

# Area\_based\_analysis

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## 1. Data Loading and Preprocessing

### 1.1 Edge Data

### 1.2 Surface Data

### 1.3 Calibration Wafer Data

### 1.4 Calibration Surface Data

## 2. Surface Area Distribution Analysis

## 3. Edge Area Distribution Analysis

## 4. Calibration Wafer Analysis - Edge

## 5. Calibration Surface Analysis

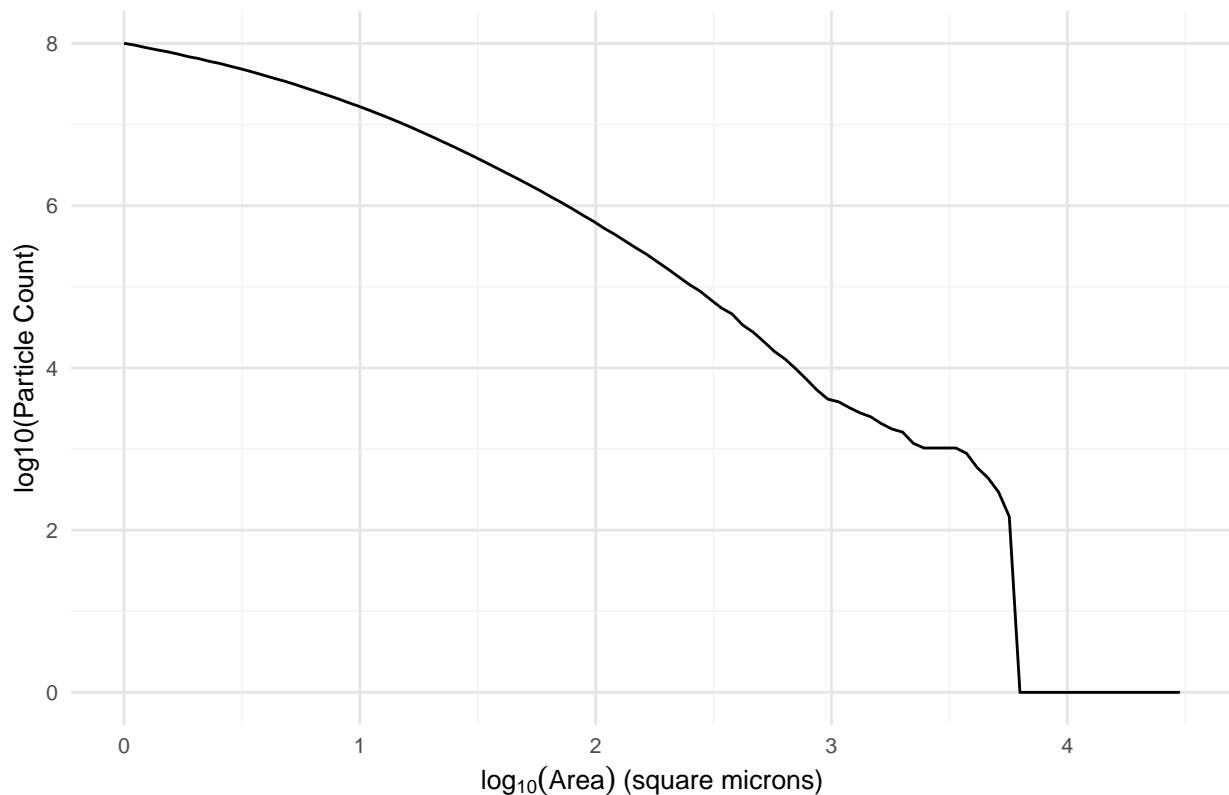
## 6. Edge Model Analysis

## 7. Straight Line Model (SLSM and SLCM)

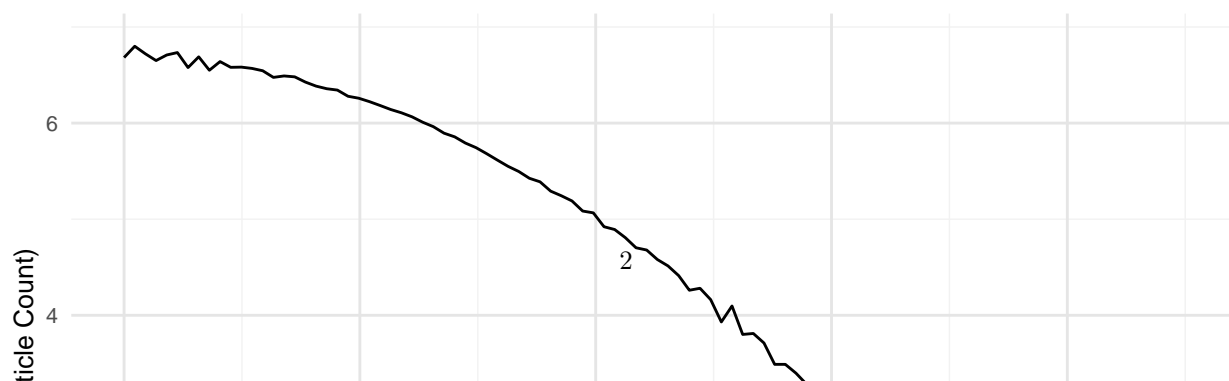
## 8. Trial Analysis

### 8.1 Trial 9

#### Surface Analysis 9: Cumulative Particle Area Distribution over 0.1 square meter

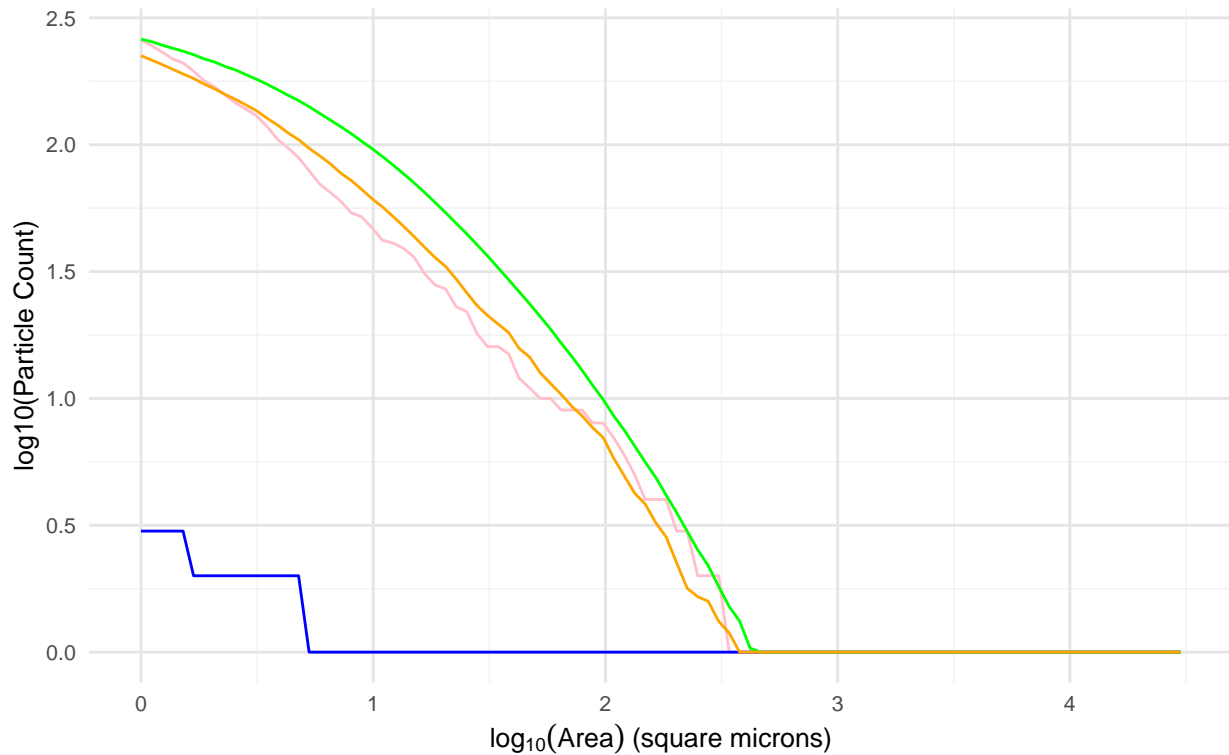


#### Surface Analysis 9: Binned Particle Size Distribution over 0.1 square meters



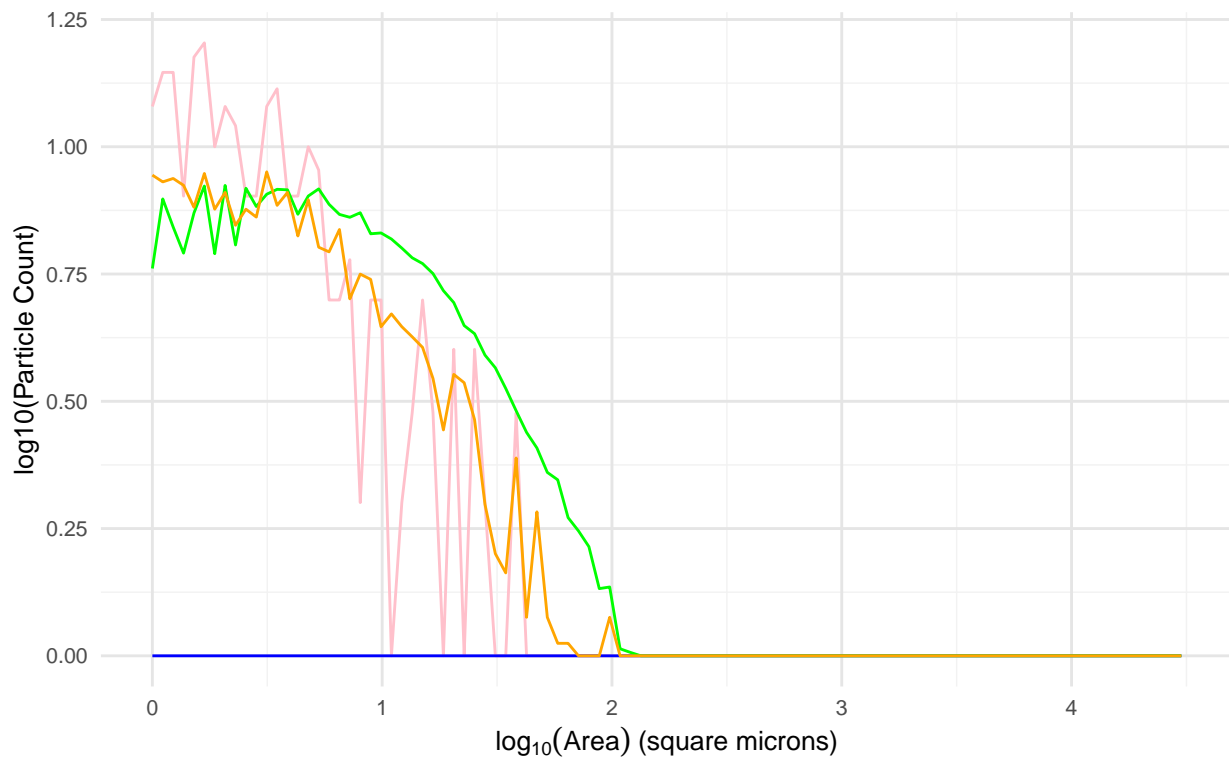
### Edge Analysis 9: Cumulative Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model, Orange: SLSM Starshade



### Edge Analysis 9: Cumulative Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model, Orange: SLSM Starshade



## Trial 9 Edge Distribution Analysis Results

```

##
## 1. Correlation Analysis:

##               comparison pearson_r      p_value
## cor Starshade Observed vs Calibration Observed 0.7027197 3.674915e-16
## cor1      Starshade Observed vs Model 0.9941039 2.254190e-96
## cor2      Starshade Observed vs SLSM Starshade 0.9973604 1.924980e-113
## cor3      Calibration Observed vs Model 0.6331472 1.569586e-12
## cor4      Calibration Observed vs SLSM Starshade 0.6735214 1.616574e-14
## cor5      Model vs SLSM Starshade 0.9972677 1.041258e-112

##
## 2. Kolmogorov-Smirnov Test Results:

##               comparison ks_statistic      p_value
## D Starshade Observed vs Calibration Observed 0.51 1.011651e-11
## D1      Starshade Observed vs Model 0.10 6.993742e-01
## D2      Starshade Observed vs SLSM Starshade 0.04 9.999982e-01
## D3      Calibration Observed vs Model 0.52 3.611663e-12
## D4      Calibration Observed vs SLSM Starshade 0.50 2.777589e-11
## D5      Model vs SLSM Starshade 0.06 9.937649e-01

##
## 3. Root Mean Square Error Between Distributions:

##               comparison      rmse
## 1 Starshade Observed vs Calibration Observed 1.07333580
## 2      Starshade Observed vs Model 0.16901537
## 3      Starshade Observed vs SLSM Starshade 0.06837033
## 4      Calibration Observed vs Model 1.21696978
## 5      Calibration Observed vs SLSM Starshade 1.10196579
## 6      Model vs SLSM Starshade 0.13266971

##
## 4. Regression Analysis for Each Distribution:

##               source      slope intercept r_squared      p_value
## log_area Starshade Observed -0.62147529 2.1990516 0.8991446 1.285514e-50
## log_area1 Calibration Observed -0.06477496 0.2019875 0.3950164 2.546405e-12
## log_area2      Model -0.68339436 2.4479841 0.9030513 1.851215e-51
## log_area3      SLSM Starshade -0.63532983 2.2429598 0.8907273 6.559785e-49

## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 4 x 2
##   source      auc
##   <chr>      <dbl>
## 1 Calibration Observed 0.247
## 2 Model 4.10
## 3 SLSM Starshade 3.66
## 4 Starshade Observed 3.60

## [1] "\n6. Distribution Summary Statistics:\n"

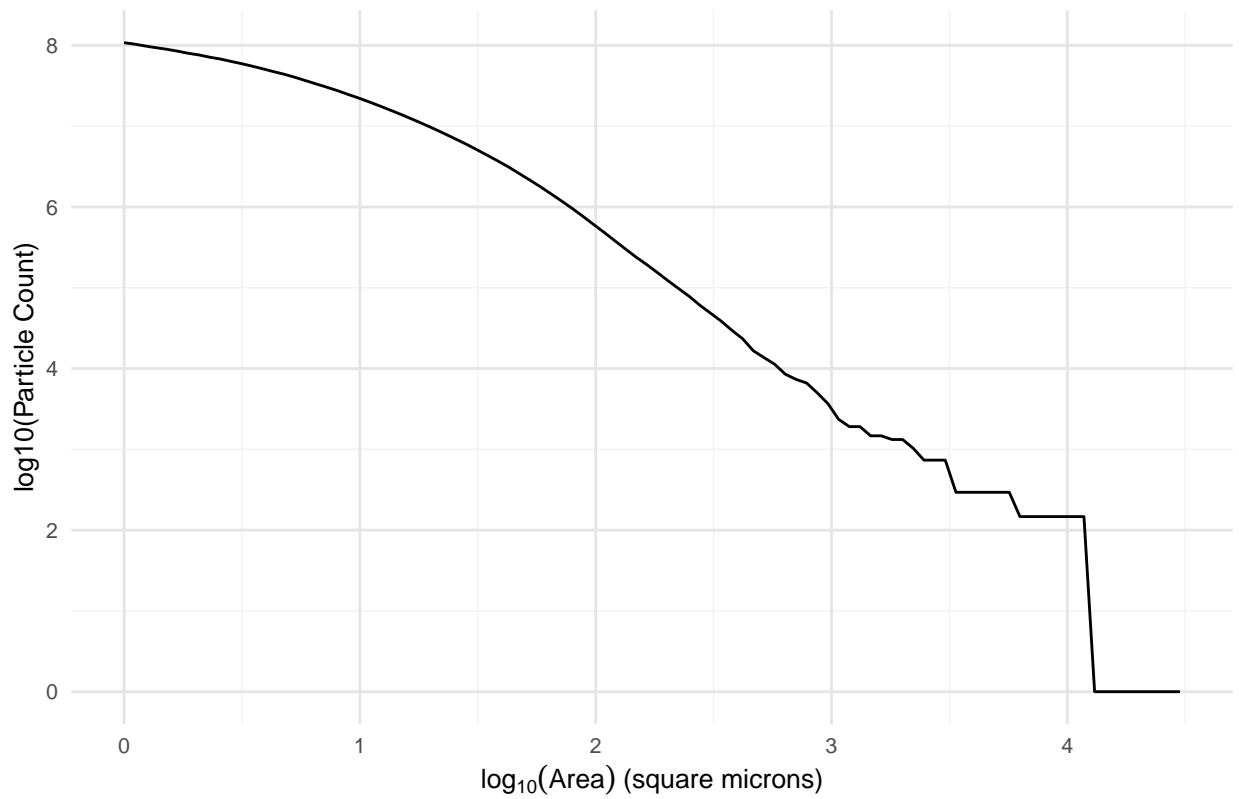
## # A tibble: 4 x 6
##   source      mean_log_count median_log_count sd_log_count min_log_count
##   <chr>      <dbl>      <dbl>      <dbl>      <dbl>
## 1 Calibration Observ~ 0.0570      0      0.135      0
## 2 Model 0.918      0.654      0.944      0

