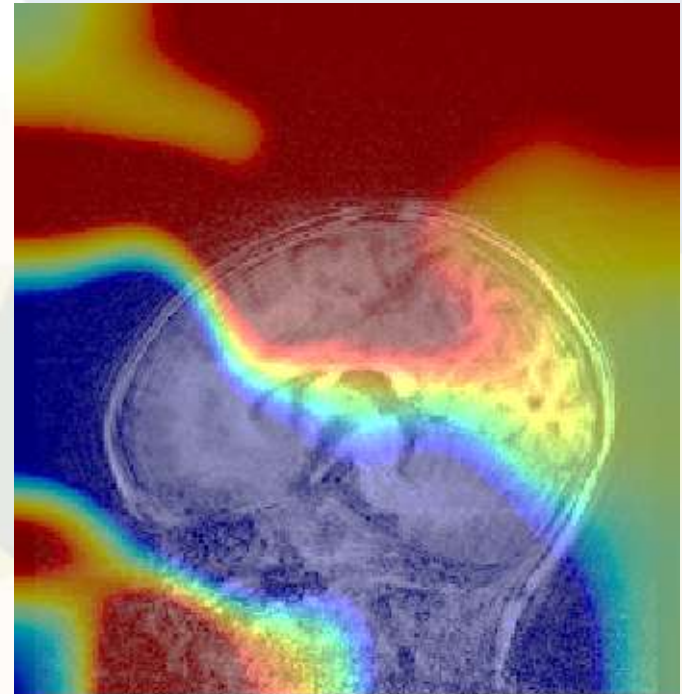
Guided Grad-CAM



Guided Grad-CAM

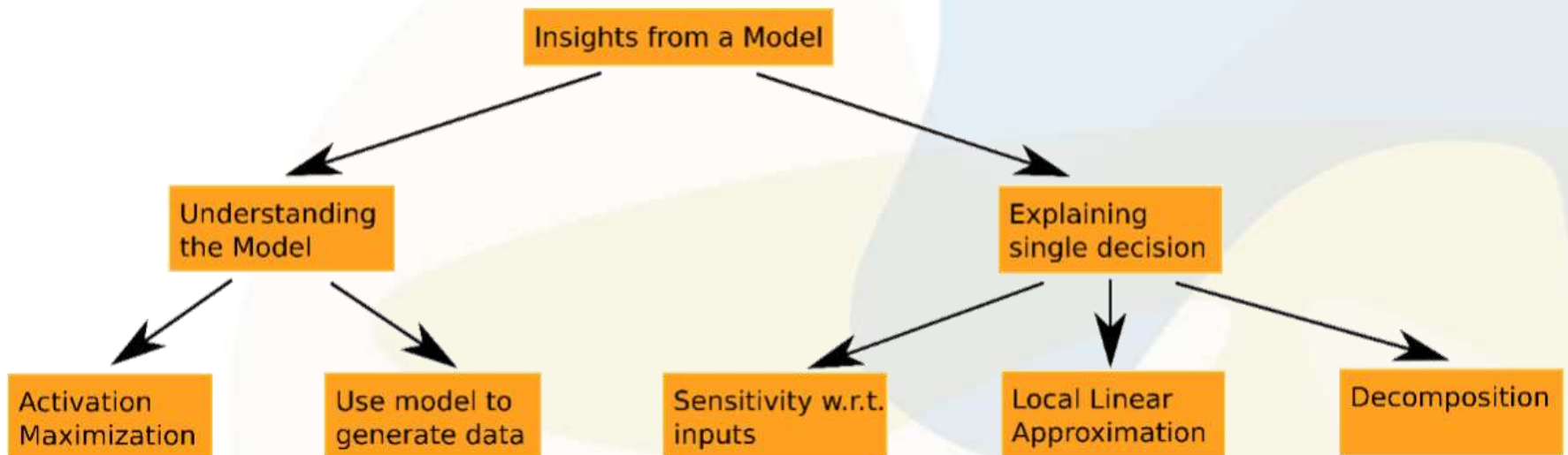


PASS



FAIL

Interpreting Predictions



Deconvolution
Guided Backprop
Saliency
Grad-CAM

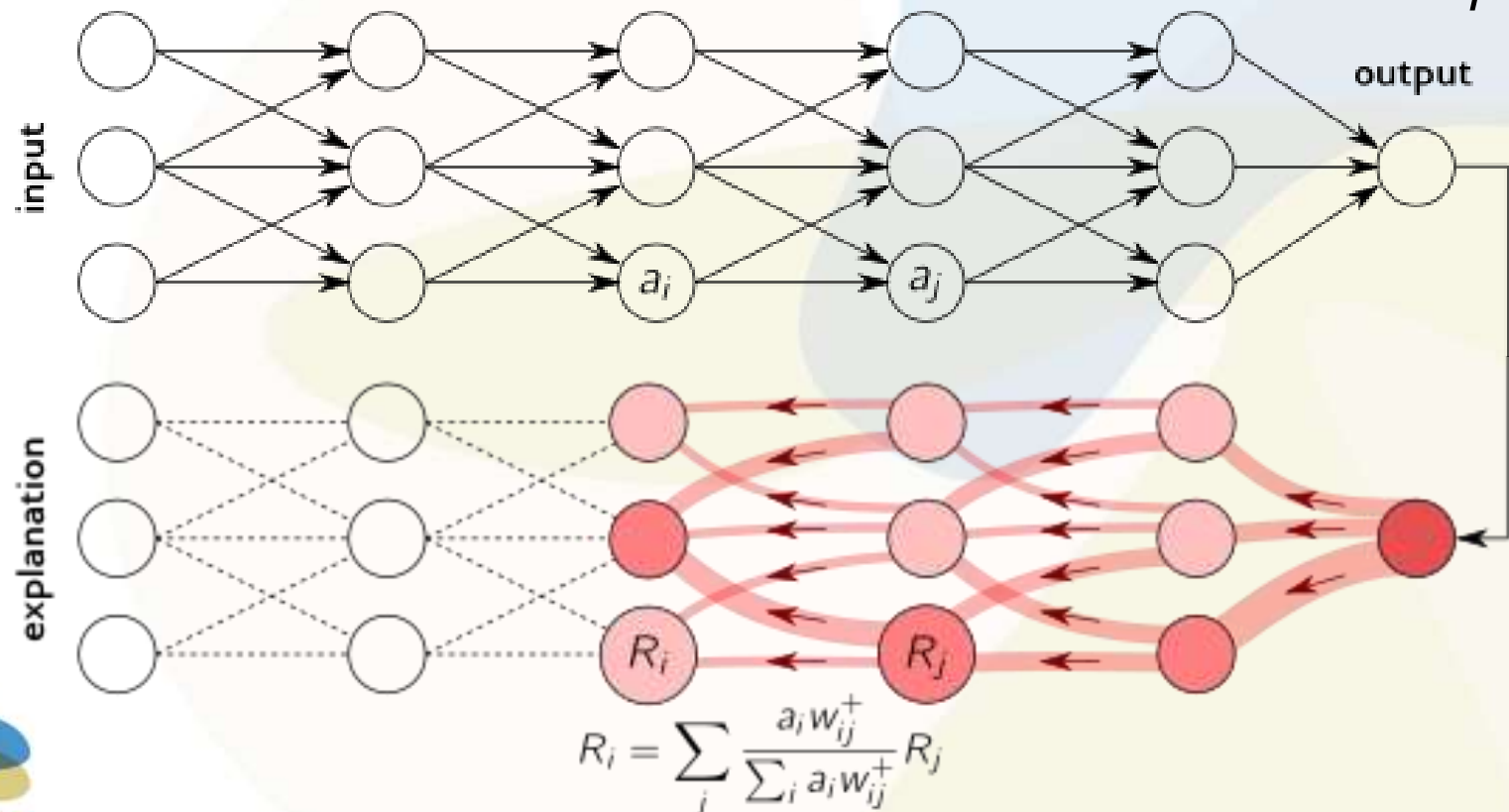
Negative Evidence



Layer-wise Relevance Propagation

$$R_i^l = \sum_j \left(\alpha \cdot \frac{(a_i \cdot w_{ij})^+}{\sum_i (a_i \cdot w_{ij})^+} + \beta \cdot \frac{(a_i \cdot w_{ij})^-}{\sum_i (a_i \cdot w_{ij})^-} \right) \cdot R_j^{l+1}$$

