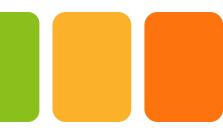


Advanced Programming Techniques in Java

Running Times & Comparability

Lecture 18 Class Objectives

- 
- Complexity & Running time (section 13.2)

- 
- Comparable Interface (section 10.2)
 - List (first subsection 11.1)



Review: ArrayList methods

<code>add(value)</code>	appends value at end
<code>add(index, value)</code>	inserts given value at index, shifting subsequent values
<code>clear()</code>	removes all elements
<code>indexOf(value)</code>	returns first index where value == given value (1 if not found)
<code>get(index)</code>	returns the value at index
<code>remove(index)</code>	removes/returns value at index, shifting subsequent values
<code>set(index, value)</code>	replaces value at given index



<code>size()</code>	returns the number of elements in the list
<code>toString()</code>	returns a string representation of the list, such as "[3, 42, -7, 12]"

Review: ArrayList methods (part 1)

<code>addAll(list)</code>	adds all elements from the given list to this list (at the end of the list, or at the specified index)
<code>contains(value)</code>	returns true if given value is contained in this list
<code>containsAll(list)</code>	returns true if this list contains all elements of the given list
<code>equals(list)</code>	returns true if given other list contains the same elements in the same order
<code>iterator()</code> <code>listIterator()</code>	returns an object used to iterate through the list (either forward or backward)



<code>lastIndexOf (value)</code>	returns last index value is
<code>remove (value)</code>	finds and removes the gi
<code>removeAll (list)</code>	removes any elements fo
<code>retainAll (list)</code>	removes any elements no
<code>subList (from, to)</code>	returns the sub-portion o indexes from (inclusive)
<code>toArray ()</code>	returns the elements in th

Review: Three main categories

- Syntax Errors

- 
- Run-time errors
 - Logic errors



Review: Efficiency

Computing time and memory are bounded resources.

Efficiency:

- Different algorithms that solve the same problem can differ significantly in their efficiency.
- More significant than differences due to hardware (CPU, memory, disks, ...) and software (OS, programming language, compiler, ...).

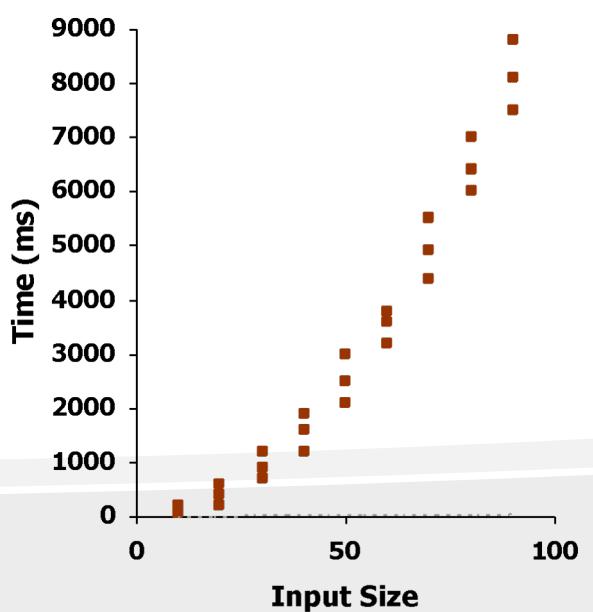


=> Running Time/Computational Complexity



Empirical Analysis

- Run time can be studied experimentally
 - Write a program implementing the algorithm
 - Run the program with inputs of varying size

