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Unifying inference and selection in singular causal explanation

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Abstract

Explaining why events occurred involves solving different information-processing problems: inferring what actually happened (causal inference) but also highlighting a subset of the causes that contributed to the outcome (causal selection). While past research has investigated causal inference and causal selection separately, we report results of an experiment (N=284) examining how people solve both problems jointly, as is the case in real-world explanation settings. We find evidence that participants infer the state of unobserved variables on the basis of available evidence, and observe common behavioral signatures of causal selection. However, explanation preferences deviate in important ways from the predictions of a computational model combining existing theories of causal inference and causal selection. In particular, participants were disproportionately likely to select inferred over observed variables. We suggest a possible preference for producing explanations that allow the explainee to benefit from inferential work performed by the explainer.

Keywords: causality; counterfactuals; explanation; inference

Introduction

Why did this car accident happen? Why did the dinosaurs go extinct? The drive to explain why a particular event happened is a core feature of human psychology, and a common topic of discussion and debate. In the field of causal cognition, this problem of *singular causal explanation* has received a large amount of attention (Lombrozo, 2006; Woodward, 2021; Lagnado, 2021). Providing a causal explanation typically involves solving several different information-processing problems. In this paper we focus on two of the most important:

-Causal inference: using one's causal beliefs to figure out what happened on the basis of the available evidence. For example, given the driver was coming back from a party, how likely is it he was drunk? Given it was winter in Canada, how likely is it there was ice on the road?

-Causal selection: highlighting one cause out of the several causes that contributed to an outcome (Hesslow, 1988; Quillien & Lucas, 2023). Suppose we know the driver was drunk, that there was ice on the road, and that both factors contributed to the accident. Which fact will we spotlight as *the* cause of the accident?

It is easy to see that both problems are crucial to causal explanation in everyday settings. The details of what happened are rarely all transparently observable, so someone looking for an explanation typically needs to piece them together from

the available evidence. In the real world, any given outcome is the end result of a complex interaction of many variables, so selection is necessary to avoid producing unhelpfully detailed explanations. In the literature, these problems have almost exclusively been studied separately. In this paper we study how people give causal explanations when they have to jointly solve both problems.

We sketch a computational framework for causal explanation in the presence of unobserved variables, and report results of an experiment testing the predictions of this model.

Background

Inference and selection in singular causal reasoning

A large literature has explored how people make inferences about whether an event happened, on the basis of information about other events that happened. In a setting where events are causally related to each other, this is a problem of causal inference, and it can be solved using the formalism of causal graphical models (Pearl, 2009). Many experiments have found that people make inferences in ways that approximate the normative prescriptions of causal models (Sloman & Lagnado, 2004; Hagmayer et al., 2007; Lagnado, 2021; Meder & Mayrhofer, 2017), although with noteworthy deviations (Davis & Rehder, 2020).

In our experiment, we focus on diagnostically inferring the value of a potential cause, after observing the effect as well as other potential causes occurring (see Pearl, 2009, for a detailed treatment of inference in causal graphical models). For example, suppose that event *C* often causes event *E*, we observe that *E* happens, and we want to infer the probability that *C* happened. We can solve this problem using Bayes' rule:

$$P(C|E) = \frac{P(E|C)P(C)}{P(E)} \quad (1)$$

where the likelihood $P(E|C)$ depends on the parameters of the causal model describing the causal system.

In contrast, research on causal selection investigates how people judge which of the factors that contributed to an outcome is the most important cause (Hesslow, 1988). For example, although the driver being drunk and the roads being icy both contributed to the accident, it is illegal to drive drunk and very often icy in winter in Canada, making the drunk driving

a better explanation as *the* cause of the accident. For simplicity, extant research on causal selection has used experimental settings where the reasoner already knows what happened. Because of this, not much is known about causal selection in contexts where people also need to make inferences about what happened.

In this paper, we study causal explanation in a context where some events are unobserved. For example, a contestant passes a cookery test if they complete either a main meal or a dessert in time, provided the judge also likes the completed dish. We can see that the contestant completed both dishes and won the show, but we don't know which dish(es) impressed the judge. Why do participants think the contestant won? This task requires causal selection (because there are four potential causes) as well as inference (because two of them are unobserved). In the next section we outline a computational framework for causal explanation in this setting.

