1. 
$$\int_{\frac{-x}{2}} x \sin 2x \, dx \text{ (by parts)}$$
$$\frac{-x}{2} \cos 2x + \frac{1}{4} \sin 2x + C$$

2. 
$$\int xe^{x^2} dx$$
 (by substitution)  
=  $\frac{1}{2}e^{x^2} + C$ 

3. 
$$\int xe^x dx \text{ (by parts)}$$
$$= xe^x - e^x$$

4. 
$$\int e^{x^2} dx$$
 (by integrand in a Taylor series)=  $1 + x^2 + \frac{1}{2}x^4\mathcal{O}(x^6)$   
 $x + \frac{x^3}{3} + \frac{x^5}{10} + C + \mathcal{O}(x^7)$ 

5. 
$$\int x\sqrt{1+x} \, dx$$
$$= \frac{2}{15}(1+x)^{\frac{3}{2}}(-2+3x) + C$$

6. 
$$\int \sec \theta \, d\theta = \ln (\sec \theta + \tan \theta) + C$$

7. 
$$\int \sec^2 \theta \, d\theta = 2 \frac{\sin \theta}{\cos \theta} + C$$

8. 
$$\int \operatorname{sech}^{2}(\theta) = \int \frac{1}{\cosh^{2}(\theta)} d\theta$$
$$= \frac{\sinh \theta}{\cosh \theta} + C$$

9. 
$$\int \frac{x^2 + 2}{7 - x^2} dx$$
$$= -x + \frac{9\sqrt{7}}{7} \arctan\left(\frac{x\sqrt{7}}{7}\right) + c$$

10. 
$$\int \frac{1}{ap - bp^2} dp$$
$$= \frac{\ln|p|}{a} - \frac{\ln|bp - a|}{a}$$