

## Recursion – Q1 (rSumUp)

A function **rSumUp()** is defined as

$$\text{rSumUp}(1) = 1$$
$$\text{rSumUp}(n) = n + \text{rSumUp}(n-1) \quad \text{if } n > 1$$

(1) Write a **recursive** function, **rSumUp()**, where the function prototype is:

**int rSumUp1(int n);**

(2) Write another version of the function using call by reference:

**void rSumUp2(int n, int \*result);**

Enter a number: **4**

rSumUp1(): 10

rSumUp2(): 10

Enter a number: **67**

rSumUp1(): 2278

rSumUp2(): 2278

### Note:

The mathematical recursive definition is given in this problem. It is quite natural to implement this function using recursive approach.

## Recursion – Q1 (rSumUp)

```
#include <stdio.h>
int rSumUp1(int n);
void rSumUp2(int n, int *result);
int main()
{
    int n, result;

    printf("Enter a number: ");
    scanf("%d", &n);
    printf("rSumUp1(): %d\n", rSumUp1(n));

    // Using call by value (return)
rSumUp2(n,&result);

    // Using call by reference
    printf("rSumUp2(): %d",result);
    return 0;
}
```

# Recursion – Q1 (rSumUp1)

## By Returning Value

```
int rSumUp1(int n)
{
    if (n == 1)
        return 1;
    else
        return n + rSumUp1(n-1);
}
```

Enter a number: **4**  
rSumUp1(): 10

main()

Enter a number: **4**  
rSumUp1(): 10

rSumUp1(4)

rSumUp1(int n)  
n=4  
return **4** + rSumUp1(3);

rSumUp1(int n)  
n=3  
return **3** + rSumUp1(2);

rSumUp1(int n)  
n=2  
return **2** + rSumUp1(1);

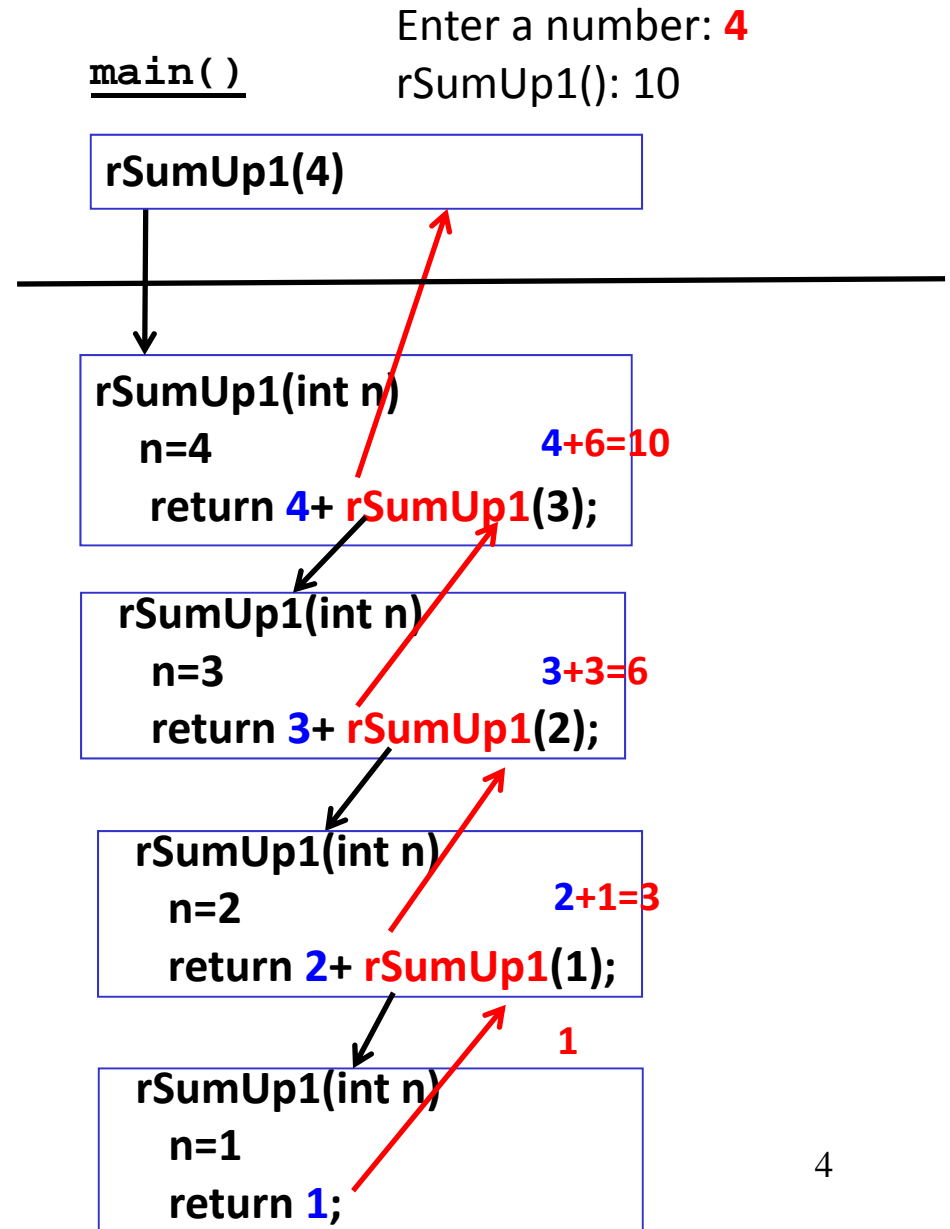
rSumUp1(int n)  
n=1  
return **1**;

# Recursion – Q1 (rSumUp1)

## By Returning Value

```
int rSumUp1(int n)
{
    if (n == 1)
        return 1;
    else
        return n + rSumUp1(n-1);
}
```

