

Calculus 1 Workbook

Functions



VERTICAL LINE TEST

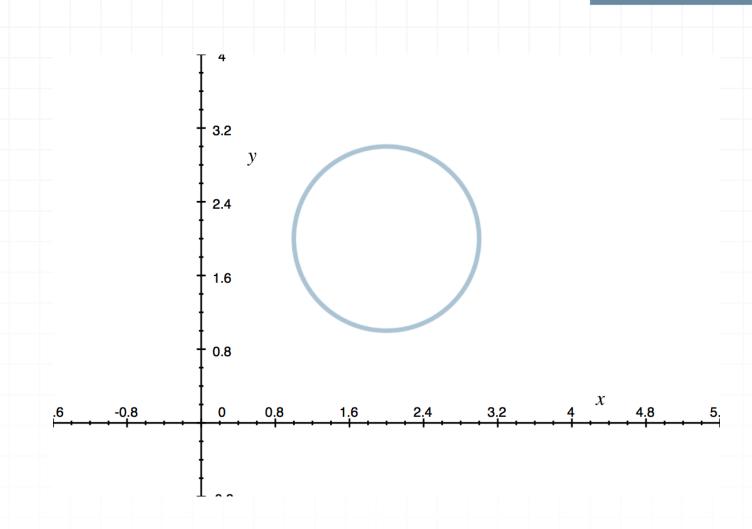
■ 1. Determine algebraically whether or not the equation represents a function.

$$(x-1)^2 + y = 3$$

■ 2. Fill in the blanks in the following statement using "equations," and "functions."

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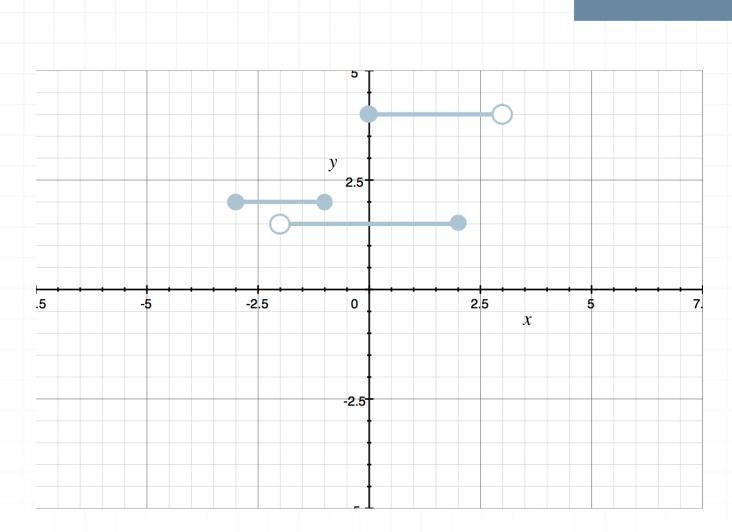
■ 3. Use the Vertical Line Test to determine whether or not the graph is the graph of a function.



■ 4. Determine algebraically whether or not the equation represents a function.

$$y^2 = x + 1$$

■ 5. Use the Vertical Line Test to determine whether or not the graph represents a function.



■ 6. Explain why the Vertical Line Test determines whether or not a graph represents a function.

■ 7. Fill in the blanks in the following statement using: equations, functions.

Not all ______ are _____.

■ 8. Determine algebraically whether or not the equation represents a function.

$$x^3 + y = 5$$

DOMAIN AND RANGE

 \blacksquare 1. Find the domain of f(x).

$$f(x) = \frac{3}{x(x+1)} + x^2$$

■ 2. Find the domain and range of the given set.

$$(-1, -3), (0,5), (-3,6), (0, -3)$$

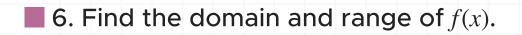
 \blacksquare 3. Find the domain and range of g(x).

$$g(x) = \frac{\sqrt{x-2}}{3}$$

■ 4. Find the domain and range of the function.

$$f(x) = \frac{2}{x} + 1$$

■ 5. Give an example of a function that has a domain of $[1,\infty)$.