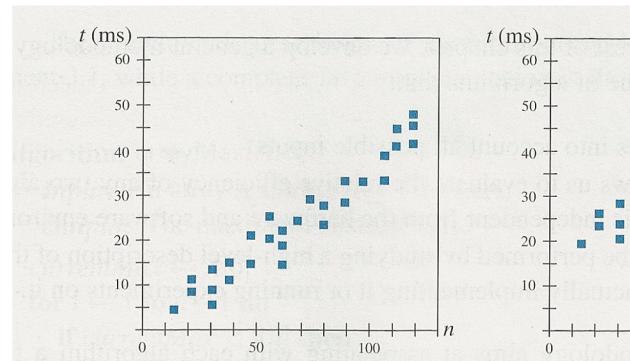


- 
- Get an accurate measure of the actual running time
 - Plot the results



Limitations of Empirical Analysis

- Experiment can be done only on a limited set of test inputs
- Difficult to compare the efficiency of two algorithms under different environments
 - Hardware environment (processor, clock, rate, memory)
 - Software environment (OS, programming language, compiler)



- Necessary to implement and execute an algorithm to

Theoretical Analysis

- General methodology for analyzing run time of algorithms
 - Consider all possible inputs
 - Can be performed studying high-level description of the algorithm

- 
- Evaluate the relative efficiency of any two algorithms in hardware and software environment

Asymptotic Performance

- We care most about *asymptotic*
 - How does the algorithm behave as the problem size grows?
 - Running time
 - Memory/storage requirements
 - Bandwidth/power requirements/etc.



Runtime Efficiency

- Assume the following:

- Any single Java statement takes the same amount of time to execute
- A method call's runtime is measured by the total number of statements it contains
 - A loop's runtime, if the loop repeats n times, is n times the runtime of one iteration
- We want to count the number of statements that are executed



Efficiency examples

```
statement1;  
statement2;  
statement3;
```

```
for (int i = 1; i <= n; i++) {  
    statement4; } for (int i = 1; i  
<= n; i++) { statement5; statement6;  
    statement7;  
}
```

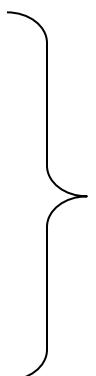
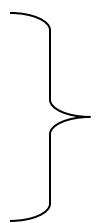
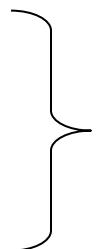


Efficiency examples

statement1;



statement2;3





```
statement3;
```

```
for (int i = 1; i <= n; i++) {n statement4;  
} 4n + 3
```

```
for (int i = 1; i <= n; i++) {  
    statement5;  
    statement6;3n statement7;  
}
```



Efficiency examples (cont.)

```
for (int i = 1; i <= n; i++) {  
    for (int j = 1; j <= n; j++) {  
        statement1;  
    }  
}
```

```
for (int i = 1; i <= n; i++)  
{ statement2; statement3;  
statement4; statement5;  
}
```



Efficiency examples (cont.)





```
for (int i = 1; i <= n; i++) {  
    for (int j = 1; j <= n; j++) {  
        statement1;      statement4;  
    }                  }  
}  
for (int i = 1; i <= n; i++) {  
    statement2;  
    statement3;
```

- How many statements will execute if n =



Algorithm growth rates

- We measure runtime in proportion to the input data size
 - **Growth rate:** Change in runtime as n changes
- Say an algorithm runs $0.4n^3 + 25n^2 + 8n + 17$
 - Consider the runtime when n is extremely large
 - We ignore constants like 25 because they are tiny next to n^3
 - The highest-order term (n^3) dominates the overall runtime
 - We say that this algorithm runs "in the order of" n^3
 - or $O(n^3)$ for short ("Big-Oh of n^3 ")
- **Big-Oh** It's a measure of the longest amount of time an algorithm to complete (upper bound)



Complexity classes

- **Complexity class:** A category of algorithm efficiency based on the input size n