```

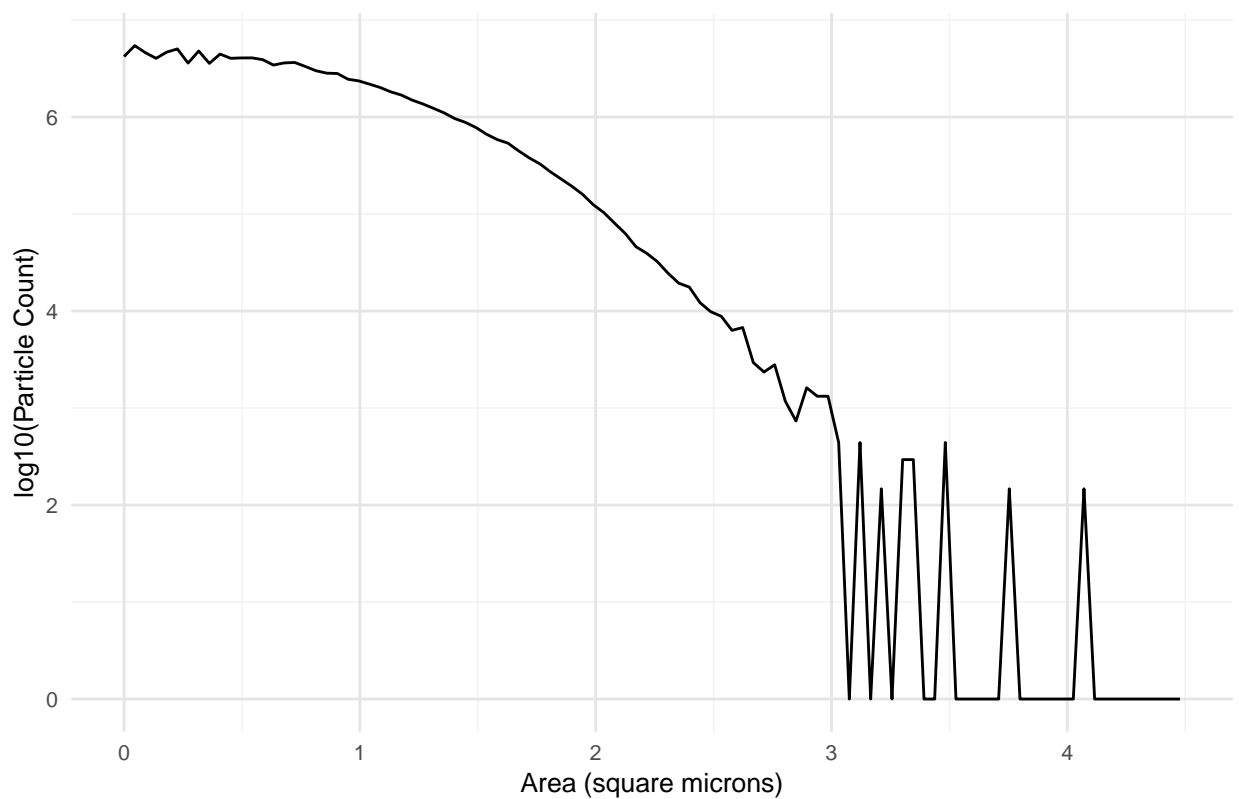
## 3 SLSM Starshade	0.821	0.482	0.883	0
## 4 Starshade Observed	0.808	0.602	0.860	0
## # i 1 more variable: max_log_count <dbl>				

## 8.2 Trial 10

### Surface Analysis 10: Cumulative Particle Area Distribution over 0.1 square meter

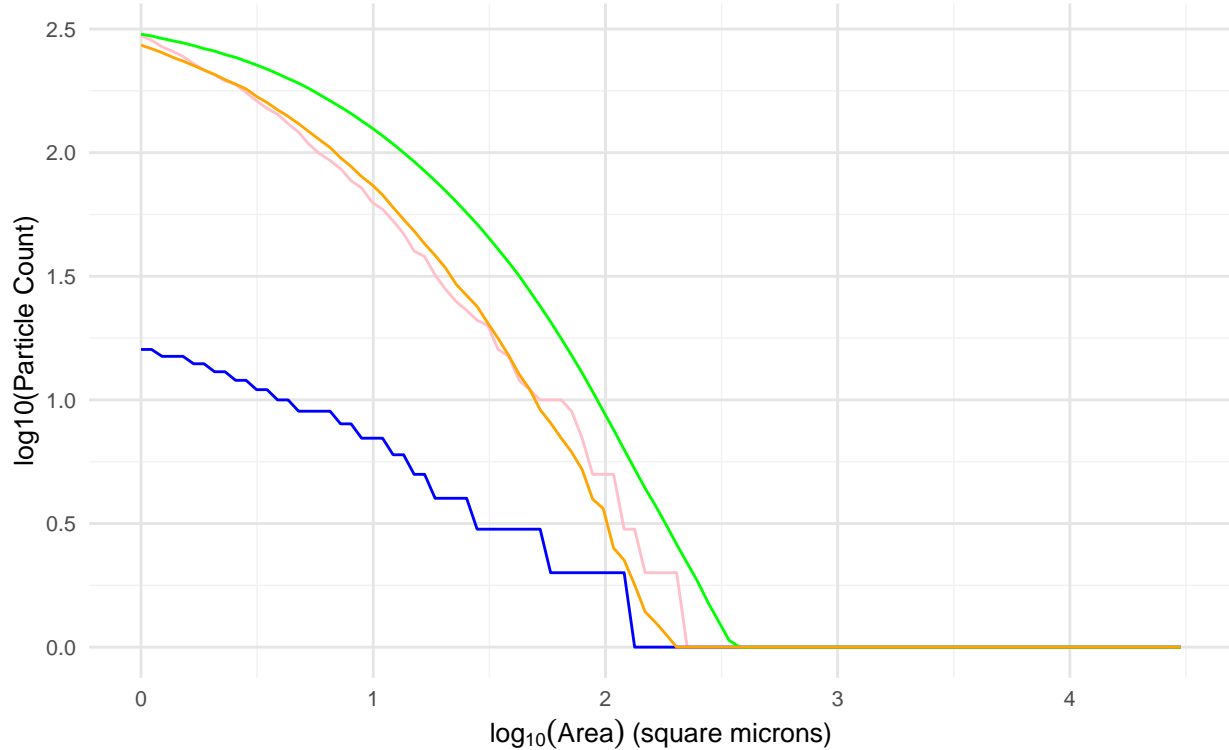


### Surface Analysis 10: Binned Particle Size Distribution over 0.1 square meters



### Edge Analysis 10: Cumulative Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model, Orange: SLSM Starshade



### Edge Analysis 10: Cumulative Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model, Orange: SLSM Starshade



## Trial 10 Edge Distribution Analysis Results

```

##
## 1. Correlation Analysis:

##               comparison pearson_r      p_value
## cor  Starshade Observed vs Calibration Observed 0.9923160 9.350211e-91
## cor1          Starshade Observed vs Model 0.9912269 6.030821e-88
## cor2      Starshade Observed vs SLSM Starshade 0.9965625 7.881738e-108
## cor3      Calibration Observed vs Model 0.9737756 7.992211e-65
## cor4      Calibration Observed vs SLSM Starshade 0.9838473 4.943497e-75
## cor5          Model vs SLSM Starshade 0.9973955 9.980779e-114

##
## 2. Kolmogorov-Smirnov Test Results:

##               comparison ks_statistic      p_value
## D  Starshade Observed vs Calibration Observed      0.34 1.908033e-05
## D1          Starshade Observed vs Model      0.09 8.127483e-01
## D2      Starshade Observed vs SLSM Starshade      0.06 9.937649e-01
## D3      Calibration Observed vs Model      0.41 1.001244e-07
## D4      Calibration Observed vs SLSM Starshade      0.36 4.705150e-06
## D5          Model vs SLSM Starshade      0.12 4.675586e-01

##
## 3. Root Mean Square Error Between Distributions:

##               comparison      rmse
## 1 Starshade Observed vs Calibration Observed 0.65600409
## 2          Starshade Observed vs Model 0.20110698
## 3      Starshade Observed vs SLSM Starshade 0.08328987
## 4      Calibration Observed vs Model 0.81652691
## 5      Calibration Observed vs SLSM Starshade 0.64818000
## 6          Model vs SLSM Starshade 0.17726385

##
## 4. Regression Analysis for Each Distribution:

##               source      slope intercept r_squared      p_value
## log_area  Starshade Observed -0.6502636 2.260122 0.8648647 2.206654e-44
## log_area1 Calibration Observed -0.3047132 1.041860 0.8289008 2.367129e-39
## log_area2          Model -0.7143903 2.539565 0.8857097 5.935652e-48
## log_area3      SLSM Starshade -0.6353298 2.242960 0.8907273 6.559785e-49

## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 4 x 2
##   source      auc
##   <chr>      <dbl>
## 1 Calibration Observed 1.60
## 2 Model 4.20
## 3 SLSM Starshade 3.66
## 4 Starshade Observed 3.58

## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 4 x 6
##   source      mean_log_count median_log_count sd_log_count min_log_count
##   <chr>      <dbl>      <dbl>      <dbl>      <dbl>
## 1 Calibration Observ~ 0.360      0      0.439      0
## 2 Model 0.940      0.533      0.996      0

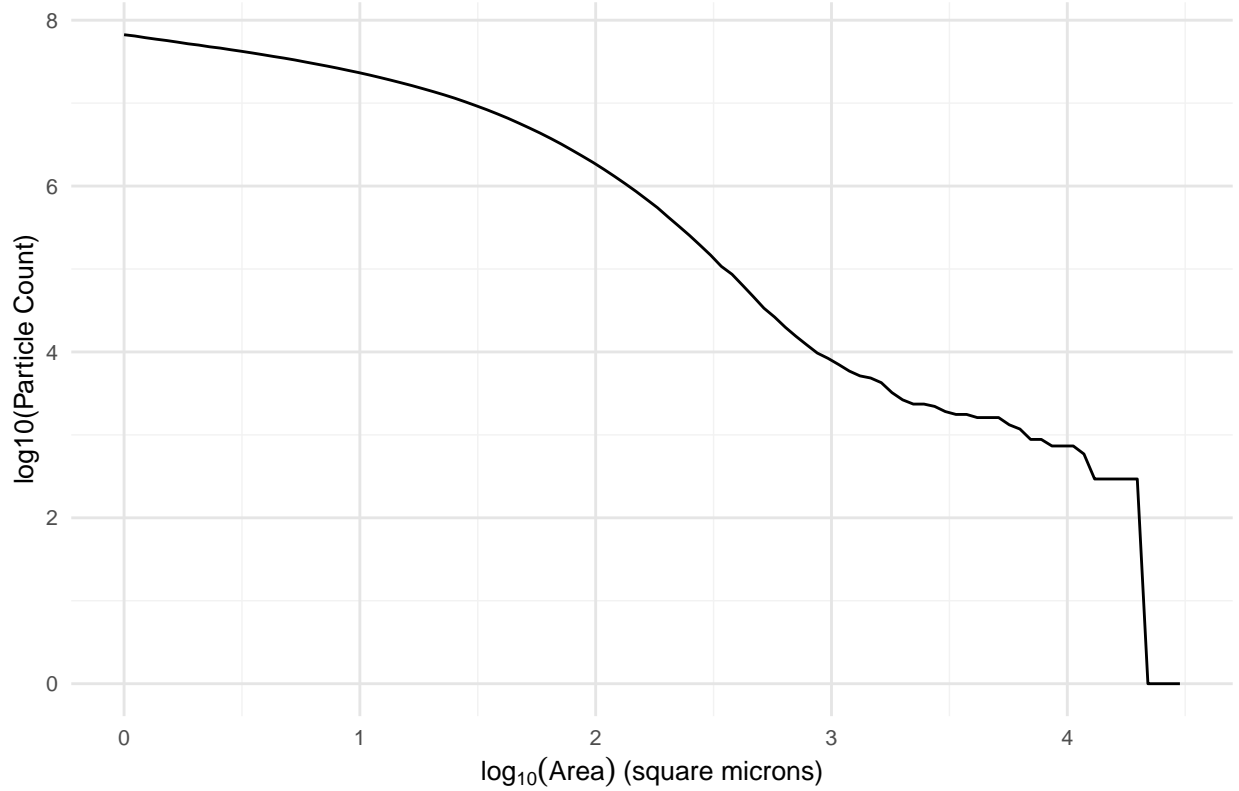
```