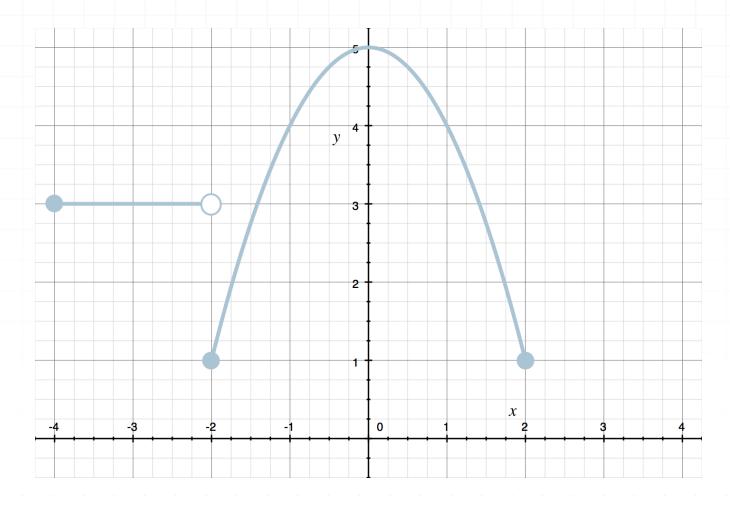


$$f(x) = \ln(x+3) + 5$$



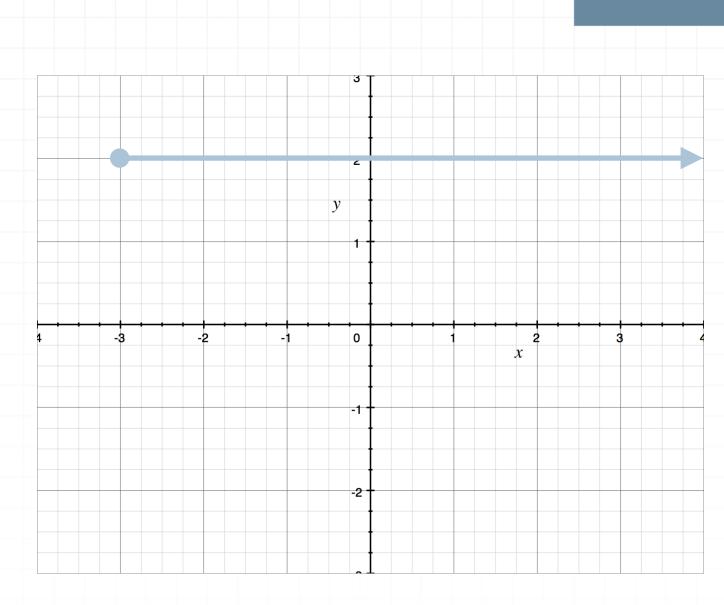
DOMAIN AND RANGE FROM A GRAPH

■ 1. What is the domain and range of the function? Assume the graph does not extend beyond the graph shown.



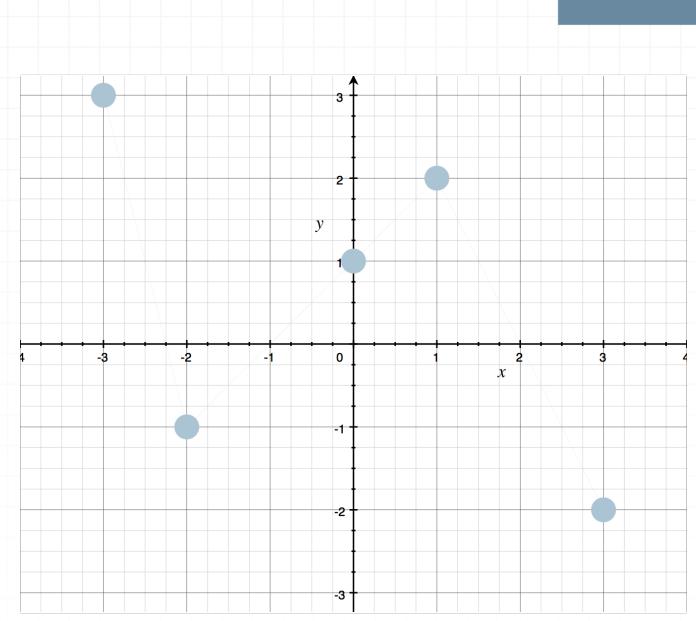
■ 2. What is the domain and range of the function?





■ 3. Determine the domain and range of the function.