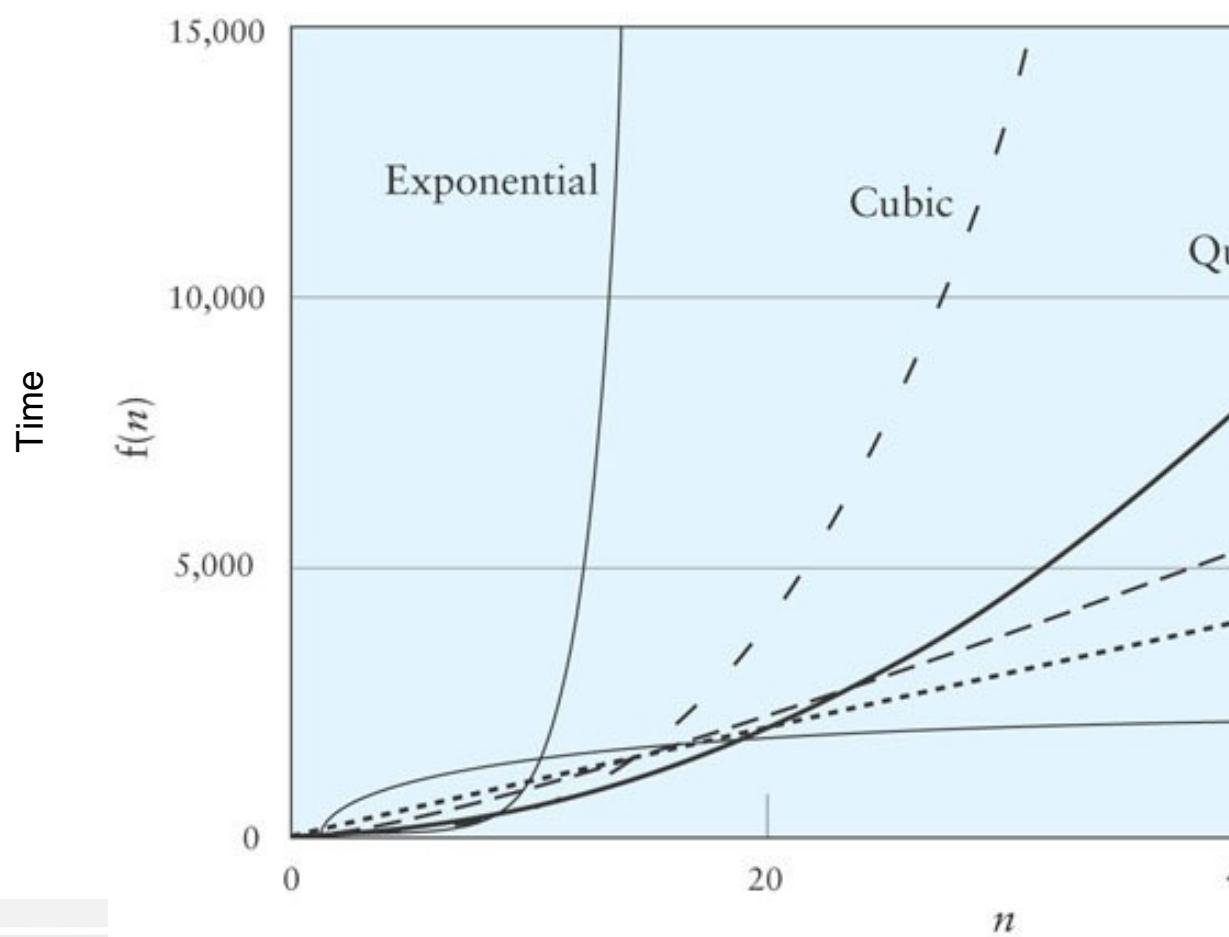
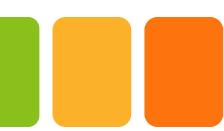


Big-O	Name
$O(1)$	Constant
$O(\log n)$	Logarithmic
$O(n)$	Linear
$O(n \log n)$	Log-linear
$O(n^2)$	Square
$O(n^3)$	Cubic
$O(2^n)$	Exponential
$O(n!)$	Factorial