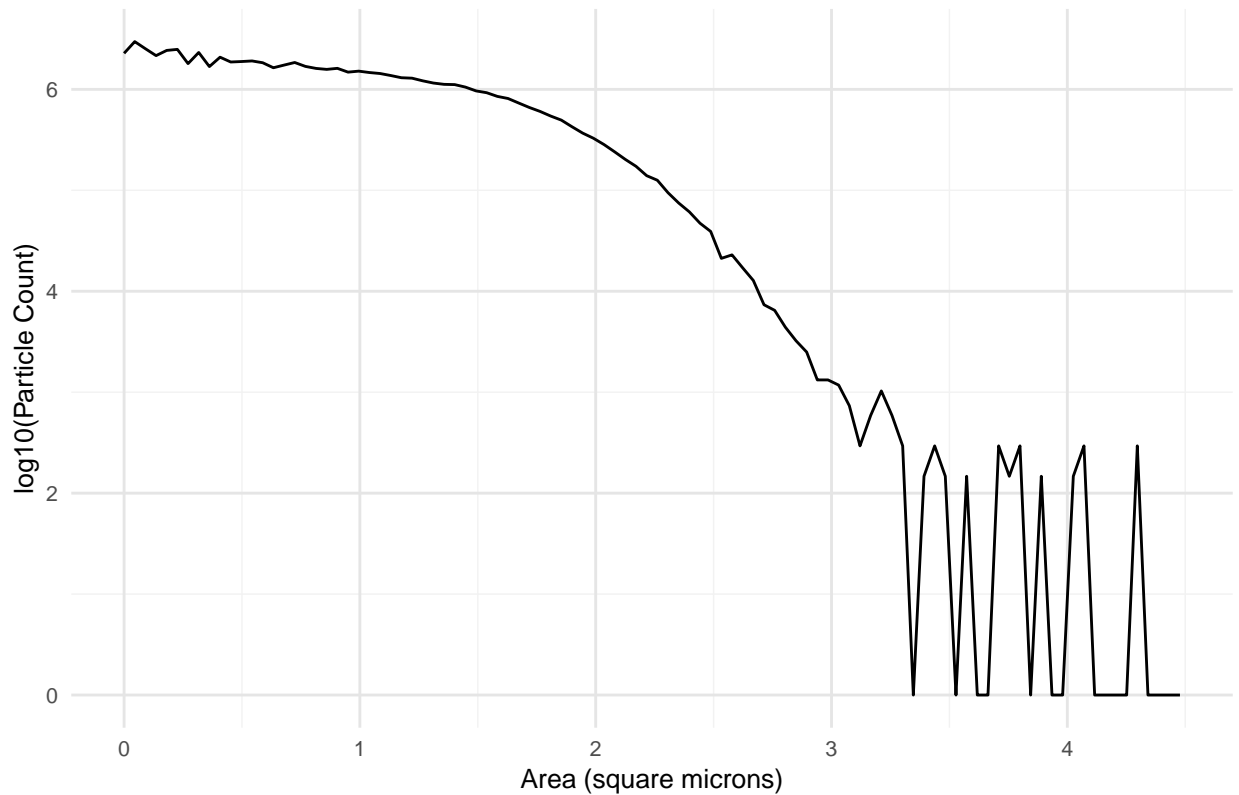
## 3 SLSM Starshade	0.821	0.482	0.883	0
## 4 Starshade Observed	0.804	0.301	0.917	0
## # i 1 more variable: max_log_count <dbl>				

### 8.3 Trial 11

#### Surface Analysis 11: Cumulative Particle Area Distribution over 0.1 square meter

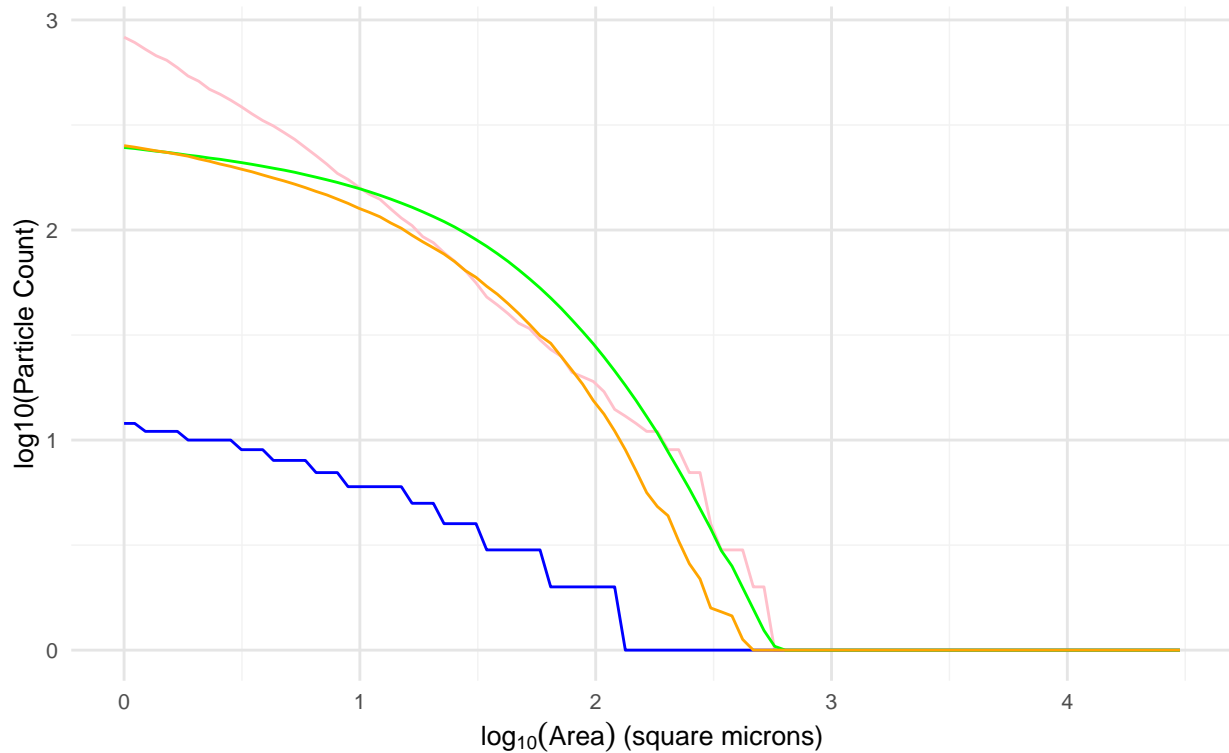


#### Surface Analysis 11: Binned Particle Size Distribution over 0.1 square meters



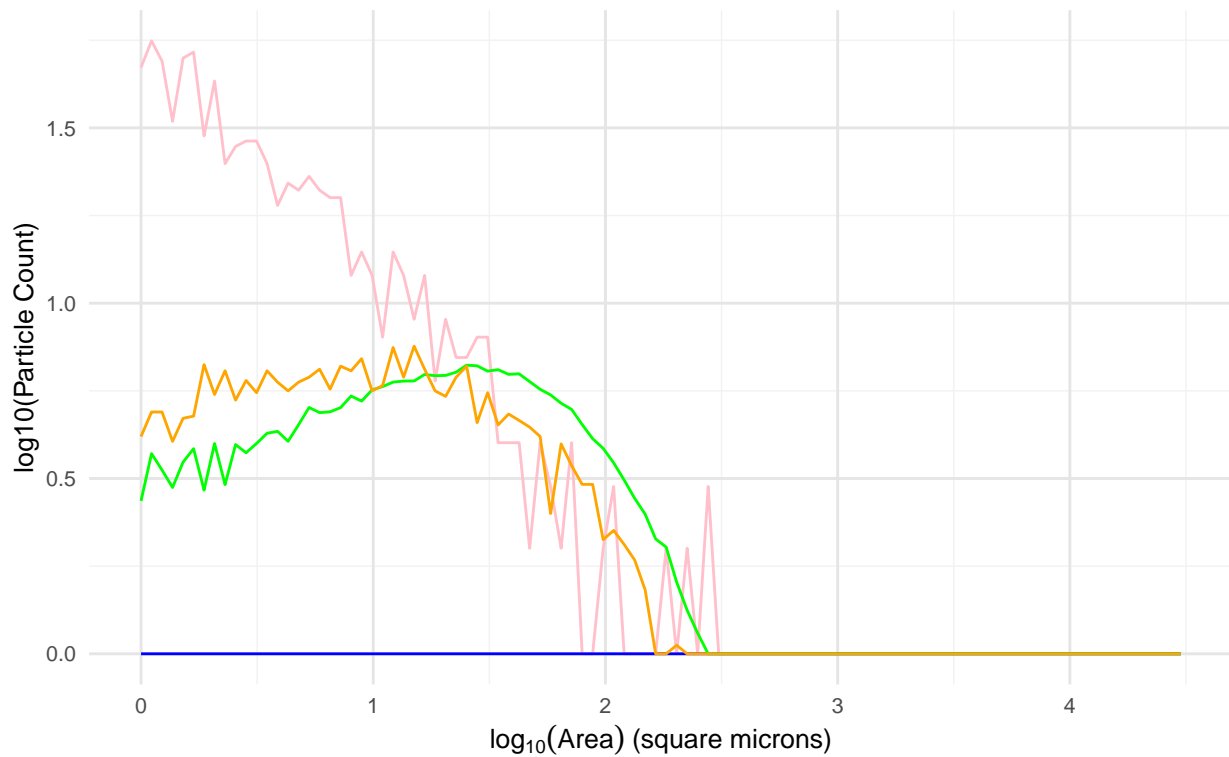
### Edge Analysis 11: Cumulative Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model, Orange: SLSM Starshade



### Edge Analysis 11: Cumulative Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model, Orange: SLSM Starshade



## Trial 11 Edge Distribution Analysis Results

```

##
## 1. Correlation Analysis:

##               comparison pearson_r      p_value
## cor Starshade Observed vs Calibration Observed 0.9630816 1.175188e-57
## cor1      Starshade Observed vs Model 0.9866425 4.779898e-79
## cor2      Starshade Observed vs SLSM Starshade 0.9882531 9.153851e-82
## cor3      Calibration Observed vs Model 0.9355902 4.226939e-46
## cor4      Calibration Observed vs SLSM Starshade 0.9891492 1.915228e-83
## cor5      Model vs SLSM Starshade 0.9703348 3.094399e-62

##
## 2. Kolmogorov-Smirnov Test Results:

##               comparison ks_statistic      p_value
## D Starshade Observed vs Calibration Observed      0.48 1.971901e-10
## D1      Starshade Observed vs Model      0.17 1.111333e-01
## D2      Starshade Observed vs SLSM Starshade      0.19 5.410262e-02
## D3      Calibration Observed vs Model      0.50 2.777589e-11
## D4      Calibration Observed vs SLSM Starshade      0.39 4.959192e-07
## D5      Model vs SLSM Starshade      0.16 1.545381e-01

##
## 3. Root Mean Square Error Between Distributions:

##               comparison      rmse
## 1 Starshade Observed vs Calibration Observed 1.0134880
## 2      Starshade Observed vs Model 0.1791888
## 3      Starshade Observed vs SLSM Starshade 0.3633847
## 4      Calibration Observed vs Model 0.9687954
## 5      Calibration Observed vs SLSM Starshade 0.6767168
## 6      Model vs SLSM Starshade 0.3626231

##
## 4. Regression Analysis for Each Distribution:

##               source      slope intercept r_squared      p_value
## log_area Starshade Observed -0.7813268 2.8501815 0.9318638 5.698289e-59
## log_area1 Calibration Observed -0.2847471 0.9822747 0.8393564 1.070844e-40
## log_area2      Model -0.7282105 2.7050619 0.9033761 1.570240e-51
## log_area3      SLSM Starshade -0.6353298 2.2429598 0.8907273 6.559785e-49

## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 4 x 2
##   source      auc
##   <chr>      <dbl>
## 1 Calibration Observed 1.53
## 2 Model 4.81
## 3 SLSM Starshade 3.66
## 4 Starshade Observed 4.91

## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 4 x 6
##   source      mean_log_count median_log_count sd_log_count min_log_count
##   <chr>      <dbl>      <dbl>      <dbl>      <dbl>
## 1 Calibration Observ~ 0.345      0      0.408      0
## 2 Model 1.07      1.07      1.01      0

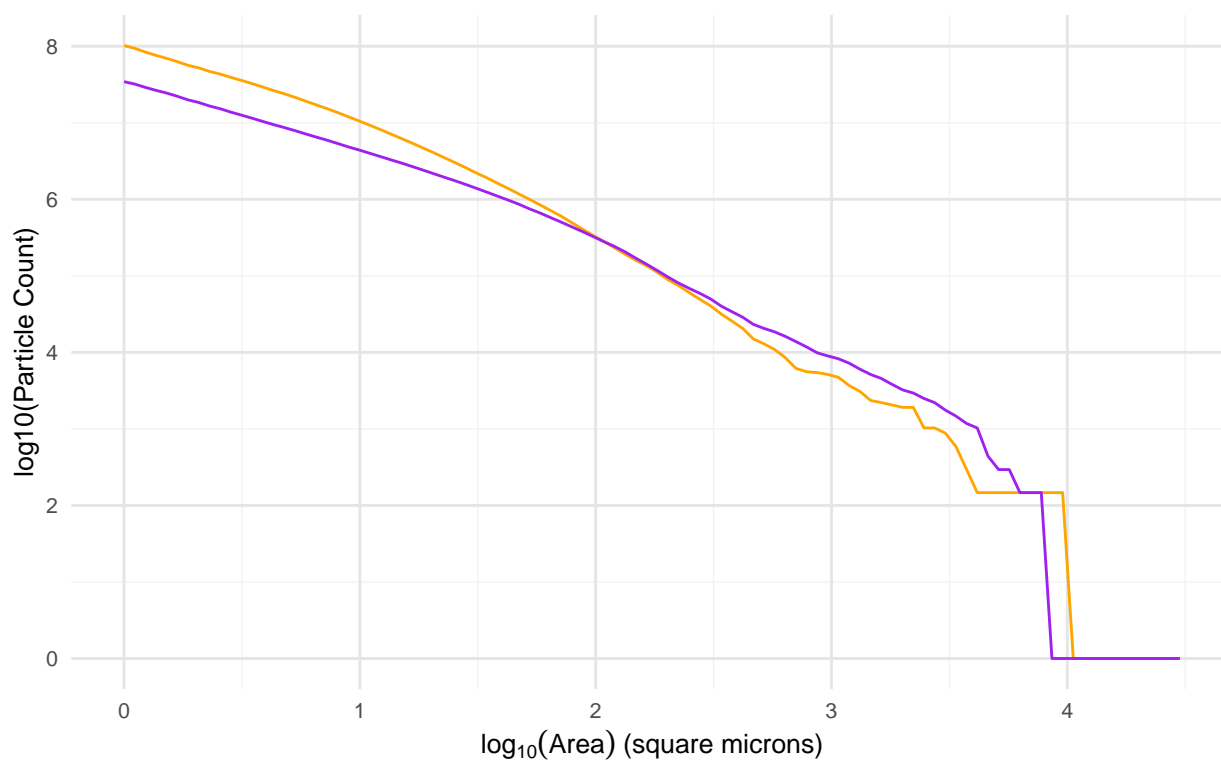
```

## 3 SLSM Starshade	0.821	0.482	0.883	0
## 4 Starshade Observed	1.10	1.04	1.06	0
## # i 1 more variable: max_log_count <dbl>				

#### 8.4 Trial 12

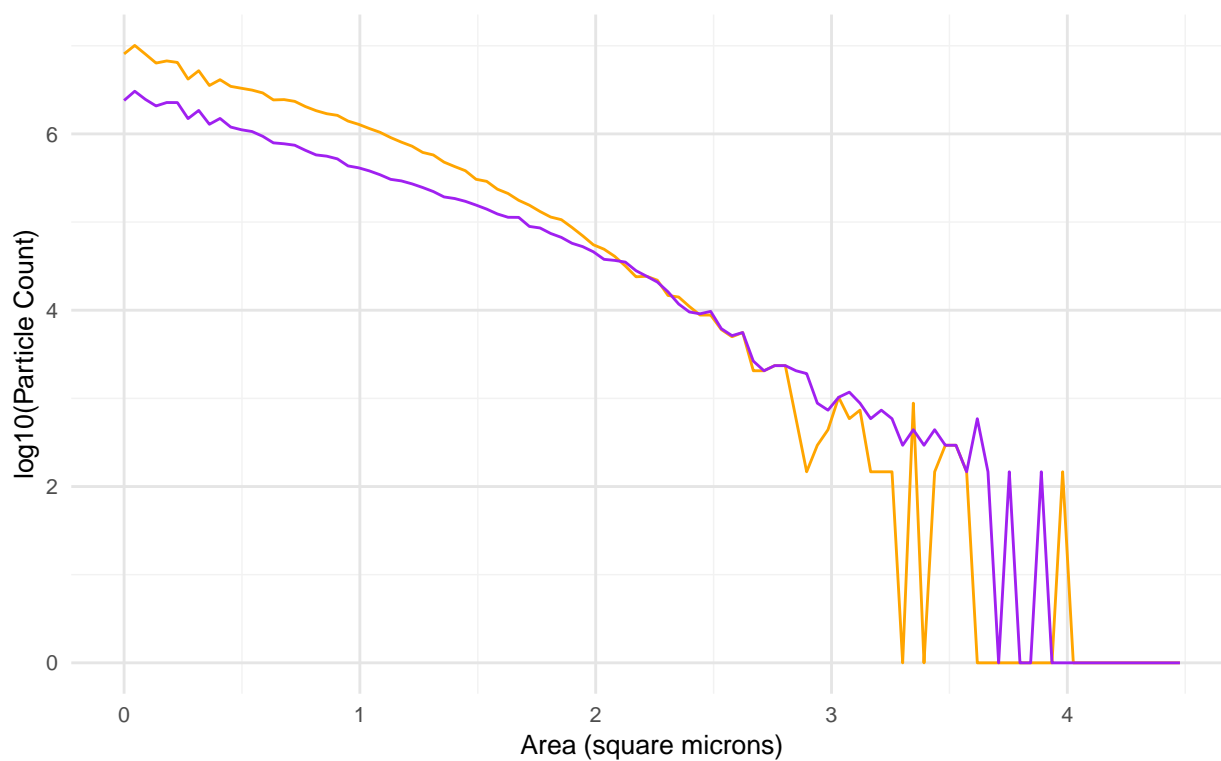
### Surface Analysis 12: Cumulative Particle Area Distribution over 0.1 square meter