Enter a number: 4  
rSumUp1(): 10

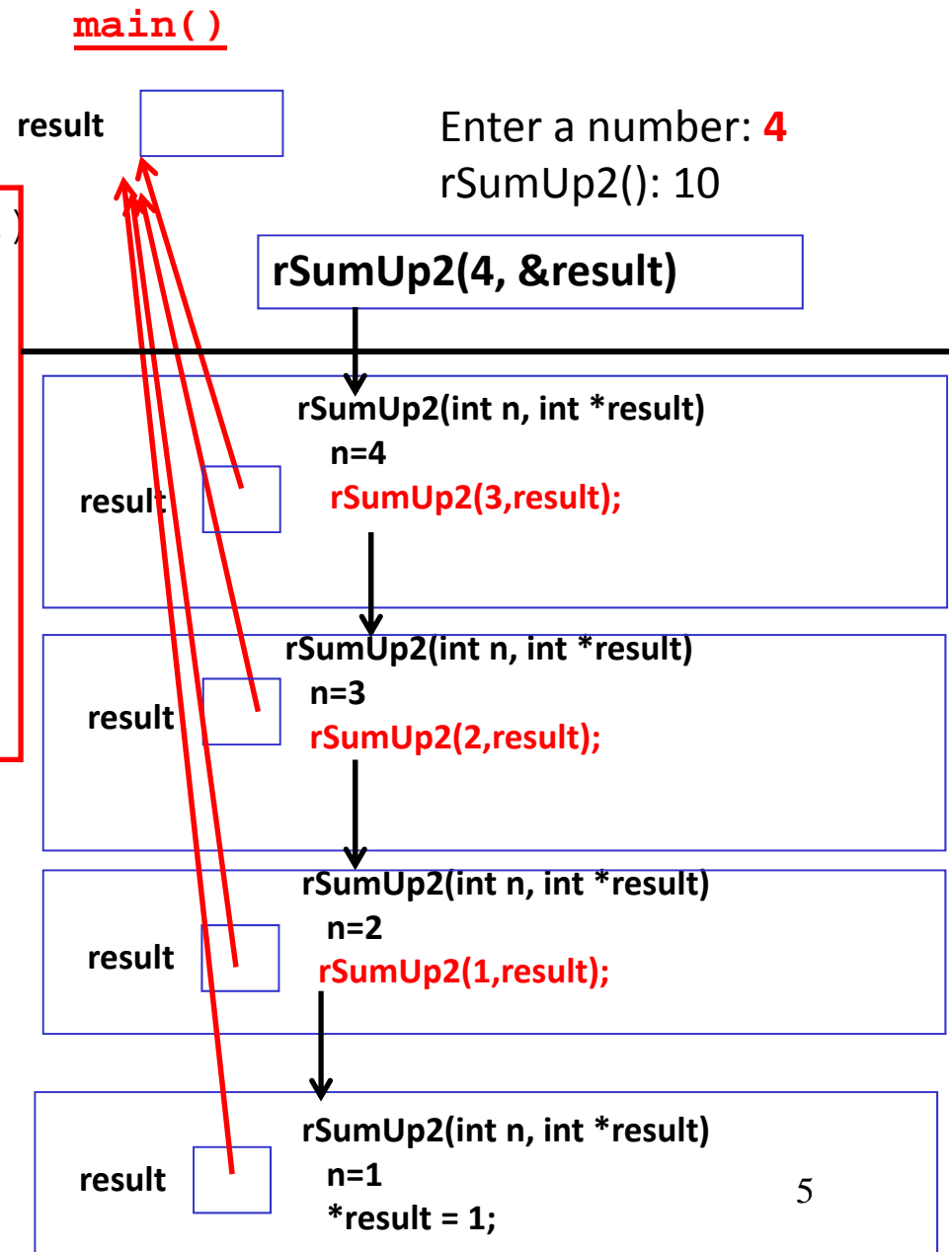


# Recursion – Q1 (rSumUp2)

## Call by reference

```
void rSumUp2(int n, int *result)
{
    if (n == 1)
        *result=1;
    else
    {
        rSumUp2(n-1, result);
        *result += n;
    }
}
```

