

# CS\_DE.R

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# ===== DIFFERENTIAL EQUATION =====
strain_Rates.01 <- function(Time, State, Parm){
  with(as.list(c(State, Parm)),{
    # function for calculating axial and lateral strain rates
    # Input must be in vector or matrix form, no data frames
    # Eqns. referenced from: SAND97-2601
    # CPar: EAT0, ETA1, ETA2, NF, AA1, PP, NSP, R1, R3, R4, QSR
    # FPar: KAP0, KAP1, KAP2, NK, DDT
    # TestData:

    # ---- Flow Potential Parameters (5) *KAP2 HELD CONST. ----
    # KAP0 <- as.numeric(FPar[1])
    # KAP1 <- as.numeric(FPar[2])
    # KAP2 <- as.numeric(FPar[3]) # Constant = 1
    # DDT <- as.numeric(FPar[4])
    # NK <- as.numeric(FPar[5])
    # ---- Creep Consolidation Parameters (11) *ETA2 HELD CONST
    # ETA0 <- as.numeric(CPar[1])
    # ETA1 <- as.numeric(CPar[2])
    # ETA2 <- 1 #as.numeric(CPar[3]) # Constant = 1
    # NF <- as.numeric(CPar[4])
    # AA1 <- as.numeric(CPar[5])
    # PP <- as.numeric(CPar[6])
    # NSP <- as.numeric(CPar[7])
    # R1 <- as.numeric(CPar[8])
    # R3 <- as.numeric(CPar[9])
    # R4 <- as.numeric(CPar[10])
    # QSR <- as.numeric(CPar[11])

    # ===== parameters hard coded into function directly =====
    KAP0 <- 10.119
    KAP1 <- 1.005
    DDT <- 0.896
    NK <- 1.331
    KAP2 <- 1

    ETA0 <- 0.102854 # -
    ETA1 <- 3.9387 # -
    ETA2 <- 1 # constant -
    NF <- 3.5122 # -
    AA1 <- 0.3147 # -
    PP <- 1.6332 # -
    NSP <- 0.557621 # -
    R1 <- 1.041 * 10 ^ -6 # [K/(MPa-sec)]
    R3 <- 15.1281 # -
    R4 <- 0.1677765 # -
    QSR <- 1077.46 # [K]
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# ---- Munson-Dawson Creep Parameters (17) ----
A1      <- 8.386e22
A2      <- 9.672e12
Q1R     <- 12581
Q2R     <- 5033
N1      <- 5.5
N2      <- 5.0
B1      <- 6.0856e6
B2      <- 3.034e-2
Q       <- 5335
S0      <- 20.57
M       <- 3
K0      <- 6.275e5
C       <- 9.198e-3
ALPHA   <- -17.37
BETA    <- -7.738
DELTA   <- 0.58
MU      <- 12400

# ==== parameters loaded into function =====
# ---- Values input into function (18) ----
# ICASE   <- as.numeric(parameters[,1]) # TEST TYPE (1:Hyd Cons;2:Shear Cons;3:compaction)
# ITEST  <- as.character(parameters[,2]) # TEST ID
# TIME    <- as.numeric(parameters[,3]) # TIME [SEC]
# DT      <- as.numeric(parameters[,4]) # DELTA TIME [SEC]
# TF      <- as.numeric(parameters[,5]) # TOTAL TEST TIME [SEC]
# TEMP    <- as.numeric(parameters[,6]) # TEMP [K]
# AS      <- as.numeric(parameters[,7]) # AXIAL STRESS [MPA]
# LS      <- as.numeric(parameters[,8]) # LATERAL STRESS [MPA]
# EVT     <- as.numeric(parameters[,9]) # TOTAL TRUE VOLUMETRIC STRAIN
# EVC     <- as.numeric(parameters[,10]) # CREEP TRUE VOLUMETRIC STRAIN
# EAT     <- as.numeric(parameters[,11]) # TOTAL TRUE AXIAL STRAIN
# EAC     <- as.numeric(parameters[,12]) # CREEP TRUE AXIAL STRAIN
# RHO     <- as.numeric(parameters[,13]) # CURRENT DENSITY [KG/M3]
# D       <- as.numeric(parameters[,14]) # FRACTIONAL DENSITY
# RHO0    <- as.numeric(parameters[,15]) # DENSITY AT THE START OF CONSOLIDATION (<RHOI)
# RHOI    <- as.numeric(parameters[,16]) # DENSITY AT THE START OF CREEP
# DD      <- as.numeric(parameters[,17]) # AVERAGE GRAIN SIZE [MM]
# W       <- as.numeric(parameters[,18]) # WATER CONENT BY PERCENT WEIGHT