Practical Complexity







Input Size



Effect of Different Growth Rates



$O(f(n))$	$f(50)$	$f(100)$
$O(1)$	1	1
$O(\log n)$	5.64	6.64
$O(n)$	50	100
$O(n \log n)$	282	664
$O(n^2)$	2500	10,000
$O(n^3)$	12,500	100,000
$O(2^n)$	1.126×10^{15}	1.27×10^{30}
$O(n!)$	3.0×10^{64}	9.3×10^{157}

Collection efficiency

- Efficiency of various operations on ArrayList:

Method
add
add (index, value)
indexof
get
remove
set
size





The Comparable



Natural ordering

- Many types have a notion of a **natural ordering** that can be "less than" or "greater than" another:
 - int, double: numeric value
 - String: lexical (alphabetical) order
- Not all types have a natural ordering:
 - Point: How would they be ordered? By y? By x?
 - GroceryList: What makes one list "less than" another?

Uses of natural ordering

- An ArrayList of orderable values can be sorted using Collections.sort()



```
ArrayList<String> words = new ArrayList<String>();
words.add("four"); words.add("score");
words.add("and"); words.add("seven");
words.add("years"); words.add("ago");

// show list before and after sorting
System.out.println("before sort, words = " + words);
Collections.sort(words);
System.out.println("after sort, words = " + words);
```

- **Output:**

```
before sort, words = [four, score, and, seven,
after sort, words = [ago, and, four, score, se
```

Comparable interface

- The natural ordering of a class is specified through the Comparable interface:



Relationship	Primitive comparison
less than	<code>if (x < y) {</code>
less than or equal	<code>if (x <= y) {</code>
equal	<code>if (x == y) {</code>
not equal	<code>if (x != y) {</code>



greater than	if (x > y) {
greater or equal	if (x >= y) {
	public interface Comparable { public int compareTo(...); }

- Classes such as String, Integer, ... implement Comparable
- compareTo returns an integer that is < 0, > 0, or 0

How to compare objects?

- For any class that implements the Comparable interface
 - You can compare to objects with the compareTo method



```
String s1 = "hello";
String s2 = "world"; if
(s1.compareTo(s2)<0) {
    System.out.println("S1 less than S2")
}
```

- You cannot use relational operators. The next is illegal

```
String s1 = "hello";
String s2 = "world";
if (s1 < s2) {
    System.out.println("S1 less than S2")
}
```

Implementing Comparable

- You can define a natural ordering for your own class interface

- 
- Comparable is a generic interface, Comparable<T>
 - When implementing it, you must write your class's name
 - Example: public class Point implements Comparable<Point>
 - You must also write a method compareTo that compares this object to a given other object
 - Example:

```
public int compareTo(Point p) {  
    ...  
}
```



Comparable example



```
public class Point implements Comparable<Point> {
    private int x; private int y;
    ...
}

// sort by x and break ties by y
public int compareTo(Point other) {
    if (x < other.x) { return -1;
    } else if (x > other.x) {
        return 1;
    } else if (y < other.y) { return -1;
        // same x, smaller y
    } else if (y > other.y) { return 1;
        // same x, larger y
    } else { return 0;      // same x and
    same y }
}
```



compareTo tricks

- *subtraction trick* - Subtracting related numeric values
want compareTo to return:

```
// sort by x and break ties by y
compareTo(Point other) { if (x != other.x)
    return x - other.x; // different x
    } else { return y - other.y;
        compare y
    }
}
```

- The idea:

- if $x > \text{other}.x$, then $x - \text{other}.x > 0$
- if $x < \text{other}.x$, then $x - \text{other}.x < 0$
- if $x == \text{other}.x$, then $x - \text{other}.x = 0$



Comparable implementation



```
// The CalendarDate class stores information about a date (month and day but no year).

public class CalendarDate implements Comparable<CalendarDate> {
    private int month;
    private int day;

    public CalendarDate(int month, int day) {
        this.month = month;
        this.day = day;
    }

    public int compareTo(CalendarDate other) {
        if (this.month != other.month) {
            return this.month - other.month;
        } else {
            return this.day - other.day;
        }
    }

    public String toString() {
        return this.month + "/" + this.day;
    }
}
```