Orange: Starshade Surface, Purple: Calibration Surface



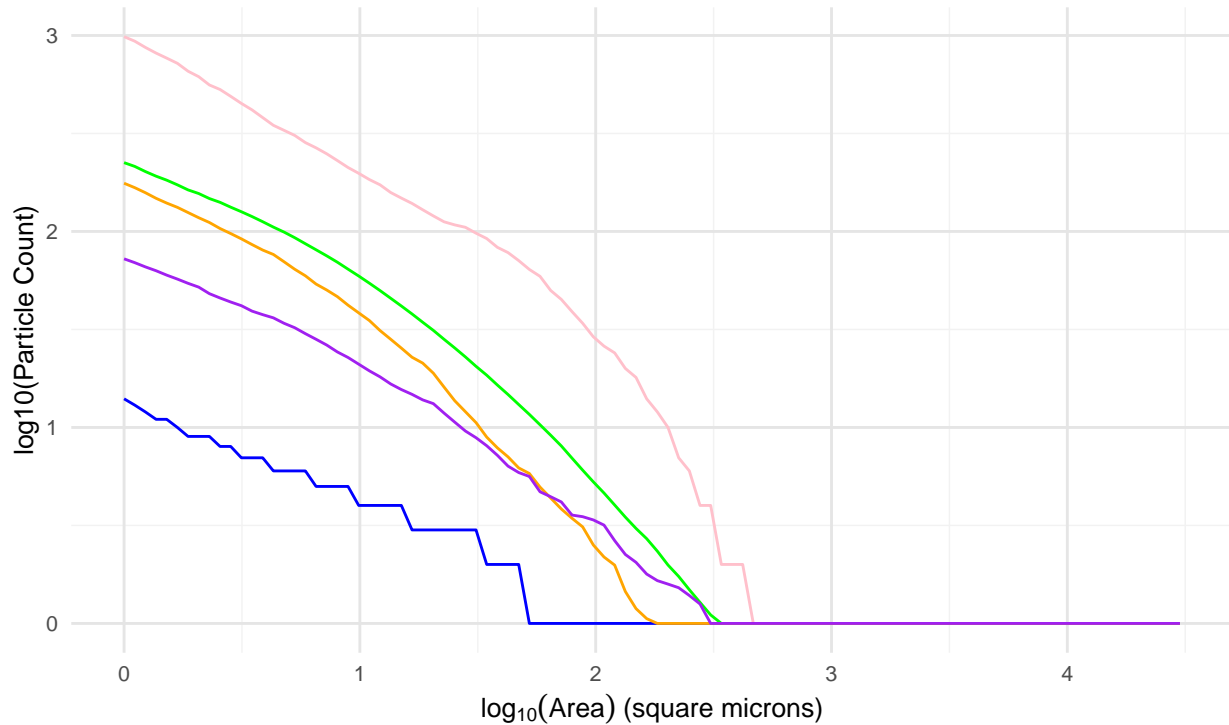
### Surface Analysis 12: Binned Particle Size Distribution over 0.1 square meters

Orange: Starshade Surface, Purple: Calibration Surface



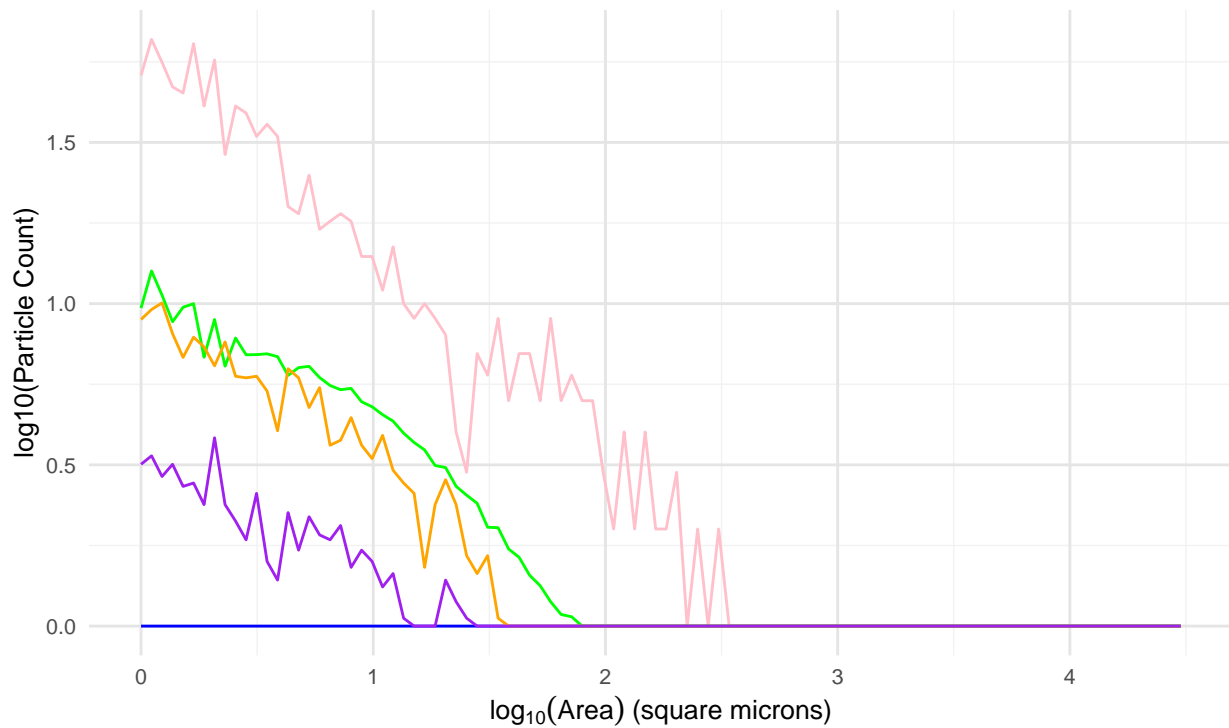
## Edge Analysis 12: Cumulative Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model,  
Orange: SLSM Starshade, Purple: SLSM Calibration



## Edge Analysis 12: Binned Particle Area Distribution over 0.1 meter

Pink: Starshade Observed, Blue: Calibration Observed, Green: Model,  
Orange: SLSM Starshade, Purple: SLSM Calibration



## Trial 12 Edge Distribution Analysis Results

```

##
## 1. Correlation Analysis:

##               comparison pearson_r      p_value
## cor Starshade Observed vs Calibration Observed 0.8856474 2.034191e-34
## cor1          Starshade Observed vs Model 0.9808596 1.882959e-71
## cor2          Starshade Observed vs SLSM Starshade 0.9858298 8.468498e-78
## cor3          Calibration Observed vs Model 0.9496741 3.334913e-51
## cor4          Calibration Observed vs SLSM Starshade 0.9422237 2.415028e-48
## cor5          Model vs SLSM Starshade 0.9994352 3.118802e-146

##
## 2. Kolmogorov-Smirnov Test Results:

##               comparison ks_statistic      p_value
## D Starshade Observed vs Calibration Observed 0.49 7.475143e-11
## D1          Starshade Observed vs Model 0.21 2.431031e-02
## D2          Starshade Observed vs SLSM Starshade 0.21 2.431031e-02
## D3          Calibration Observed vs Model 0.37 2.267454e-06
## D4          Calibration Observed vs SLSM Starshade 0.38 1.071070e-06
## D5          Model vs SLSM Starshade 0.03 1.000000e+00

##
## 3. Root Mean Square Error Between Distributions:

##               comparison      rmse
## 1 Starshade Observed vs Calibration Observed 1.19592655
## 2          Starshade Observed vs Model 0.47497254
## 3          Starshade Observed vs SLSM Starshade 0.44501388
## 4          Calibration Observed vs Model 0.74702009
## 5          Calibration Observed vs SLSM Starshade 0.76972481
## 6          Model vs SLSM Starshade 0.03724995

##
## 4. Regression Analysis for Each Distribution:

##               source      slope intercept r_squared      p_value
## log_area Starshade Observed -0.8194974 2.9920279 0.9171047 8.542547e-55
## log_area1 Calibration Observed -0.2493649 0.8291678 0.7464043 5.891392e-31
## log_area2          Model -0.6280351 2.2044739 0.8812621 3.863310e-47
## log_area3          SLSM Starshade -0.6353298 2.2429598 0.8907273 6.559785e-49

## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 4 x 2
##   source      auc
##   <chr>      <dbl>
## 1 Calibration Observed 1.20
## 2 Model 3.56
## 3 SLSM Starshade 3.66
## 4 Starshade Observed 5.17

## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 4 x 6
##   source      mean_log_count median_log_count sd_log_count min_log_count
##   <chr>      <dbl>      <dbl>      <dbl>      <dbl>
## 1 Calibration Observ~ 0.271      0      0.379      0
## 2 Model 0.798      0.401      0.878      0

```



```

## 3 SLSM Starshade          0.821          0.482          0.883          0
## 4 Starshade Observed      1.16           1.11           1.12           0
## # i 1 more variable: max_log_count <dbl>

## Trial 12 Surface Distribution Analysis Results

##
## 1. Correlation Analysis:

##               comparison pearson_r      p_value
## cor Starshade Observed vs Calibration Observed 0.9859644 5.323202e-78
##
## 2. Kolmogorov-Smirnov Test Results:

##               comparison ks_statistic  p_value
## D Starshade Observed vs Calibration Observed      0.12 0.4675586
##
## 3. Root Mean Square Error Between Distributions:

##               comparison      rmse
## 1 Starshade Observed vs Calibration Observed 0.4265422
##
## 4. Regression Analysis for Each Distribution:

##               source      slope intercept r_squared      p_value
## log_area      Starshade Observed -1.815463  8.791456 0.9580624 2.641805e-69
## log_area1 Calibration Observed -1.681296  8.392893 0.9160102 1.625447e-54
## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 2 x 2
##   source      auc
##   <chr>      <dbl>
## 1 Calibration Observed 20.8
## 2 Starshade Observed 21.2
## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 2 x 6
##   source      mean_log_count median_log_count sd_log_count min_log_count
##   <chr>      <dbl>          <dbl>          <dbl>          <dbl>
## 1 Calibration Observ~ 4.63            5.11            2.31            0
## 2 Starshade Observed 4.73            5.09            2.43            0
## # i 1 more variable: max_log_count <dbl>

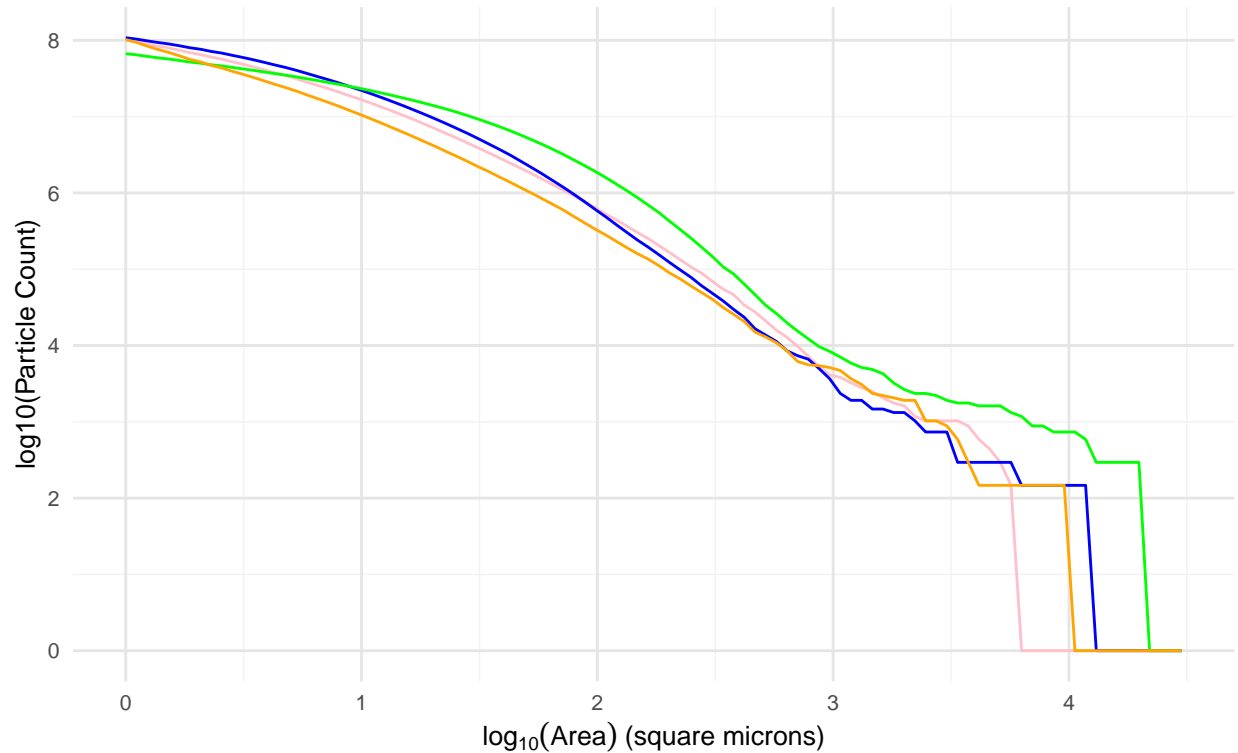
```

