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CS241 - Winter 2024 - Course Notes

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Section 1: Lectures

Lecture 1

- Definition: A bit is a binary digit. That is, a 0 or 1 (off or on)
- Definition: A nibble is 4 bits.
 - Example: 1001
- Definition: A byte is 8 bits.
 - Example: 10011101
- in C/C++:
 - Char: 8 bits
 - Unsigned char: 8 bits
 - Short: 2 bytes/16 bits
 - int: 4 bytes
 - longlong: 16 bytes
- Definition: A word is a machine-specific grouping of bytes. For us, a word will be 4 bytes (32-bit architecture) though 8-byte (or 64-bit architectures) words are more common now.
- Definition (Hexadecimal Notation): The base-16 representation system is called the hexadecimal system. It consists of the numbers from 0 to 9 and the letters a, b, c, d, e, f (which convert to the numbers from 10 to 15 in decimal notation)
 - Sometimes we denote the base with a subscript like 10011101_2 and $9d_{16}$.
 - Also, for hexadecimal, you will routinely see the notation $0x9d$. (The $0x$ denotes a hexadecimal representation in computer science).
 - Note that each hexadecimal character is a nibble (4 bits).
- Conversion Table
 - Note: upper case letters are also used for hexadecimal notation. Context should make things clear.

Binary	Decimal	Hex
0000	0	0
0001	1	1
0010	2	2
0011	3	3
0100	4	4
0101	5	5
0110	6	6
0111	7	7

Binary	Decimal	Hex
1000	8	8
1001	9	9
1010	10	a
1011	11	b
1100	12	c
1101	13	d
1110	14	e
1111	15	f

- Notation:
 - Binary: 0, 1
 - Decimal(Base 10): 0, ..., 9
 - Hexadecimal: 0, ..., 9, A(10), B(11), C(12), D(13), E(14), F(15)
- Examples:
 - 0000(base 2) -> 0x0(base 16)
 - 1111(base 2) -> 0xf(base 16)
- What do bytes represent?
 - Numbers
 - Characters
 - Garbage in memory
 - Instructions (Words, or 4 bytes, will correspond to a compute instruction in our computer system)
- Bytes as Binary Numbers
 - Unsigned (non-negative integers)
 - $b_7 \dots b_0(\text{base } 2) = b_7 \times 2^7 + \dots + b_0 \times 2^0(\text{base } 10)$
 - Example: $01010101 = 0 \times 2^7 + \dots + 1 \times 2^0$
 - Converting to Binary:

- One way: Take the largest power of 2 less than the unsigned integer, subtract and repeat
- Another way is to constantly divide by 2, get the remainder for each division, reading *from the bottom to up* at the end, and that will be the binary representation of this unsigned integer

▪ Example: 38

Number	Quotient	Remainder
38	19	0
19	9	1
9	4	1
4	2	0
2	1	0
1	0	1

▪ Brief Explanation: Consider

$$N = b_0 + 2b_1 + 2^2b_2 + \dots$$

The remainder when dividing N by 2 gives the b_0 value. After doing $\frac{N-b_0}{2}$, we end of with

$$\frac{N - b_0}{2} = b_1 + 2b_2 + 2^2b_3 + \dots$$

and we can repeat the process. (This is why we have to read bottom-up as we get b_0 first, then $b_1 \dots$)

◦ Signed integers

- Attempt 1: make the first bit a signed bit. This is called the "sign-magnitude" representation
 - Problems:
 - Two representations of 0(wasteful and awkward)
 - Arithmetic is tricky. Is the sum of a positive number and a negative number positive or negative? It depends!
- Attempt 2: Two's complement form
 - Similar to "sign-magnitude" representation in spirit, first bit is 0 if non-negative, 1 if negative
 - Negate a value by just subtracting from zero and *letting it overflow*.
 - Decimal to Two's Complement:
 - A trick to the same thing of negating a value:
 - Take the complement of all bits (flip the 0 bits to 1 and 1 bits to 0)
 - Add 1
 - A slightly faster trick is to locate the rightmost 1 bit and flip all the bits to the left of it
 - Example: 11011010 Negating: 00100110 = 00100101 + 1
 - Note: Flipping the bits and adding 1 is the same as
 - subtracting 1 and flipping the bits for non-zero numbers
 - subtracting from 0
 - Example: compute -38_{10} using this notation in one byte of space:
 - Step 1: $38_{10} = 00100110_2$
 - Step 2: take the complement of all the bits: 11011001_2
 - Step 3: plus 1: 11011010_2
 - Two's Complement to Decimal
 - Let's compute -38_{10} using one-byte Two's complement. First, write 38 in binary: $38_{10} = 00100110_2$. Next, take the complement of all the bits 11011001_2 . Finally, add 1: 11011010_2 . This last value is -38_{10} .
 - To convert 11011010_2 , a number in Two's complement representation, to decimal, one method is to flip the bits and add 1: $00100110_2 = 2^5 + 2^2 + 2^1 = 38$. Thus, the corresponding positive number is 38 and so the original number is -38 .

