The purpose of this assignment is to construct model problems related to heat conduction that illustrate several concepts discussed in class. For problems 2 to 4 you are asked to construct model problems different from those provided in the notes or in class.

- 1. Provide a written summary of the relevant theory. Be sure to include definitions of terms.
- 2. Provide (i) the data to problems that provide smooth solutions (of class  $C^{\infty}$ ) and (ii) the solutions(if they exist) that illustrate
  - (a) two well posed problems, one with Drichlet and one with mixed boundary conditions, and
  - (b) an ill-posed problem. Show explicitly why it is ill-posed.
- 3. Provide the data and the solution for a problem where the solution is strong but not of class  $C^2$ .
- 4. Provide the data and the solution for a problem where the solution is weak.
- 5. Provide one set of boundary conditions and the forcing function consistent with a manufactured solution of your choice for which the conductivity is given by

$$K^{A}(x) = K_{0}^{A} + (K_{1}^{A} - K_{0}^{A})H[x - a] + K_{2}^{A} \sin\left(\frac{\pi x}{2L}\right)$$

$$K_{0}^{A}, K_{1}^{A} \text{ and } K_{2}^{A} - \text{constants}$$

Sketch  $K^A$  and Q as functions of x.