Part I. (105 points) Do all calculations in R. All R code for the assignment should be included with the part of the problem it addresses (for code and output use a fixed-width font, such as Courier). Code is used to calculate result. Text is used to report and interpret results. Do not report or interpret results in the code. Also:

1. Clearly define population parameters in each problem. That is, give a verbal description of what the population mean is in the context of the problem.
2. Clearly specify hypotheses when appropriate (not every problem involves a test of hypothesis).
3. Write a coherent conclusion based on each CI or test.

(10^{pts}) **1. ET:** A 1997 survey conducted by M.I.T. reported that 16% of the 1,014 adults surveyed would be willing to support tax hikes to find extra-terrestrials.

    (a) (5 pts) Find a 95% CI for the proportion p of all adults that favor such a tax hike.

    (b) (5 pts) Suppose it was known that in 1990 that the proportion of all adults willing to support tax hikes to find extra-terrestrials was 0.2. Is there evidence that the proportion of adults in 1997 willing to spring for tax hikes for this purpose has changed since 1990? Carry out a test to answer this question. Use $\alpha = 0.05$.

(15^{pts}) **2. Side effects:** Prof. Ed Bedrick was involved in a study that examined the extent of side effects from using amphetamines to treat children with traumatic brain injuries. Prior information suggests that the probability of major side effects is very small, so it is of interest to estimate the maximum plausible value that the probability of major side effects might be. In the study none of the 15 children had major side effects.

    (a) (10 pts) Compute an exact upper 95% confidence bound for the probability of major side effects. Write a short conclusion to your analysis, interpreting the results of the exact bound in the context of the problem.

    (b) (5 pts) What would your reponse be to someone asking you to compute the bound based on the normal distribution, and why?

(25^{pts}) **3. Suicides:** The National Center for Health Statistics (NCHS) gave the following data on the distribution of suicides in the U.S. by month in 1990. Is there any evidence that the suicide rate varies monthly, or are the data consistent with the hypothesis that the rate is constant?

To simplify your analysis, assume the months have the same numbers of days. Compare the observed proportions across months qualitatively and through a formal goodness-of-fit test. Write a short and coherent summary to this problem. Make sure to include relevant graphical summaries with your presentation. The code below will create a data.frame for you to get started.

```
# read data from space delimited text
suicide <- read.table(text="
  Month  Suicides
  01Jan      1867
  02Feb      1789
  03Mar      1944
  04Apr      2094
  05May      2097
  06Jun      1981
  07Jul      1887
  08Aug      2024
  09Sep      1928
  10Oct      2032
  11Nov      1978
  12Dec      1859
", header=TRUE)
```

```
# show the structure of the data.frame
str(suicide)

## 'data.frame': 12 obs. of  2 variables:
##  $ Month   : Factor w/ 12 levels "01Jan","02Feb",..: 1 2 3 4 5 6 7 8 9 10 ...
##  $ Suicides: int  1867 1789 1944 2094 2097 1981 1887 2024 1928 2032 ...
```

(15$^{\text{pts}}$)   **4. Welsh and Breton:** The rising tide of national and regional loyalties around the world has bearing on the survival of minority or secondary languages. The article "Language Maintenance and Shift in a Breton and Welsh Sample," (Word, 1983; p. 67–88) describes one of the first comparative studies in this area. A random sample of 86 Welsh bilingual adults yielded 76 who spoke Welsh fluently, while another random sample of 77 bilingual adults from Brittany resulted in 57 who spoke Breton fluently. Both Welsh and Breton are southern Celtic in origin. Do these data support the conclusion that the true proportion of fluent speakers among Welsh bilingual adults differs from the corresponding proportion for Breton bilingual adults?

To answer this question, carry out an appropriate test at the 5% level, and quantify the difference in population proportions using a 95% CI.

(40$^{\text{pts}}$)   **5. Hawaiian blood:** There are four major blood groups in humans: O, A, B, and AB. A sample of individuals with records at the Blood Bank of Hawaii was selected. Each individual was classified according to blood type and ethnicity. The following two-way table of counts was obtained.

```
# read data from space delimited text
    # skip=3 skips the blank line, "Ethnicity" line, and "-----" line
blood <- read.table(text="
                             Ethnicity
                 -----------------------------------------------------
 Blood_Type    Hawaiian   Hawaiian_White   Hawaiian_Chinese   White
     O           1903          4469             2206          53759
     A           2490          4671             2368          50008
     B            178           606              568          16252
    AB             99           236              243           5001
", header=TRUE, skip=3)

# reshape into matrix for chisq.test()
blood.matrix <- matrix(c(blood[,2], blood[,3], blood[,4], blood[,5]),
                 ncol = 4, byrow = FALSE,
                 dimnames = list("Blood_type" = c("O", "A", "B", "AB"),
   "Ethnicity" = c("Hawaiian", "Hawaiian_White", "Hawaiian_Chinese", "White")))
```

(a) (15 pts) Summarize these data, focusing on comparing the proportions or percents in the 4 blood categories across the 4 ethnic groups.

Create a plot of each population's proportions (y) over blood type (x) to help determine how the populations differ. (You can calculate proportions, reshape the data, then plot the proportions on the same axes or using facets.)

(b) (15 pts) Is there evidence that blood type and ethnicity are associated in Hawaii? Explain.

(c) (10 pts) Carry out any additional analyses that you deem relevant, and summarize your findings. For example, there are a number of possible additional analyses that could be done here.
  - All six pairwise comparisons of blood type distributions between each pair of ethnicities.
  - Comparisons between pairs suggested by ethnicities, for example: (White, Hawaiian), (White, Hawaiian-White), (Hawaiian, Hawaiian-White), and (Hawaiian, Hawaiian-Chinese).
  - There are other sensible comparisons.

Then, in each of these, if you find significant differences between blood type proportions for a pair of ethnicities, you can continue to look at individual proportion comparisons (such as a two-sample proportion test of White vs Hawaiian blood type A).

You don't need to do tons of this. Do some amount of additional analysis to show that you understand the comparison principles. Then indicate (describe) some addition analyses that *could* be done.