- Another way to do this computation is to treat the original number 11011010_2 as an unsigned number, convert to decimal and subtract 28 from it (since we have 8 bits, and the first bit is a 1 meaning it should be a negative value). This also gives -38

$$\begin{aligned} 11011010_2 &= 2^7 + 2^6 + 2^4 + 2^3 + 2^1 - 2^8 \\ &= 128 + 64 + 16 + 8 + 2 - 256 \\ &= 218 - 256 \\ &= -38 \end{aligned}$$

- The idea behind [one byte] Two's Complement notation is based on the following observations:
 - The range for unsigned integers is 0 to 255. Recall that 255 is 11111111_2 . If we add 1 to 255, then, after discarding overflow bits, we get the number 0.
 - Thus, let's treat 2^8 as 0, i.e., let's work modulo $2^8 = 256$. In this vein, we set up a correspondence between the positive integer k and the unsigned integer $2^8 - k$. Since we are working modulo 2^8 , subtracting a positive integer k from 0 is the same as subtracting it from 2^8 .
 - In this case, note that $255 = 2^8 - 1 = 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0$ and in general

$$2^n - 1 = \sum_{i=0}^{n-1} 2^i$$

- As an explicit example (which can be generalized naturally) take a number, say $38_{10} = 00100110_2 = 2^5 + 2^2 + 2^1$. What should the corresponding negative number be? Well, note that we've said subtracting a positive integer k from 0 is the same as subtracting it from 2^8 :

$$\begin{aligned} 2^8 - 1 &= 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 \\ 2^8 - 1 &= 38 + 2^7 + 2^6 + 2^4 + 2^3 + 2^0 \\ 2^8 - 38 &= 2^7 + 2^6 + 2^4 + 2^3 + 2^0 + 1 \end{aligned} \quad (\text{flip the bits and add 1})$$

- We mentioned that another method of negating a two's complement number is to flip the bits to the left of the rightmost 1. Justify why this technique works.
 - Every bit to the right of the rightmost 1 is a 0. When we "flip the bits", these become 1s. When we "add 1", the carry propagates up until the position of the "rightmost 1" (the "rightmost 1" is 0 after flip and will stop propagating when the carry reaches this point, and everything on the left of the "rightmost 1" is flipped).
- The main difference between signed and unsigned binary arithmetic is that we are now working modulo 256 (or, more generally, 2^n in the case of n -bit Two's complement numbers)
- When working in Two's complement, overflow occurs when adding numbers if the original two numbers have the same sign, but the result has a different sign.
- Arithmetic of Signed Integers
 - All of the arithmetic works by ignoring overflow precisely because arithmetic works in \mathbb{Z}_{256} !
- What is the range of numbers expressible in one-byte Two's Complement notation?
 - $-128 \sim 127$
- Definitions: The Most Significant Bit (MSB) is the left-most bit (highest value/sign bit); The Least Significant Bit (LSB) is the right-most bit (lowest value).

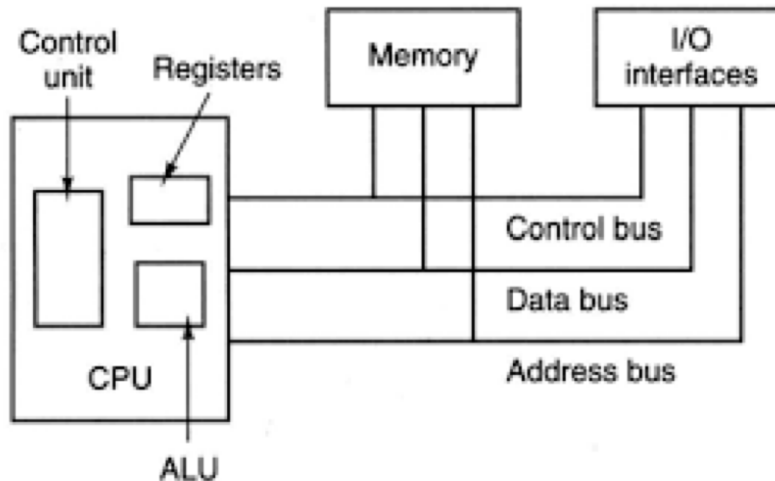
Lecture 2

- ASCII (American Standard Code for Information Interchange) uses 7 bits to represent characters.

```
char c = '0';
printf("%c", c);
// stdout: 0
printf("%d", (int)c);
// stdout: 48
```