Enter a number: **4**  
rSumUp2(): 10

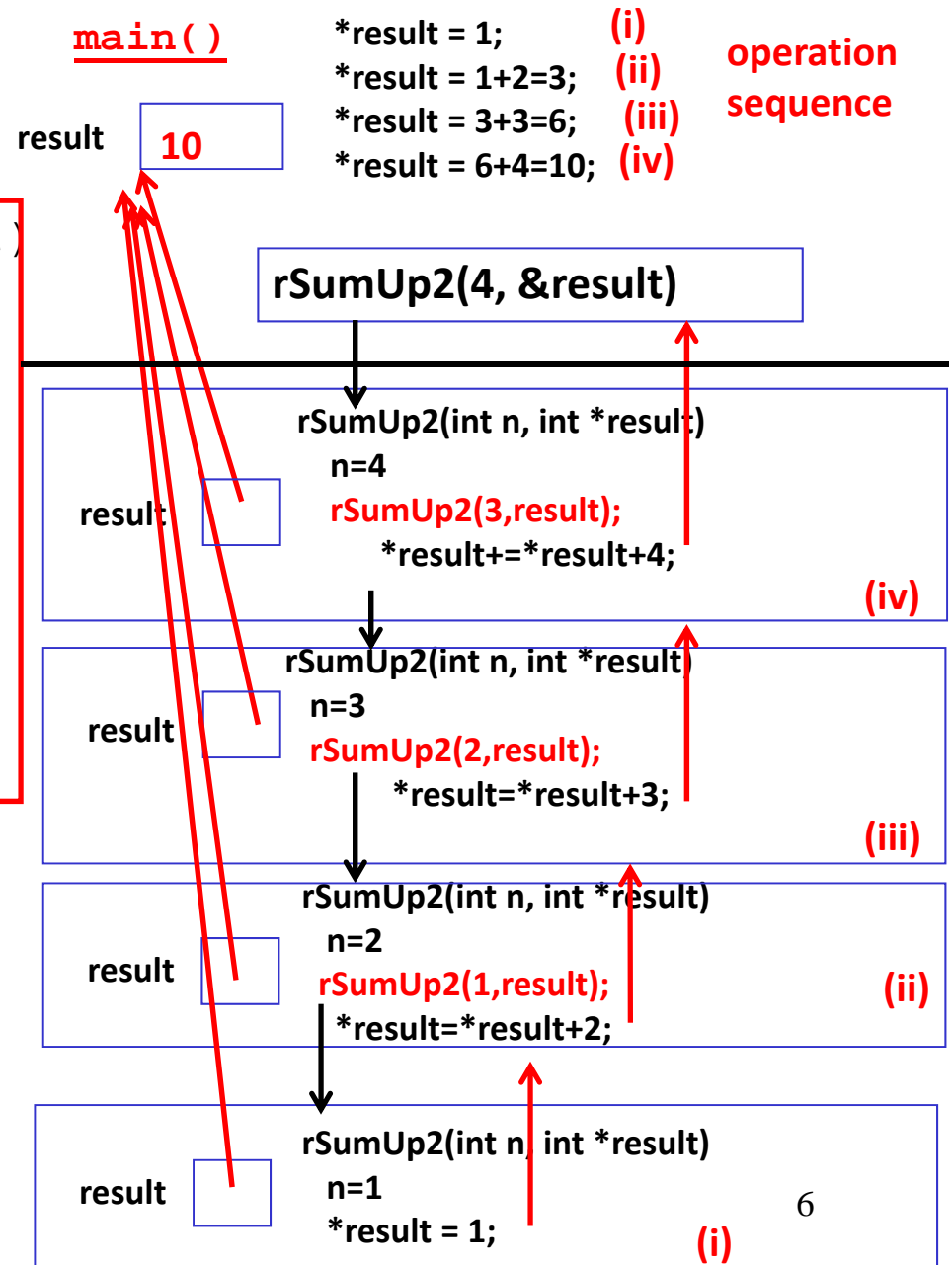


# Recursion – Q1 (rSumUp2)

## Call by reference

```
void rSumUp2(int n, int *result)
{
    if (n == 1)
        *result=1;
    else
    {
        rSumUp2(n-1, result);
        *result += n;
    }
}
```

Enter a number: **4**  
rSumUp2(): 10



## Recursion: Q2 (rdigitValue)

```
#include <stdio.h>
int rdigitValue1(int num, int k);
void rdigitValue2(int num, int k, int *result);
int main(){
    int k;
    int number, digit;

    printf("Enter a number: ");
    scanf("%d", &number);
    printf("Enter the position: ");
    scanf("%d", &k);
    printf("rdigitValue1(): %d\n", rdigitValue1(number, k));
    rdigitValue2(number, k, &digit);
    printf("rdigitValue2(): %d\n", digit);
    return 0;
}
```

## Application Example (2): rdigitValue1

By Returning Value

```
int rdigitValue1(int num, int k)
{
    if (k==0)
        return 0;
    else if (k==1)
        return num%10;
    else
        return rdigitValue1(num/10, k-1);
}
```

Enter a number: **1284567**

Enter the digit position: **3**

rdigitValue1(): 5

main()

number=1284567, k=3

rdigitValue1(number,k)

rdigitValue1(int num,int k)  
num=1284567, k=3  
return rdigitValue1(num/10,k-1);

rdigitValue1(int num,int k)  
num=128456, k=2  
return rdigitValue1(num/10,k-1);

rdigitValue1(int num,int k)  
num=12845, k=1  
return num%10; (i.e. 12845%10=5)



## Application Example (2): rdigitValue1

By Returning Value

```
int rdigitValue1(int num, int k)
{
    if (k==0)
        return 0;
    else if (k==1)
        return num%10;
    else
        return rdigitValue1(num/10, k-1);
}
```

Enter a number: **1284567**

Enter the digit position: **3**

rdigitValue1(): 5

main()

number=1284567, k=3

rdigitValue1(number,k)

rdigitValue1(int num,int k)  
num=1284567, k=3  
return rdigitValue1(num/10,k-1);

rdigitValue1(int num,int k)  
num=128456, k=2  
return rdigitValue1(num/10,k-1);

rdigitValue1(int num,int k)  
num=12845, k=1  
return num%10; (i.e. 12845%10=5)

