

# PGAS Data Structure for Unbalanced Tree-Based Algorithms at Scale

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# Outline

1 Motivation

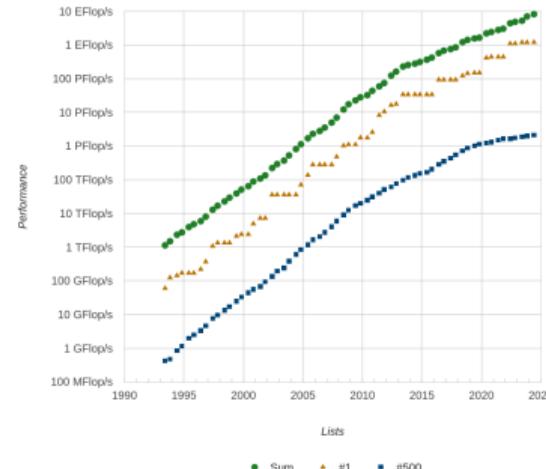
2 The DistBag\_DFS data structure

3 Experimental evaluation

4 Conclusions & Future works

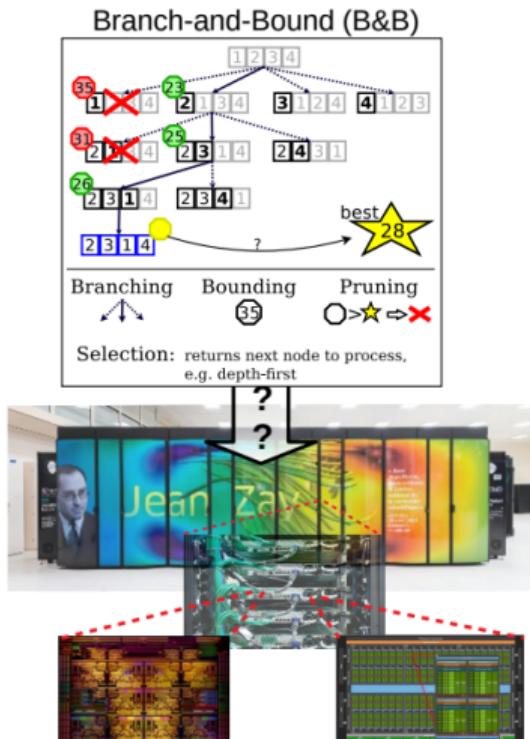
# Motivation

- Exascale era of computation;
- Increasingly large (millions of cores), heterogeneous (CPU-GPU, etc.), and less and less reliable (Mean Time Between Failures – MTBF < 1h) systems<sup>1</sup>;
- "Evolutionary approaches" (MPI+X) vs. "revolutionary approaches" (e.g., Partitioned Global Address Space (PGAS) -based environments).

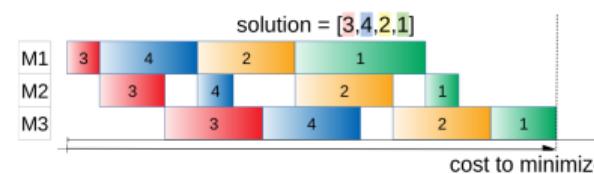


<sup>1</sup>Bi-annual TOP500 ranking, <https://www.top500.org/>.

# Motivation



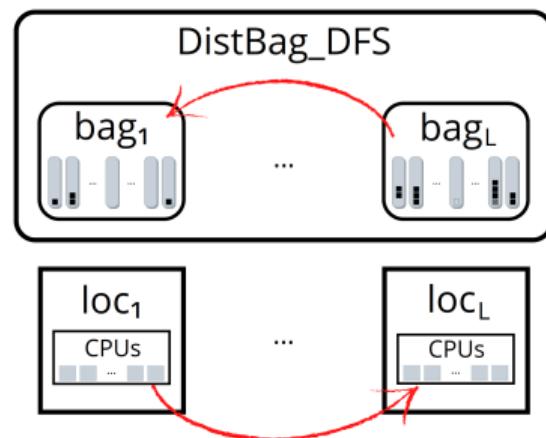
- Focus on parallel tree-search methods for solving combinatorial problems, e.g., Backtracking and Branch-and-Bound (B&B):
  - Large trees → efficient data structure
  - Irregular trees → efficient load balancing
- Motivating example: Permutation Flowshop Scheduling Problem (PFSP). Search trees for hard PFSP instances contain up to  $10^{15}$  explored nodes.