- Bit-Wise Operators

- Example: suppose we have unsigned char $a=5$, $b=3$;, which means $a = 00000101$, $b = 00000011$
 - Bitwise not $\sim a$, for example $c = \sim a$; gives $c = 11111010$
 - Bitwise and $\&$, for example $c = a \& b$; gives $c = 00000001$
 - Bitwise or $|$, for example $c = a | b$; gives $c = 00000111$
 - Bitwise exclusive \wedge (only true if the bit in a and b is different), for example $c = a \wedge b$; gives $c = 00000110$
 - Bitwise shift right or left $>>$ and $<<$, for example
 - $c = a >> 2$; gives $c = 00000001$ and
 - $c = a << 3$; gives $c = 00101000$
 - $a << 1$ equivalent to $a * 2$
 - $a >> 1$ equivalent to $a / 2$
 - These can even be combined with the assignment operator: $c \&= 5$;



- CPU with Memory
- MIPS has 32 registers that are called “general purpose”
 - Some general-purpose registers are special:
 - $\$0$ is always 0
 - $\$31$ is for return address
 - $\$30$ is our stack pointer
 - $\$29$ is our frame pointer
- Problem: We only know from context what bits have what meaning, and in particular, which are instructions.
 - Solution: Convention is to set memory address 0 in RAM to be an instruction. $0x0$: instruction $i1$
- Problem: How does MIPS know what to do next?
 - Solution: Have a special register called the Program Counter (or PC for short) to tell us what instruction to do next.
- Problem: How do we put our program into RAM?
 - Solution: A program called a loader puts our program into memory and sets the PC to be the first address.
- Algorithm 1 Fetch-Execute Cycle

```
PC=0
while true do
  IR = MEM[PC]
  PC += 4
  Decode and execute instruction in IR
end while
```

- Write a program in MIPS that adds the values of registers $\$8$ and $\$9$ and stores the result in register $\$3$.

```
add $d, $s, $t
0000 00ss ssst tttt dddd d000 0010 0000
```

- Why 5 bits for each? Because there are 32 registers $\$0 - \31 and $2^5 = 32$
- Adds registers $\$s$ and $\$t$ and stores the sum in register $\$d$. Important! The order of $\$d$, $\$s$ and $\$t$ are shifted in the encoding.

Lecture 3

- **Putting values in registers** Load immediate and skip. This places the next value in RAM [an immediate] into $\$d$ and increments the program counter by 4 (it skips the next line which is usually not an instruction).

```
lis $d: 0000 0000 0000 0000 dddd d000 0001 0100
# What it really does is
$d = MEM[PC]
PC = PC + 4
```

- How do we get the value we care about into the next location in RAM?

```
.word i: iiii iiii iiii iiii iiii iiii iiii iiii
```

- The above is an assembler directive (not a MIPS instruction). The value i , as a two's complement integer, is placed in the correct memory location in RAM as it occurs in the code.
 - Can also use hexadecimal values: $0xi$
 - Decimal is also allowed.
- Example:

```
lis $1
.word 10
# At this moment, $1 = 10
add $1, $1, $0
```

- Example: Write a MIPS program that adds together 11 and 13 and stores the result in register $\$3$.

```
lis $1
.word 11
list $2
.word 13
add $3, $1, $2
# Solution on the course notes
lis $8      0000 0000 0000 0000 0100 0000 0001 0100
.word 11    0000 0000 0000 0000 0000 0000 0000 1011
lis $9      0000 0000 0000 0000 0100 1000 0001 0100
.word 0xd   0000 0000 0000 0000 0000 0000 0000 1101
add $3,$8,$9 0000 0001 0000 1001 0001 1000 0010 0000
# The code on the left is what we call Assembly Code.
# The code on the right is what we call Machine Code.
```

- Jump Register. Sets the pc to be $\$s$.

```
jr $s
0000 00ss sss0 0000 0000 0000 0000 1000
```

- For us, our return address will typically be in $\$31$, so we will typically call the below. This command returns control to the loader.

```
jr $31
0000 0011 1110 0000 0000 0000 0000 1000
```