# Application Example (2): rdigitValue2

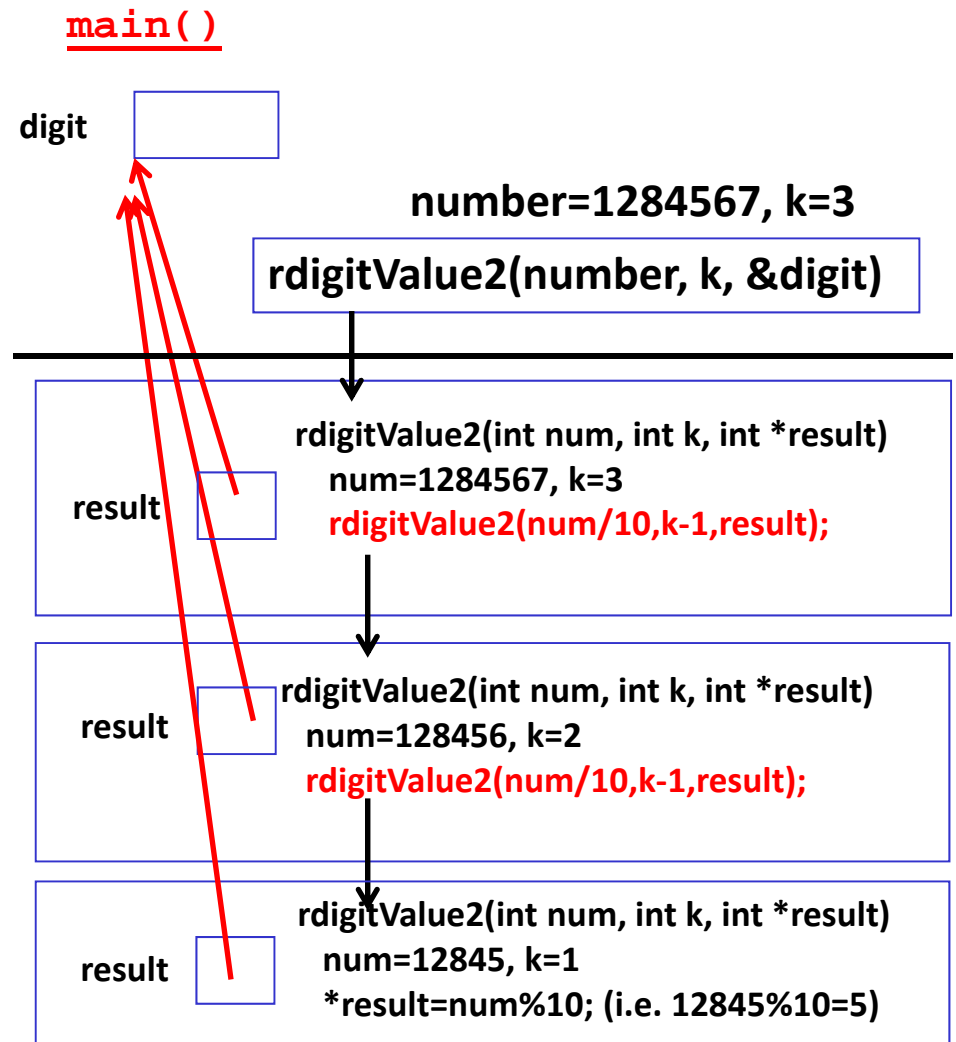
Call by reference

```
void rdigitValue2(int num, int k,
int *result)
{
    if (k==0)
        *result = 0;
    else if (k==1)
        *result = num%10;
    else
        rdigitValue2(num/10, k-1,
            result);
}
```

Enter a number: **1284567**

Enter the digit position: **3**

rdigitvalue2(): 5



## Application Example (2): rdigitValue2

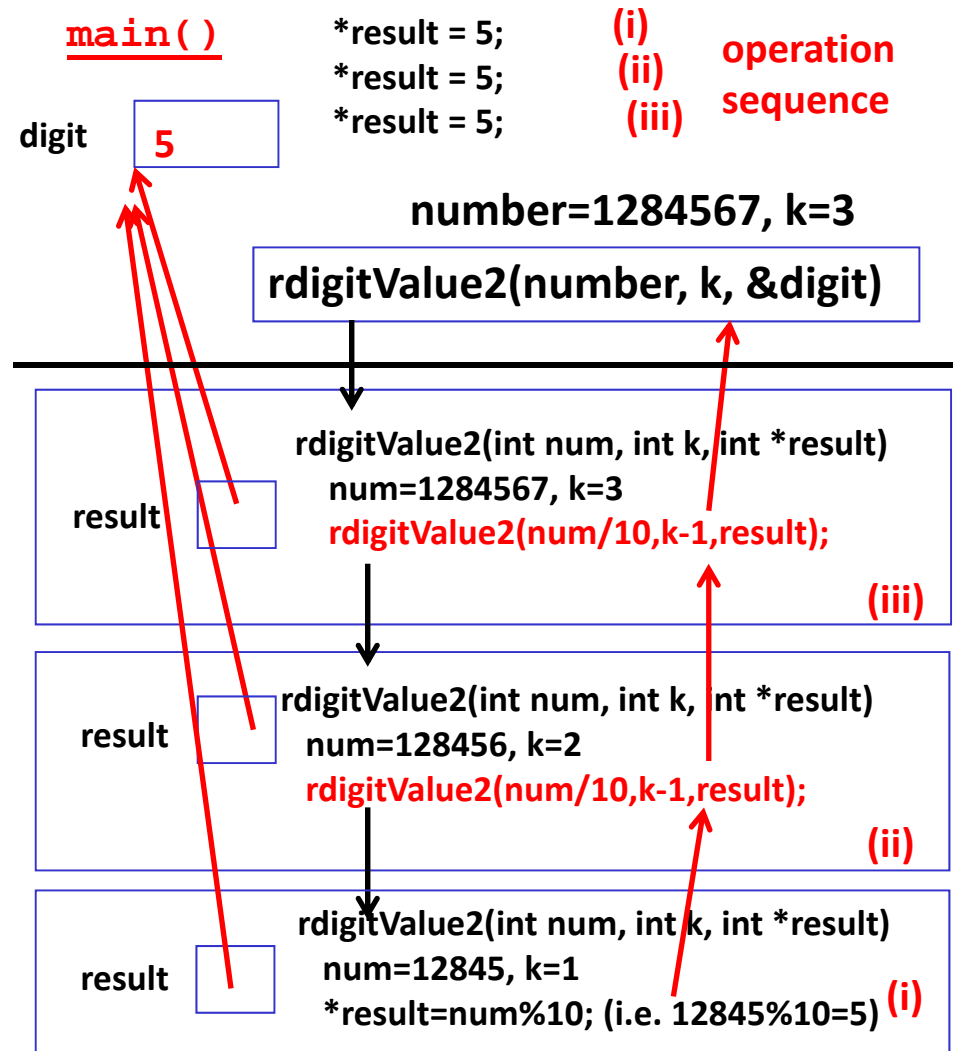
Call by reference

```
void rdigitValue2(int num, int k,
int *result)
{
    if (k==0)
        *result = 0;
    else if (k==1)
        *result = num%10;
    else
        rdigitValue2(num/10, k-1,
            result);
}
```