# ---- fitting assumptions ----
RHOIS <- 2160.0 # ASSUMED IN SITU SALT DENSITY
DSP   <- 0.64   # FRACTIONAL DENSITY OF RANDOM DENSE SPHERICAL PARTICLES

# ---- interpolated input variables ----
TIME <- time.interp(Time)
TEMP <- temp.interp(Time)
AS   <- as.interp(Time)
LS   <- ls.interp(Time)
D    <- d.interp(Time)

# ---- calculate variables ----
MS <- (2.0 * LS + AS) / 3 # MEAN STRESS

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DS <- LS - AS                                # STRESS DIFFERENCE
# ELC <- (EVC - EAC) / 2                     # CREEP TRUE LATERAL STRAIN
DO <- 1382.4 / RHOIS                          # EMPLACED FRACTIONAL DENSITY (0.64 FRAC DENSITY)
DI <- RHOI / RHOIS                           # INITIAL FRACTIONAL DENSITY

# ==== this portion has been moved to lambda <- function() ====
#WT1 <- DT / NTIME    # WEIGHTING FUNCTION FOR CREEP CONSOLIDATION PARAMETERS
#WT    <- 1           # WEIGHTING FUNCTION FOR FLOW PARAMETERS
# =====

# Z1    <- yini[1] # Predicted axial strain (initial values)
# Z2    <- yini[2] # Predicted lateral strain (initial values)
# Z3    <- yini[3] # internal variable "xi" for the transient function (FU)
# integral of Eqn 2-27, (initial values)

# ==== define the differential equation ====
# DZ <- ifelse(cbind(TIME > 0, TIME > 0, TIME > 0),{
VOL    <- Z1 + 2*Z2                                # VOLUMETRIC STRAIN
VOLT   <- VOL + log(DSP/DI)                        # USED FOR INITIAL ESTIMATE OF VOLUMETRIC STRAIN
#DEN    <- DI/exp(VOL)                             # CURRENT FRACTIONAL DENSITY
DEN    <- D                                          # CURRENT FRACTIONAL DENSITY

# ifelse(D >= 1,{
# MD <- 0 # if fractional density is 1, dislocation creep = 0
# SP <- 0},# if fractional density is 1, pressure solutioning = 0
# {VAR <- ifelse(DEN <= DDT, DDT, DEN) # DEFINE DENSITY CEILING ISH

VAR <- ifelse(DEN <= DDT, DDT, DEN) # DEFINE DENSITY CEILING ISH

# ---- Equivalent Stress ----
OMEGAA <- ((1 - DEN) * NF / (1 - (1 - DEN)^(1/NF)))^NF^(2/(NF + 1))
OMEGAK <- ((1 - VAR) * NK / (1 - (1 - VAR)^(1/NK)))^NK^(2/(NK + 1))
ETA    <- ETA0 * OMEGAA^ETA1
KAP    <- KAP0 * OMEGAK^KAP1
TERMA  <- ((2 - DEN)/DEN)^((2 * NF)/(NF + 1))
TERMK  <- ((2 - DEN)/DEN)^((2 * NK)/(NK + 1))

