### Rio 2016 Olympics Data Analysis

#### April 12, 2018

```
In [1]: #import statements for visualization and data analysis
        import pandas as pd
        import numpy as np
        from pandas import DataFrame as df
        import matplotlib.pyplot as plt
        from datetime import datetime
        from datetime import date
        import seaborn as sns
        import math
        import random
        from math import sqrt
        from scipy import stats
        from sklearn.svm import SVC
        from sklearn.model_selection import GridSearchCV
        import warnings
        warnings.filterwarnings("ignore")
        from mpl_toolkits.mplot3d import Axes3D
        from numpy.linalg import pinv
```

#### 0.1 Initialize Data

Import 'athletes.csv' and store the data in a DataFrame

```
In [2]: ath_data = pd.read_csv('athletes.csv', index_col=0)
    dobs = ath_data['dob'].values
    #calculates the person's age
    ages = []
    for i in range(dobs.size):
        dob = datetime.strptime((dobs[i]), '%m/%d/%Y')
        age = int((date.today()-dob.date()).days/365)
        ages.append(age)
    #appends the list of age to the existing DataFrame
    ath_data['age']=ages
    #appends the total amount of medals earned from an athlete to the DataFrame
    col_list=['gold', 'silver', 'bronze']
    ath_data['totals'] = ath_data[col_list].sum(axis=1)
```

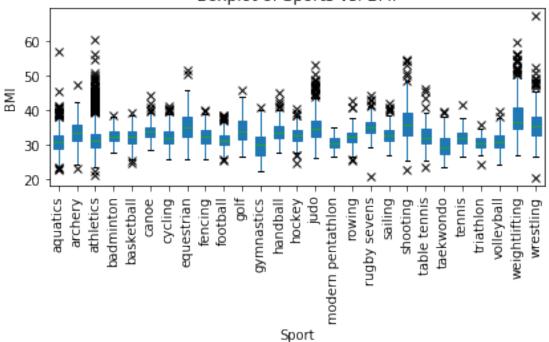
```
col_list = ['height', 'weight', 'age', 'sex']
physical=ath_data[col_list]
physical = physical[physical.height.notnull()]
physical = physical[physical.weight.notnull()]
physical['BMI'] = (physical[col_list].sum(axis=1))/(physical['height'])**2

col_list = ['height', 'weight']
physical2 = physical
physical2['sport'] = ath_data['sport']
```

# 1 Investigation 1: Comparing Mean BMI Across Gymnastics, Aquatics, and Weightlifting

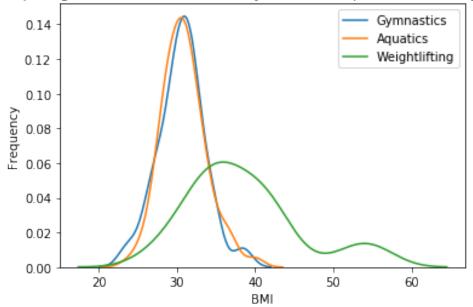
Is the mean height/weight distribution (i.e BMI) equal across aquatics, gymnastics, and weightlifting? If not, which sports have different means?

#### Boxplot of Sports vs. BMI



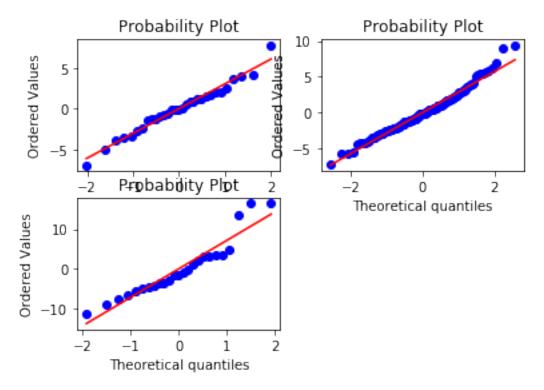
```
In [79]: #pulls respective Series of aq/gy/wl athletes of their BMIs
         gy = physical[physical['sport'] == 'gymnastics']['BMI']
         aq = physical[physical['sport']=='aquatics']['BMI']
         wl = physical[physical['sport'] == 'weightlifting']['BMI']
         sampleintgy = [random.randint(0, gy.shape[0]-1) for i in range(int(.1*gy.shape[0]))]
         sampleintaq = [random.randint(0, aq.shape[0]-1) for i in range(int(.1*aq.shape[0]))]
         sampleintwl = [random.randint(0, wl.shape[0]-1) for i in range(int(.1*wl.shape[0]))]
         gy = gy.iloc[sampleintgy]
         aq = aq.iloc[sampleintaq]
         wl = wl.iloc[sampleintwl]
         #density plot of BMI distribution
         sns.distplot(gy, hist=False, label='Gymnastics')
         sns.distplot(aq, hist=False, label='Aquatics')
         sns.distplot(wl, hist=False, label='Weightlifting')
         plt.xlabel('BMI')
         plt.ylabel('Frequency')
         plt.title("Comparing the BMI Distribution of Gymnastics, Aquatics, and Weightlifting"
         plt.show()
```