Example Client Program

```
// Short program that creates a list of the birthdays of the US Presidents and that puts them into sorted order.

import java.util.*;

public class CalendarDateTest { public
    static void main(String[] args) {
        ArrayList<CalendarDate> dates = new
        ArrayList<CalendarDate>(); dates.add(new CalendarDate(22));
        dates.add(new CalendarDate(10, 30)); dates.add(new CalendarDate(4, 13));
        dates.add(new CalendarDate(3, 28)); dates.add(new CalendarDate(4, 28));

        System.out.println("birthdays before sorting = " + dates);
        Collections.sort(dates);
        System.out.println("birthdays after sorting = " + dates)
    }
}
```

OUTPUT:



birthdays before sorting = [2/22, 10/30, 4/13, 3/16, 4/28]

birthdays after sorting = [2/22, 3/16, 4/13, 4/28, 10/30]

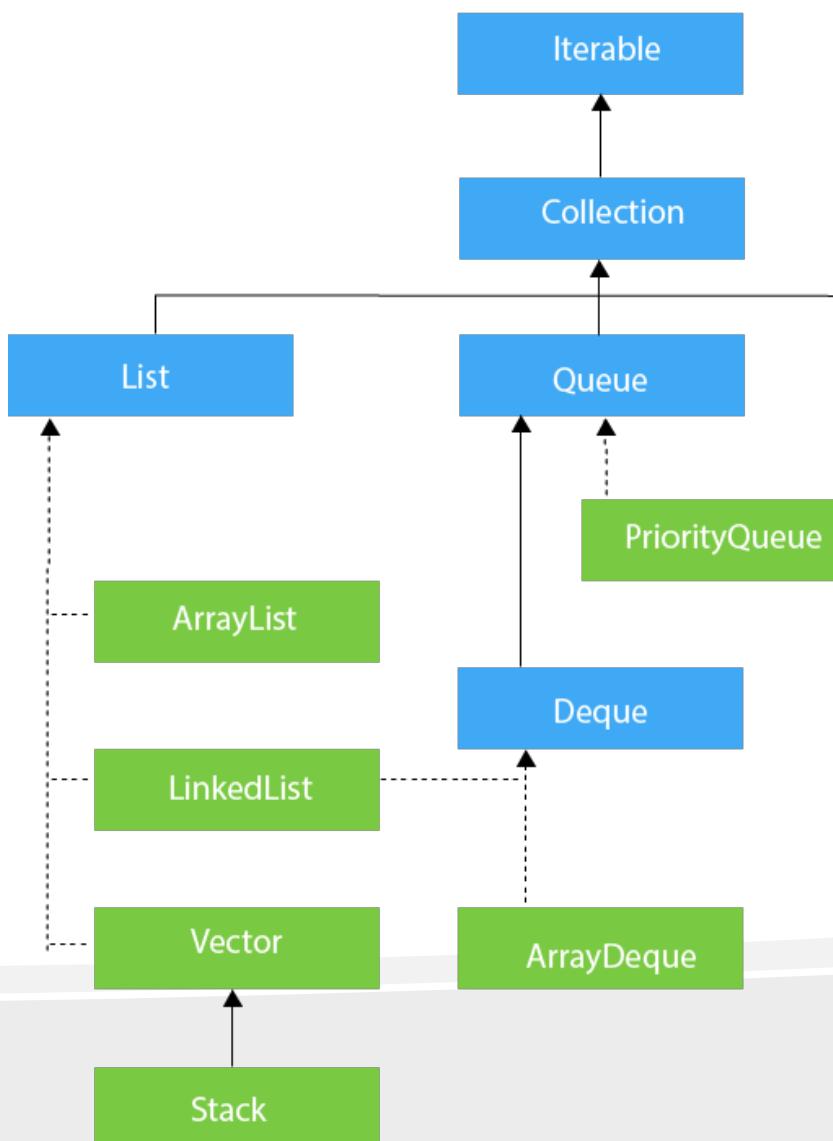




Collection



Collections Framework Diagram





Collections

- **Collection** is an object that stores data inside it
- The data stored are called **elements**
- Some collections maintain an ordering, some don't
- Some collections allow duplicates, some don't