# Related work

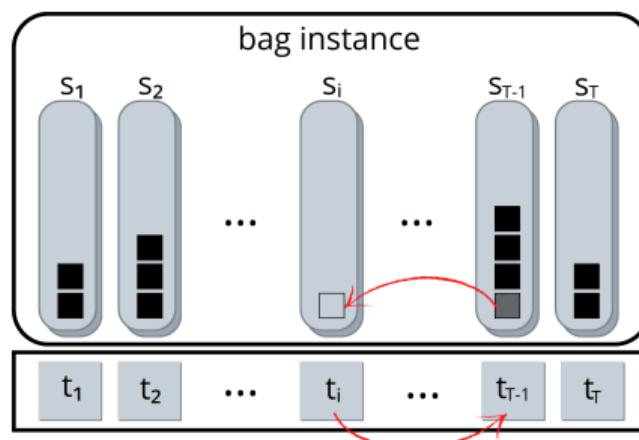
- Limitations of existing MPI+X data structures and load balancing for parallel tree-search algorithms, e.g. [1, 2]:
  - focus only on performance
  - combine low-level programming environments
- PGAS-based load balancing techniques also exist [3, 4, 5], but none in Chapel.
- In PGAS Chapel, we introduced the **DistBag\_DFS** distributed data structure [6], but ...
  - The description of the data structure could be extended
  - Load balancing mechanism not evaluated
  - Lack of performance evaluation at scale
  - Not included in the language (user-defined library)

# DistBag\_DFS's components: bag instances



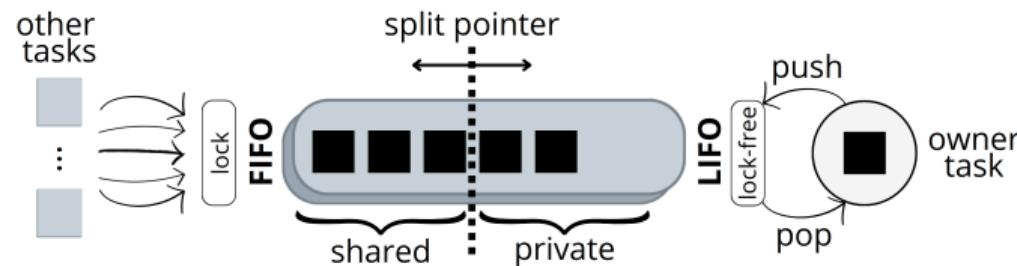
- One bag instance per Chapel *locales*  
→ Exploit inter-node level of parallelism
- Each bag instance maintains a multi-pool

# DistBag\_DFS's components: multi-pools



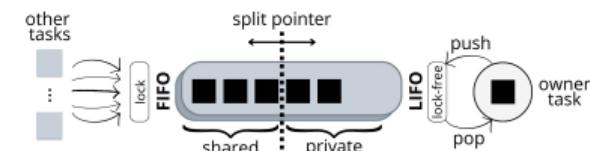
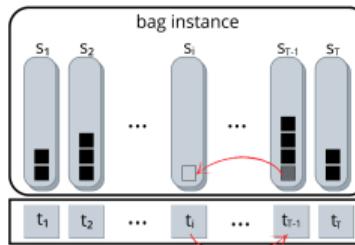
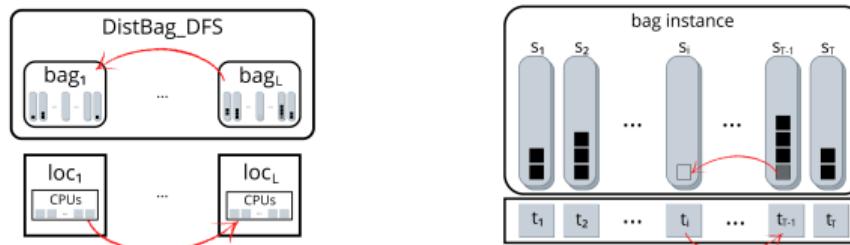
- One pool per Chapel *tasks*  
→ Exploit intra-node level of parallelism
- Each pool is indexed by a task ID  
→ Ensure DFS