Computational framework

We assume that the reasoner knows the causal structure of the relevant system, and we make use of the formalism of Structural Causal Models, in which *variables* represent whether a given event occurs (for example $C = 1$ means that event C happened), and *structural equations* describe the causal relationships between variables (see Pearl, 2009, for details).

We consider a causal system where two variables A and B can have a causal influence on outcome variable E . For each cause variable X there is an associated unobserved variable X_u that determines whether X can have an effect on E . Figure 1 shows a graphical model of such a causal system. We study a disjunctive and a conjunctive structure. In the disjunctive structure, E happens if either both A and A_u happen or both B and B_u happen:

$$E := (A \wedge A_u) \vee (B \wedge B_u) \quad (2)$$

In the conjunctive structure E happens if all variables happen:

$$E := (A \wedge A_u) \wedge (B \wedge B_u) \quad (3)$$

While the values of A and B are observed, the values of A_u and B_u are not. To give a causal explanation for why E happened, the reasoner must i) infer the value of A_u and B_u , ii) engage in causal selection, iii) integrate the two processes. We discuss each component in turn.

Causal inference

We assume the reasoner infers the values of A_u and B_u using Bayes' rule:

$$P(A_u, B_u | A, B, E) = \frac{P(E | A_u, B_u, A, B) P(A_u, B_u)}{P(E | A, B)} \quad (4)$$

Causal selection

According to an increasingly popular family of accounts, people engage in causal selection by imagining counterfactual

possibilities (Icard et al., 2017; Quillien, 2020; Henne et al., 2019), see also Gerstenberg et al. (2021). We use a recent computational model of causal selection based on this idea.

The *Counterfactual Effect Size Model* (CES; Quillien, 2020; Quillien & Lucas, 2023) holds that people judge whether event C was a cause of event E by: i) simulating many different alternative ways the situation could have happened ii) computing a measure of the dependence between C and E across these possibilities.

Each counterfactual possibility is simulated by sampling each cause variable from a probability distribution, and then setting the effect variables according to their structural equations. Each cause variable V is sampled from the probability distribution $s\delta(V) + (1-s)P(V)$, where $\delta(V)$ is the value of V in the actual world, $P(V)$ is the prior probability of V , and s is a 'stability' parameter. We set $s = .7$ on the basis of past empirical data (Lucas & Kemp, 2015; Quillien & Lucas, 2023).

The CES score of C for E is then computed on the basis of the simulated possibilities. In our setting, it is equivalent to the Pearson correlation coefficient between C and E across the simulated counterfactual possibilities.

The CES model has successfully explained data from past experiments on causal judgments (Lagnado et al., 2013; Gerstenberg & Icard, 2020; Icard et al., 2017; Morris et al., 2019; O'Neill et al., 2024). For example, it can explain the phenomenon of *abnormal inflation*, whereby people tend to select causes that are abnormal (i.e. infrequent or norm-violating). The model can also explain *abnormal deflation*, the tendency to select normal causes when the outcome was over-determined — i.e. when either cause would have been sufficient to produce the outcome (Icard et al., 2017). The model also made successful new predictions, both in simple experimental settings (Quillien & Lucas, 2023; Konuk et al., 2023) and in a real-world context (Quillien & Barlev, 2022). However, to our knowledge it has not been tested in settings like ours where the state of some variables is unobserved.

Causal explanation with unobserved variables

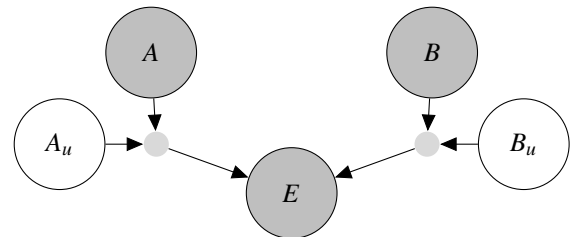


Figure 1: Graphical representation of our causal structure. Grey nodes (A, B, E) denote observed variables; white nodes (A_u, B_u) denote unobserved variables.