## 9. Combined Analysis and Comparison

### 9.1 Cumulative Comparison

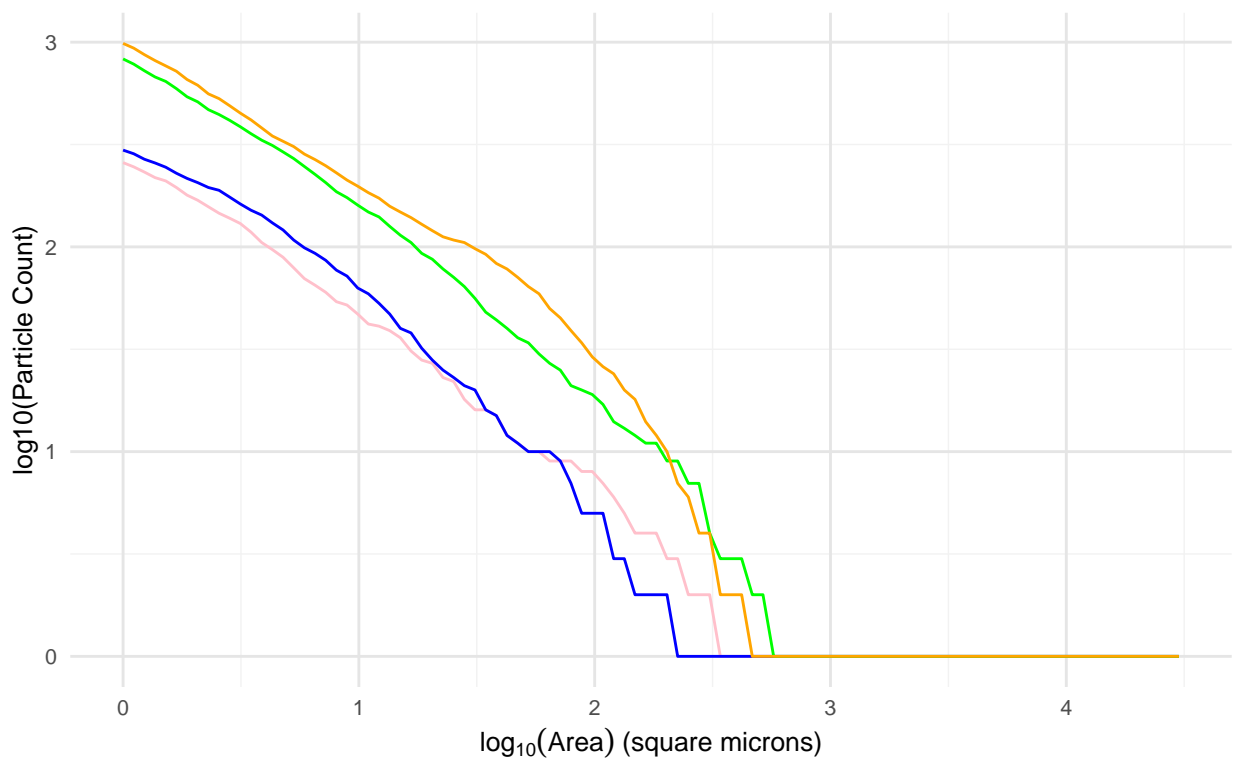
#### Starshade Surface Analysis: Cumulative Particle Area Distribution over 0.1 square meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



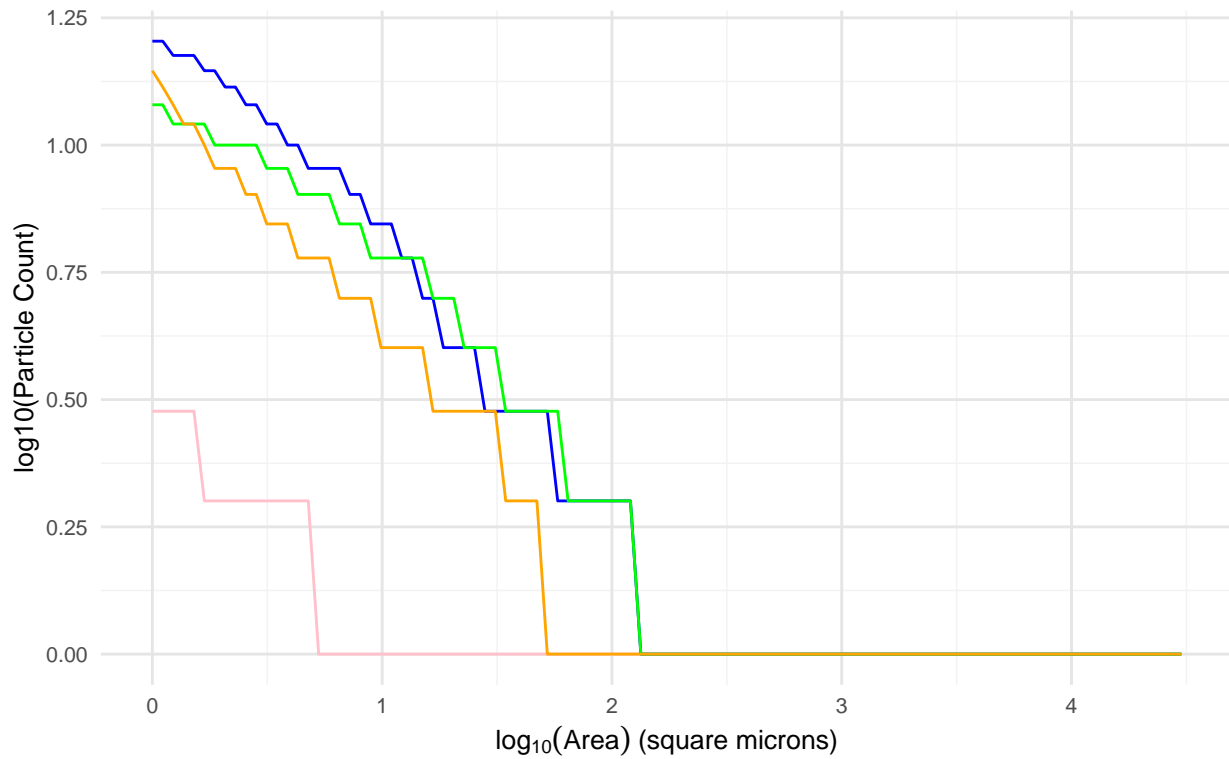
#### Starshade Edge Analysis: Cumulative Particle Area Distribution over 0.1 meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



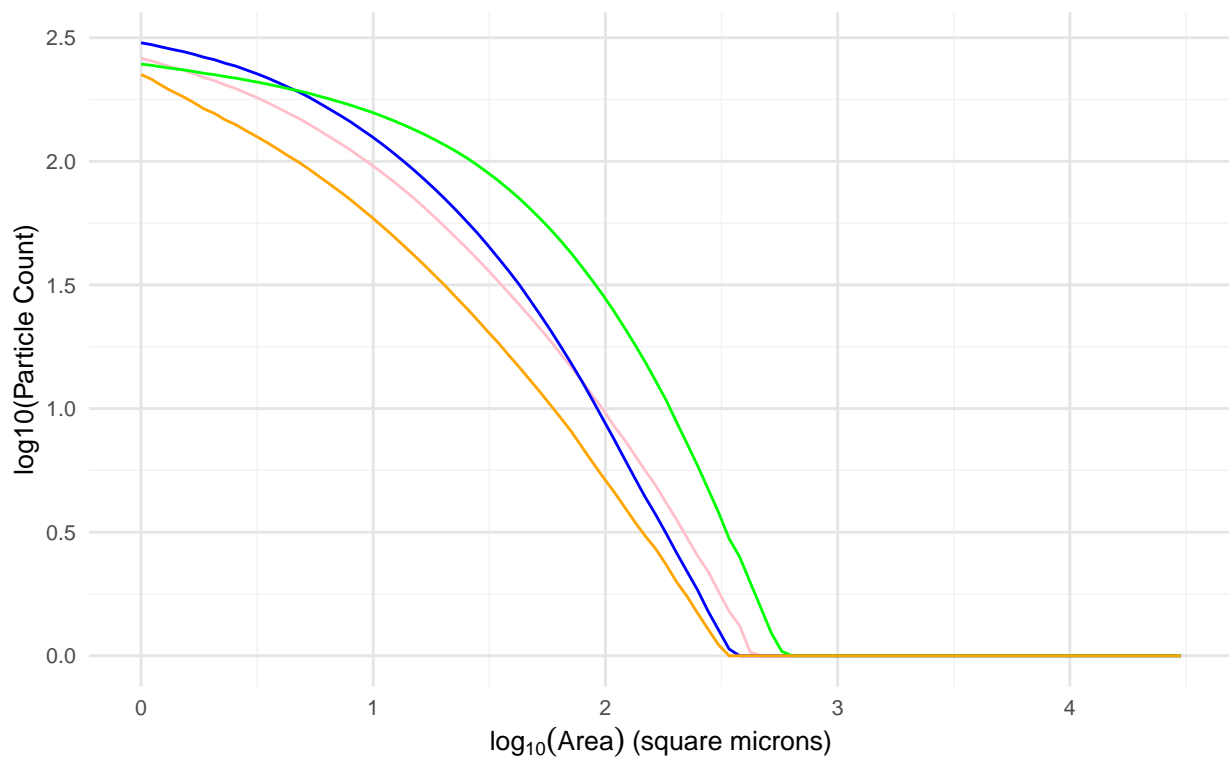
### Calibration Edge Analysis: Cumulative Particle Area Distribution over 0.1 meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



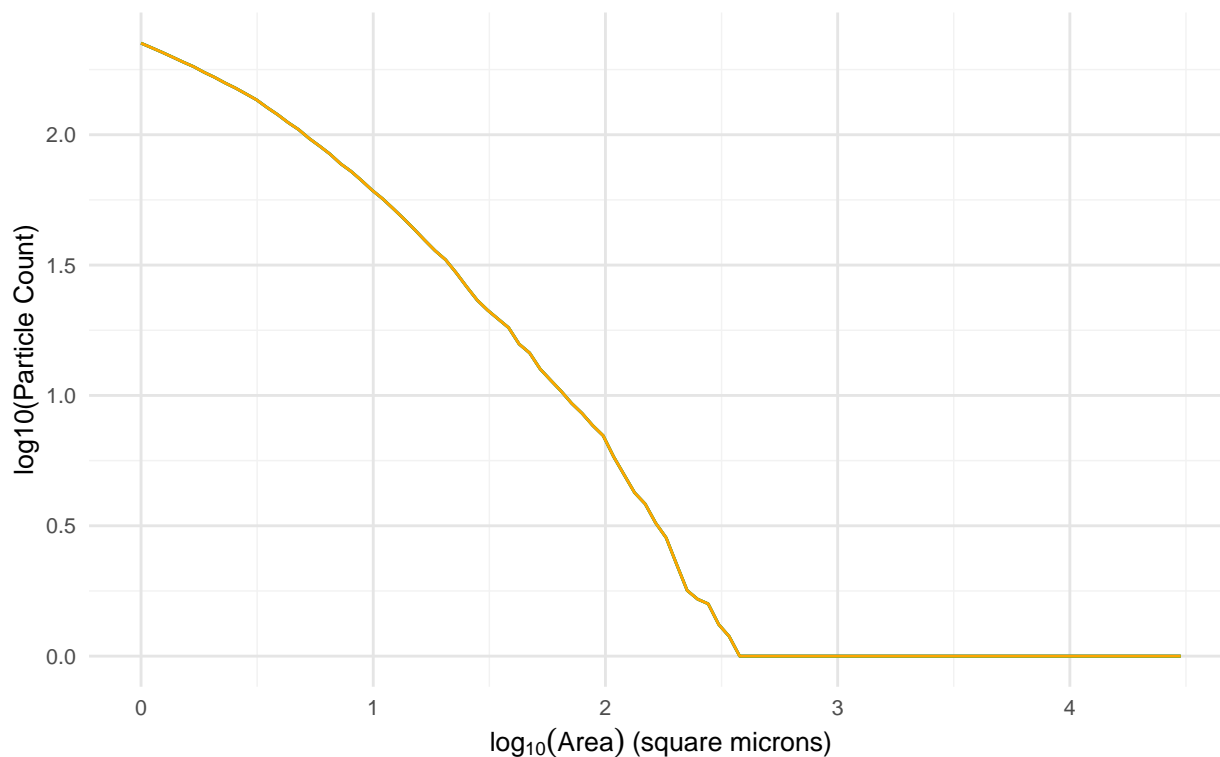
### Model Edge Analysis: Cumulative Particle Area Distribution over 0.1 meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



## SLSM Edge Analysis: Cumulative Particle Area Distribution over 0.1 meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



### ## All Trials Surface Distribution Analysis Results

##

#### ## 1. Correlation Analysis:

##	comparison	pearson_r	p_value
## cor	Trial 9 vs Trial 10	0.9767104	2.554861e-67
## cor1	Trial 9 vs Trial 11	0.9605212	2.953926e-56
## cor2	Trial 9 vs Trial 12	0.9819394	1.122806e-72
## cor3	Trial 10 vs Trial 11	0.9817243	1.995089e-72
## cor4	Trial 10 vs Trial 12	0.9906245	1.539446e-86
## cor5	Trial 11 vs Trial 12	0.9710947	8.835377e-63

##

#### ## 2. Kolmogorov-Smirnov Test Results:

##	comparison	ks_statistic	p_value
## D	Trial 9 vs Trial 10	0.07	0.9670685
## D1	Trial 9 vs Trial 11	0.13	0.3667264
## D2	Trial 9 vs Trial 12	0.05	0.9996333
## D3	Trial 10 vs Trial 11	0.13	0.3667264
## D4	Trial 10 vs Trial 12	0.07	0.9670685
## D5	Trial 11 vs Trial 12	0.16	0.1545381

##

#### ## 3. Root Mean Square Error Between Distributions:

##	comparison	rmse
## 1	Trial 9 vs Trial 10	0.5892228
## 2	Trial 9 vs Trial 11	0.9925532

```

## 3 Trial 9 vs Trial 12 0.5236460
## 4 Trial 10 vs Trial 11 0.6850030
## 5 Trial 10 vs Trial 12 0.3781914
## 6 Trial 11 vs Trial 12 0.8432413

##
## 4. Regression Analysis for Each Distribution:

##           source      slope intercept r_squared      p_value
## log_area   Trial 9 -1.948892  9.125252 0.9367151 1.523466e-60
## log_area1 Trial 10 -1.850231  9.040215 0.9603213 1.750396e-70
## log_area2 Trial 11 -1.565777  8.799607 0.9329998 2.498670e-59
## log_area3 Trial 12 -1.815463  8.791456 0.9580624 2.641805e-69

## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 4 x 2
##   source      auc
##   <chr>    <dbl>
## 1 Trial 10  22.0
## 2 Trial 11  23.8
## 3 Trial 12  21.2
## 4 Trial 9   21.4

## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 4 x 6
##   source      mean_log_count median_log_count sd_log_count min_log_count
##   <chr>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 Trial 10         4.90            5.24            2.48            0
## 2 Trial 11         5.29            5.79            2.13            0
## 3 Trial 12         4.73            5.09            2.43            0
## 4 Trial 9          4.76            5.35            2.64            0
## # i 1 more variable: max_log_count <dbl>

## All Trials Edge Distribution Analysis Results

##
## 1. Correlation Analysis:

##           comparison pearson_r      p_value
## cor   Trial 9 vs Trial 10 0.9929732 1.188271e-92
## cor1  Trial 9 vs Trial 11 0.9907104 9.827838e-87
## cor2  Trial 9 vs Trial 12 0.9866390 4.839999e-79
## cor3  Trial 10 vs Trial 11 0.9757956 1.651127e-66
## cor4  Trial 10 vs Trial 12 0.9704842 2.425167e-62
## cor5  Trial 11 vs Trial 12 0.9957379 2.909056e-103

##
## 2. Kolmogorov-Smirnov Test Results:

##           comparison ks_statistic      p_value
## D   Trial 9 vs Trial 10      0.05 0.99963329
## D1  Trial 9 vs Trial 11      0.17 0.11113334
## D2  Trial 9 vs Trial 12      0.21 0.02431031
## D3  Trial 10 vs Trial 11     0.15 0.21055163
## D4  Trial 10 vs Trial 12     0.17 0.11113334
## D5  Trial 11 vs Trial 12     0.07 0.96706849

##