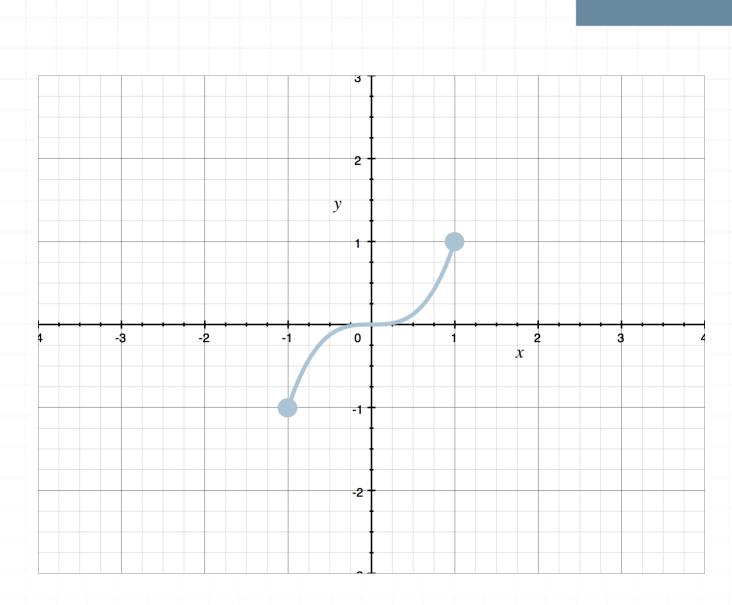




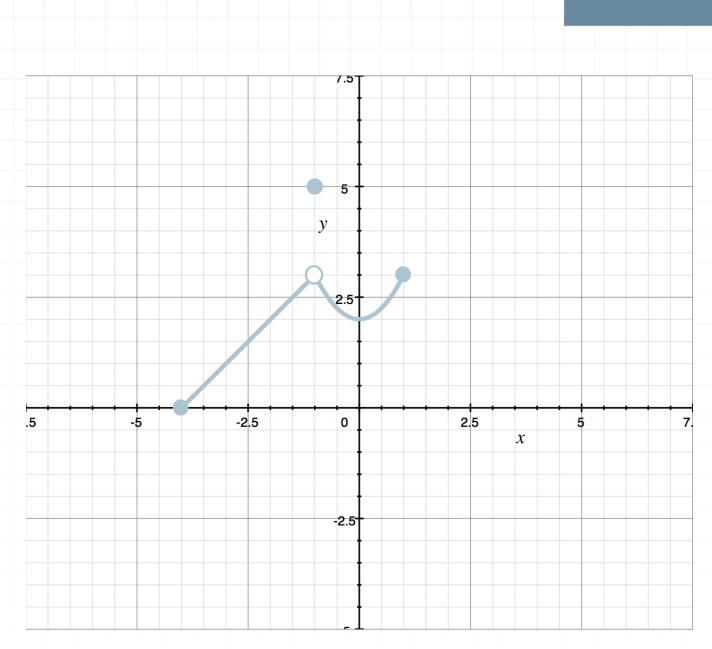
■ 4. Fill in the blanks in the following description of the domain of a graph.

"The domain is all the values of the graph from _____ to

■ 5. What is the domain and range of the function? Assume the graph does not extend beyond the graph shown.



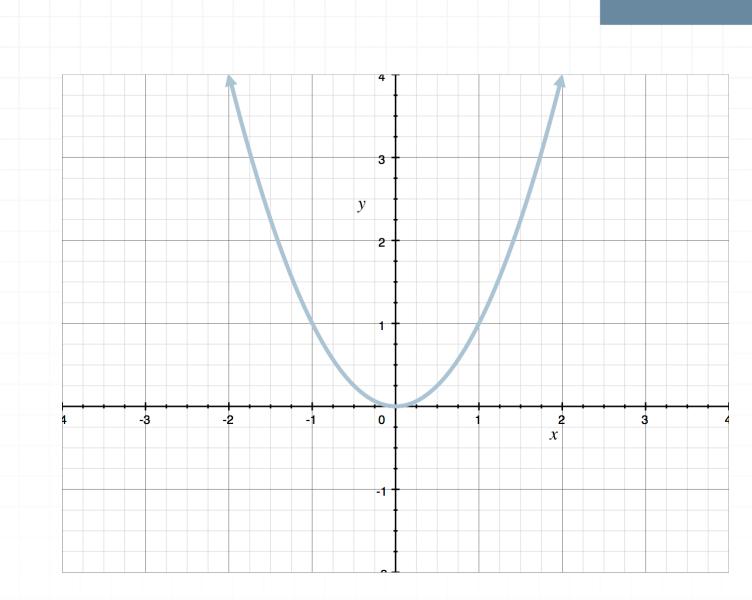
■ 6. What is the domain and range of the function? Assume the graph does not extend beyond the graph shown.



■ 7. Fill in the blanks in the following description of the range of a graph.

"The range is all the values of the graph from _____ to ."

■ 8. What is the domain and range of the function?