- Typical operations:
- Add element, remove element, clear all elements, contains
- Most collections are built with particular operations or

Collections

- A collection is an object that groups multiple ele

- 
- Very useful
 - Store, retrieve and manipulate data
 - Transmit data from one method to another
 - Data structures and methods written already for you

Collection examples

- **List:** Collection of elements
- **Set:** A collection of elements that is guaranteed to be unique and can be searched efficiently
- **Map:** A collection of (key, value) pairs in which each key is associated with exactly one corresponding value
- **Stack:** A collection where the last element added is the first element returned

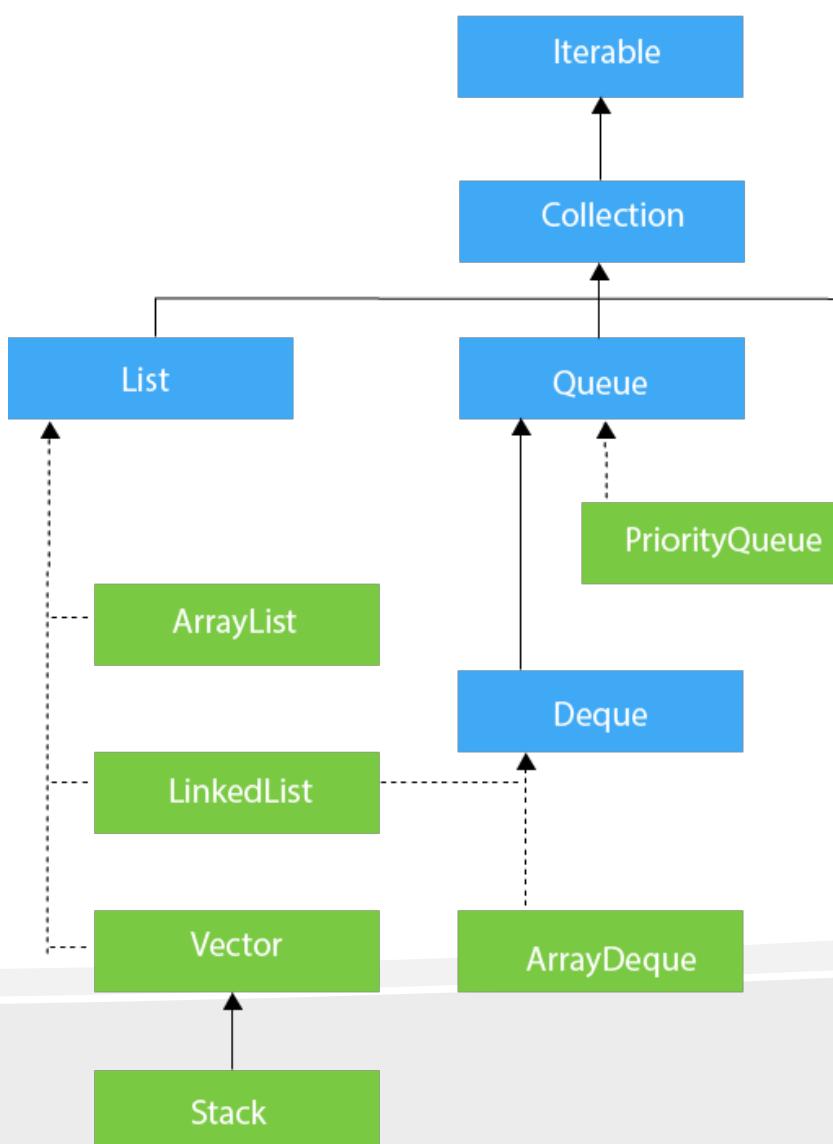
- 
- **Queue:** A collection where elements are removed from one end and added