```

```
## 3. Root Mean Square Error Between Distributions:

##           comparison      rmse
## 1 Trial 9 vs Trial 10 0.1194225
## 2 Trial 9 vs Trial 11 0.3784343
## 3 Trial 9 vs Trial 12 0.4649738
## 4 Trial 10 vs Trial 11 0.3941772
## 5 Trial 10 vs Trial 12 0.4760085
## 6 Trial 11 vs Trial 12 0.1300165

##
## 4. Regression Analysis for Each Distribution:

##           source      slope intercept r_squared      p_value
## log_area Trial 9 -0.6214753  2.199052 0.8991446 1.285514e-50
## log_area1 Trial 10 -0.6502636  2.260122 0.8648647 2.206654e-44
## log_area2 Trial 11 -0.7813268  2.850182 0.9318638 5.698289e-59
## log_area3 Trial 12 -0.8194974  2.992028 0.9171047 8.542547e-55

## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 4 x 2
##   source      auc
##   <chr>    <dbl>
## 1 Trial 10  3.58
## 2 Trial 11  4.91
## 3 Trial 12  5.17
## 4 Trial 9   3.60

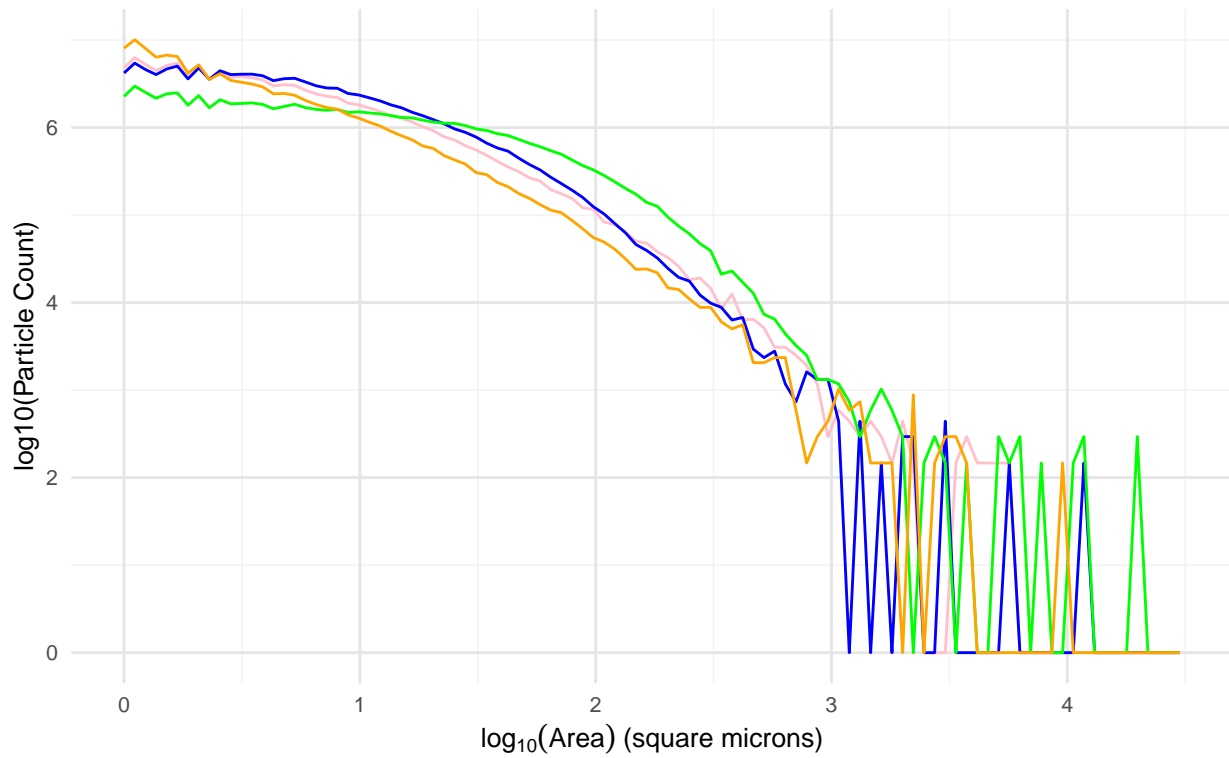
## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 4 x 6
##   source      mean_log_count median_log_count sd_log_count min_log_count
##   <chr>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 Trial 10      0.804          0.301          0.917           0
## 2 Trial 11      1.10          1.04          1.06           0
## 3 Trial 12      1.16          1.11          1.12           0
## 4 Trial 9       0.808          0.602          0.860           0
## # i 1 more variable: max_log_count <dbl>
```

## 9.2 Binned Comparison

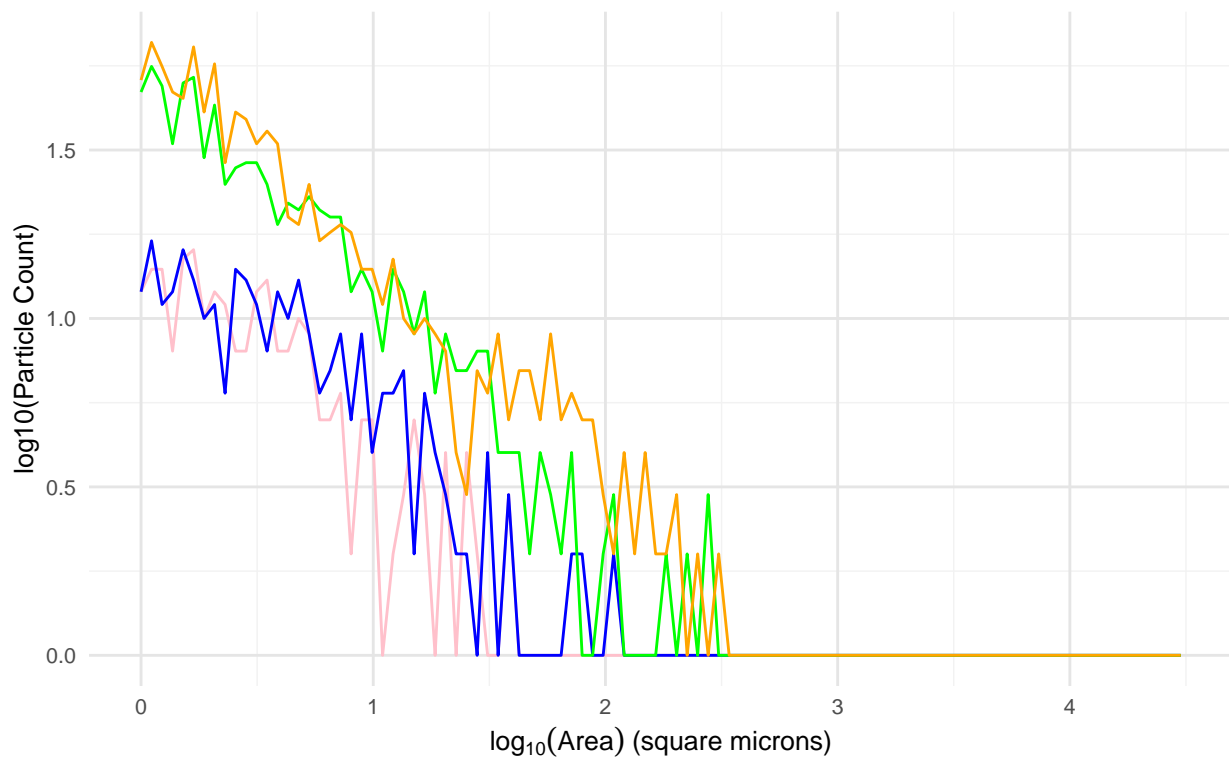
### Starshade Surface Analysis: Binned Particle Area Distribution over 0.1 square meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



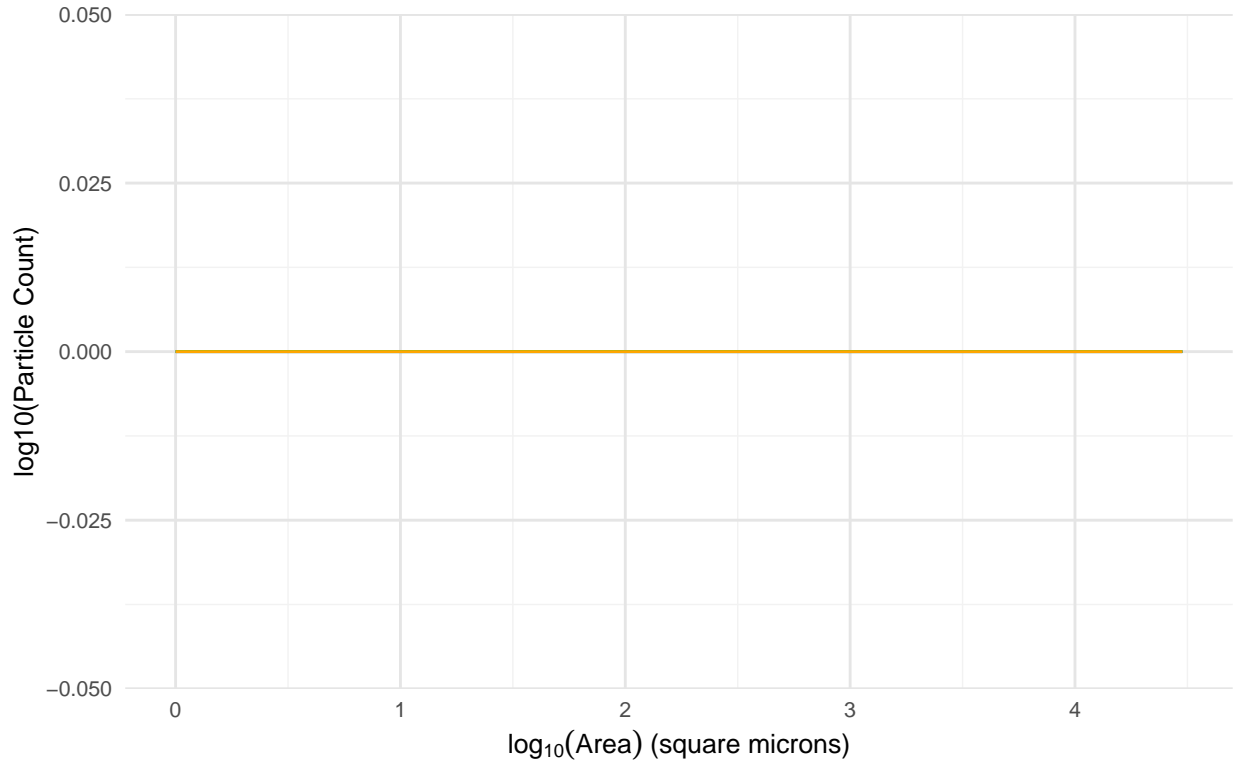
### Starshade Edge Analysis: Binned Particle Area Distribution over 0.1 meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



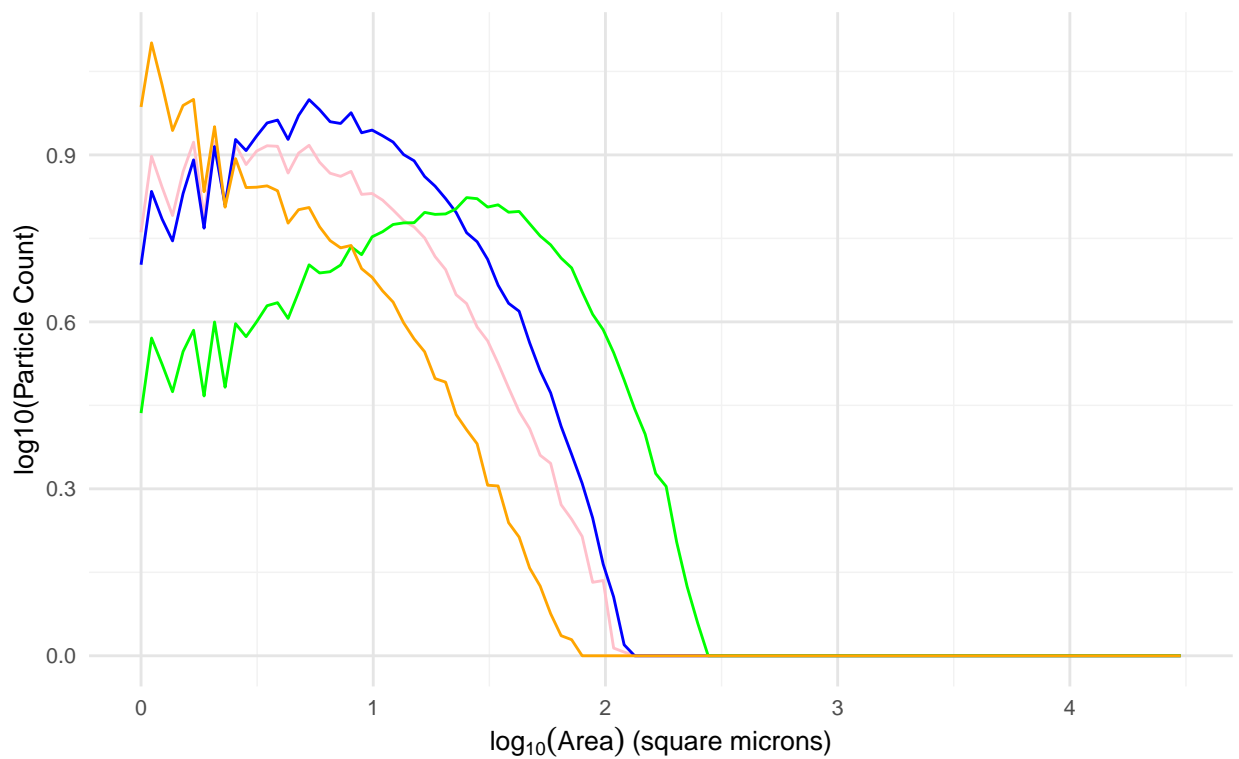
## Calibration Edge Analysis: Binned Particle Area Distribution over 0.1 meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



## Model Edge Analysis: Binned Particle Area Distribution over 0.1 meter

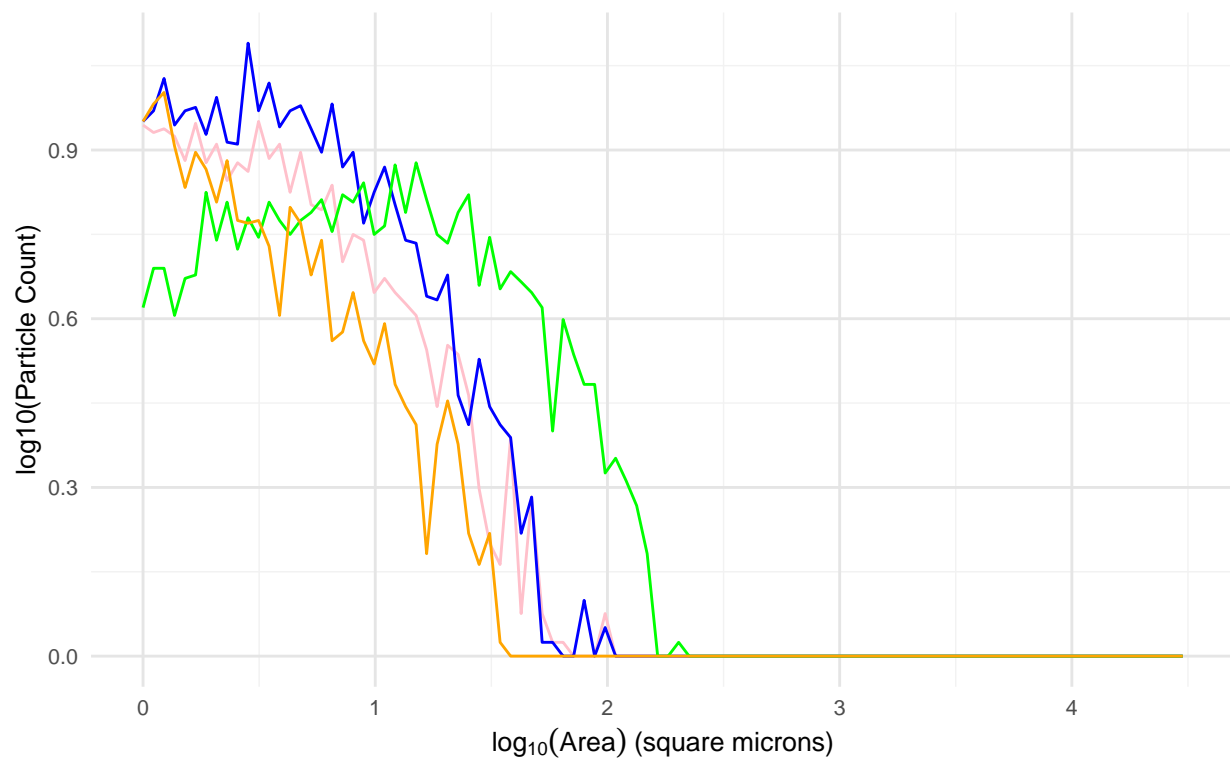
Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12