- So the complete example for the example is (so that the while loop will terminate)

```
lis $8      0000 0000 0000 0000 0100 0000 0001 0100
.word 11    0000 0000 0000 0000 0000 0000 0000 1011
lis $9      0000 0000 0000 0000 0100 1000 0001 0100
.word 0xd   0000 0000 0000 0000 0000 0000 0000 1101
add $3,$8,$9 0000 0001 0000 1001 0001 1000 0010 0000
jr $31     0000 0011 1110 0000 0000 0000 0000 1000
```

- To multiply two words, we need to use the two special registers `hi` and `lo`.
 - `hi` is most significant 4 bytes
 - `lo` is least significant 4 bytes

```
mult $s, $t
0000 00ss ssst tttt 0000 0000 0001 1000
```

- The above performs the multiplication and places the most significant word (largest 4 bytes) in `hi` and the least significant word in `lo`.
- `div $s, $t` performs integer division and places the quotient s/t in `lo` [`lo quo`] and the remainder `st` in `hi`. Note the sign of the remainder matches the sign of the divisor stored in `$s`.

```
div $s, $t
0000 00ss ssst tttt 0000 0000 0001 1010
```

- Multiplication and division happen on these special registers `hi` and `lo`. How can I access the data?
 - Move from register `hi` into register `$d`.

```
mfhi $d
0000 0000 0000 0000 dddd d000 0001 0000
```

- Move from register `lo` into register `$d`.

```
mflo $d
0000 0000 0000 0000 dddd d000 0001 0010
```

- RAM
 - Large[r] amount of memory stored off the CPU.
 - RAM access is slower than register access (but is larger, as a tradeoff).
 - Data travels between RAM and the CPU via the bus.
 - Modern day RAM consists of in the neighbourhood of 10^{10} bytes.
 - Instructions occur in RAM starting with address 0 and increase by the word size (in our case 4).
 - But, this simplification will vanish later...
 - Each memory block in RAM has an address; say from 0 to $n - 1$
 - Words occur every 4 bytes, starting with byte 0. Indexed by 0, 4, 8, ... $n - 4$.
 - Words are formed from consecutive, aligned (usually) bytes.
 - Cannot directly use the data in the RAM. Must transfer first to registers.
- Load word. Takes a word from RAM and places it into a register. Specifically, load the word in `MEM[$s + i]` and store in `$t`.

```
lw $t, i($s)
1000 11ss ssst tttt iiii iiii iiii iiii
# which is equivalent to
$t = MEM[$s + i]
# Example
lw $1, -4($30)
# which means
$1 <- MEM[$30 - 4]
```

- Store word. Takes a word from a register and stores it into RAM. Specifically, load the word in `$t` and store it in `MEM[$s + i]`.

```
sw $t, i($s)
1010 11ss ssst tttt iiii iiii iiii iiii
```

- Note that `i` must be an immediate, NOT another register! It is a 16-bit Two's complement immediate
- Example: Suppose that `$1` contains the address of an array of words, and `$2` takes the number of elements in this array (assume less than 220). Place the number 7 in the last possible spot in the array.

```
# First element in the array is arr, then the second element is arr + 4 ... the last element in the array is
arr + 4 * (length - 1)
lis $8 ; 7
.word 7
lis $9 ; 4
```

```
.word 4
mult $2, $9 ; length * 4
mflo $3 ; length * 4
add $3, $3, $1 ; arr + length 4
sw $8, -4($3) ; MEM[$3 - 4] = $8
jr $31
```

- Branch on equal. If $\$s == \t then $pc += i * 4$. That is, skip ahead i many instructions if $\$s$ and $\$t$ are equal.

```
beq $s, $t, i
0001 00ss ssst tttt iiii iiii iiii iiii
# It is like
if ($s == $t) {
    PC += i*4
}
```

- Branch on not equal. If $\$s != \t then $pc += i * 4$. That is, skip ahead i many instructions if $\$s$ and $\$t$ are not equal.

```
bne $s, $t, i
0001 01ss ssst tttt iiii iiii iiii iiii
# It is like
if ($t != $s) {
    PC += i*4
}
```

- Example:

```
beq $0, $0, 0 ; This executes the next instruction as PC has been updated to +4 already
beq $0, $0, 1 ; This executes the second next instruction
```