We now offer a model of causal judgment that integrates the two components above. Our goal is to assign an overall causal score $C(X = x)$ to each event, such that an event with a higher causal score is a better candidate to be a causal explanation. For convenience we will denote the posterior distri-

bution in abbreviated form as $P(A_u, B_u | A, B, E) = P_\alpha(A_u, B_u)$. It will also be useful to define $K(X = x)$ as the CES score of event $X = x$. We will also write $K(X = x | \mathbf{V} = \mathbf{v})$ to express the CES score that would be assigned to $X = x$ under the assumption that $\mathbf{V} = \mathbf{v}$ in the actual world (this is useful notation when we need to consider several possible hypotheses about the actual world consistent with our observations).

The CES model is defined for situations where we already know the full state of the world. To apply it to the present case (where this assumption doesn't hold), we must make some choices as to how to handle the uncertainty over A_u and B_u .

One intuitive way to do this is to compute a CES score for each possible state of the actual world compatible with what we know, and then compute a weighted average of these scores, where the weights are the probabilities of the states of the world. For example to compute the CES score for $A = a$, denoted $K(A = a)$, we compute:

$$K(A = a) = \sum_{A_u, B_u} K(A = a | A = a, B = b, A_u, B_u) P_\alpha(A_u, B_u) \quad (5)$$

where a and b are the actual-world values of A and B , and $K(X = x | \mathbf{V} = \mathbf{v})$ is the CES score we would compute for $X = x$ if we knew that the actual-world values of \mathbf{V} were \mathbf{v} .

Computing the CES score for the unobserved variables introduces one additional complication: we typically don't know whether the variable has value 1 or 0. One intuition is that people will tend to say ' $A_u = 1$ caused the outcome' if i) it is in fact likely that $A_u = 1$ in the actual world, ii) $A_u = 1$ has a high CES score. One way to implement this is to compute C by multiplying the CES score K by the posterior probability of the variable value. For example for $A_u = 1$:

$$C(A_u = 1) = K(A_u = 1) P_\alpha(A_u = 1) \quad (6)$$

$$= \sum_{B_u} K(A_u = 1 | A = a, B = b, A_u = 1, B_u) \times P_\alpha(B_u | A_u = 1) P_\alpha(A_u = 1) \quad (7)$$

$$= \sum_{B_u} K(A_u = 1 | A = a, B = b, A_u = 1, B_u) \times P_\alpha(A_u = 1, B_u) \quad (8)$$

Actual causation

In addition to causal selection, people also engage in a more categorical kind of causal judgment, differentiating between variables that had at least some contribution to an outcome and those that did not contribute at all. In our computational model we use a simple heuristic to exclude events that do not qualify as actual causes. Specifically, we assign a causal score of $C(X) = 0$ to any variable X whose value does not match the value of the outcome (e.g., if $E = 1$, then $B = 0$ is not an actual cause of E) and to unobserved variables if their observed counterpart has value 0 (e.g., if $A = 0$, $C(A_u \in 0, 1) = 0$). More sophisticated computational accounts of categorical actual causation exist (Halpern, 2016).

General mathematical framework

Here we give a more general formalization of our proposal, generalizing from the examples above. We consider whether variable realization $X = x$ was the cause of outcome $E = e$. We denote \mathbf{V} the set of variables other than E and X . The CES score K of $X = x$ is computed by i) assuming $X = x$ in the actual world, and ii) marginalizing across all possible values of the other variables, weighted by their posterior probabilities:

$$K(X = x) = \sum_{\mathbf{v} \in \mathbf{V}} K(X = x | \mathbf{V} = \mathbf{v}, X = x) P_\alpha(\mathbf{v} | X = x) \quad (9)$$

The overall causal score $C(X = x)$ is then computed by weighing K by the posterior probability of $X = x$. We also check for actual causation. Formally:

$$C(X = x) = K(X = x) P_\alpha(X = x) T(X = x) \quad (10)$$

where $T(X = x)$ is 1 if $X = x$ is an actual cause of E , and 0 otherwise.