# DistBag\_DFS's components: pools



- Non-blocking double-ended queues (deques) [7]
  - lock-free local access to the private portion
  - copy-free transfer between shared and private portions
- Dynamic-sized:  $1024 \times 2^k$

# DistBag\_DFS's components: dynamic load balancing



Dynamic Work Stealing (WS):

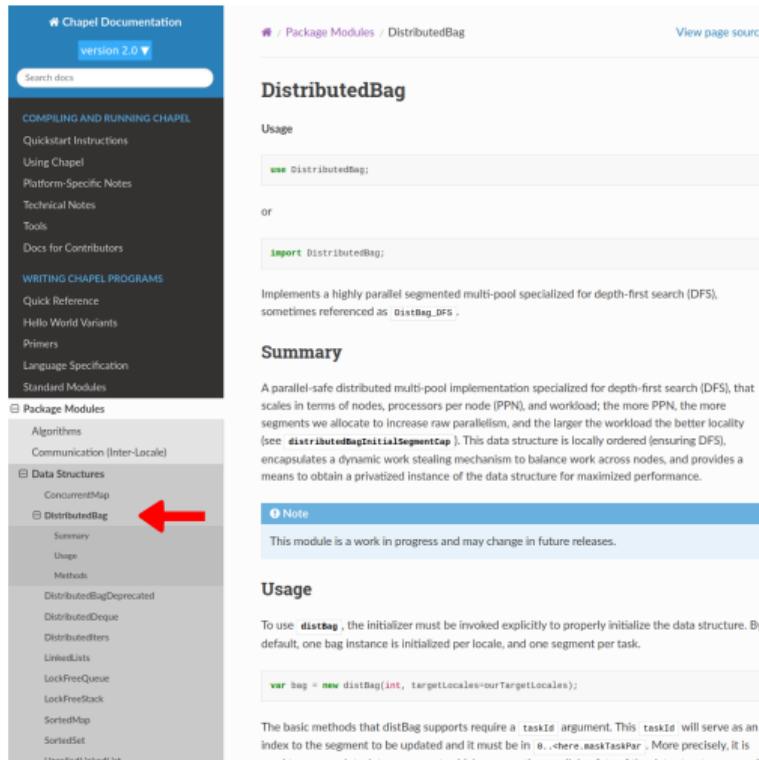
- Locality-aware: local, then global
- Random victim selection
- Steal-one strategy locally, steal-half otherwise

WS fails when all pools have been visited and no work has been stolen.

# DistBag\_DFS's user interface

- Two initialization variables: `eltType` and `targetLocales`
- Three local procedures:
  - `add`: insert an element
  - `addBulk`: insert elements in bulk
  - `remove`: remove an element (contains WS)
- Four global procedures:
  - `clear`: clear `DistBag_DFS`
  - `these`: iterate over `DistBag_DFS`
  - `contains`: check if a given element is in `DistBag_DFS`
  - `getSize`: get the global size of `DistBag_DFS`