Lecture 4

- Write an assembly language MIPS program that places the value **3** in register $\$2$ if the signed number in register $\$1$ is odd and places the value **11** in register $\$2$ if the number is even.

```
lis $8 ; $8 = 2
.word 2
lis $9 ; $9 = 3
.word 3
lis $2 ; $2 = 11
.word 11
div $1, $8
mfhi $3
beq $3, $0, 1
add $2, $9, $0
jr $31
```

- Set Less Than. Sets the value of register $\$d$ to be **1** provided the value in register $\$s$ is less than the value in register $\$t$ and sets it to be **0** otherwise.

```
slt $d, $s, $t
0000 00ss ssst tttt dddd d000 0010 1010
# which basically means
if ($s < $t) {
    $d = 1 (true)
} else {
    $d = 0 (false)
}
```

- Example: Write an assembly language MIPS program that negates the value in register $\$1$ provided it is positive.

```
slt $2, $1, $0
bne $2, $0, 1
sub $1, $0, $1
jr $31
```


- Exercise: Write an assembly language MIPS program that places the absolute value of register *1inregister2*.

```
add $2, $1, $0 ; $2 = $1
slt $3, $0, $1 ; 0 < $1
bne $3, $0, 1
sub $2, $0, $2 ; $2 = 0 - $2
jr $31
```

- Looping exmaple: Write an assembly language MIPS program that adds together all even numbers from 1 to 20 inclusive. Store the answer in register \$3.
 - Note: semicolons for comments in MIPS assembly

```
lis $2
.word 20
lis $1
.word 2
add $3, $0, $0
add $3, $3, $2 ; line -3
sub $2, $2, $1 ; line -2
bne $2, $0, -3 ; line -1 from here
jr $31
```

- Labels aren't machine code, so don't take words. That means that for `beq` and `bne`, *labels don't have "line numbers" on their own*. A label at the end of code is allowed. It has the address of what would be the first instruction after the program.

```
label: operation commands
```

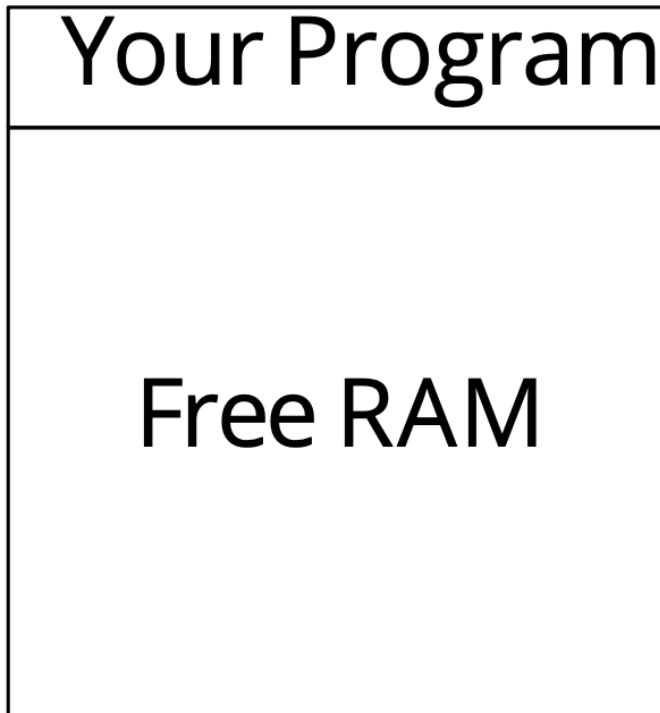
- Example: `sample` has the address `0x4`, which is the location of `add $1, $0, $0`.

```
sub $3, $0, $0
sample:
add $1, $0, $0
```