Softmax choice model

The sections above specify how the model assigns causal scores to variables. To convert these causal scores to predicted choice proportions, we assume that participants are soft-maxing over the causal scores:

$$P(\text{choice} = X) \propto \exp\left(\frac{C(X)}{\tau}\right) \quad (11)$$

where τ is a temperature parameter (higher values indicate more stochasticity) that we fit to the data.

Lesioned models

We will also explore 'lesioned' models to assess our claim that when people make a causal judgment, they engage both in inference (about the value of unobserved causes) and in causal selection.

Lesioning inference Our first lesioned model lesions the inference module. That is, we have $P_\alpha(A_u, B_u) = P(A_u, B_u)$. In words, instead of setting $P_\alpha(A_u, B_u)$ to be the posterior, we 'freeze' it as the prior distribution. The model otherwise works exactly as above.

Lesioning causal selection The second model lesions the causal selection module. We assume that people do not engage in counterfactual simulation when making causal judgments. Once they determine which variables are actual causes of E , they select these variables simply in function of their posterior probabilities. In terms of the mathematical framework defined above, we replace all CES scores K by 1.

Lesioning both inference and selection This model assumes that people select among actual causes almost indiscriminately. That is, they assign a causal score of $C = 1$ to observed variable values, and a causal score of $C = P(X_u = x_u)$ to unobserved variables, where $P(X_u = x_u)$ is the prior probability of that variable.

Lesioning actual causation We will also test variants of the models defined above that do not check if an event is an actual cause of the outcome.

Methods

We conducted a behavioral experiment to test our models. You can see it [here](#) (at quiz, select: Yes, No, True, 12).

Design

We investigated how participants select causes in scenarios containing four binary causes: two observed variables A and B , and latent success rates A_u and B_u , where the variables are grouped in two pairs as in Figure 1. We asked each participant to give causal explanations for variable E 's occurrence or non-occurrence across the 12 different logically possible combinations of observed variables and effect E ('worlds').¹ Each trial presented the underlying causal structure as a simple story, including prior probabilities for all four variables, along with a simplified graphical representation of what happens in general. Then participants were shown a concrete state of observed variables ('what happened *this time*'), and were asked to explain outcome E by selecting one of the eight possible variable values ($4 \times \{0, 1\}$); Figure 2. (Of the eight, two are always incoherent — the values the observed variables did not take — and so are excluded from analysis).

The structure of the causal system was presented verbally as a vignette. We used three cover stories: 1) a cookery TV show (loosely based on Zultan et al. (2012)), 2) a university reading group and 3) a job interview. For each trial, one probability set and one cover story ('cookery show', 'reading group', or 'job interview') was randomly selected. Our analyses collapse across cover stories. The prior probabilities were manipulated across three settings.

Table 1: Event probability manipulation: Three settings

	Setting 1	Setting 2	Setting 3
$P(A = 1)$.1	.5	.1
$P(A_u = 1)$.5	.1	.7
$P(B = 1)$.8	.5	.8
$P(B_u = 1)$.5	.8	.5

Participants

We recruited 284 fluent-English participants (125 female, 1 other, age Mean \pm sd 36.8 ± 12.4 , range 18-78) using the Prolific subject pool. They were paid £2.50 and the experiment took Mean \pm sd 17.7 ± 7.8 minutes.

Stimuli

Each trial was a series of text and pictures following the same format, created using JSPsych 6.3.1 html plugins (De Leeuw,

¹Five worlds involve the conjunctive structure defined in Equation 3, and seven involve the disjunctive structure defined in Equation 2. Unequal split is due to the fact some events are possible for the disjunctive but not conjunctive structure (e.g., $A = 1$, $B = 0$, $E = 1$).

2015). The general schema presented the base rates at which all four events usually happen, and the causal setup of the world (i.e. whether conjunctive — both events needed for the outcome to occur, or disjunctive — just one), and then gave the value of the observed variables *this time*. See Figure 2 for an example of the cookery show for a disjunctive setting where $A = 0$, $B = 1$, $E = 1$. Finally participants selected one among all eight possible explanations (e.g., in the example shown in Figure 2, plausible explanations may include 'The chef completed the dessert' ($B = 1$), 'The dessert impressed the panel' ($B_u = 1$), etc).