Enter a number: **1284567**

Enter the digit position: **3**

rdigitvalue2(): 5



# Recursion – Q3

```
#include <stdio.h>
#define BLANK ' '
void saveChar();
int main()
{
    printf("Enter your word and end it
with a space => ");
    saveChar();
    putchar('\n');
    return 0;
}
void saveChar()
{
    char ch;
    ch = getchar();
    if (ch != BLANK)
        saveChar();
    else
        putchar('\n');
    putchar(ch);
}
```

Enter your word and end it with a space => **ward**

**draw**

Please note that there is a blank character at the end of the input word before the “enter” key is pressed.

Basically, this program prints an input string, which ends with a space character, in the reversed order.

# Recursion – Q3

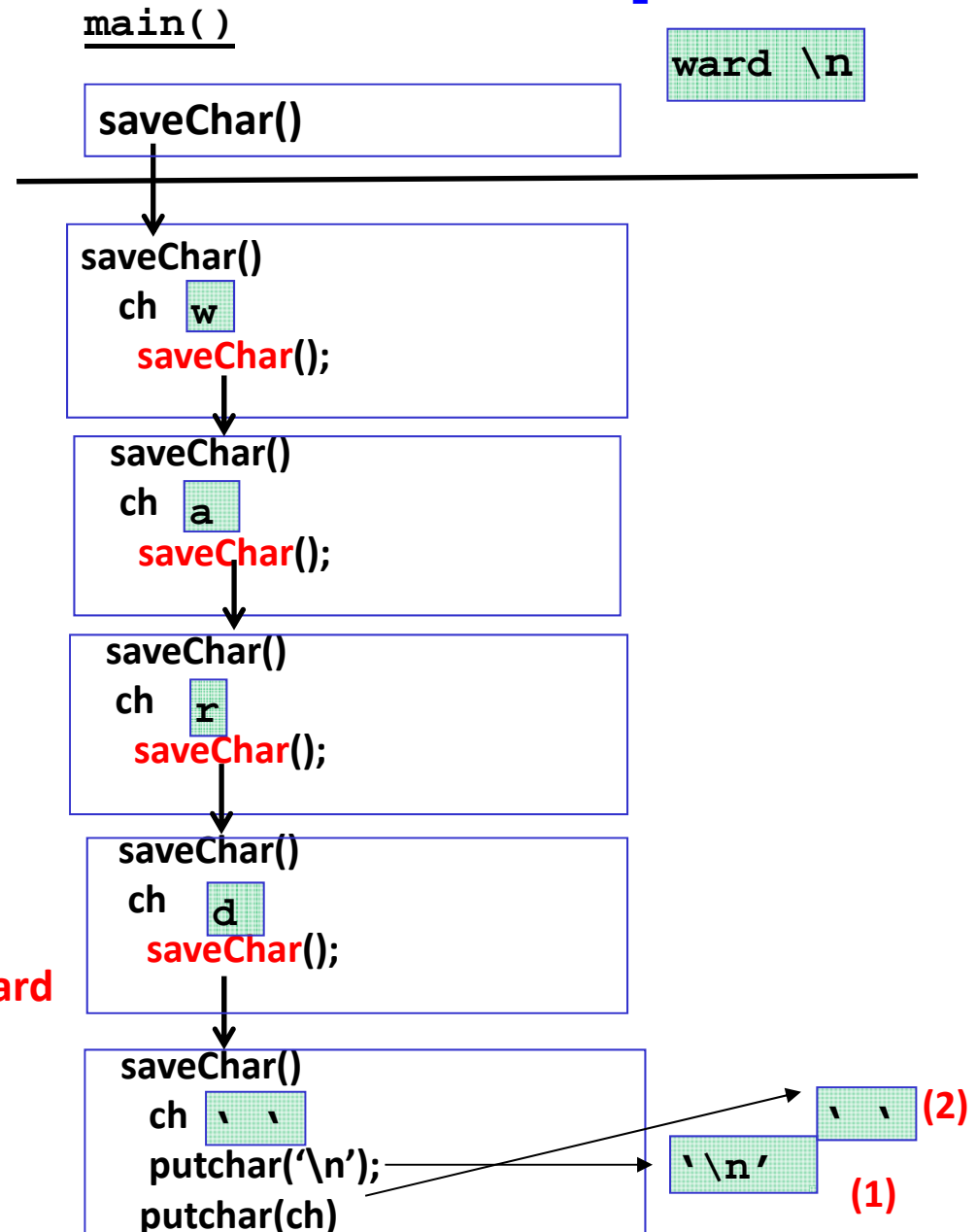
```
#include <stdio.h>
#define BLANK ' '
void saveChar();
int main()
{
    printf("Enter your word and end it
    with a space => ");
    saveChar();
    putchar('\n');
    return 0;
}
void saveChar()
{
    char ch;
    ch = getchar();
    if (ch != BLANK)
        saveChar();
    else
        putchar('\n');
    putchar(ch);
}
```