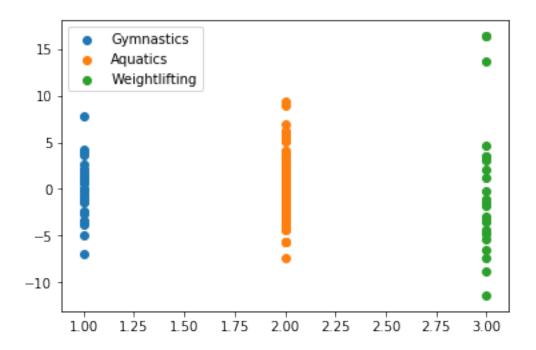
#### Comparing the BMI Distribution of Gymnastics, Aquatics, and Weightlifting



```
In [80]: print("n1 =", len(sampleintgy))
         print("n2 =", len(sampleintaq))
         print("n3 =", len(sampleintwl))
         n1 = len(sampleintgy)
         n2 = len(sampleintaq)
         n3 = len(sampleintwl)
         gy_sum = sum(gy)
         gy_sample_sq = gy**2
         gy_sum_sq = sum(gy_sample_sq)
         gy_avg = gy.mean()
         aq_sum = sum(aq)
         aq\_sample\_sq = aq**2
         aq_sum_sq = sum(aq_sample_sq)
         aq_avg = aq.mean()
         wl_sum = sum(wl)
         wl_sample_sq = wl**2
         wl_sum_sq = sum(wl_sample_sq)
         wl_avg = wl.mean()
         total_sum = gy_sum+aq_sum+wl_sum
n1 = 31
```

```
n2 = 139
n3 = 25
```





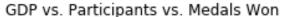
```
In [83]: ss_{total} = (gy_sum_sq+aq_sum_sq+wl_sum_sq) - ((total_sum)**2)/(n1+n2+n3)
       print("SS_total =", ss_total)
        print("SS_treatments =", ss_treat)
        ss_error = ss_total-ss_treat
       print("SS_error =", ss_error)
       ms_treat = ss_treat/2
       print("MS_treatments =", ms_treat)
       ms_error = ss_error/((n1+n2+n3)-2)
       print("MS_error =", ms_error)
       F0 = ms_treat/ms_error
       print("Test statistic =", F0)
SS_{total} = 3903.76623784
SS_{treatments} = 1272.7589348
SS_error = 2631.00730304
MS_treatments = 636.379467401
MS_error = 13.6321621919
Test statistic = 46.6822106752
In [84]: print("Gymnastics Average BMI:", gy_avg)
```

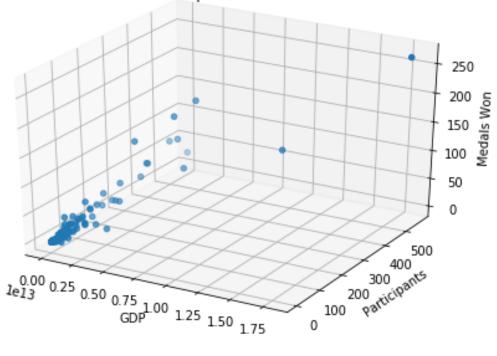
print("Aquatics Average BMI:", aq\_avg)
print("Weightlifting Average BMI:", wl\_avg)

```
LSD_gyaq = 1.972*sqrt(ms_error*(1/n1+1/n2))
        gyaq_diff = abs(gy_avg-aq_avg)
        print("Mean difference of average BMI between Gymnastics and Aquatics is", gyaq_diff)
        print("LSD of Gymnastics and Aquatics is", LSD_gyaq)
        LSD_gywl = 1.972*sqrt(ms_error*(1/n1+1/n3))
        gywl_diff = abs(gy_avg-wl_avg)
        print("Mean difference of average BMI between Gymnastics and Weightlifting is", gywl_
        print("LSD of Gymnastics and Weightlifting is", LSD_gywl)
        LSD_aqwl = 1.972*sqrt(ms_error*(1/n2+1/n3))
        aqwl_diff = abs(aq_avg-wl_avg)
        print("Mean difference of average BMI between Aquatics and Weightlifting is", aqwl_di
        print("LSD of Aquatics and Weightlifting is", LSD_aqwl)
Gymnastics Average BMI: 30.6090364501
Aquatics Average BMI: 30.8733894514
Weightlifting Average BMI: 38.4616688617
Mean difference of average BMI between Gymnastics and Aquatics is 0.264353001303
LSD of Gymnastics and Aquatics is 1.4461904740385871
Mean difference of average BMI between Gymnastics and Weightlifting is 7.85263241152
LSD of Gymnastics and Weightlifting is 1.9571875530052536
Mean difference of average BMI between Aquatics and Weightlifting is 7.58827941022
LSD of Aquatics and Weightlifting is 1.5817352834614762
```