Collections Framework

- Unified architecture for representing/storing and manipulating data
- It has:
- **interfaces** (Set, List, Queue, Deque)
- **classes** (ArrayList, Vector, LinkedList, PriorityQueue, HashSet, TreeSet)
- algorithms



Collections Framework Diagram





Java's Collection interface

- `Collection<E>` represents many kinds of collections. It defines the following methods:

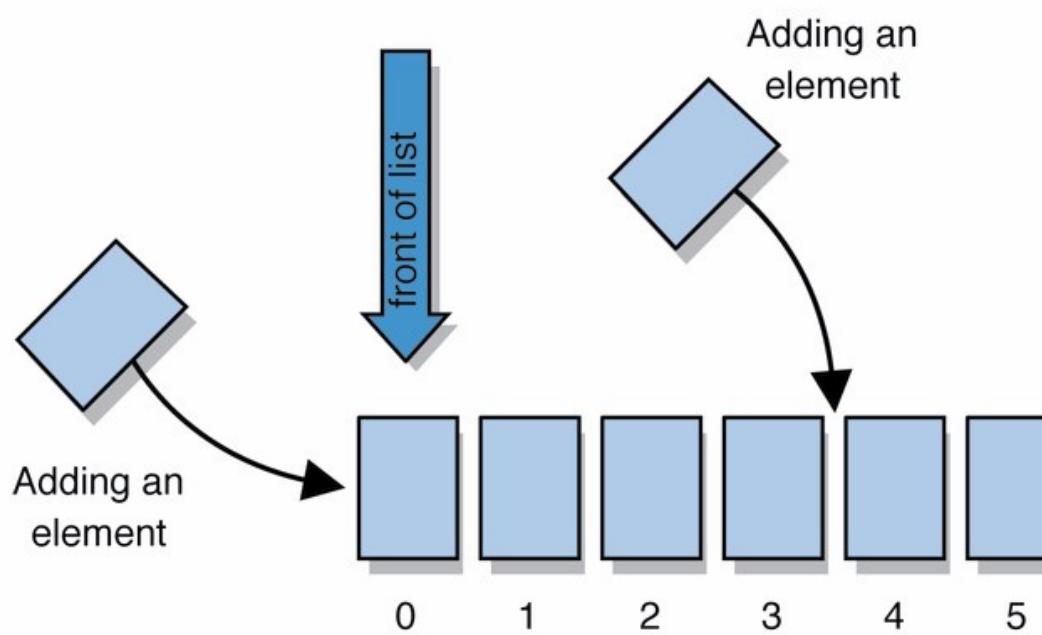
Method name	
<code>add(<i>value</i>)</code>	adds the given <i>value</i> to the collection. If the collection changed the size, it returns true, otherwise false.
<code>addAll(<i>collection</i>)</code>	adds all elements from the specified collection to this collection. Returns true if the collection changed the size, otherwise false.
<code>clear()</code>	removes all elements from this collection.
<code>contains(<i>value</i>)</code>	returns true if this collection contains the specified element.
<code>containsAll(<i>collection</i>)</code>	true if this collection contains all elements of the specified collection.
<code>isEmpty()</code>	true if the collection contains no elements.
<code>removeAll(<i>collection</i>)</code>	removes all elements from this collection that are contained in the specified collection.



retainAll (<i>collection</i>)	retains the collection
remove (E element)	removes the element
iterator ()	returns a specific iterator
size ()	returns the size of the list
toArray ()	returns an array containing all elements

List

- **List** is an ordered sequence of elements. One of the most common interfaces.