$$\alpha + \beta = 1$$



LRP

Conservation

$$\sum_p R_p^l = \sum_p R_p^{l+1}$$

Positivity

$$R_p > 0$$

Continuity

Small changes in input should produce small changes in relevance

Selectivity

Removing relevant features should decrease prediction accuracy

LIME

Local Interpretable Model-agnostic Explanations

$$\xi(x) = \operatorname{argmin}_{g \in G} L(f, g, \pi_x) + \Omega(g)$$

f : model

g : interpretable model version

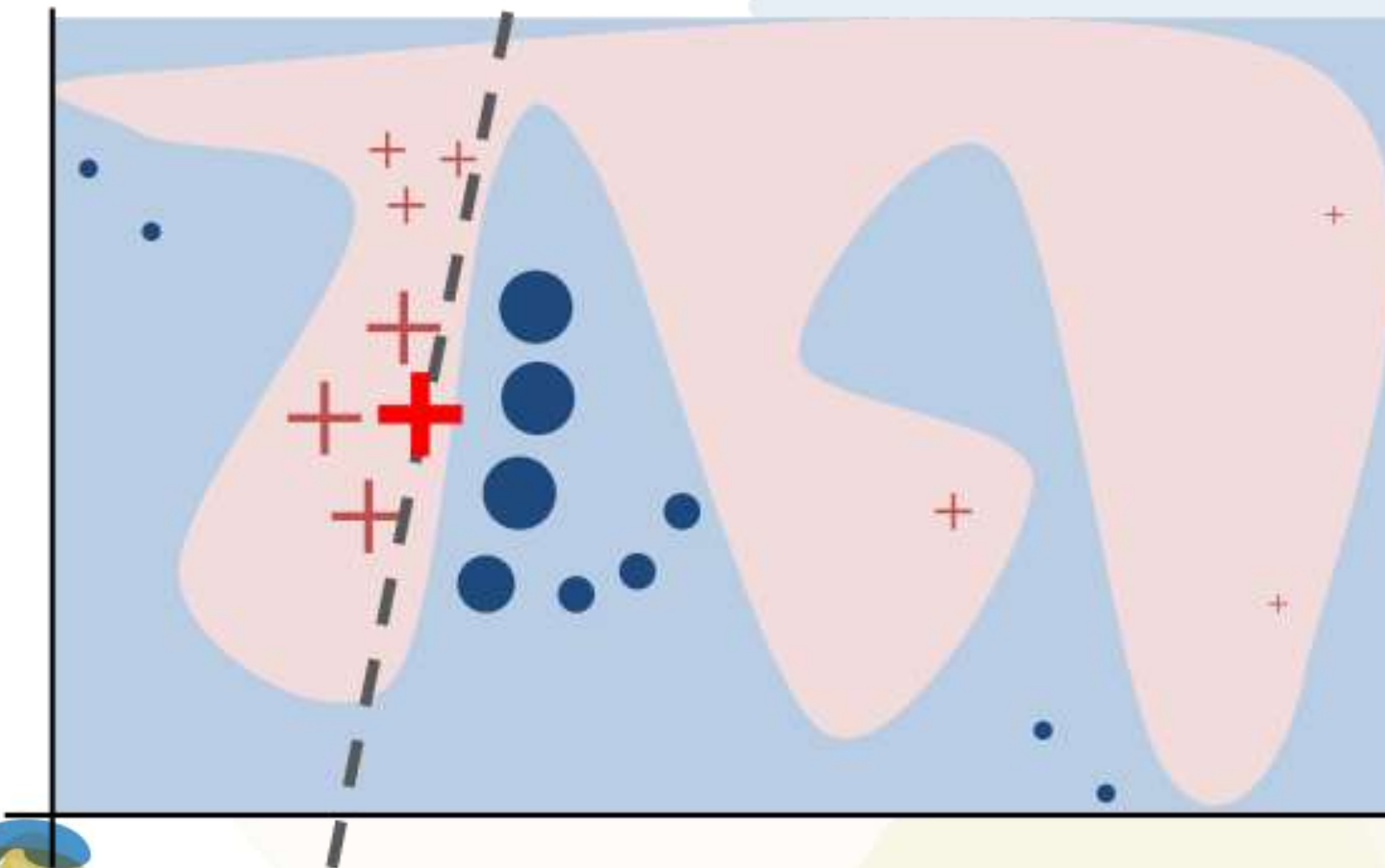
ξ : explanation

L : how bad g is at approximating real model f

π_x : proximity measure that determines what is “local”