### 1.1 INVESTIGATION 2: Determining Relationship Between GDP, Participants, and Medals Won

```
In [3]: ath_data_copy = ath_data
        country_data = pd.read_csv('countries.csv', index_col=0)
        country_data['gdp']=country_data['gdp_per_capita']*country_data['population']
        country_data = country_data.drop('gdp_per_capita', 1)
        country_data = country_data.rename(index = str, columns={"code":"nationality"})
        ath_data_copy = ath_data_copy.merge(country_data, on='nationality', how='left')
        ath_data_copy = ath_data_copy.sort_values(by='gdp')
        ath_data_copy = ath_data_copy[ath_data_copy.gdp.notnull()]
        gdp_data = ath_data_copy.groupby(by="gdp")['totals'].agg(['count', 'sum'])
        fig = plt.figure()
        ax = Axes3D(fig)
        ax.scatter(xs=gdp_data.index, ys= gdp_data['count'], zs=gdp_data['sum'], marker='o')
        ax.set_xlabel('GDP')
        ax.set_ylabel('Participants')
        ax.set_zlabel('Medals Won')
        plt.title("GDP vs. Participants vs. Medals Won")
        plt.show()
```





```
In [4]: n = len(gdp_data.index.values)
        x1 = gdp_data.index.values.reshape(n,1)
       x2 = gdp_data['count'].values.reshape(n,1)
       ones = np.ones((n, 1), dtype=int)
       X = np.concatenate((ones, x1, x2), axis=1)
        y = gdp_data['sum'].values.reshape(n,1)
       xtxinv = np.linalg.inv(np.dot(X.T, X))
        b = np.dot(np.dot(xtxinv, X.T), y)
        print("B0 =", b[0][0])
       print("B1 =", b[1][0])
        print("B2 =", b[2][0])
        print("Fitted Linear Regression Model: medals_pred = ", round(b[0][0], 3)," + ", b[1][
              "*Participants", sep='')
        SSE = np.dot(y.T, y)-np.dot(np.dot(b.T, X.T), y)
        sigmasq = SSE/(n-3)
        print("sigmasq =", sigmasq[0][0])
       C = np.linalg.inv(np.dot(X.T, X))
       b1_lower = b[1][0]-1.974*sqrt(sigmasq*C[1][1])
```

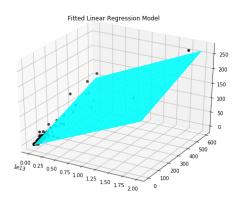
print("95% CI of B1 is [",b1\_lower, ",", b1\_upper, "].", sep='')

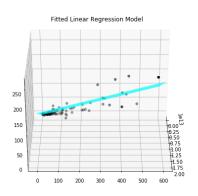
b1\_upper = b[1][0]+1.974\*sqrt(sigmasq\*C[1][1])

 $b2\_lower = b[2][0]-1.974*sqrt(sigmasq*C[2][2])$ 

```
print("95% CI of B2 is [",b2_lower, ",", b2_upper, "].", sep='')
        print("Therefore, because 0 is not included in either confidence intervals, both feature
         are statistically significant.")
        SST = SSE + np.dot(np.dot(b.T, X.T), y)
        print("R^2 = ", 1-(SSE/SST)[0][0])
        fig = plt.figure(figsize=(20,15))
        ax = fig.add_subplot(221, projection='3d')
        xx, yy = np.meshgrid(range(0, int(2e13), int(1e11)), range(600))
        z = b[0][0]+b[1][0]*xx+b[2][0]*yy
        ax.plot_surface(xx, yy, z, color='cyan', rstride=10, cstride=10, shade=False)
        ax.scatter(xs=gdp_data.index, ys= gdp_data['count'], zs=gdp_data['sum'], marker='o', c
        plt.title("Fitted Linear Regression Model")
        ax2 = fig.add_subplot(222, projection='3d')
        ax2.plot_surface(xx, yy, z, color='cyan', rstride=10, cstride=10, shade=False)
        ax2.scatter(xs=gdp_data.index, ys= gdp_data['count'], zs=gdp_data['sum'], marker='o',
        plt.title("Fitted Linear Regression Model")
        ax2.view_init(azim=360)
       plt.show()
B0 = -2.9481511314
B1 = 8.254217349e-12
B2 = 0.170736770254
Fitted Linear Regression Model: medals_pred = -2.948 + 8.254217349e-12*GDP + 0.171*Participant
sigmasq = 134.695368088
95% CI of B1 is [6.84841639149e-12,9.66001830651e-12].
95% CI of B2 is [0.148252468415,0.193221072094].
Therefore, because 0 is not included in either confidence intervals, both features (GDP and nu
R^2 = 0.880472589569
```