Enter your word and end it with a space => **ward**

draw

13

Input buffer



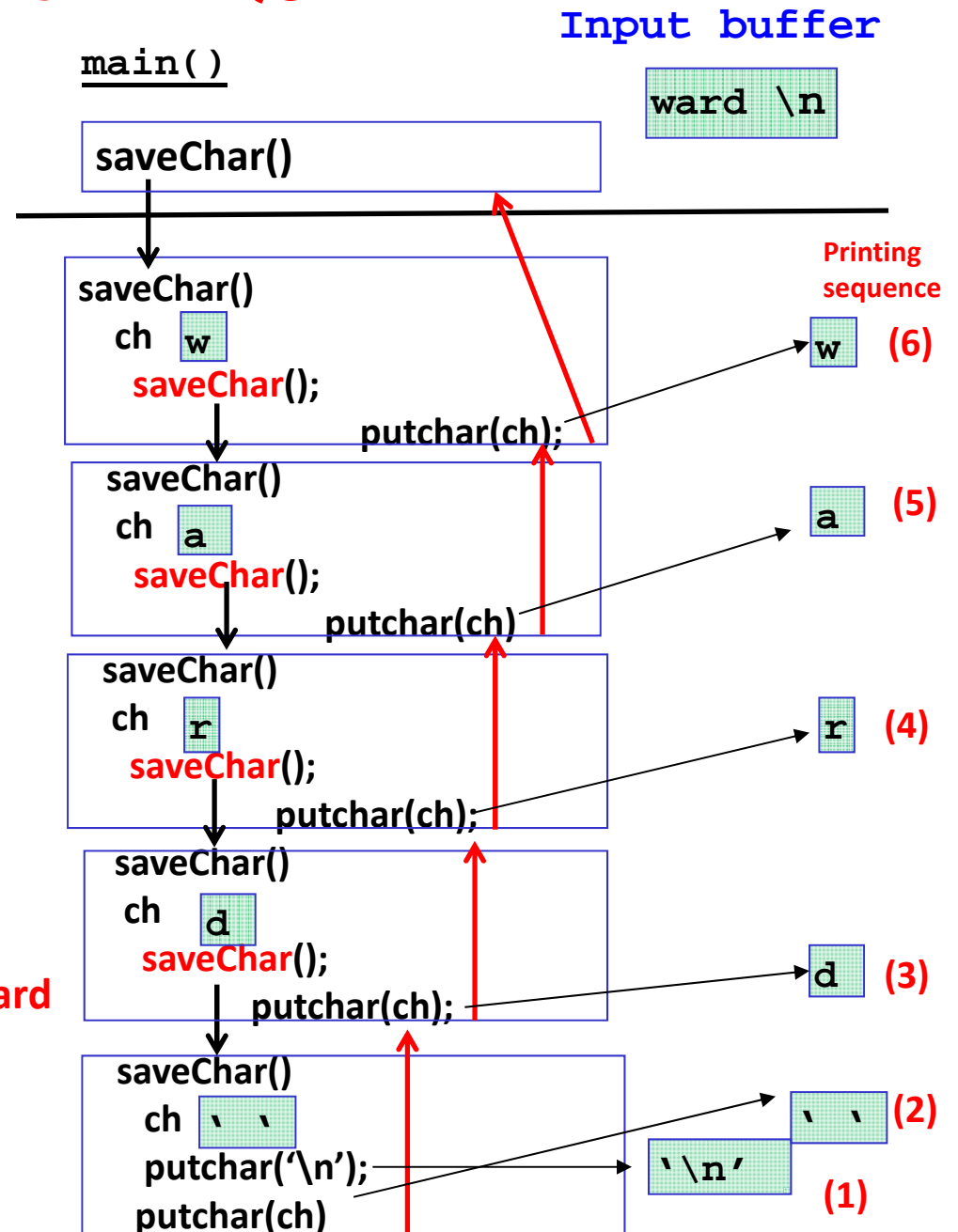
# Recursion – Q3

```
#include <stdio.h>
#define BLANK ' '
void saveChar();
int main()
{
    printf("Enter your word and end it
    with a space => ");
    saveChar();
    putchar('\n');
    return 0;
}
void saveChar()
{
    char ch;
    ch = getchar();
    if (ch != BLANK)
        saveChar();
    else
        putchar('\n');
    putchar(ch);
}
```

Enter your word and end it with a space => **ward**

draw

14



# Recursion – Q4

**(rCountArray)** Write a recursive C function that returns the number of times the integer ' $a$ ' appears in the array which has ' $n$ ' integers in it. Assume that  $n$  is greater than or equal to 1. The function prototype is:

**`int rCountArray(int array[ ], int  $n$ , int  $a$ )`**

Write a C program to test the functions.

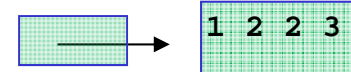
**Sample input and output sessions:**

Enter array size: **4**  
Enter 4 numbers: **1 2 2 3**  
Enter the target number: **2**  
`rCountArray()` = 2  
`rCountArray2()` = 2

```
#include <stdio.h>
#define SIZE 10
int rCountArray(int array[], int n, int a);
int rCountArray2(int array[], int n, int a);
int main()
{
    int array[SIZE];
    int index, count, target, size;

    printf("Enter array size: ");
    scanf("%d", &size);
    printf("Enter %d numbers: ", size);
    for (index = 0; index < size; index++)
        scanf("%d", &array[index]);
    printf("Enter the target: ");
    scanf("%d", &target);
    count = rCountArray(array, size, target); // approach 1
    printf("rCountArray() = %d\n", count);
    count = rCountArray2(array, size, target); // approach 2
    printf("rCountArray2() = %d", count);
    return 0;
}
```

