

11-5-14 BCL

$$\underline{F} = \frac{\partial \chi_i}{\partial X_j} \underline{e}_i \otimes \underline{E}_j = \cancel{\chi_{ij}} \underline{e}_i \otimes \underline{E}_j$$

$$= \overset{e-E}{F_{ij}} \underline{e}_i \otimes \underline{E}_j$$

$$\underline{F}^T = \overset{e-E}{F_{ji}} \underline{e}_i \otimes \underline{E}_j = \overset{e-E}{F_{ij}} \underline{e}_j \otimes \underline{E}_i$$

$$\underline{U}^2 = \underline{F}^T \cdot \underline{F} = \overset{e-E}{F_{ij}} \underline{e}_j \otimes \underline{E}_i \cdot \overset{e-E}{F_{kl}} \underline{e}_k \otimes \underline{E}_l = \overset{e-E}{F_{ij}} \overset{e-E}{F_{ik}} \underline{e}_j \otimes \underline{E}_k$$

Say:  $\underline{1} = \alpha X_1 \underline{e}_1 + \beta X_2 \underline{e}_2 + X_3 \underline{e}_3 \Rightarrow$

$$d\underline{1} = \underline{F} \cdot d\underline{B} \Rightarrow \underline{F} = \overset{e-E}{F_{ij}} \underline{e}_i \otimes \underline{E}_j \Rightarrow \overset{e-E}{\begin{bmatrix} \alpha & 0 & 0 \\ 0 & \beta & 0 \\ 0 & 0 & 1 \end{bmatrix}}$$

$$\underline{F}^T = \overset{e-E}{F_{ij}} \underline{e}_j \otimes \underline{E}_i \Rightarrow \overset{e-E}{\begin{bmatrix} \alpha & 0 & 0 \\ 0 & \beta & 0 \\ 0 & 0 & 1 \end{bmatrix}}$$

all indices

$$\underline{U}^2 = \underline{F}^T \cdot \underline{F} = \overset{e-E}{F_{ij}} \overset{e-E}{F_{ik}} \underline{e}_j \otimes \underline{E}_k = \overset{e-E}{U_{jk}} \underline{e}_j \otimes \underline{E}_k =$$

$$\begin{array}{ccc} \downarrow \sum & \downarrow \sum & \downarrow \sum \\ \begin{bmatrix} \alpha & 0 & 0 \\ 0 & \beta & 0 \\ 0 & 0 & 1 \end{bmatrix} & \Rightarrow & \begin{bmatrix} \alpha^2 & 0 & 0 \\ 0 & \beta^2 & 0 \\ 0 & 0 & 1^2 \end{bmatrix} \Rightarrow \underline{U}^2, \text{ this is what I did} \end{array}$$

↓  
Σ on the "i" index