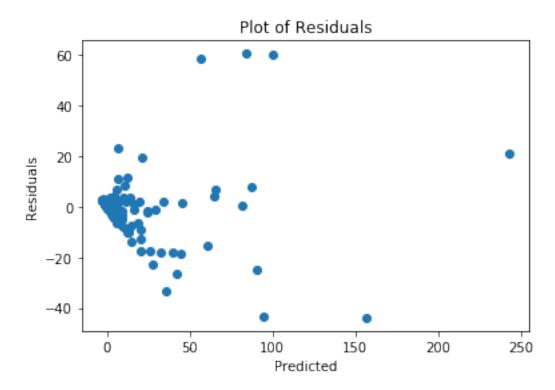
 $b2\_upper = b[2][0]+1.974*sqrt(sigmasq*C[2][2])$ 

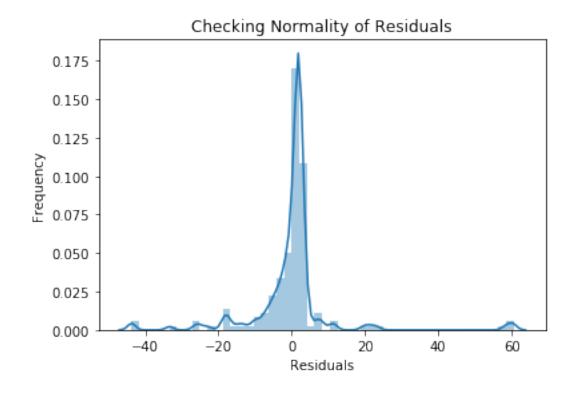


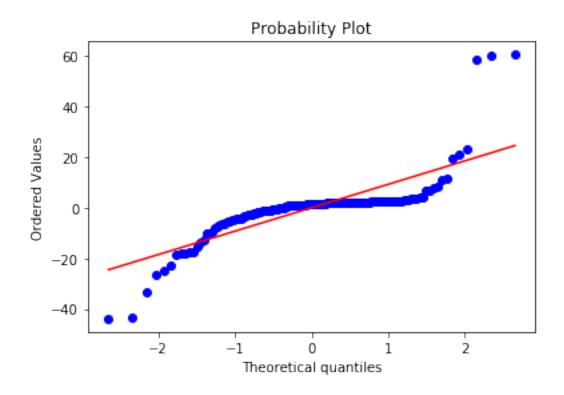


In [5]: 
$$yhat = b[0][0]+b[1][0]*x1+b[2][0]*x2$$
  
residuals = y-yhat

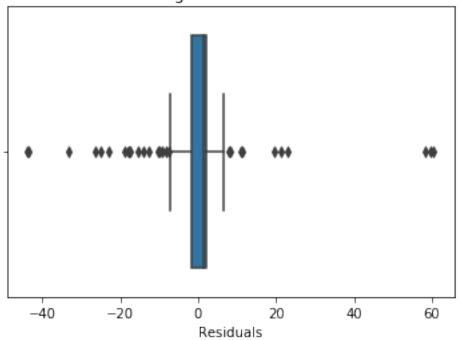
```
plt.scatter(yhat, residuals)
plt.title("Plot of Residuals")
plt.xlabel('Predicted')
plt.ylabel('Residuals')
plt.show()
sns.distplot(residuals, hist=True)
plt.title("Checking Normality of Residuals")
plt.xlabel("Residuals")
plt.ylabel("Frequency")
plt.show()
stats.probplot(residuals.T[0], plot=plt)
plt.show()
sns.boxplot(residuals)
plt.title("Detecting Outliers in Residuals")
plt.xlabel('Residuals')
plt.show()
```