# Integration to Chapel



The screenshot shows the Chapel Documentation website for version 2.0. The left sidebar contains navigation links for 'COMPILING AND RUNNING CHAPEL' (Quickstart Instructions, Using Chapel, Platform-Specific Notes, Technical Notes, Tools, Docs for Contributors) and 'WRITING CHAPEL PROGRAMS' (Quick Reference, Hello World Variants, Primers, Language Specification, Standard Modules). Under 'Standard Modules', 'Data Structures' is expanded, showing 'ConcurrentMap', 'DistributedBag' (which is highlighted with a red arrow), 'DistributedBagDeprecated', 'DistributedDeque', 'DistributedIterators', 'LinkedLists', 'LockFreeQueue', 'LockFreeStack', 'SortedMap', 'SortedSet', and 'UnorderedMap'. The main content area is titled 'DistributedBag' and includes sections for 'Usage' (code snippets: `use DistributedBag;` and `import DistributedBag;`), 'Description' (text: 'Implements a highly parallel segmented multi-pool specialized for depth-first search (DFS), sometimes referenced as `DistBag_DFS`.'), and 'Summary' (text: 'A parallel-safe distributed multi-pool implementation specialized for depth-first search (DFS), that scales in terms of nodes, processors per node (PPN), and workload; the more PPN, the more segments we allocate to increase raw parallelism, and the larger the workload the better locality (see `distributedBagInitialSegmentCap`). This data structure is locally ordered (ensuring DFS), encapsulates a dynamic work stealing mechanism to balance work across nodes, and provides a means to obtain a privatized instance of the data structure for maximized performance.'). A note at the bottom states: 'This module is a work in progress and may change in future releases.'

Released in Chapel 2.0 (March 2024) in the **DistributedBag** package module:



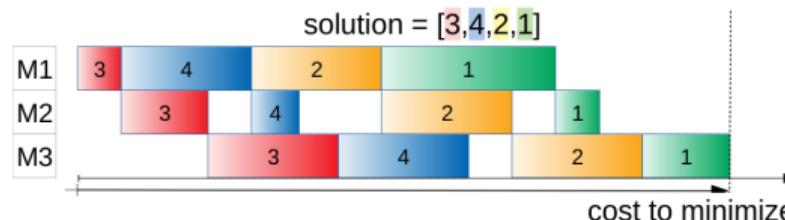
The screenshot shows the 'Usage' section of the 'DistributedBag' package module. It contains four numbered code snippets:

- 1 `use DistributedBag;`
- 2
- 3 `var bag = new distBag(int);`
- 4 `// your code ...`

# Experimental protocol

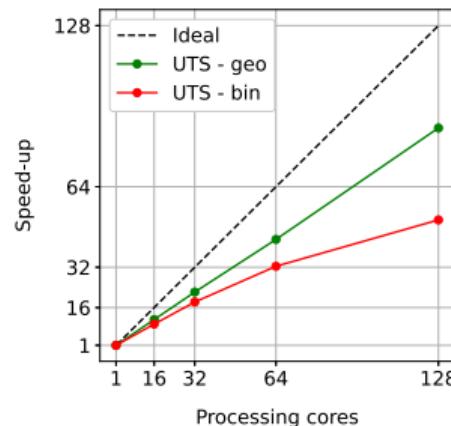
## ■ Applications:

- Backtracking applied to the Unbalanced Tree-Search (UTS) benchmark [8], with binary- and geometric-shaped trees
- B&B applied to the Permutation Flowshop Scheduling Problem (PFSP)



- Testbed: MeluXina - Cluster module (<https://docs.lxp.lu/>)
  - 400 compute nodes × 2 AMD EPYC Rome 7H12 64 cores @ 2.6 GHz CPUs and 512 GB of RAM;
  - InfiniBand HDR high-speed fabric.
- Chapel 1.31.0

# Speed-up solving UTS instances



- 68% of the ideal speed-up solving UTS-geo
- 40% more than UTS-bin
- High ratio of WS success

Fig. 1: Speed-up achieved solving geometrical and binomial synthetic UTS trees.