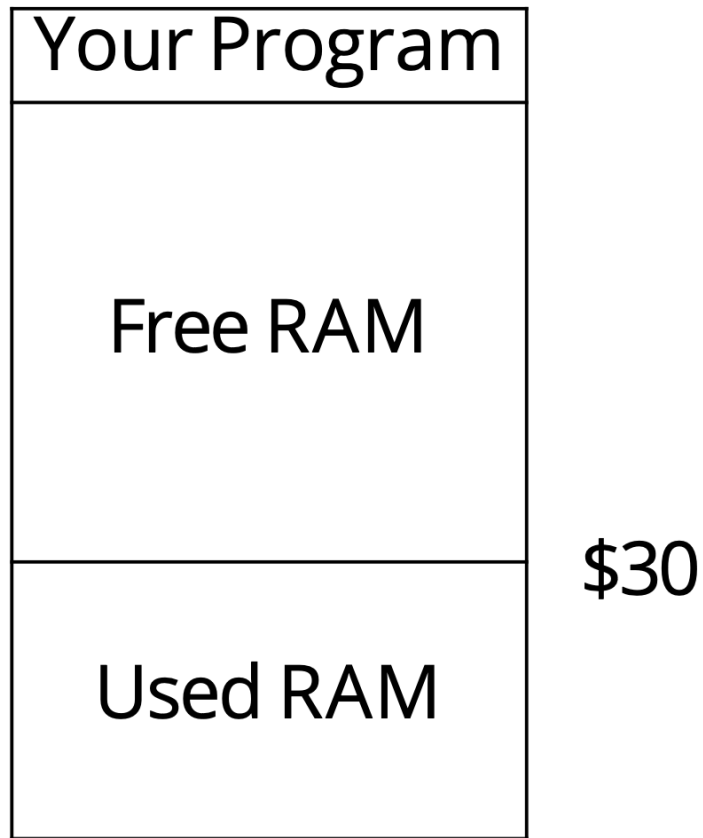
- A better way to loop without hard-coding `-3` in the previous example is (otherwise, if we were to, say, add a new instruction in between the lines specified by our branching, all our numbers would be incorrect.)
 - Note that `top` in `bne` is computed by the assembler to be the *difference between the program counter and top*. That is, here it computes $(top - PC)/4$ which is $(0x14 - 0x20)/4 = -3$
 - `PC` is the line number after the current line

```
lis $2
.word 20
lis $1
.word 2
add $3, $0, $0
top:
    add $3, $3, $2
    sub $2, $2, $1
    bne $2, $0, top
jr $31
```

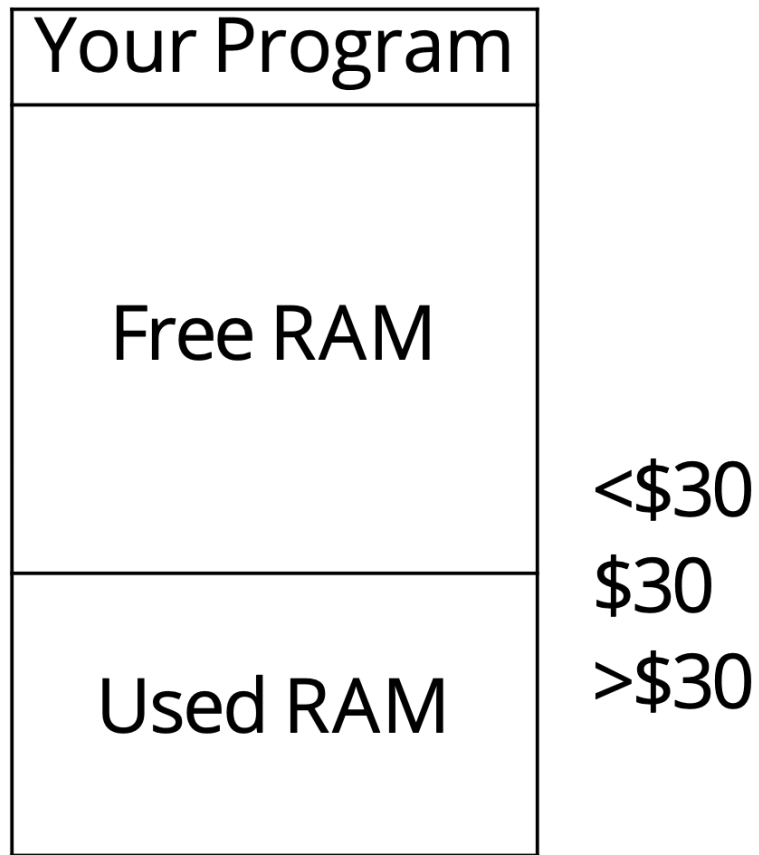
- RAM



- Register `$30` initially points to the very bottom of the free RAM. It can be used as a bookmark to separate the used and unused free RAM if we allocate from the one end, and push and pop things like a stack! In other words, we will use `$30` as a pointer to the top of a stack.
- Really, `$30` points to the top of the stack of memory in RAM.