Ω : complexity

LIME



LIME

$$\xi(x) = \operatorname{argmin}_{g \in G} L(f, g, \pi_x) + \Omega(g)$$

Ω : complexity, g : interpretable model, π_x : proximity, L : error

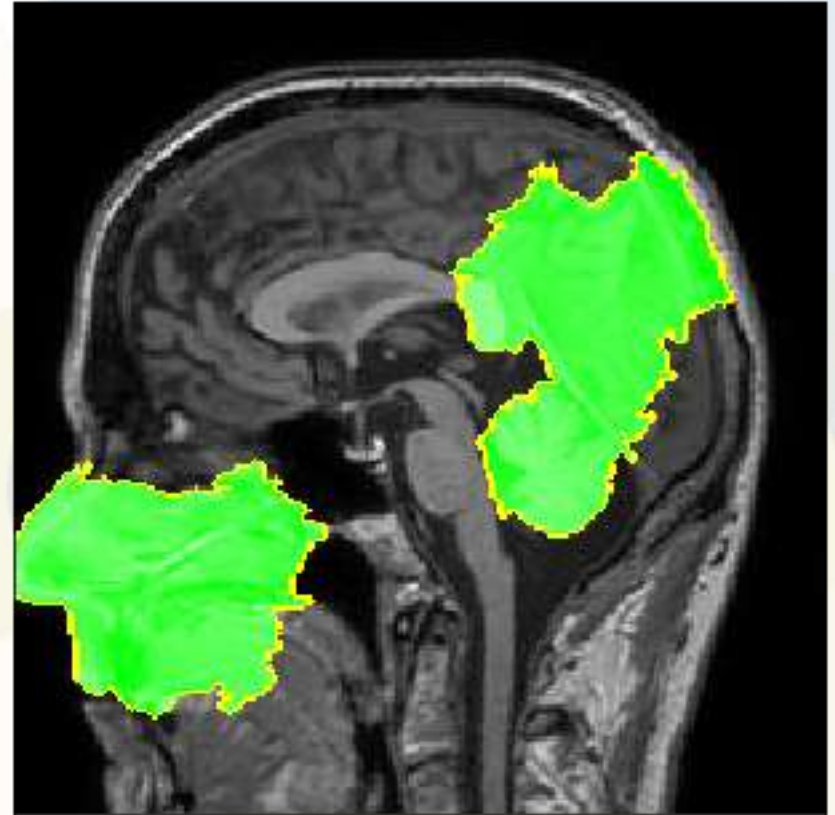
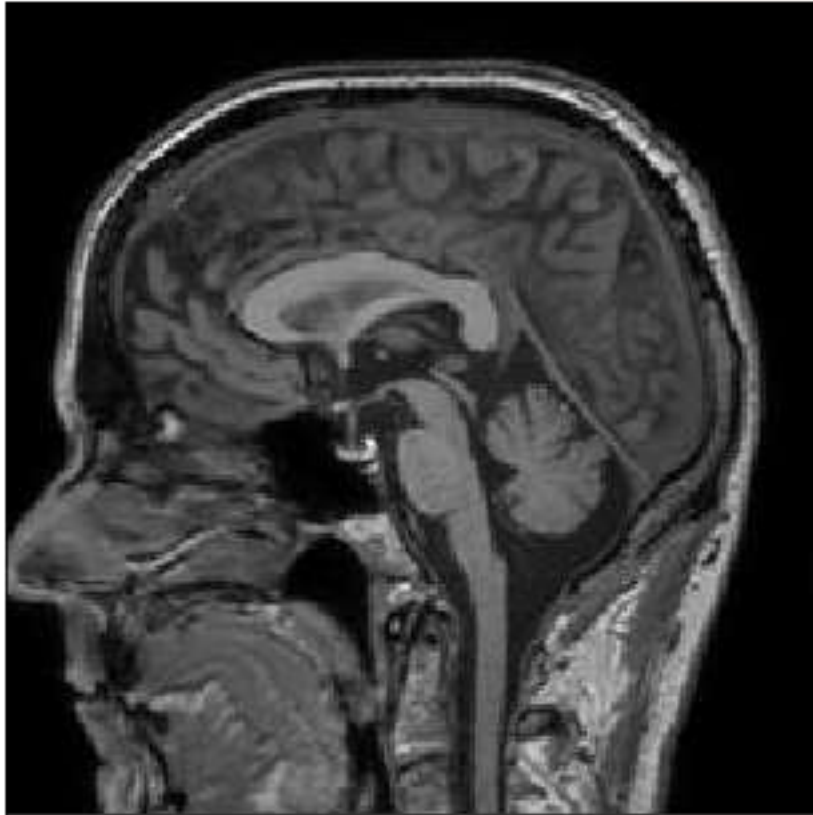
$$g(z') = w_g \cdot z' \quad \longleftarrow \text{Linear models}$$

$$\pi_x(z) = e^{\frac{-(x-z)^2}{\sigma^2}} \quad \longleftarrow \text{Negative exponential of Euclidean distance}$$