### **Detecting Outliers in Residuals**

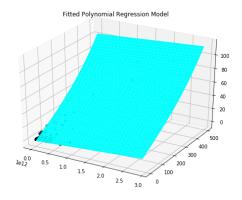


In [6]:  $y = y[\sim(residuals>5) \& \sim(residuals<-10)]$ 

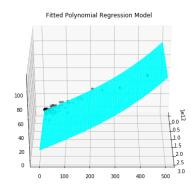
C = np.linalg.inv(np.dot(X.T, X))

```
n=len(y)
y = y.reshape(n, 1)
x1 = x1[\sim(residuals>5) \& \sim(residuals<-10)].reshape(n,1)
x2 = x2[~(residuals>5) \& ~(residuals<-10)].reshape(n,1)
z1 = (x2**3).reshape(n,1)
ones = np.ones((len(y), 1), dtype=int)
X = np.concatenate((ones, x1, x2, z1), axis=1)
xtxinv = np.linalg.inv(np.dot(X.T, X))
b = np.dot(np.dot(xtxinv, X.T), y)
for i in list(range(0,4)):
    print("B", i, " = ", b[i][0], sep='')
print("Fitted Polynomial Regression Model: medals_pred = ", round(b[0][0], 3)," + ", b
      "*Participants + ", b[3][0], "*Participants^3", sep='')
yhat = b[0][0]+b[1][0]*x1+b[2][0]*x2+b[3][0]*z1
residuals = y-yhat
SSE = np.dot(y.T, y)-np.dot(np.dot(b.T, X.T), y)
sigmasq = SSE/(n-3)
print("sigmasq =", sigmasq[0][0])
```

```
b_lower = b[i][0]-1.977*sqrt(sigmasq*C[i][i])
            b_upper = b[i][0]+1.977*sqrt(sigmasq*C[i][i])
            print("95% CI of B", i, " is [", b_lower, ",", b_upper, "].", sep='')
        print("Therefore, because 0 is not included in any confidence intervals, all features
        fig = plt.figure(figsize=(20,15))
        ax = fig.add_subplot(221, projection='3d')
        xx, yy = np.meshgrid(range(0, int(3e12), int(1e11)), range(500))
        z = b[0][0]+b[1][0]*xx+b[2][0]*yy+b[3][0]*(yy**3)
        ax.plot_surface(xx, yy, z, color='cyan', shade=False)
        plt.title("Fitted Polynomial Regression Model")
        ax.scatter(xs=x1, ys= x2, zs=y, marker='o', color='black')
        ax2 = fig.add_subplot(222, projection='3d')
        ax2.plot_surface(xx, yy, z, color='cyan', shade=False)
        ax2.scatter(xs=x1, ys= x2, zs=y, marker='o', color='black')
        plt.title("Fitted Polynomial Regression Model")
        ax2.view_init(azim=360)
       plt.show()
B0 = -1.69714550936
B1 = 3.69931707676e-12
B2 = 0.149460048144
B3 = 2.41768698958e-07
Fitted Polynomial Regression Model: medals_pred = -1.697 + 3.69931707676e-12*GDP + 0.149*Parti
sigmasq = 5.86699973489
95% CI of B1 is [7.767010926e-13,6.62193306092e-12].
95% CI of B2 is [0.135815345994,0.163104750294].
95% CI of B3 is [1.47978077257e-07,3.35559320659e-07].
Therefore, because 0 is not included in any confidence intervals, all features are statistical
```

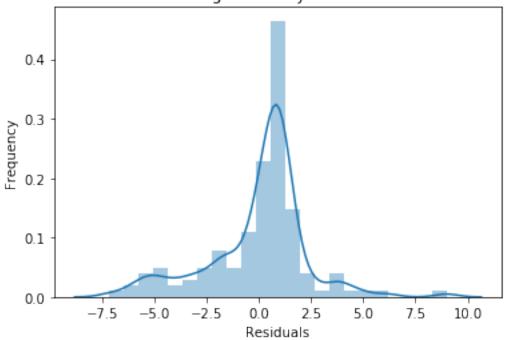


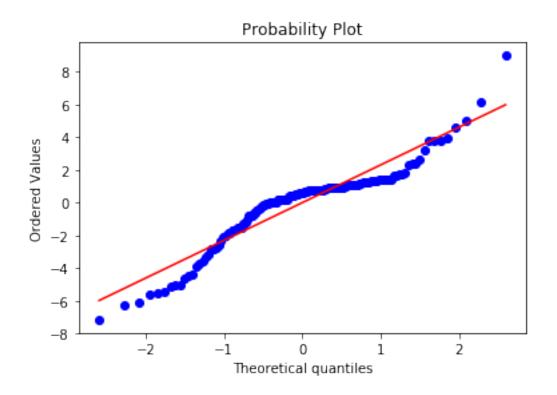
for i in list(range(1,4)):

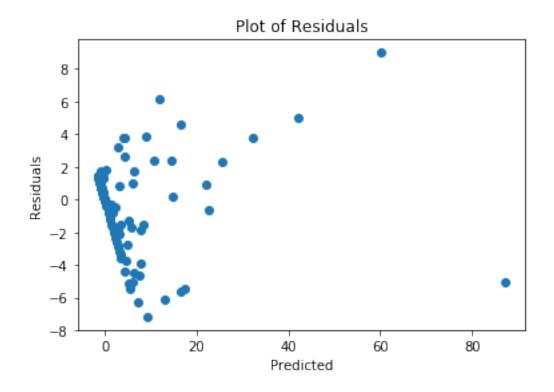


```
In [7]: sns.distplot(residuals, hist=True)
        plt.title("Checking Normality of Residuals")
        plt.xlabel("Residuals")
        plt.ylabel("Frequency")
        plt.show()
        stats.probplot(residuals.T[0], plot=plt)
        plt.show()
        plt.scatter(yhat, residuals)
        plt.title("Plot of Residuals")
        plt.xlabel('Predicted')
        plt.ylabel('Residuals')
        plt.show()
        sns.boxplot(residuals)
        plt.title("Detecting Outliers in Residuals")
        plt.xlabel('Residuals')
        plt.show()
```