Inst.	Nb. of nodes ( $10^6$ )	Time (s)	nodes/s ( $10^3$ )	WS attempts (% success)
UTS-geo	171.1	37.38	4,577	48,433 (99.0%)
UTS-bin	131.7	37.11	3,548	1,473,048 (96.8%)

# Load balancing solving the UTS-bin instance

Workload distribution solving UTS-bin using 16, 32, 64, and 128 Chapel tasks:

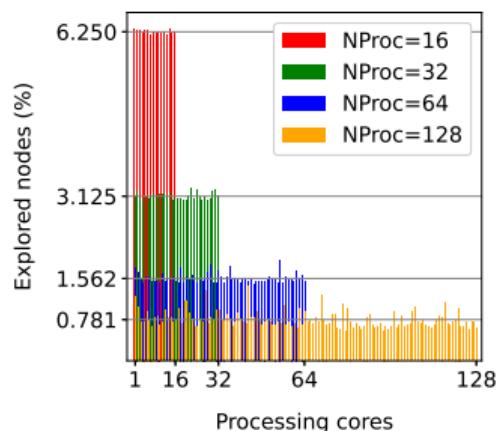


Fig. 2: Percentage of explored nodes per Chapel tasks solving the UTS-bin instance.

Even workload distribution for each experiment, i.e.,  $100/\text{NbTasks}$ .

# Strong scaling efficiency solving PFSP instances

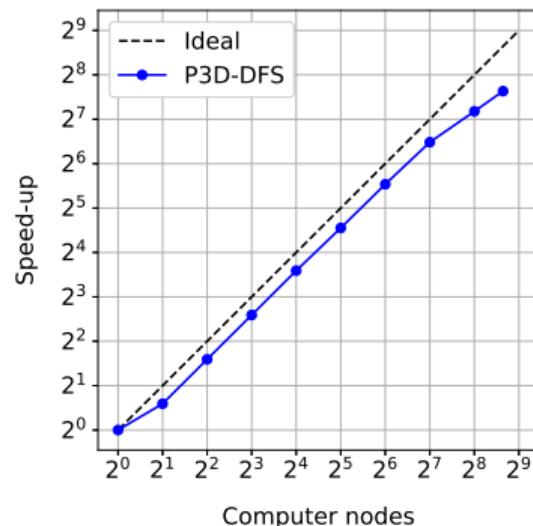


Fig. 3: Speed-up achieved solving **ta056**, compared to a multi-core version.

50% of strong scaling efficiency using 400 compute nodes (51,200 CPU cores) solving **ta056**

# Conclusions

In the context of tree-search methods for combinatorial problems:

- DistBag\_DFS provides high-level abstractions for unbalanced tree-search at scale
- 68% of the linear speed-up on a fine-grain backtracking application in single-node setting
- 50% of strong scaling efficiency using 400 compute nodes on a B&B application

# Future works

- Pursue **DistBag\_DFS** development:
  - Investigate ways to remove the required task ID in insertion/retrieval operations
  - Track its performance along Chapel's releases
  - Improve existing features and/or add new ones
  - Collect users feedbacks
- Further experiment **DistBag\_DFS**:
  - Solve unsolved PFSP instances
  - Solve other problems (e.g., 0/1-Knapsack)
  - Extend our **DistBag\_DFS**-based algorithms with a fault-tolerance mechanism

# References

- [1] T. Carneiro Pessoa, J. Gmys, F. H. de Carvalho Júnior, and et al., “GPU-accelerated backtracking using CUDA Dynamic Parallelism,” *Concurrency and Computation: Practice and Experience*, vol. 30, no. 9, p. e4374, 2018.
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- [3] J. Dinan, D. B. Larkins, P. Sadayappan, and et al., “Scalable Work Stealing,” in *Proceedings of the Conference on High Performance Computing Networking, Storage and Analysis*, Association for Computing Machinery, 2009.
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- [7] T. van Dijk and J. C. van de Pol, “Lace: Non-blocking Split Deque for Work-Stealing,” in *Euro-Par 2014: Parallel Processing Workshops*, pp. 206–217, 2014.
- [8] S. Olivier, J. Huan, J. Liu, and et al., “UTS: An Unbalanced Tree Search Benchmark,” in *Languages and Compilers for Parallel Computing*, pp. 235–250, 2007.

# Thank you for your attention.

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