$$\Omega(g) \quad \longleftarrow \text{Choose } K \text{ features}$$

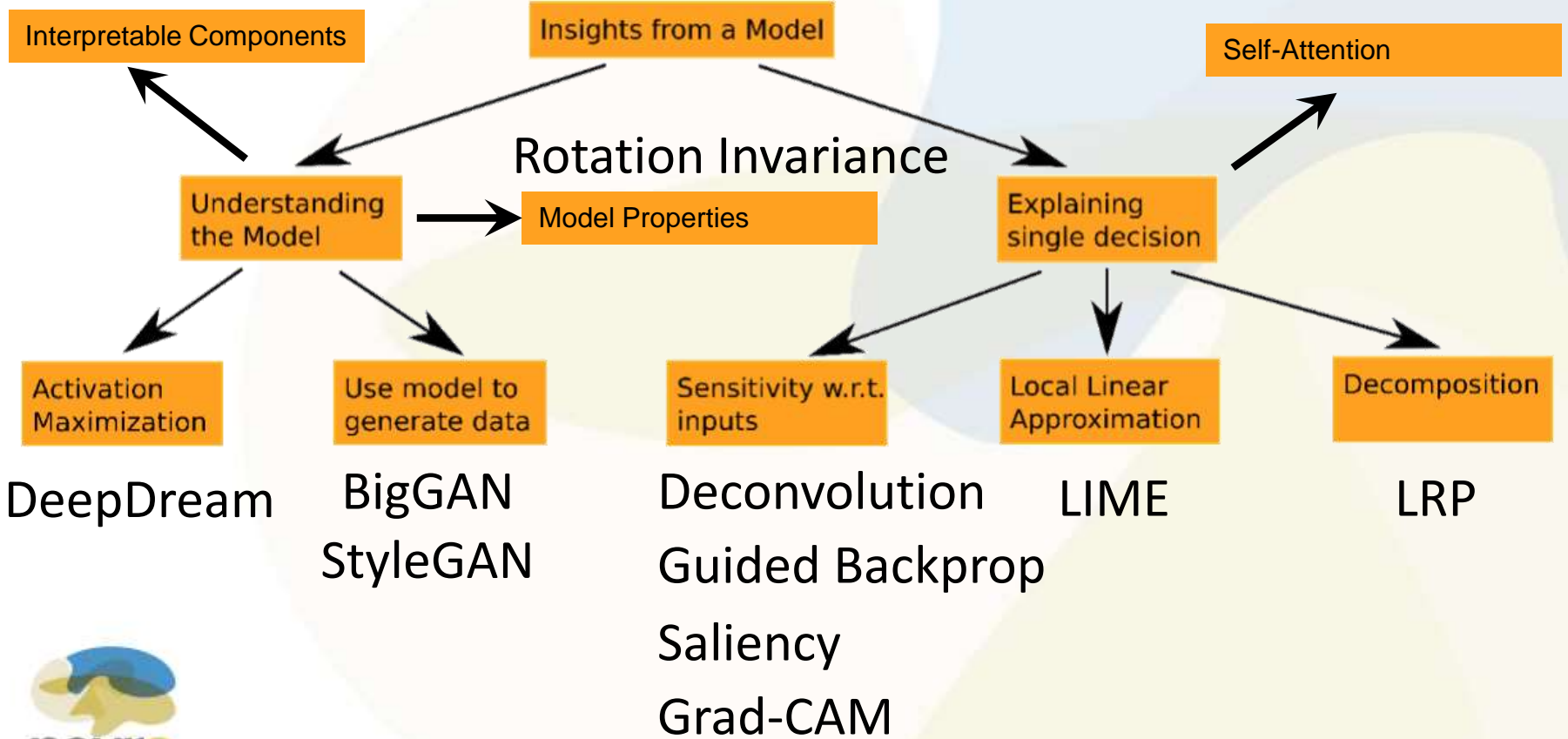
$$L(f, g, \pi_x) = \sum_{z, z' \in Z} \pi_x(z) \cdot (f(z) - g(z'))^2$$

Defacing Detector



Interpreting Predictions

Spatial Transformers



Interpretability

- Causality
- Transparency
- Simulatability
- Decomposability
- Algorithmic guarantees

Danger!

- LIME: <https://github.com/marcotcr/lime>
- Saliency / Grad-CAM:
<https://github.com/raghakot/keras-vis>
- StyleGAN: <https://github.com/NVlabs/stylegan>
- BigGAN:
https://colab.research.google.com/github/tensorflow/hub/blob/master/examples/colab/biggan_generation_with_tf_hub.ipynb

Interpretability