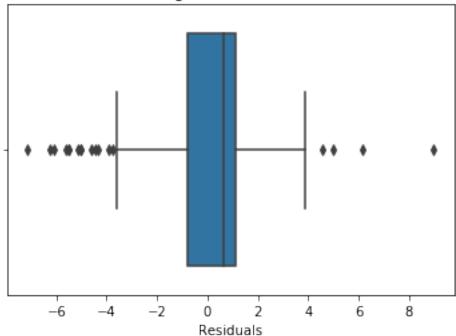
#### Checking Normality of Residuals





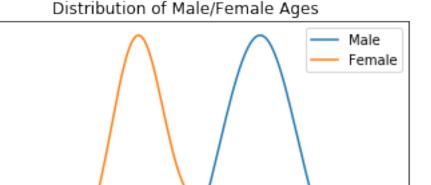






# 2 INVESTIGATION 3: Comparing Mean Age of Male/Female Medalists in Gymnastics

```
In [222]: gymnastics = ath_data[ath_data['sport'] == 'gymnastics']
          gymnastics_m = gymnastics[gymnastics['sex']=='male']
          gymnastics_f = gymnastics[gymnastics['sex']=='female']
          sampleintgy_m = [random.randint(0, gymnastics_m.shape[0]-1) for i in
              range(int(.5*gymnastics_m.shape[0]))]
          sampleintgy_f = [random.randint(0, gymnastics_f.shape[0]-1) for i in
              range(int(.5*gymnastics_f.shape[0]))]
          gymnastics_m = gymnastics_m.iloc[sampleintgy_m]
          gymnastics_f = gymnastics_f.iloc[sampleintgy_f]
          gymnastics_winners_m = gymnastics_m[gymnastics_m['totals']>0]['age']
          gymnastics_winners_f = gymnastics_f[gymnastics_f['totals']>0]['age']
          sns.distplot(gymnastics_winners_m, hist=False, label='Male')
          sns.distplot(gymnastics_winners_f, hist=False, label='Female')
          plt.title("Distribution of Male/Female Ages")
          plt.ylabel('Frequency')
          plt.show()
```



0.16

0.14

0.12

0.10

0.08

0.06

0.04

0.02

0.00

15

Average age of female gymnastics medalists: 21.85

20

Frequency

 $n_male = 11$ 

```
In [223]: gymnastics = ath_data[ath_data['sport'] == 'gymnastics']
          gymnastics_m = gymnastics[gymnastics['sex']=='male']
          gymnastics_f = gymnastics[gymnastics['sex']=='female']
          sampleintgy_m = [random.randint(0, gymnastics_m.shape[0]-1) for i in
              range(int(.5*gymnastics_m.shape[0]))]
          sampleintgy_f = [random.randint(0, gymnastics_f.shape[0]-1) for i in
              range(int(.5*gymnastics_f.shape[0]))]
          gymnastics_m = gymnastics_m.iloc[sampleintgy_m]
          gymnastics_f = gymnastics_f.iloc[sampleintgy_f]
          gymnastics_winners_m = gymnastics_m[gymnastics_m['totals']>0]['age']
          gymnastics_winners_f = gymnastics_f[gymnastics_f['totals']>0]['age']
          print("Average age of male gymnastics medalists:", gymnastics_winners_m.mean())
          print("Average age of female gymnastics medalists:", gymnastics_winners_f.mean())
          print("Standard deviation of ages of male gymnastics medalists:", gymnastics_winners
          print("Standard deviation of ages of female gymnastics medalists:", gymnastics_winne
          print("n_male =", gymnastics_winners_m.shape[0])
          print("n_female =", gymnastics_winners_f.shape[0])
Average age of male gymnastics medalists: 25.5454545455
```