# ---- Eqn. 2-3 (SAND97-2601) ----
# Equivalent stress measure for Disl. Creep and Press Sol'ing
SEQF   <- sqrt(ETA * MS^2 + ETA2 * TERMA * DS^2)
# Equivalent stress measure for Flow Potential
SEQ    <- sqrt(KAP * MS^2 + KAP2 * TERMK * DS^2)

# ---- Eqn. 2-17 (SAND97-2601) ----
ALPHA2 <- KAP * MS / 3
BETA2  <- KAP2 * TERMK * DS

# ---- Eqn. 2-20, WithOUT dislocation creep and pressure solutioning ----
F2A <- (ALPHA2 - BETA2)/SEQ    # fit to axial strains
F2L <- (ALPHA2 + 0.5 * BETA2)/SEQ # fit to lateral strains
F2V <- 3 * ALPHA2 / SEQ       # fit to volumetric strains

# ==== START: equivalent inelastic strain rate form for dislocation creep ====

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# ---- Steady State Strain Rate Calc ----
ES1 <- A1 * (SEQF / MU)^N1 * exp(-Q1R/TEMP) # Dislocation climb - Eqn. 2-30
ES2 <- A2 * (SEQF / MU)^N2 * exp(-Q2R/TEMP) # Undefined Mechanism - Eqn. 2-31

# Slip - Eqn. 2-32 (SAND98-2601)
H <- SEQF - S0 # HEAVISIDE FUNCTION
ARG <- Q * (SEQF - S0) / MU
ES3 <- ifelse(H > 0, 0.5 * (B1 * exp(-Q1R / TEMP) +
                           (B2 * exp(-Q2R / TEMP)) *
                           (exp(ARG) - exp(-ARG))),0)

ESS = ES1 + ES2 + ES3 # Steady-state strain rate, Eqn. 2-29 (SAND97-2601)

# ---- EVALUATE TRANSIENT FUNCTION, 3 branches: work hardening, equilibrium, recovery
EFT <- K0 * exp(C * TEMP) * (SEQF / MU) ^ M # Transient Strain Limit, Eqn. 2-28
BIGD <- ALPHA + BETA * log10(SEQF / MU) # Work-Hardening parameter, Eqn 2-28

# ---- add an event function ----

FU <- ifelse(Z3 == EFT, 1, ifelse(Z3 < EFT, exp(BIGD * (1 - Z3 / EFT) ^ 2),
                                exp(-DELTA * (1 - Z3 / EFT) ^ 2)))

MD <- FU * ESS # equivalent inelastic strain rate form for dislocation creep, Eqn 2-23

# ==== START: Equivalent Inelastic Strain Rate Form for Pressure Solutioning ====
# ---- Calculate initial volumetric strain - Based on spherical packing ----
CR <- abs(exp(VOLT) - 1)

# ---- Determine functional form - either large or small strains, Eqn 2-34 ----
GAMMA <- ifelse(CR <= 0.15, 1, abs((DO - exp(VOLT)) / ((1 - DO) * exp(VOLT))) ^ NSP)
# Small Strains (Vol Strain > - 15%)
# Large Strains (Vol Strain < - 15%)

# ---- component of eqn 2-35 ---
X3 <- exp((R3 - 1) * VOLT) / (abs(1 - exp(VOLT))) ^ R4

# ---- determine value of moisture function (w) ----
M2 <- ifelse (W == 0, 0, W ^ AA1)

# ---- Equivalent Inelastic Strain Rate Form for Pressure Solutioning, Eqn 2-35
G2 <- 1 / DD ^ PP # calculate grain size function
T2 <- exp(-QSR / TEMP) / TEMP
SP <- R1 * M2 * G2 * T2 * X3 * GAMMA * SEQF #})

DZ1 <- (MD + SP) * F2A # derivative: axial strain rate
DZ2 <- (MD + SP) * F2L # derivative: lateral strain rate
DZ3 <- (FU - 1) * ESS # derivative of internal variable "xi"

# cbind(DZ1, DZ2, DZ3)},{cbind(0,0,0)})

return(list(c(DZ1, DZ2, DZ3)))
})
}

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