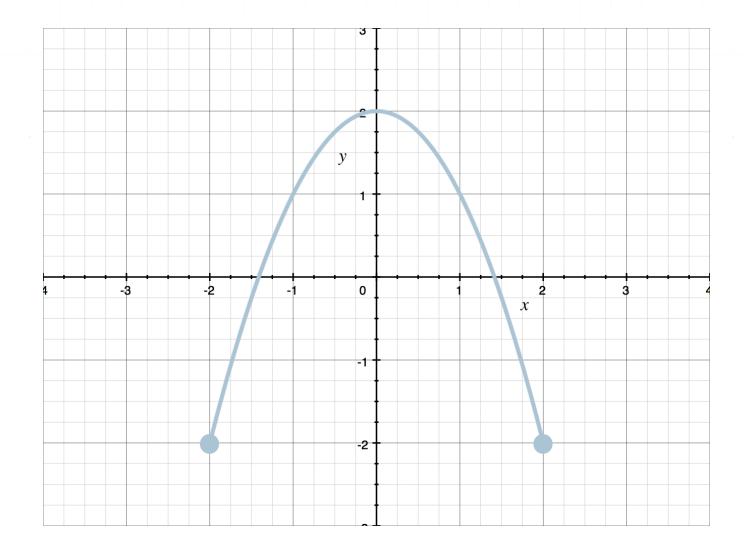


EVEN, ODD, OR NEITHER

■ 1. Is the function even, odd, or neither?

$$f(x) = -x^5 + 2x^2 - 1$$

- 2. Describe the symmetry of an even function, and give an example of an even function.
- 3. Determine if the graph is the graph of a function that is even, odd, or neither.





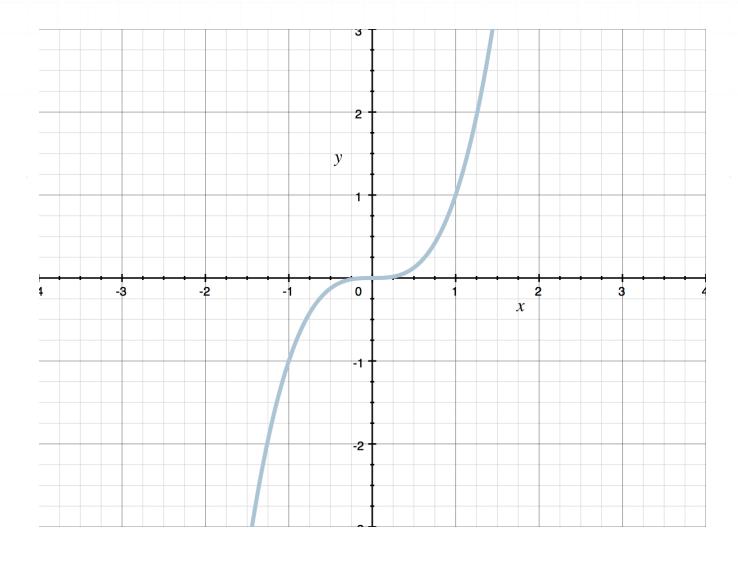
■ 4. Is the function even, odd, or neither?

$$g(x) = -3x^2 + 5x^6$$

■ 5. Show that the function is neither even nor odd.

$$f(x) = x^2 - 5x + 7$$

■ 6. Determine if the graph is the graph of a function that is even, odd, or neither.



■ 7. Is the function even, odd, or neither?

$$h(x) = x^3 - 3x$$

■ 8. Describe the symmetry of an odd function, and give an example of an odd function.



INDEPENDENT AND DEPENDENT VARIABLES

■ 1. In the following function, determine which variable is the independent variable and which is the dependent variable.

$$2y + 2 - x^2 = 3x^2 - 5 + y$$

- 2. Sarah drives at a constant speed of 30 mph. The time she drives is given by h = d/30, where d denotes the distance and h denotes the total number of hours she drove. Which variable is the independent variable? Explain your answer.
- \blacksquare 3. Give a definition for "independent variable" and give an example of an equation in which k is the independent variable.
- \blacksquare 4. Give an example of a function with independent variable t and dependent variable s.
- 5. Identify the independent variable(s) and dependent variable(s) in the following function.

$$x = a - b^2$$



- 6. You open a bag of chips and eat 11 of them. Let a be the number of chips remaining and b be the number of chips in the bag before you ate any. Identify the dependent and independent variables in the relationship between a and b.
- 7. You're buying candy bars and soda from the store. Each candy bar costs \$1, and each soda costs \$2. What is the dependent variable?
- 8. Each month, a cell phone bill is calculated using the total number of minutes used and the total number of text messages sent during that month. Which variable(s) is/are the independent variable(s)?
- 9. You make your bed and sweep the floor to earn some money around the house. Each time you make your bed, you earn \$5. Each time you sweep the floor, you earn \$3. What is/are the independent variable(s)?
- 10. Give a definition for "dependent variable" and an example of a function in which s is a dependent variable.



■ 11. Identify the independent variable(s) and dependent variable(s) in the following function.

$$T + 5 = 3x + y^2 - 4xy$$