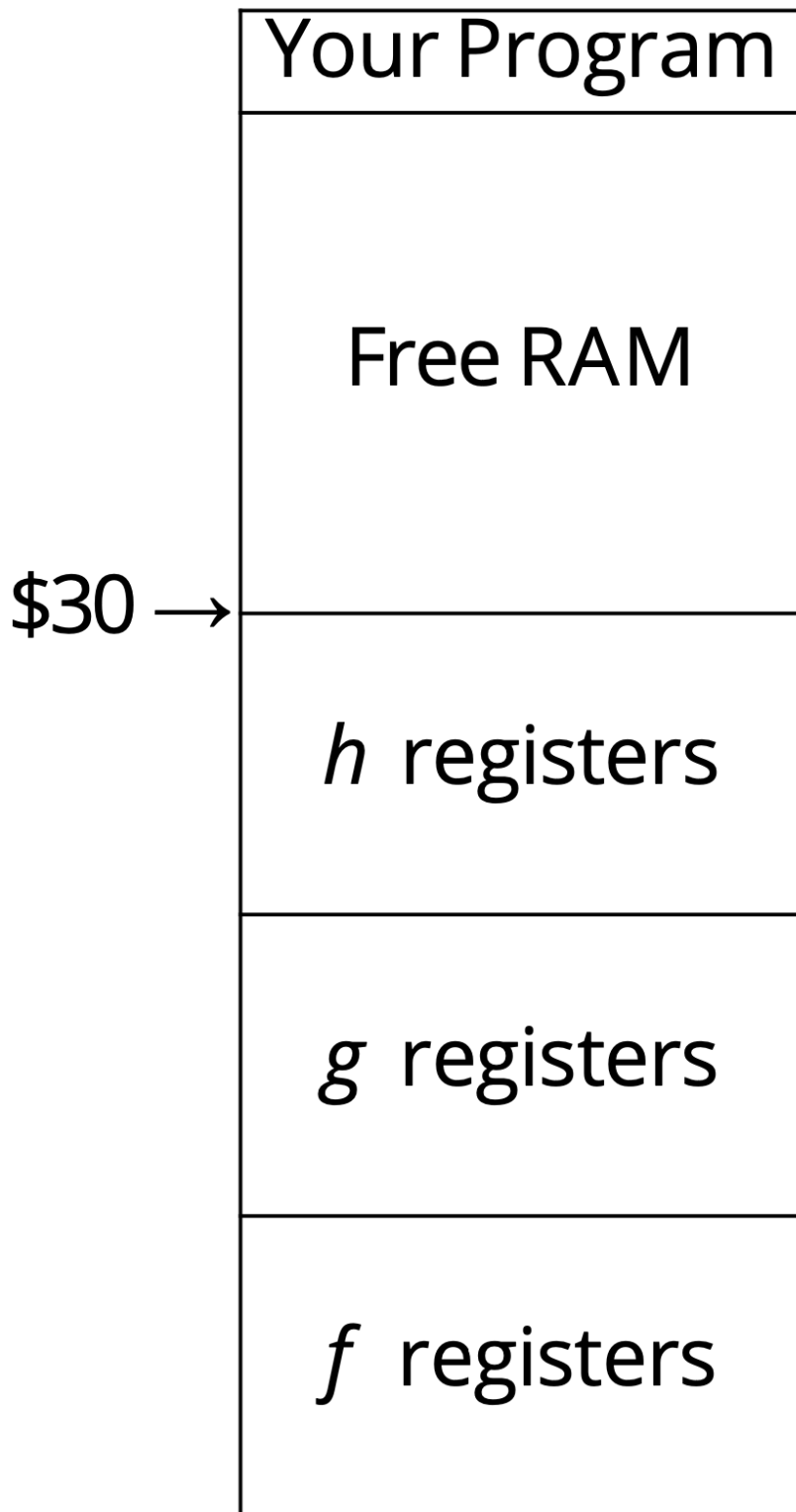


- Because our program is at zero, the stack grows from high memory to low memory, so pushing involves reducing the value of \$30.



- Example: Suppose procedures f , g and h are such that:

```
f calls procedure g
  g calls procedure h
    h returns
  g returns
f returns.
```



- In the previous example:
 - Calling procedures pushes more registers onto the stack and returning pops them off.
 - This is a stack, and we call \$30 our **stack pointer**.
 - We can also use the stack for local storage if needed in procedures. Just reset \$30 before procedures return.
- Template for a procedure *f* that modifies registers \$1 and \$2:

```
f:
sw $1, -4($30) ; Push registers we modify
sw $2, -8($30)
lis $2 ; Decrement stack pointer
.word 8
```

```

sub $30, $30, $2
; Insert procedure here
add $30, $30, $2 ; Assuming $2 is still 8
lw $2, -8($30) ; Pop = restore
lw $1, -4($30)
; Uh oh! How do we return?