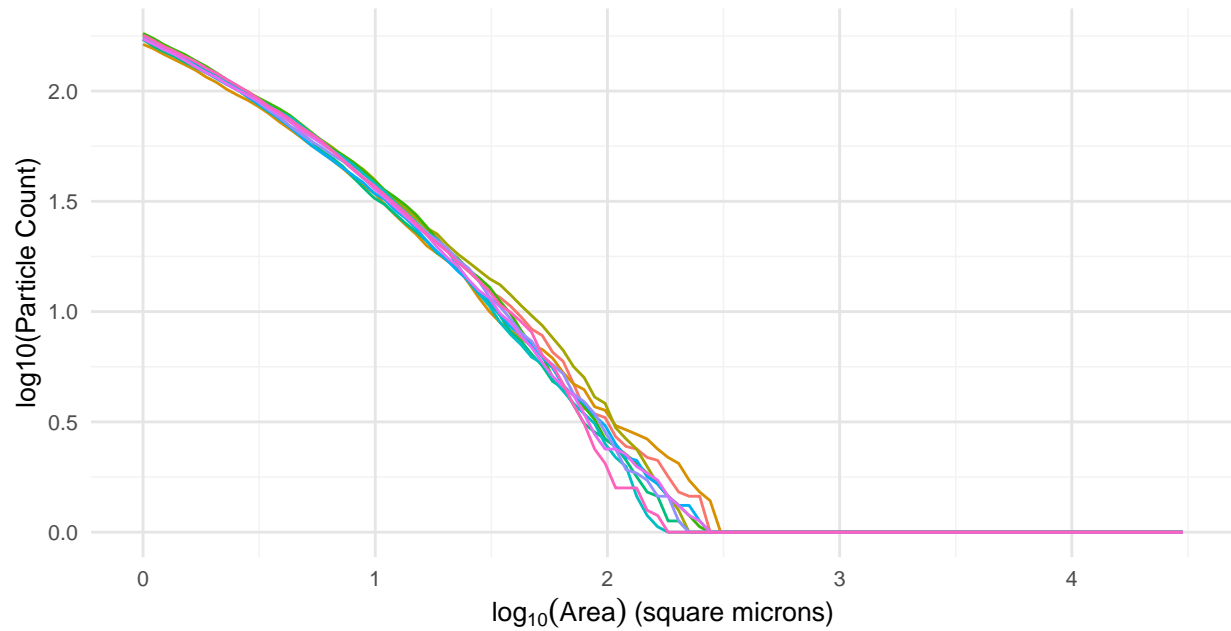
# SLSM Edge Analysis: Binned Particle Area Distribution over 0.1 meter

Pink: Trial 9, Blue: Trial 10, Green: Trial 11, Orange: Trial 12



## 10. Multiple Line analysis

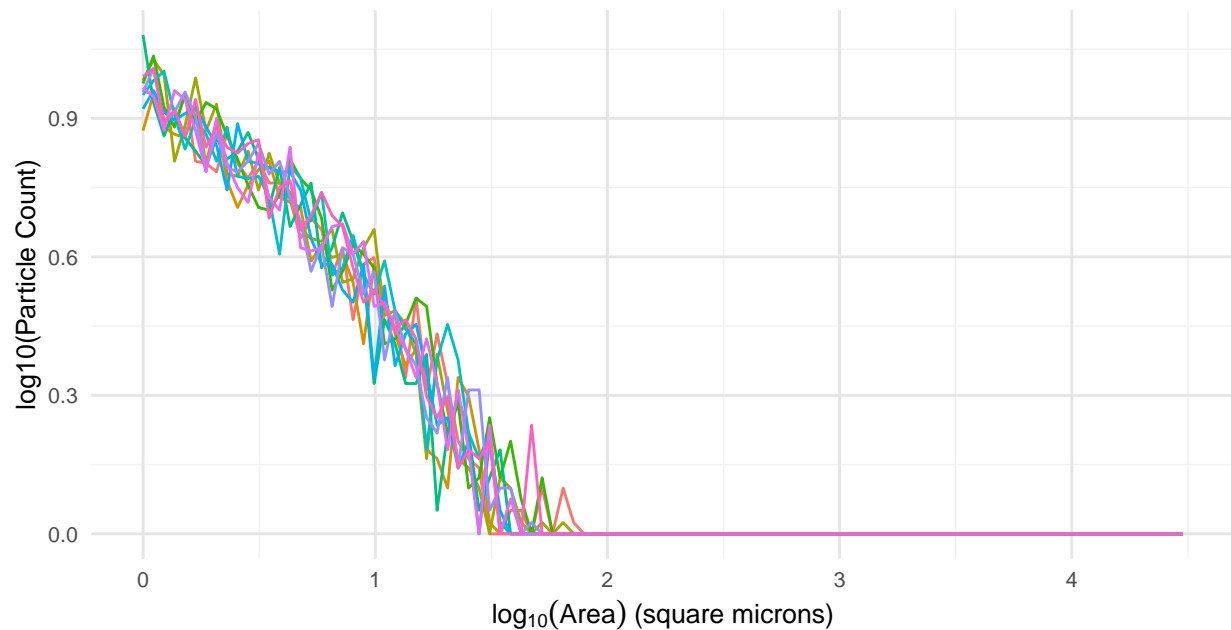
### Starshade Multiple Line Analysis: Cumulative Particle Area Distribution over 0.1 m



factor(line\_index)

1	3	5	7	9
2	4	6	8	10

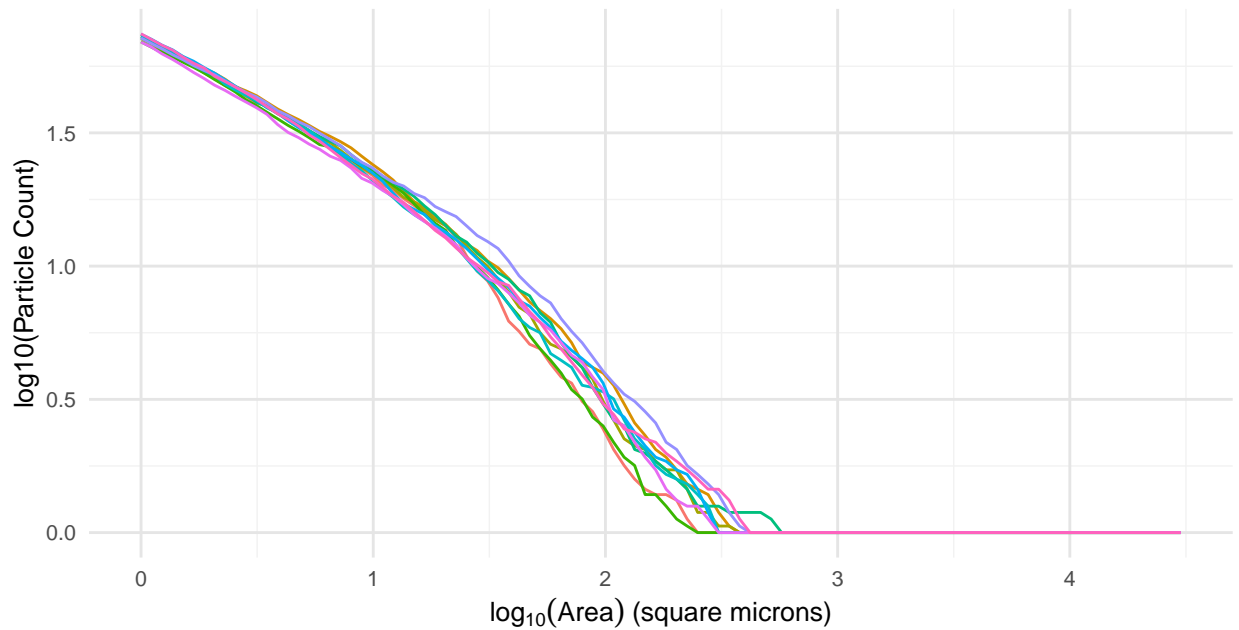
### Starshade Multiple Line Analysis: Binned Particle Area Distribution over 0.1 m



factor(line\_index)

1	3	5	7	9
2	4	6	8	10

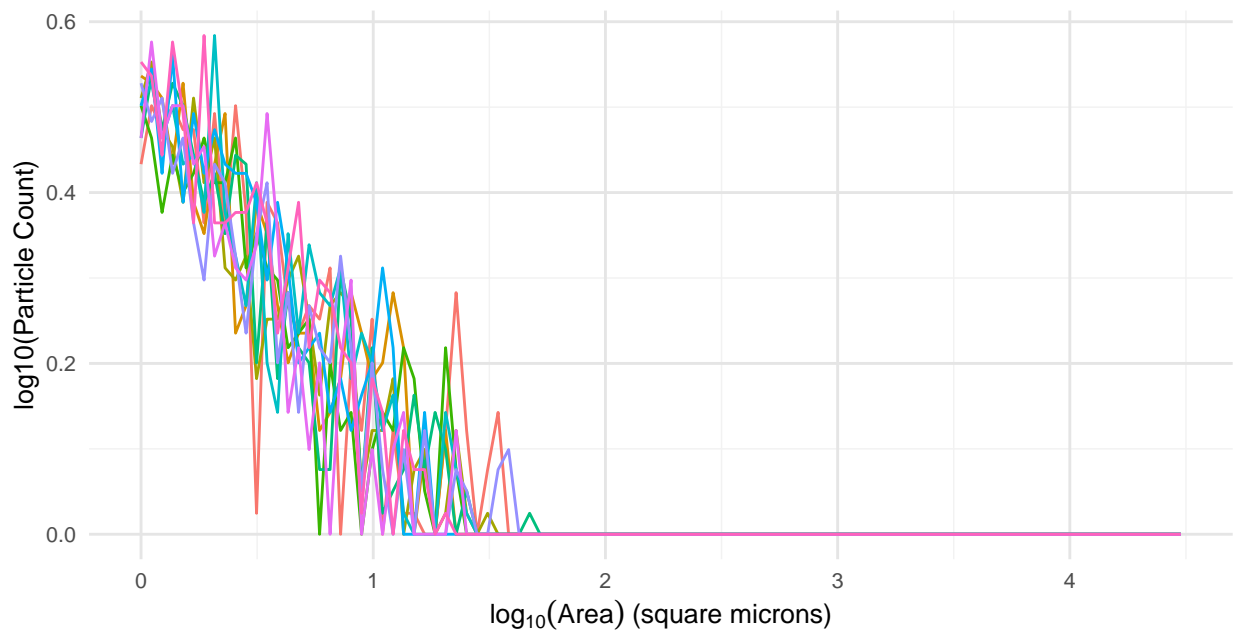
## Calibration Multiple Line Analysis: Cumulative Particle Area Distribution over 0.1 n



factor(line\_index)

1	3	5	7	9
2	4	6	8	10

## Calibration Multiple Line Analysis: Binned Particle Area Distribution over 0.1 me



factor(line\_index)

1	3	5	7	9
2	4	6	8	10

## All Lines Starshade Surface Model Distribution Analysis Results

##

## ## 1. Correlation Analysis:

##	comparison	pearson_r	p_value
## cor	1 vs 2	0.9988358	7.564024e-131
## cor1	1 vs 3	0.9989636	2.552176e-133
## cor2	1 vs 4	0.9991493	1.607047e-137
## cor3	1 vs 5	0.9981329	8.397415e-121
## cor4	1 vs 6	0.9968097	2.044465e-109
## cor5	1 vs 7	0.9992770	5.555589e-141
## cor6	1 vs 8	0.9988692	1.823520e-131
## cor7	1 vs 9	0.9990585	2.302382e-135
## cor8	1 vs 10	0.9968905	5.832676e-110
## cor9	2 vs 3	0.9971344	1.071306e-111
## cor10	2 vs 4	0.9976550	5.872171e-116
## cor11	2 vs 5	0.9965330	1.196001e-107
## cor12	2 vs 6	0.9946640	1.717183e-98
## cor13	2 vs 7	0.9983562	1.644275e-123
## cor14	2 vs 8	0.9970609	3.700220e-111
## cor15	2 vs 9	0.9978239	1.511973e-117
## cor16	2 vs 10	0.9938425	1.876590e-95
## cor17	3 vs 4	0.9985084	1.412129e-125
## cor18	3 vs 5	0.9977402	9.603163e-117
## cor19	3 vs 6	0.9967342	6.428044e-109
## cor20	3 vs 7	0.9985922	8.307438e-127
## cor21	3 vs 8	0.9989090	3.146807e-132
## cor22	3 vs 9	0.9980707	4.178564e-120
## cor23	3 vs 10	0.9967482	5.206339e-109
## cor24	4 vs 5	0.9995119	2.453363e-149
## cor25	4 vs 6	0.9988176	1.618303e-130
## cor26	4 vs 7	0.9997190	4.352269e-161
## cor27	4 vs 8	0.9996894	5.934717e-159
## cor28	4 vs 9	0.9998563	2.327759e-175
## cor29	4 vs 10	0.9985817	1.195578e-126
## cor30	5 vs 6	0.9994688	1.546511e-147
## cor31	5 vs 7	0.9994843	3.603954e-148
## cor32	5 vs 8	0.9995238	7.277024e-150
## cor33	5 vs 9	0.9996181	1.473628e-154
## cor34	5 vs 10	0.9990339	8.161006e-135
## cor35	6 vs 7	0.9986209	3.027076e-127
## cor36	6 vs 8	0.9990423	5.309737e-135
## cor37	6 vs 9	0.9988178	1.604735e-130
## cor38	6 vs 10	0.9991555	1.122184e-137
## cor39	7 vs 8	0.9995994	1.528436e-153
## cor40	7 vs 9	0.9997220	2.560420e-161
## cor41	7 vs 10	0.9981863	2.027753e-121
## cor42	8 vs 9	0.9995264	5.556977e-150
## cor43	8 vs 10	0.9988575	3.009166e-131
## cor44	9 vs 10	0.9986334	1.940138e-127