Procedure

The experiment was implemented in JavaScript, hosted on Prolific and participants completed it in the browser on their own devices. After calibrating their computer screen, they were presented with the study's information sheet and consent form. Participants were then given instructions for completing the experiment and shown examples of the stimuli. They then completed a four-item quiz to test their understanding before beginning the experiment. All participants saw all 12 worlds one by one in a random order. The left/right presentation position on screen of the variables and their prior probabilities was counterbalanced between participants.

Analysis

Data were analysed using R version 4.1. Package *lme4* (Bates et al., 2014) was used for mixed effects regression models following recommendations of Meteyard & Davies (2020), via package *lmerTest* (Kuznetsova et al., 2017) for tests. The Data and the R code for modeling and analysis are available in our Repository.

We excluded from analyses those values of variables A and B which were inconsistent with their observed values, as these cannot be selected by the model (e.g., $A = 1$ is incoherent when $A = 0$). This resulted in discarding 1.4% of participant responses.

Results

Figure 3 shows the choice proportions of participants and our full computational model. Firstly, people's judgments are clearly non-uniform across the worlds (all item-level goodness-of-fit $\chi^2 > 137$, $df = 7$, $p < 1.85e - 26^{***}$ for all 36 probability setting/world combinations). Secondly, people choose actual causes over non-actual (on 88.2% of trials, $\chi^2 = 1993$, $p < .001^{***}$); non-actual are the gray error bars in Figure 3. Thirdly, they choose unobserved variables over observed 61.2% of the time ($\chi^2 = 170.4$, $p < .001^{***}$, see Figure 4 and subsection below).

Abnormal inflation as evidence for causal selection

Of special interest is whether participants' judgments exhibit the signature patterns of causal selection documented in past work (Morris et al., 2019). Human causal selection typically exhibits an effect called *abnormal inflation*, whereby people attribute greater causal responsibility to causes that are

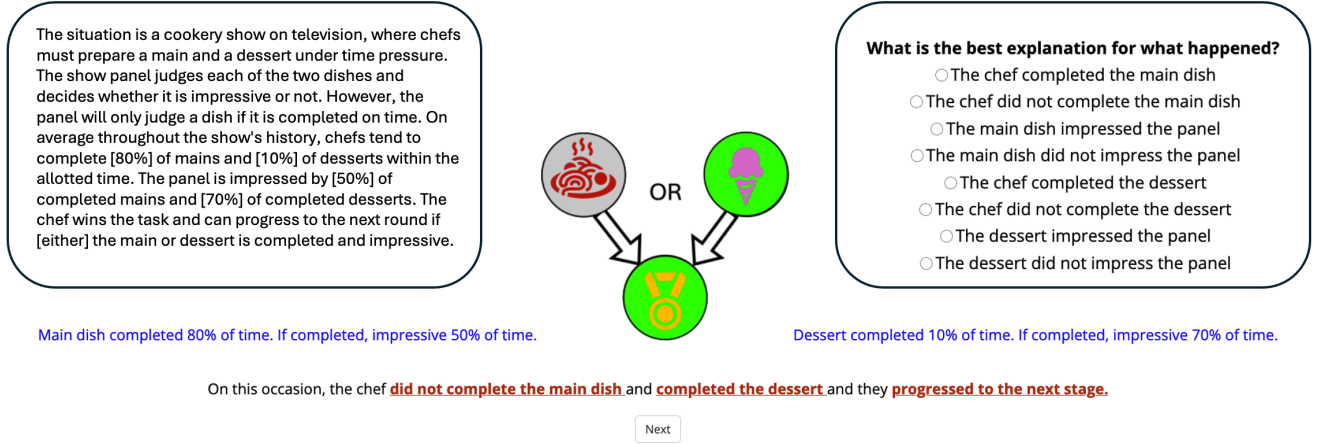


Figure 2: Simplified schematic of one trial: blue text gives base rates; grey/red text and graph describe what happened this time.