```

- There is a problem with returning:

```

main:
lis $8
.word f ; Recall f is an address
jr $8 ; Jump to the first line of f
(NEXT LINE)

```

- Once *f* completes, we really want to jump back to the line labelled above as (NEXT LINE), i.e., set the program counter back to that line. How do we do that?
- Jump and Link Register. Sets \$31 to be the PC and then sets the PC to be \$s. Accomplished by `temp = $s` then `$31 = PC` then `PC = temp`.

```

jalr $s
0000 00ss sss0 0000 0000 0000 1001

```

- Main Changes

```

main:
lis $8
.word f
sw $31, -4($30) ; Push $31 to stack
lis $31 ; Use $31 since it's been saved .word 4
sub $30, $30, $31
jalr $8 ; Overwrites $31
lis $31 ; Use $31 since we'll restore it .word 4
add $30, $30, $31
lw $31, -4($30) ; Pop $31 from stack
jr $31 ; Return to loader

```

- Procedure Changes

```

f:
sw $1, -4($30) ; Push registers we will modify
sw $2, -8($30)
lis $2
.word 8
sub $30, $30, $2 ; Decrement stack pointer
; Insert procedure here
add $30, $30, $2 ; Assuming $2 is still 8
lw $2, -8($30) ; Pop registers to restore
lw $1, -4($30)
jr $31 ; New line!

```

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Section 2: Tutorials

Tutorial 1

- What is Binary?
 - Binary - ways our machines encode info, and $b \in 0, 1$
- Eg. what is 1000 be
 - $2^3 = 8$ unsigned magnitude
 - -8 2's complement
 - $[T, F, F, F]$ array of bools
 - "backspace char" in ASCII
 - **Representation matters**
- Unsigned binary: n-bit binary number is represented as $b_{n-1}, b_{n-2}, \dots, b_0$, where $b \in 0, 1$
- To convert to decimal: $2^{n-1} \times b_{n-1} + \dots + 2^0 \times b_0$
- Decimal to binary
 - Idea 1: take the highest powers of 2 from the decimal (inefficient)
 - Idea 2: Repeatedly divide the number by 2, tracking the quotient & remainder
 - Eg. Convert 23 to binary

Number	Quotient	Remainder
23/2	11	1
11/2	5	1

Number	Quotient	Remainder
5/2	2	1
2/2	1	0
1/2	0	1

- and read from bottom to up, that will be $10111_2 = 23_{10}$
- 2's complement
 - Range of values for n-ary
 - Unsigned Binary $0 \sim 2^n - 1$
 - 2's complement $-2^{n-1} \sim 2^{n-1} - 1$
- Convert decimal to 2's complement
 - if number is ≥ 0 : use the unsigned representation
 - if number is < 0 :
 - Get the binary rep of the positive number
 - flip the bits
 - then add 1
- Convert from 2's complement to decimal
 - Method 1: if $b_{n-1} = 1$, then flip the bits, add 1 and negate the positive decimal
 - Method 2: Treat $b_{n-1} = 1$ as -2^{n-1} , and add the rest as unsigned representation
- Assembly
 - CS 241: MIPS
 - Runs programs \$ stores its data all in MEM (RAM)
 - 32 bits system where instructions are encoded as 4 bytes (1 word)
 - Registers hold 1 word of info
 - Special registers
 - 0 = 0\$, immutable
 - 31\$, end address in RAM, jr \$31 means return address
 - 3, 29, 30\$
 - *iii* ... <- 2's complement number
 - divu, multu, addi ... treats the register values as unsigned binary
 - **Programs live in the same space in MEM (RAM) as the data they operate on**
 - PC cannot distinguish the two
 - Fetch-Execute Cycle

```
PC = 0x00
while True do:    // until PC = $31
    IR = MEM[PC]
    PC = PC + 4
    ... decode $ execute IR ...
done
```

- Constant Values
 - Use the Load Immediate Skip command (`lis $s`) followed by an instruction to save into `$s`.
 - `lis $s` -> skip the next instruction -> store that instruction into `$s`
 - Use with `.word i` to store `i` into `$s`
 - Eg. Store 10 into `$5`

```
lis $5
.word 10
; the above two lines of commands skips the .word 10 & sets $5 = 10
```

- Machine Code (based on the order of machine code horizontally for `lis $5`)
 - 000000 (operating code)
 - 000000 (`$s`)
 - 000000 (`$t`)
 - 00101 (`$d`)
 - 000000 (dead code, always be 0)

- 010100 (function code)
- Machine Code (.word 10)
 - 00000 000 001010

Section 3: Reviews

Final Review