25

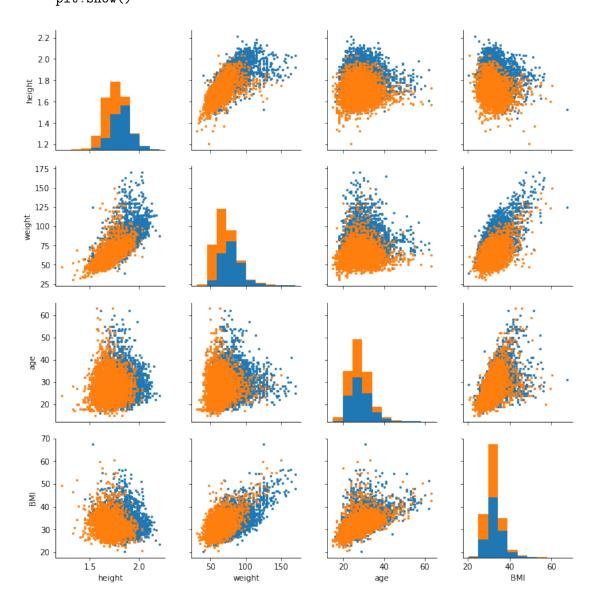
age

30

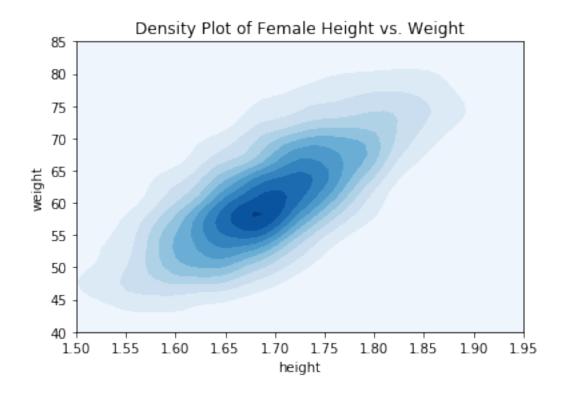
35

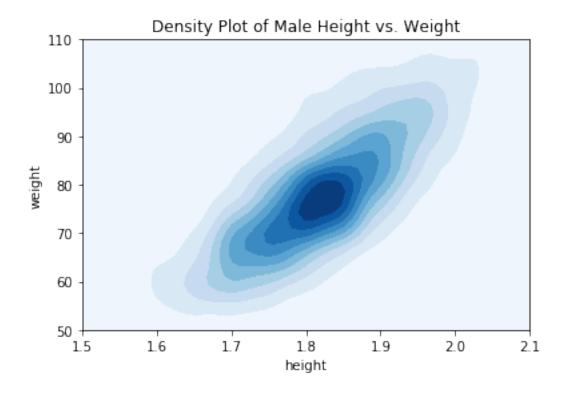
Standard deviation of ages of male gymnastics medalists: 2.65945995885 Standard deviation of ages of female gymnastics medalists: 3.54334067765

## 3 INVESTIGATION 4: Analyzing Heights/Weights Between Male/Female Athletes



```
In [89]: #plots density plot of female/male height vs. weight
    physical_f=physical[physical['sex']=='female']
    physical_m=physical[physical['sex']=='male']
    sns.kdeplot(physical_f.height, physical_f.weight, cmap="Blues", shade=True)
    plt.xlim(1.5, 1.95)
    plt.ylim(40, 85)
    plt.title('Density Plot of Female Height vs. Weight')
    plt.show()
    sns.kdeplot(physical_m.height, physical_m.weight, cmap="Blues", shade=True)
    plt.xlim(1.5, 2.1)
    plt.title('Density Plot of Male Height vs. Weight')
    plt.ylim(50,110)
    plt.show()
```



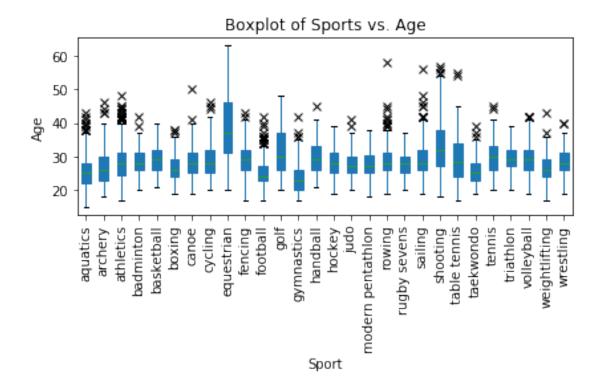


```
In [138]: male = physical[physical['sex']=='male']
          female = physical[physical['sex']=='female']
          sampleint m = [random.randint(0, male.shape[0]-1) for i in
              range(int(.5*male.shape[0]))]
          sampleint_f = [random.randint(0, female.shape[0]-1) for i in
             range(int(.5*female.shape[0]))]
          male = male.iloc[sampleint_m]
          female = female.iloc[sampleint_f]
          print("num_males = ", len(sampleint_m))
          print("num_females = ", len(sampleint_f))
          print("Male average height is ", male['height'].mean())
          print("Female average height is ", female['height'].mean())
          print("Male height standard deviation is ", male['height'].std())
          print("Female height standard deviation is ", female['height'].std())
num males = 2931
num_females = 2498
Male average height is 1.82363357216
Female average height is 1.69742994396
Male height standard deviation is 0.102126874276
Female height standard deviation is 0.0879301891154
In [139]: print("Male average weight is ", male['weight'].mean())
          print("Female average weight is ", female['weight'].mean())
```

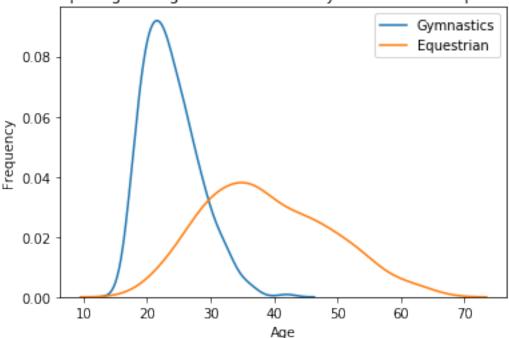
```
print("Male weight standard deviation is ", male['weight'].std())
print("Female weight standard deviation is ", female['weight'].std())
```

Male average weight is 79.9099283521 Female average weight is 62.5940752602 Male weight standard deviation is 15.646524449 Female weight standard deviation is 11.5126715776

