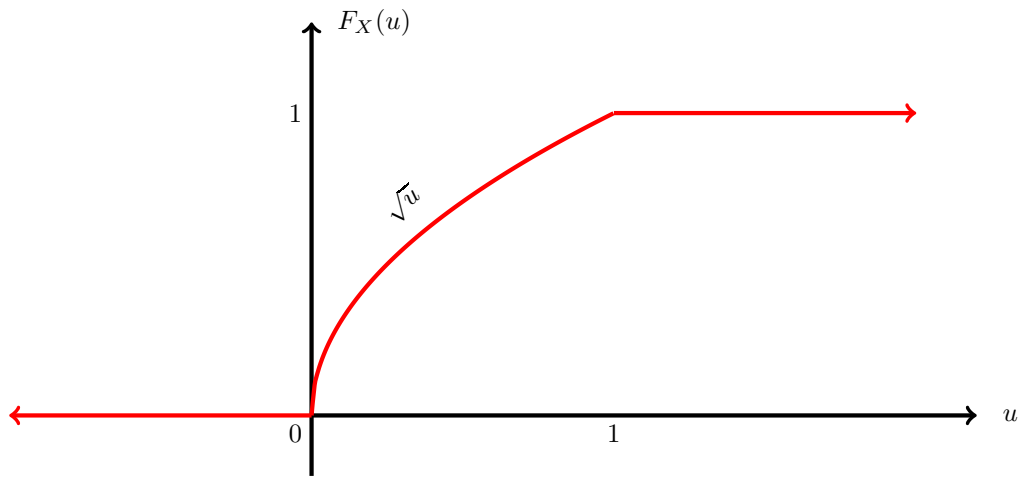
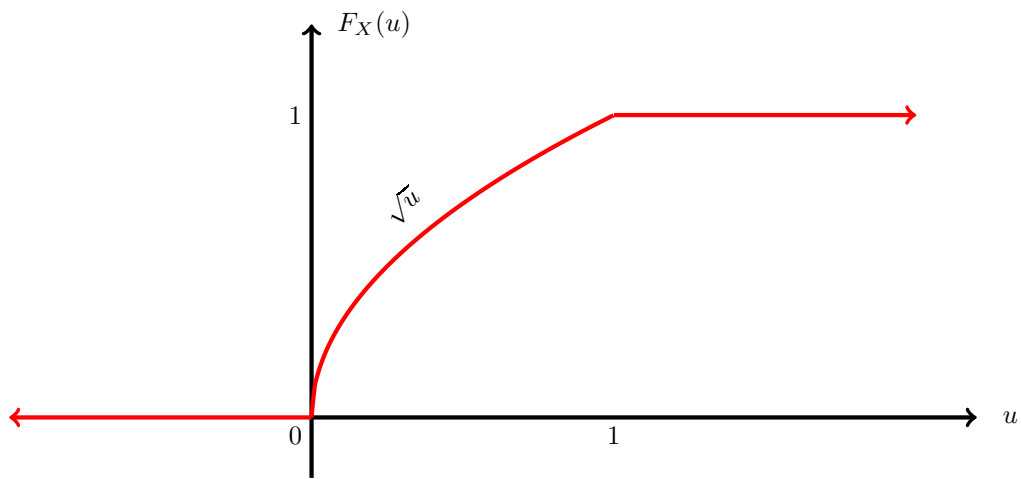


Let X be a random variable, whose cumulative distribution function equals \sqrt{u} in the interval $[0, 1]$, as shown below. If $Y = 6 - 9X$, then what is the CDF of Y evaluated at 5 ?



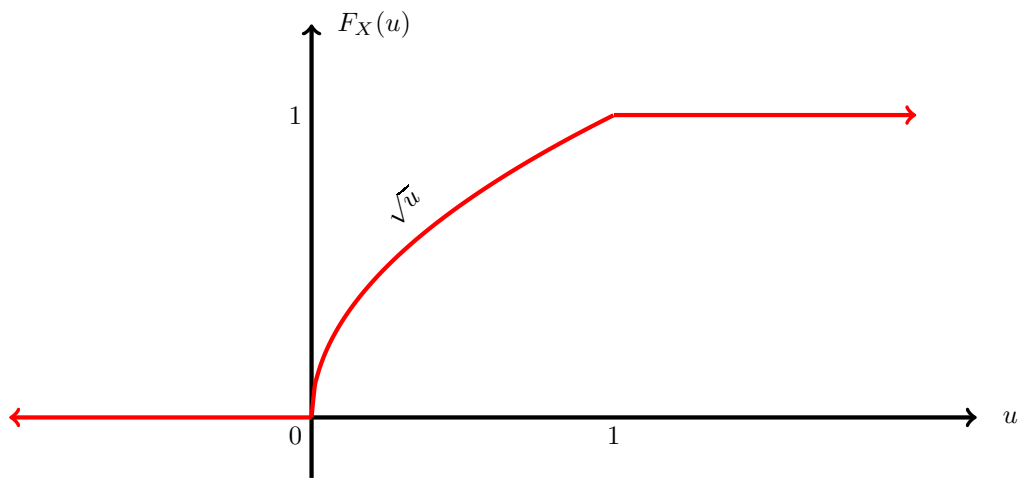
- (a) $2/3$
- (b) $1/3$
- (c) $\sqrt{5}$
- (d) $1/\sqrt{5}$
- (e) $1/15$
- (f) $1/9$
- (g) 0
- (h) 1
- (i) $1/2$
- (j) None of these

Let X be a random variable, whose cumulative distribution function equals \sqrt{u} in the interval $[0, 1]$, as shown below. If $Y = 7 - 16X$, then what is the CDF of Y evaluated at 6 ?



- (a) $3/4$
- (b) $1/4$
- (c) $\sqrt{6}$
- (d) $1/\sqrt{6}$
- (e) $1/23$
- (f) $1/16$
- (g) 0
- (h) 1
- (i) $1/2$
- (j) None of these

Let X be a random variable, whose cumulative distribution function equals \sqrt{u} in the interval $[0, 1]$, as shown below. If $Y = 8 - 25X$, then what is the CDF of Y evaluated at 7 ?



- (a) $4/5$
- (b) $1/5$
- (c) $\sqrt{7}$
- (d) $1/\sqrt{7}$
- (e) $1/33$
- (f) $1/25$
- (g) 0
- (h) 1
- (i) $1/2$
- (j) None of these

Solution:

If $A > 0$, then

$$\begin{aligned}F_Y(u) &= P(B - Ax \leq u) \\&= P(x \geq (B - u)/A) \\&= 1 - F_X((B - u)/A) \\&= 1 - \sqrt{(B - u)/A}.\end{aligned}$$

This requires $(B - u)/A \in [0, 1]$.

If $(B - u)/A = 1/k^2$, then $F_Y(u) = (k - 1)/k$.