array



size

4

target

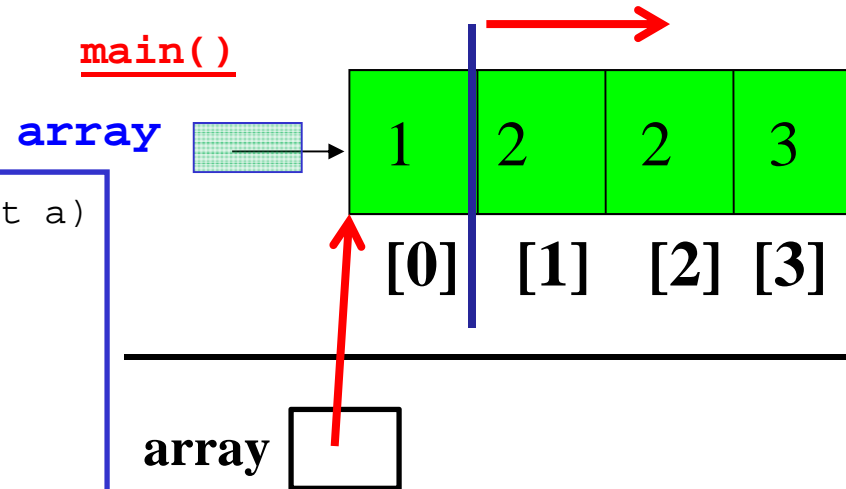
2

# Recursion – Q4

## Approach 1

```
int rCountArray(int array[], int n, int a)
{
    if (n == 1)
    {
        if (array[0] == a)
            return 1;
        else
            return 0;
    }
    if (array[0] == a)
        return 1+rCountArray(&array[1],n-1,a);
    else
        return rCountArray(&array[1], n-1, a);
}
```

Enter array size: **4**  
Enter 4 numbers: **1 2 2 3**  
Enter the target number: **2**  
rCountArray() = 2



The idea is to check the array element from the beginning of the array **array[0]**, and reduce the size of array by 1 when doing the recursive call.



# Recursion – Q4

## Approach 1

```
int rCountArray(int array[], int n, int a)
{
    if (n == 1)
    {
        if (array[0] == a)
            return 1;
        else
            return 0;
    }
    if (array[0] == a)
        return 1+rCountArray(&array[1],n-1,a);
    else
        return rCountArray(&array[1], n-1, a);
}
```

Enter array size: **4**  
Enter 4 numbers: **1 2 2 3**  
Enter the target number: **2**  
rCountArray() = 2

17

main()      array={1,2,2,3},  
size=4, target=2

rCountArray(array,size,target)

rCountArray(int array[], int n, int a)  
array={**1**,2,2,3}, n=4,a=**2**  
(array[0]!=a), therefore  
return rCountArray(&array[1],n-1,a);

rCountArray(int array[], int n, int a)  
array={**2**,2,3}, n=3, a=**2**  
(array[0]==a), therefore  
return 1+rCountArray(&array[1],n-1,a);

rCountArray(int array[], int n, int a)  
array={**2**,3}, n=2, a=**2**  
(array[0]==a), therefore  
return 1+rCountArray(&array[1],n-1,a);

rCountArray(int array[], int n, int a)  
array={**3**}, n=1, a=**2**  
return **0**; (because array[0] != 2)

# Recursion – Q4

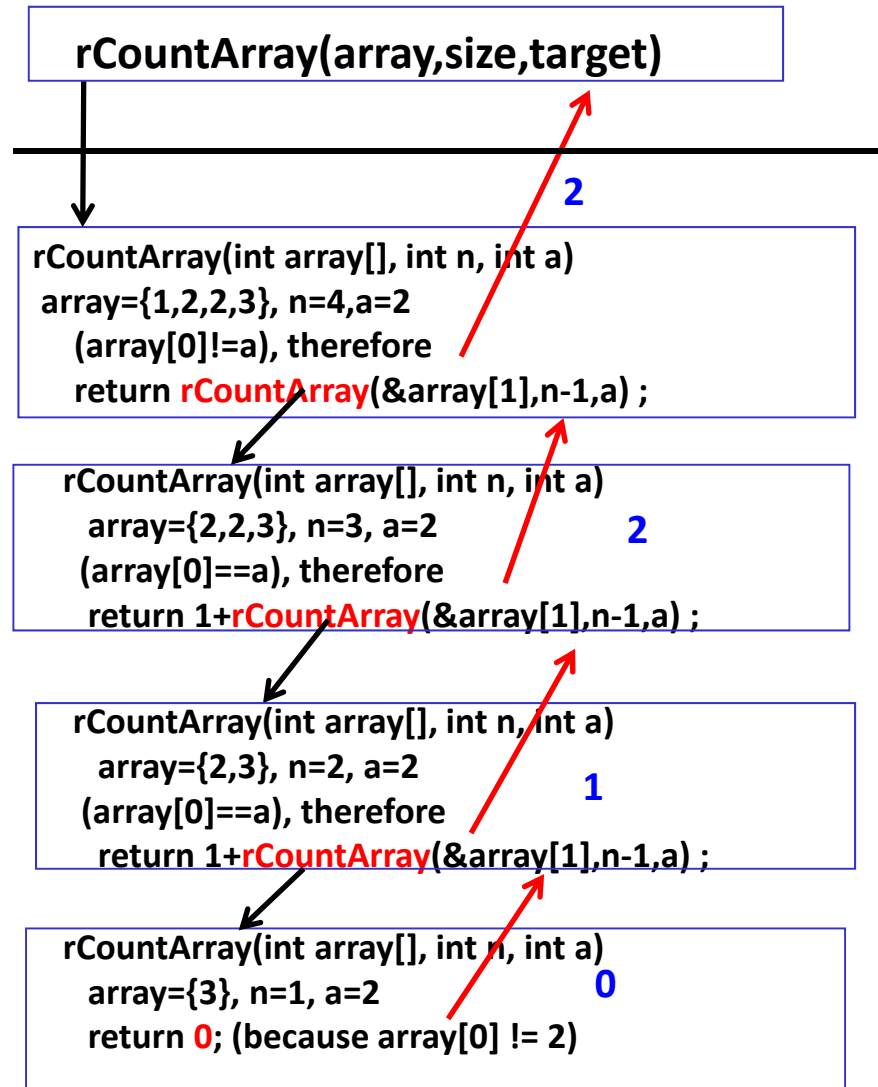
## Approach 1

```
int rCountArray(int array[], int n, int a)
{
    if (n == 1)
    {
        if (array[0] == a)
            return 1;
        else
            return 0;
    }
    if (array[0] == a)
        return 1+rCountArray(&array[1],n-1,a);
    else
        return rCountArray(&array[1], n-1, a);
}
```

