

Chapter 9 – Additional Problems with Solution – Helpful for the Homework, and Chapter Quiz on Chapter 9**Problem 1:**

Suppose that you are taking a T/F exam and you have no idea at all about the answers to the last three questions. You choose answers randomly and therefore have a 50/50 chance of being correct on any one question.

- 1) What is the probability that you guessed right on exactly one of the three questions?
- 2) What is the probability that you guessed right on zero of the three questions?
- 3) What is the probability that you guessed right on at least two of the questions?

Solution:

- 1) Guessed right on 1st question, wrong on 2nd and 3rd question. Probability = $1/2 \times 1/2 \times 1/2 = 1/8$
Guessed right on 2nd question, wrong on 1st and 3rd question. Probability = $1/2 \times 1/2 \times 1/2 = 1/8$
Guessed right on 3rd question, wrong on 1st and 2nd question. Probability = $1/2 \times 1/2 \times 1/2 = 1/8$
Total Probability = $1/8 + 1/8 + 1/8 = 3/8$
- 2) Guessed wrong on 1st question. Probability = $1/2$
Guessed wrong on 2nd question. Probability = $1/2$
Guessed wrong on 3rd question. Probability = $1/2$
So, the probability that you guessed right on zero of the three questions = $1/2 \times 1/2 \times 1/2 = 1/8$
- 3) Guessed right on question 1 and question 2. Probability = $1/2 \times 1/2 \times 1/2 = 1/8$
Guessed right on question 2 and question 3. Probability = $1/2 \times 1/2 \times 1/2 = 1/8$
Guessed right on question 1 and question 3. Probability = $1/2 \times 1/2 \times 1/2 = 1/8$
Guessed right on question 1, question 2 and question 3. Probability = $1/2 \times 1/2 \times 1/2 = 1/8$
So, the overall probability = $1/8 + 1/8 + 1/8 + 1/8 = 1/2$

Problem 2:

How many numbers from 1-999 do NOT have any repeated digits?

Solution:

9 single digits

+ 9*9 double digits

+ 9*9*8 triple digits = **738**

Problem 3:

A certain college class has 100 students. The youngest is 20 years old, the oldest is 37. You want to make a bet that the class contains at least X students of the same age. How large can you make X and still be certain to win your bet?

Solution:

$N = \text{youngest age} = 20 \text{ years}$

$M = \text{eldest age} = 37 \text{ years.}$

So, $(M - N + 1) = (37 - 20 + 1) = 18$

Therefore, $X = \text{Ceiling}(100/18) = 6$

Problem 4:

Normal six-sided dice have a different number of pips (dots) on each face, from 1 to 6. You roll two such dice and add the result.

What is the probability of rolling 10+ (rolling 10 and higher than 10)?

Solution:

Combinations of pips for 10+ includes (4, 6) (4 pips on die 1, and 6 pips on die 2), (5, 5), (6, 4), (6, 5), (5, 6), (6, 6) – for a total of 6. The total possible combination of pips $= 6 \times 6 = 36$.

So, the probability of rolling 10+ $= 6 / 36 = 1 / 6$.