##

## ## 2. Kolmogorov-Smirnov Test Results:

##	comparison	ks_statistic	p_value
## D	1 vs 2	0.03	1.0000000
## D1	1 vs 3	0.03	1.0000000

## D2	1 vs 4	0.03 1.0000000
## D3	1 vs 5	0.04 0.9999982
## D4	1 vs 6	0.06 0.9937649
## D5	1 vs 7	0.03 1.0000000
## D6	1 vs 8	0.04 0.9999982
## D7	1 vs 9	0.03 1.0000000
## D8	1 vs 10	0.06 0.9937649
## D9	2 vs 3	0.04 0.9999982
## D10	2 vs 4	0.04 0.9999982
## D11	2 vs 5	0.05 0.9996333
## D12	2 vs 6	0.07 0.9670685
## D13	2 vs 7	0.04 0.9999982
## D14	2 vs 8	0.06 0.9937649
## D15	2 vs 9	0.05 0.9996333
## D16	2 vs 10	0.08 0.9062064
## D17	3 vs 4	0.03 1.0000000
## D18	3 vs 5	0.04 0.9999982
## D19	3 vs 6	0.04 0.9999982
## D20	3 vs 7	0.04 0.9999982
## D21	3 vs 8	0.03 1.0000000
## D22	3 vs 9	0.03 1.0000000
## D23	3 vs 10	0.05 0.9996333
## D24	4 vs 5	0.03 1.0000000
## D25	4 vs 6	0.04 0.9999982
## D26	4 vs 7	0.02 1.0000000
## D27	4 vs 8	0.02 1.0000000
## D28	4 vs 9	0.02 1.0000000
## D29	4 vs 10	0.05 0.9996333
## D30	5 vs 6	0.03 1.0000000
## D31	5 vs 7	0.03 1.0000000
## D32	5 vs 8	0.02 1.0000000
## D33	5 vs 9	0.03 1.0000000
## D34	5 vs 10	0.03 1.0000000
## D35	6 vs 7	0.05 0.9996333
## D36	6 vs 8	0.04 0.9999982
## D37	6 vs 9	0.05 0.9996333
## D38	6 vs 10	0.03 1.0000000
## D39	7 vs 8	0.02 1.0000000
## D40	7 vs 9	0.02 1.0000000
## D41	7 vs 10	0.05 0.9996333
## D42	8 vs 9	0.02 1.0000000
## D43	8 vs 10	0.04 0.9999982
## D44	9 vs 10	0.05 0.9996333

##

## 3. Root Mean Square Error Between Distributions:

##	comparison	rmse
## 1	1 vs 2	0.04560622
## 2	1 vs 3	0.03944914
## 3	1 vs 4	0.03633549
## 4	1 vs 5	0.06031709
## 5	1 vs 6	0.07218678
## 6	1 vs 7	0.03888501
## 7	1 vs 8	0.04315660

```

## 8      1 vs 9 0.04105515
## 9      1 vs 10 0.07106682
## 10     2 vs 3 0.07168801
## 11     2 vs 4 0.06417193
## 12     2 vs 5 0.07237352
## 13     2 vs 6 0.09106474
## 14     2 vs 7 0.04919926
## 15     2 vs 8 0.06610239
## 16     2 vs 9 0.05758095
## 17     2 vs 10 0.09753202
## 18     3 vs 4 0.04743684
## 19     3 vs 5 0.07060149
## 20     3 vs 6 0.07576008
## 21     3 vs 7 0.05579387
## 22     3 vs 8 0.04758050
## 23     3 vs 9 0.05937966
## 24     3 vs 10 0.07452611
## 25     4 vs 5 0.03960796
## 26     4 vs 6 0.04504994
## 27     4 vs 7 0.03031912
## 28     4 vs 8 0.02497469
## 29     4 vs 9 0.02235435
## 30     4 vs 10 0.04750144
## 31     5 vs 6 0.03103146
## 32     5 vs 7 0.02843356
## 33     5 vs 8 0.02972391
## 34     5 vs 9 0.02612048
## 35     5 vs 10 0.04105053
## 36     6 vs 7 0.04678188
## 37     6 vs 8 0.03814762
## 38     6 vs 9 0.04202460
## 39     6 vs 10 0.03396742
## 40     7 vs 8 0.02474454
## 41     7 vs 9 0.02011513
## 42     7 vs 10 0.05355944
## 43     8 vs 9 0.02505910
## 44     8 vs 10 0.04159827
## 45     9 vs 10 0.04546680

```

```
##
```

```
## 4. Regression Analysis for Each Distribution:
```

##	source	slope	intercept	r_squared	p_value
##	log_area	1 -0.5745947	1.991477	0.8626897	4.831235e-44
##	log_area1	2 -0.5615357	1.951405	0.8707654	2.467110e-45
##	log_area2	3 -0.5815099	2.014236	0.8589816	1.786614e-43
##	log_area3	4 -0.5778383	1.990227	0.8490061	5.116960e-42
##	log_area4	5 -0.5636019	1.932306	0.8397044	9.626891e-41
##	log_area5	6 -0.5716532	1.955292	0.8314698	1.126230e-39
##	log_area6	7 -0.5655892	1.948491	0.8516637	2.140208e-42
##	log_area7	8 -0.5702904	1.962300	0.8465250	1.138847e-41
##	log_area8	9 -0.5688896	1.957308	0.8475658	8.154343e-42
##	log_area9	10 -0.5735963	1.962319	0.8304943	1.495185e-39

```
## [1] "\n5. Area Under Curve Analysis:\n"
```

```

## # A tibble: 10 x 2
##   source auc
##   <dbl> <dbl>
## 1     1 3.14
## 2     2 3.09
## 3     3 3.17
## 4     4 3.10
## 5     5 2.98
## 6     6 3.00
## 7     7 3.04
## 8     8 3.05
## 9     9 3.04
## 10    10 3.02

## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 10 x 6
##   source mean_log_count median_log_count sd_log_count min_log_count
##   <dbl>         <dbl>         <dbl>         <dbl>         <dbl>
## 1     1         0.705         0.289         0.812           0
## 2     2         0.694         0.358         0.790           0
## 3     3         0.712         0.191         0.823           0
## 4     4         0.697         0.191         0.823           0
## 5     5         0.671         0.107         0.807           0
## 6     6         0.675         0.0123        0.823           0
## 7     7         0.682         0.191         0.804           0
## 8     8         0.686         0.163         0.813           0
## 9     9         0.684         0.199         0.811           0
## 10    10         0.678         0.0379        0.826           0
## # i 1 more variable: max_log_count <dbl>

## All Lines Calibration Surface Model Distribution Analysis Results

##
## 1. Correlation Analysis:

##   comparison pearson_r      p_value
## cor      1 vs 2 0.9951516 1.585809e-100
## cor1     1 vs 3 0.9980309 1.133750e-119
## cor2     1 vs 4 0.9996635 2.967063e-157
## cor3     1 vs 5 0.9972659 1.074680e-112
## cor4     1 vs 6 0.9977437 8.888355e-117
## cor5     1 vs 7 0.9963519 1.443638e-106
## cor6     1 vs 8 0.9912174 6.357962e-88
## cor7     1 vs 9 0.9974059 8.211316e-114
## cor8     1 vs 10 0.9960779 4.987475e-105
## cor9     2 vs 3 0.9990980 2.826783e-136
## cor10    2 vs 4 0.9956136 1.186185e-102
## cor11    2 vs 5 0.9989762 1.398791e-133
## cor12    2 vs 6 0.9988876 8.141502e-132
## cor13    2 vs 7 0.9995798 1.590111e-152
## cor14    2 vs 8 0.9990443 4.795013e-135
## cor15    2 vs 9 0.9990832 6.262543e-136
## cor16    2 vs 10 0.9988805 1.114875e-131
## cor17    3 vs 4 0.9980244 1.331972e-119
## cor18    3 vs 5 0.9994264 6.612416e-146

```

```

## cor19      3 vs 6 0.9993988 6.650110e-145
## cor20      3 vs 7 0.9994928 1.600257e-148
## cor21      3 vs 8 0.9973050 5.318698e-113
## cor22      3 vs 9 0.9994168 1.496608e-145
## cor23      3 vs 10 0.9989620 2.743538e-133
## cor24      4 vs 5 0.9976441 7.370042e-116
## cor25      4 vs 6 0.9976520 6.252802e-116
## cor26      4 vs 7 0.9964772 2.614028e-107
## cor27      4 vs 8 0.9917808 2.501950e-89
## cor28      4 vs 9 0.9978268 1.417424e-117
## cor29      4 vs 10 0.9960215 1.003350e-104
## cor30      5 vs 6 0.9986322 2.027655e-127
## cor31      5 vs 7 0.9990655 1.601072e-135
## cor32      5 vs 8 0.9975328 7.051565e-115
## cor33      5 vs 9 0.9991998 8.012992e-139
## cor34      5 vs 10 0.9989044 3.859015e-132
## cor35      6 vs 7 0.9993785 3.372592e-144
## cor36      6 vs 8 0.9964680 2.967844e-107
## cor37      6 vs 9 0.9991261 5.993121e-137
## cor38      6 vs 10 0.9989494 4.960029e-133
## cor39      7 vs 8 0.9981711 3.053264e-121
## cor40      7 vs 9 0.9995037 5.519521e-149
## cor41      7 vs 10 0.9990765 8.956911e-136
## cor42      8 vs 9 0.9970648 3.466921e-111
## cor43      8 vs 10 0.9977610 6.102946e-117
## cor44      9 vs 10 0.9983836 7.216465e-124

```

```
##
```

## ## 2. Kolmogorov-Smirnov Test Results:

##	comparison	ks_statistic	p_value
## D	1 vs 2	0.06	0.9937649
## D1	1 vs 3	0.05	0.9996333
## D2	1 vs 4	0.02	1.0000000
## D3	1 vs 5	0.08	0.9062064
## D4	1 vs 6	0.05	0.9996333
## D5	1 vs 7	0.06	0.9937649
## D6	1 vs 8	0.07	0.9670685
## D7	1 vs 9	0.04	0.9999982
## D8	1 vs 10	0.08	0.9062064
## D9	2 vs 3	0.03	1.0000000
## D10	2 vs 4	0.07	0.9670685
## D11	2 vs 5	0.05	0.9996333
## D12	2 vs 6	0.04	0.9999982
## D13	2 vs 7	0.02	1.0000000
## D14	2 vs 8	0.03	1.0000000
## D15	2 vs 9	0.04	0.9999982
## D16	2 vs 10	0.03	1.0000000
## D17	3 vs 4	0.05	0.9996333
## D18	3 vs 5	0.06	0.9937649
## D19	3 vs 6	0.02	1.0000000
## D20	3 vs 7	0.02	1.0000000
## D21	3 vs 8	0.04	0.9999982
## D22	3 vs 9	0.03	1.0000000
## D23	3 vs 10	0.04	0.9999982



```

## D24      4 vs 5      0.09 0.8127483
## D25      4 vs 6      0.05 0.9996333
## D26      4 vs 7      0.06 0.9937649
## D27      4 vs 8      0.07 0.9670685
## D28      4 vs 9      0.04 0.9999982
## D29      4 vs 10     0.08 0.9062064
## D30      5 vs 6      0.06 0.9937649
## D31      5 vs 7      0.06 0.9937649
## D32      5 vs 8      0.04 0.9999982
## D33      5 vs 9      0.06 0.9937649
## D34      5 vs 10     0.04 0.9999982
## D35      6 vs 7      0.03 1.0000000
## D36      6 vs 8      0.05 0.9996333
## D37      6 vs 9      0.03 1.0000000
## D38      6 vs 10     0.03 1.0000000
## D39      7 vs 8      0.03 1.0000000
## D40      7 vs 9      0.03 1.0000000
## D41      7 vs 10     0.03 1.0000000
## D42      8 vs 9      0.05 0.9996333
## D43      8 vs 10     0.04 0.9999982
## D44      9 vs 10     0.05 0.9996333

```

```
##
```

```
## 3. Root Mean Square Error Between Distributions:
```

```

##      comparison      rmse
## 1      1 vs 2 0.08061827
## 2      1 vs 3 0.04924833
## 3      1 vs 4 0.01778867
## 4      1 vs 5 0.06143171
## 5      1 vs 6 0.04950316
## 6      1 vs 7 0.06588700
## 7      1 vs 8 0.10817392
## 8      1 vs 9 0.05213392
## 9      1 vs 10 0.06769087
## 10     2 vs 3 0.03571660
## 11     2 vs 4 0.07835248
## 12     2 vs 5 0.03250816
## 13     2 vs 6 0.04315720
## 14     2 vs 7 0.02461213
## 15     2 vs 8 0.03347406
## 16     2 vs 9 0.04698409
## 17     2 vs 10 0.03780540
## 18     3 vs 4 0.04949169
## 19     3 vs 5 0.02538749
## 20     3 vs 6 0.02480585
## 21     3 vs 7 0.02255071
## 22     3 vs 8 0.06117038
## 23     3 vs 9 0.02850054
## 24     3 vs 10 0.03200326
## 25     4 vs 5 0.05885528
## 26     4 vs 6 0.05018166
## 27     4 vs 7 0.06518483
## 28     4 vs 8 0.10606138
## 29     4 vs 9 0.04777213

```

```

## 30    4 vs 10 0.06794804
## 31    5 vs 6 0.03988339
## 32    5 vs 7 0.02958268
## 33    5 vs 8 0.05366749
## 34    5 vs 9 0.03778891
## 35    5 vs 10 0.03318666
## 36    6 vs 7 0.02772706
## 37    6 vs 8 0.07122050
## 38    6 vs 9 0.02927052
## 39    6 vs 10 0.03309176
## 40    7 vs 8 0.05017981
## 41    7 vs 9 0.03078581
## 42    7 vs 10 0.02992986
## 43    8 vs 9 0.07199508
## 44    8 vs 10 0.05542910
## 45    9 vs 10 0.04207640

##
## 4. Regression Analysis for Each Distribution:

##      source      slope intercept r_squared      p_value
## log_area      1 -0.4799373  1.655257 0.8485806 5.874869e-42
## log_area1     2 -0.4913128  1.725389 0.8838731 1.297678e-47
## log_area2     3 -0.4839446  1.688698 0.8727120 1.171503e-45
## log_area3     4 -0.4782786  1.650797 0.8486298 5.781843e-42
## log_area4     5 -0.4866653  1.705628 0.8794854 8.006856e-47
## log_area5     6 -0.4805276  1.674285 0.8729008 1.089199e-45
## log_area6     7 -0.4857015  1.699302 0.8789826 9.821404e-47
## log_area7     8 -0.4926665  1.743552 0.8943796 1.237636e-49
## log_area8     9 -0.4752808  1.656676 0.8706598 2.567988e-45
## log_area9    10 -0.4818688  1.689285 0.8850458 7.886536e-48

## [1] "\n5. Area Under Curve Analysis:\n"

## # A tibble: 10 x 2
##   source auc
##   <dbl> <dbl>
## 1     1  2.58
## 2     2  2.79
## 3     3  2.70
## 4     4  2.58
## 5     5  2.74
## 6     6  2.66
## 7     7  2.73
## 8     8  2.86
## 9     9  2.64
## 10    10  2.72

## [1] "\n6. Distribution Summary Statistics:\n"

## # A tibble: 10 x 6
##   source mean_log_count median_log_count sd_log_count min_log_count
##   <dbl>      <dbl>      <dbl>      <dbl>      <dbl>
## 1     1         0.581         0.143         0.684         0
## 2     2         0.625         0.297         0.686         0
## 3     3         0.605         0.252         0.680         0
## 4     4         0.580         0.121         0.681         0

```

```
## 5      5      0.616      0.252      0.681      0
## 6      6      0.598      0.235      0.675      0
## 7      7      0.612      0.275      0.680      0
## 8      8      0.641      0.375      0.684      0
## 9      9      0.593      0.199      0.668      0
## 10     10     0.610      0.318      0.672      0
## # i 1 more variable: max_log_count <dbl>
```

## 11. Paper Comparisons