Enter array size: **4**  
Enter 4 numbers: **1 2 2 3**  
Enter the target number: **2**  
rCountArray() = 2

18

main()      array={1,2,2,3},  
size=4, target=2

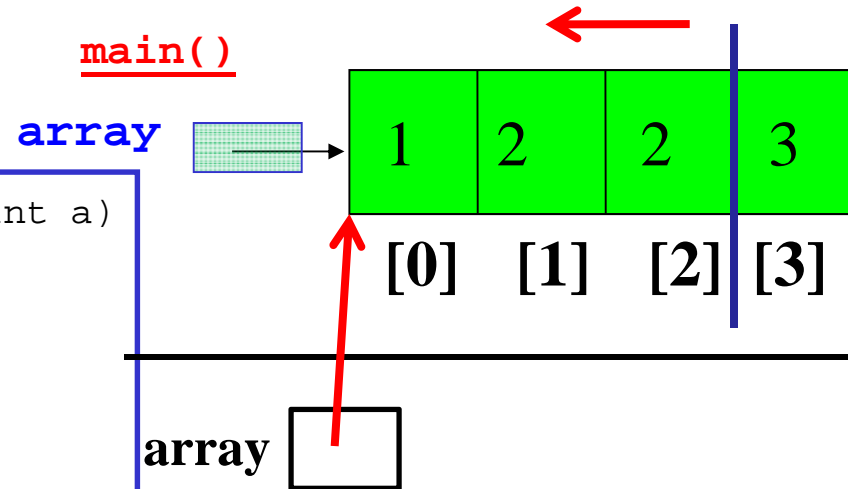


# Recursion – Q4

## Approach 2

```
int rCountArray2(int array[], int n, int a)
{
    if (n == 1)
    {
        if (array[0] == a)
            return 1;
        else
            return 0;
    }
    if (array[n-1] == a)
        return 1+rCountArray2(&array[0],n-1,a);
    else
        return rCountArray2(&array[0], n-1, a);
}
```

Enter array size: **4**  
Enter 4 numbers: **1 2 2 3**  
Enter the target number: **2**  
rCountArray2() = 2



The idea is to check the array element from the end of the array **array[n-1]**, and reduce the size of array by 1 when doing the recursive call.

# Recursion – Q4

## Approach 2

```
int rCountArray2(int array[], int n, int a)
{
    if (n == 1)
    {
        if (array[0] == a)
            return 1;
        else
            return 0;
    }
    if (array[n-1] == a)
        return 1+rCountArray2(&array[0],n-1,a);
    else
        return rCountArray2(&array[0], n-1, a);
}
```

Enter array size: **4**  
Enter 4 numbers: **1 2 2 3**  
Enter the target number: **2**  
rCountArray2() = 2

main()

array={1,2,2,3},  
size=4, target=2

rCountArray2(array,size,target)

rCountArray2(int array[], int n, int a)  
array={1,2,2,3}, n=4, a=2  
(array[n-1]!=a), therefore  
return rCountArray2(&array[0],n-1,a);

rCountArray2(int array[], int n, int a)  
array={1,2,2}, n=3, a=2  
(array[n-1]==a), therefore  
return 1+rCountArray2(&array[0],n-1,a);

rCountArray2(int array[], int n, int a)  
array={1,2}, n=2, a=2  
(array[n-1]==a), therefore  
return 1+rCountArray2(&array[0],n-1,a);

rCountArray2(int array[], int n, int a)  
array={1}, n=1, a=2  
return 0; (because array[0] != 2)

# Recursion – Q4

## Approach 2

```
int rCountArray2(int array[], int n, int a)
{
    if (n == 1)
    {
        if (array[0] == a)
            return 1;
        else
            return 0;
    }
    if (array[n-1] == a)
        return 1+rCountArray2(&array[0],n-1,a);
    else
        return rCountArray2(&array[0], n-1, a);
}
```

Enter array size: **4**  
Enter 4 numbers: **1 2 2 3**  
Enter the target number: **2**  
rCountArray2() = 2

21

main()      array={1,2,2,3},  
size=4, target=2

rCountArray2(array,size,target)

rCountArray2(int array[], int n, int a)  
array={1,2,2,3}, n=4, a=2  
(array[n-1]!=a), therefore  
return rCountArray2(&array[0],n-1,a);

rCountArray2(int array[], int n, int a)  
array={1,2,2}, n=3, a=2  
(array[n-1]==a), therefore  
return 1+rCountArray2(&array[0],n-1,a);

rCountArray2(int array[], int n, int a)  
array={1,2}, n=2, a=2  
(array[n-1]==a), therefore  
return 1+rCountArray2(&array[0],n-1,a);

rCountArray2(int array[], int n, int a)  
array={1}, n=1, a=2  
return 0; (because array[0] != 2)