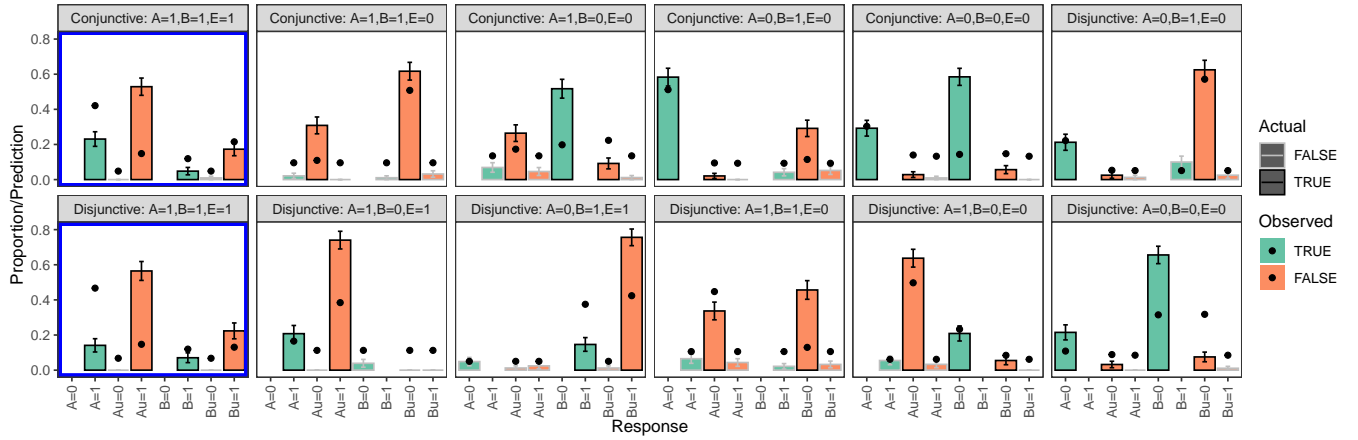


Figure 3: Results in Setting 3 $P(A) = .1, P(A_u) = .7, P(B) = .8, P(B_u) = .5$. Participants (bars) plus *Full* model with fitted τ (black circles). Blue highlights for canonical “everything happened” world ($A = 1, B = 1, E = 1$), expanded in Figure 4. See Repository for plots of the other probability settings.

rare, infrequent or otherwise abnormal (Gerstenberg & Icard, 2020; Icard et al., 2017). In this analysis we focus on trials where $A = 1, B = 1, E = 1$ in both the conjunctive and disjunctive structure, because these are the trials that are closer to those investigated in past work on causal selection. In these trials, the CES model predicts abnormal inflation.²

To test whether participants reliably choose the abnormal variable, we ran a logistic mixed-effect regression predicting selection of the abnormal observed variable with random intercepts for condition and participant, on settings 1 and 3, where the two observed variables A and B have different probabilities. This shows a significant difference in the expected

direction (odds ratio, estimate = .396, se = .349, CI [.204 .768], $Z = -2.74, p < .01^{**}$).

This result suggests that our experiment engaged some of the same cognitive mechanisms as other causal selection tasks. Since the abnormal inflation effect is predicted by a counterfactual model, the effect provides some evidence that this process of causal selection involved counterfactual reasoning.

Unobserved vs observed variables

Participants could select an observed or unobserved event in their explanation. For example, they can say that the reading group was successful because the lecturer attended (an observed event), or because (presumably) the lecturer talked about the paper (an unobserved event that can be inferred from the available evidence). We find that participants i) preferred to select unobserved relative to observed events on average, ii) selected unobserved events to a larger extent than

²Note the prediction for the disjunctive case contrasts with previous research which found *abnormal deflation* (a preference for the most normal variable) in disjunctive structures (Gerstenberg & Icard, 2020; Icard et al., 2017). However, our disjunctive structure is more complex than in previous research, consisting of a disjunction of conjunctions (Eq. 2). The CES model predicts abnormal inflation in this structure.

predicted by our main computational model, see Figure 4.

To test this effect, we sampled an explanation from the model for each participant observation. We ran a binomial logistic mixed-effect regression predicting ‘answer unobserved’ with a fixed effect for group (participant v model), and random effects for condition and participant. We found a main effect of group (odds ratios, estimate = 1.50, se = .052, CI [1.34 1.64], $Z = 7.58$, $p < .001^{***}$), whereby unobserved variables were cited more often by participants than by the model. We discuss this finding in the Discussion.