List features

- Maintains elements in the order they were added (by default)
 - Duplicates are allowed
 - add element to the list
 - insert element at given index
 - clear all elements
 - search for element
 - get element at given index
 - remove element at given index
 - get size
- Operations:



- some of these operations are inefficient
- The list manages its own size; the user of the list does not

Java's List interface

- Java has an interface `List<E>` to represent a list of elements, those in `Collection<E>`:
- **`public void add(int index, E element)`**
Inserts the specified element at the specified position.
- **`public E get(int index)`**



Returns the element at the specified position in this list.

- **public int indexOf(E element)**
Returns the index in this list of the first occurrence of the specified element; if this list does not contain it, it returns -1
- ...
- **List interface, cont'd.**
- **public int lastIndexOf(Object o)**
Returns the index in this list of the last occurrence of the specified element; if this list does not contain it, it returns -1

- 
- **public E remove(int index)**
Removes the object at the specified position in this
 - **public E set(int index, E element)**
Replaces the element at the specified position in the
 - Notice that the methods added to Collection<E>
 - **A list has indexes while a general collection may not.**
ArrayList
 - ArrayList implements the List interface
 - It implements all the methods of that interface



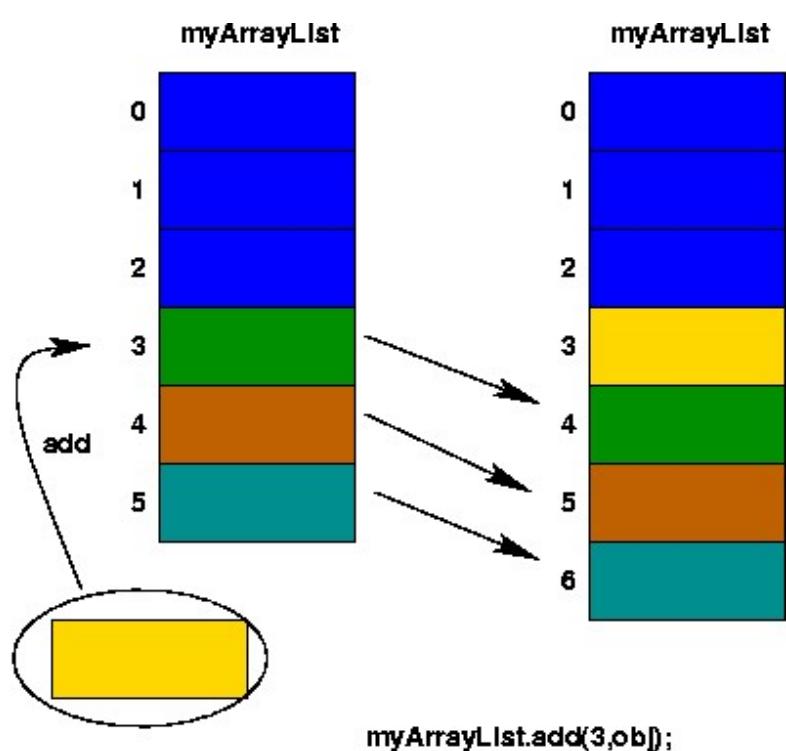
```
input: ArrayList<String> list
    int i=0;
    while (i < list.size()) { String element =
        (element.length()%2 == 0) { list.remove(i);
        for large files
            else { i++; // skip to next
                element
            }
        }
    }
```

- Read a list of strings and remove elements with even length



ArrayList limitations

- An add or remove operation on an ArrayList require elements to be shifted
- This can be slow for a large list
- What is the worst possible case?





Internals of ArrayList

- It is internally stored in an array. So, it has a certain capacity.
- Capacity: size of the array used to store the elements in the list.
- It is always at least as large as the list size.
- As elements are added to an `ArrayList`, its capacity increases.
- Random access to elements.
- `set/get` an element to/at specific index position has O(1) time complexity.
- To add at the end of the `ArrayList` it takes **O(1)** time complexity.
- Remove, or add at a specified index operations have O(n) time complexity.



The underlying issue

- The elements of an `ArrayList` are too tightly attached to them ■ Can we break the element storage apart into a structure?