## 4 INVESTIGATION 5: Comparing Variability of Ages of Equestrians and Gymnasts



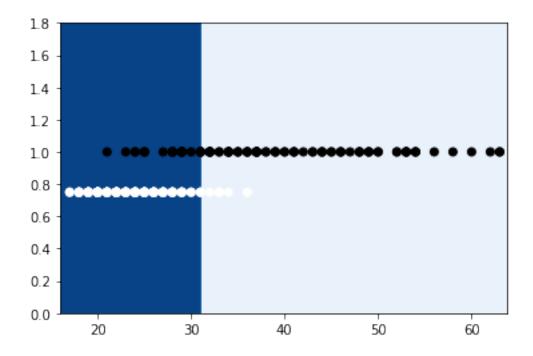
#### Comparing the Age Distribution of Gymnastics and Equestrian



```
print("Mean of gymnast ages is", gymnastics_age.mean())
         print("Mean of equestrian ages is", equestrian_age.mean())
         print("Standard deviation of gymnast ages is", gymnastics_age.std())
         print("Standard deviation of equestrian ages is", equestrian_age.std())
n_{gymnasts} = 162
n_{equestrians} = 111
Mean of gymnast ages is 23.5432098765
Mean of equestrian ages is 39.4234234234
Standard deviation of gymnast ages is 4.24424896301
Standard deviation of equestrian ages is 9.57415987252
In [63]: data = gymnastics.append(equestrian)
         sample_gym = [random.randint(0, gymnastics.shape[0]) for i in
             range(int(.8*gymnastics.shape[0]))]
         sample_test_gym = []
         for i in list(range(gymnastics.shape[0])):
             if i not in sample_gym:
                 sample_test_gym.append(i)
         train = data.iloc[sample_gym]
         ones = [1 for i in range(train.shape[0])]
         train['label'] = ones
         test = data.iloc[sample_test_gym]
         n1 = len(sample_test_gym)
         sample_eq = [gymnastics.shape[0]-1+random.randint(0, equestrian.shape[0]) for i in
             range(int(.8*equestrian.shape[0]))]
         sample_test_eq = []
         list_range = list(range(gymnastics.shape[0]-1, gymnastics.shape[0]-1+equestrian.shape
         for i in list_range:
             if i not in sample_eq:
                 sample_test_eq.append(i)
         eq_train = data.iloc[sample_eq]
         zeros = [0 for i in range(eq_train.shape[0])]
         eq_train['label']=zeros
         train = train.append(eq_train)
         eq_test = data.iloc[sample_test_eq]
         test = test.append(eq_test)
         param_grid = {'C': [1, 5, 10, 50], 'kernel': ['linear']},
         grid = GridSearchCV(SVC(), param_grid, cv=5, scoring='accuracy')
         grid.fit(train['age'].values.reshape(-1,1), train['label'])
         print("Best values of the parameters for the SVM are", grid.best_params_, "with an ac
         predict = grid.predict(test['age'].values.reshape(-1,1))
         h = 0.2
         x_{min}, x_{max} = min(test['age']) - 1, max(test['age']) + 1
         y_min, y_max = 0, 2
```

```
xx, yy = np.meshgrid(
    np.arange(x_min, x_max, h),
    np.arange(y_min, y_max, h))
Z = grid.predict(np.c_[xx.ravel()])
Z = Z.reshape(xx.shape)
plt.contourf(xx, yy, Z, cmap="Blues")
ones = [1 for i in range(test.shape[0])]
color= ['black' if l == 'equestrian' else 'white' for l in test['sport']]
vec = []
for i in list(range(test.shape[0])):
    if test['sport'].iloc[i] == 'gymnastics':
        vec.append(0.75)
    else:
        vec.append(1)
plt.scatter(test['age'].values, vec, c=color, cmap=plt.cm.Paired)
plt.figure
plt.show()
```

Best values of the parameters for the SVM are {'C': 10, 'kernel': 'linear'} with an accuracy of



### 5 INVESTIGATION 6: Comparing Proportion of Male and Female Medalists

```
In [56]: males = ath_data[ath_data['sex'] == 'male']
         females = ath_data[ath_data['sex'] == 'female']
         sampleint_m = [random.randint(0, males.shape[0]-1) for i in
             range(int(.5*males.shape[0]))]
         sampleint_f = [random.randint(0, females.shape[0]-1) for i in
             range(int(.5*females.shape[0]))]
         males = males.iloc[sampleint_m]
         females = females.iloc[sampleint_f]
         male_winners = males[males['totals']>0]
         female_winners = females[females['totals']>0]
        print("n_males =", males.shape[0])
         print("n_females =", females.shape[0])
         print("Proportion of male medalists:", male_winners.shape[0]/males.shape[0])
         print("Proportion of female medalists:", female_winners.shape[0]/females.shape[0])
n_{males} = 3166
n_females = 2602
Proportion of male medalists: 0.15476942514213518
Proportion of female medalists: 0.16986933128362797
```