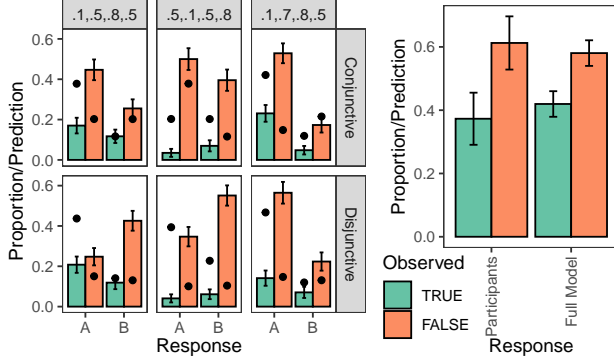


Figure 4: Left: Comparing $A = 1$, $B = 1$, $E = 1$ scenarios across probability settings 1-3 and conjunctive vs disjunctive structures. Upper facet labels show the probability of A , A_u , B and B_u in that order. Settings 1 and 3 show abnormal inflation in both structures for observed variables. Right: Overall propensity to select observed vs unobserved variables ($M \pm SE$ across worlds). Participants cite a larger proportion of unobserved variables than the full model.

Model fit

We fit the models to the 98.6% coherent data by minimising negative log likelihood, with the softmax temperature parameter τ as a free parameter, optimised with Brent method as implemented by R’s `optim` function. See Table 2 for the model fits. The full model (containing the three modules of causal selection, inference and actual causation) fit well, but was beaten by the model lesioned to have no causal selection. The item-level Pearson correlation coefficient between the full model and participants’ average judgments was $r(286) = .74$, $p < .001^{***}$, and between the best-fitting causal-selection-lesioned model and participants’ average judgments was $r(286) = .78$, $p < .001^{***}$.

The fact that lesioning the causal selection module improves the fit of the model is surprising given the presence of abnormal inflation in participants’ judgments, an effect predicted by our causal selection model. This poor performance can be explained by the fact that the causal selection module tends to assign high causal responsibility to observed variables in situations where participants actually prefer unobserved variables. It also makes wrong predictions in many cases where the outcome does not happen ($E = 0$). In sum,

Model	τ	LogL	BIC
full	.299	-5112	10233
noActual	.341	-5075	10157
noInference	.310	-5442	10892
noSelection	.366	-4257	8522
noActnoInf	.337	-5202	10412
noActnoSelect	.342	-4675	9359
noInfnoSelect	.534	-5083	10174
noActnoInfnoSelect	.761	-5743	11494

Table 2: Temperature parameter τ and model performance metrics LogL and BIC.

while we have some evidence that participants are engaged in causal selection (they are not simply selecting randomly among observed causes of the outcome), our model does not fully capture how they do so.

In contrast, lesioning the causal inference module resulted in a worse fit (see Table 2). This result suggests that participants make approximately sound inferences about the probability that an unobserved event happened, and leveraged these inferences in their causal explanations.

Discussion

Causal explanation is a complex cognitive activity that requires solving multiple sub-problems. Research on causal cognition has typically focused on one sub-problem at a time: some experiments focus on causal inference while other experiments focus on causal selection. This strategy has been fruitful, but has also led to a neglect of the study of the general problem of causal explanation where both problems are in play, as is typically the case in the real world. Here we considered how reasoners give causal explanations in a setting where some events are unobserved, such that reasoners need to engage in both causal inference and causal selection. First, we sketched a computational framework for how these two processes might be integrated by the mind. Then we reported the results of an experiment testing how people give causal explanations in this setting.

Our experimental data suggests people engage in inference and selection in a way that is partially predicted by existing theories of these processes. We also uncover phenomena not predicted by our computational framework: in particular that people prefer to explain an outcome by citing an unobserved event, rather than an observed event, and that this preference is stronger than predicted by our model. We speculate this finding reflects the fact the explainer had to perform some computational work to infer whether the unobserved event happened. Offering this explanation spares the explaineer this work, a form of computational kindness (Christian & Griffiths, 2016). Exploring this hypothesis is a fruitful direction for future research.

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