

#### **Jeremy Cole**

Geek, electronics nerd, database nerd, aviation nerd, father of three.

# Search this blog

Search ...

#### **Pages**

About Me InnoDB Need help?

#### **Recent Posts**

Black History Month Join me... Invest in Humanity, too Invest in Humanity 2016 A response to those supporting Trump based on his abortion position

A constructive start for post-election 2016

# Recent Tweets

My Tweets



### Categories

Select Category

# B+Tree index structures in InnoDB

[This post refers to innodb\_ruby version 0.8.8 as of February 3, 2014.]

In <u>On learning InnoDB: A journey to the core</u>, I introduced the <u>innodb diagrams</u> project to document the InnoDB internals, which provides the diagrams used in this post. Later on in <u>A quick introduction to innodb ruby</u> I walked through installation and a few quick demos of the <code>innodb\_space</code> command-line tool.

The physical structure of InnoDB's INDEX pages was described in <a href="The physical structure of InnoDB">The physical structure of InnoDB</a> index pages. We'll now look into how InnoDB logically structures its indexes, using some practical examples.

### An aside on terminology: B+Tree, root, leaf, and level

InnoDB uses a <u>B+Tree structure</u> for its indexes. A B+Tree is particularly efficient when data doesn't fit in memory and must be read from the disk, as it ensures that a fixed maximum number of reads would be required to access any data requested, based only on the depth of the tree, which scales nicely.

An index tree starts at a "root" page, whose location is fixed (and permanently stored in the InnoDB's data dictionary) as a starting point for accessing the tree. The tree may be as small as the single root page, or as large as many millions of pages in a multi-level tree.

Pages are referred to as being "leaf" pages or "non-leaf" pages (also called "internal" or "node" pages in some contexts). Leaf pages contain actual row data. Non-leaf pages contain only pointers to other non-leaf pages, or to leaf pages. The tree is balanced, so all branches of the tree have the same depth.

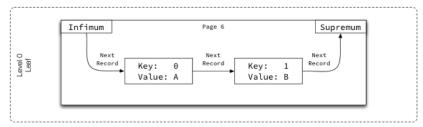
InnoDB assigns each page in the tree a "level": leaf pages are assigned level 0, and the level increments going up the tree. The root page level is based on the depth of the tree. All pages that are neither leaf pages nor the root page can also be called "internal" pages, if a distinction is important.

# Leaf and non-leaf pages

For both leaf and non-leaf pages, each record (including the infimum and supremum system records) contain a "next record" pointer, which stores an offset (within the page) to the next record. The linked list starts at infimum and links all records in ascending order by key, terminating at supremum. The records are not physically ordered within the page (they take whatever space is available at the time of insertion); their only order comes from their position in the linked list.

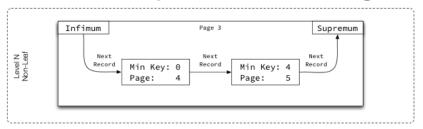
Leaf pages contain the non-key values as part of the "data" contained in each record:

# B+Tree Simplified Leaf Page



Non-leaf pages have an identical structure, but instead of non-key fields, their "data" is the page number of the child page, and instead of an exact key, they represent the *minimum key* on the child page they point to:

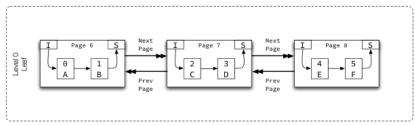
# B+Tree Simplified Non-Leaf Page



# Pages at the same level

Most indexes contain more than one page, so multiple pages are linked together in ascending and descending order:

# **B+Tree Simplified Level**

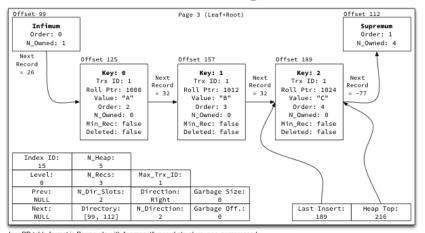


Each page contains pointers (in the FIL header) for "previous page" and "next page", which for INDEX pages are used to form a doubly-linked list of pages at the same level (e.g. leaf pages, at level 0 form one list, level 1 pages form a separate list, etc.).

# A detailed look at a single-page table

Let's take a look at most of what's B+Tree related in a single index page:

# B+Tree Detailed Page Structure



InnoDB table format is Barracuda with "compact" record structure, non-compressed. Table created with: CREATE TABLE t (1 INT NOT NULL, s CHAR(18) NOT NULL, PRIMARY KEY(1)) ENGINE=InnoDB; Table populated with: INSERT INTO t (1, s) VALUES (8,  $^{\rm M-N}$ ), (1,  $^{\rm BP}$ ), (2,  $^{\rm m-N}$ ); Record size: 5 (header) + 4 (PK) + 6 (TRX\_ID) + 7 (ROLL\_PTR) + 10 (non-key fields) = 32 bytes

#### Create and populate the table

The test table in use in the illustration above can be created and populated with (make sure you're using innodb\_file\_per\_table and using Barracuda file format):

```
CREATE TABLE t_btree (
i INT NOT NULL,
s CHAR(10) NOT NULL,
PRIMARY KEY(i)
) ENGINE=InnoDB;

INSERT INTO t_btree (i, s)
VALUES (0, "A"), (1, "B"), (2, "C");
```

While this table is quite small and not realistic, it does demonstrate nicely how records and record traversal works.

#### Verify the basic structure of the space file

The table should match what we've examined before, with the three standard overhead pages (FSP\_HDR, IBUF\_BITMAP, and INODE) followed by a single INDEX page for the root of the index, and in this case two unused ALLOCATED pages.

<pre>\$ innodb_</pre>	_space -f	t_btree.ibd	space-page-type-regions
start	end	count	type
0	0	1	FSP_HDR
1	1	1	IBUF_BITMAP
2	2	1	INODE
3	3	1	INDEX
4	5	2	FREE (ALLOCATED)

The **space-index-pages-summary** mode will give us a count of records in each page, and is showing the expected 3 records:

<pre>\$ innodb_sp</pre>	ace -f t	t_btree.i	bd space	-index-p	ages-summary
page	index	level	data	free	records
3	18	0	96	16156	3
4	0	0	0	16384	0
5	0	0	0	16384	0

(Note that <code>space-index-pages-summary</code> also shows the empty <code>ALLOCATED</code> pages as empty pages with zero records, since that's often what you're interested in for plotting purposes.)

The **space-indexes** mode will show the stats about our **PRIMARY KEY** index, which is consuming a single page on its **internal** file segment:

<pre>\$ innodb_space -f t_btree.ibd space-indexes</pre>						
id	root	fseg	used	allocated	fill_factor	
18	3	internal	1	1	100.00%	
18	3	leaf	0	0	0.00%	

#### Set up a record describer

In order for innodb\_ruby to parse the contents of records, we need to provide a record describer, which is just a Ruby class providing a method that returns a description of an index:

```
class SimpleTBTreeDescriber < Innodb::RecordDescriber
type :clustered
key "i", :INT, :NOT_NULL
row "s", "CHAR(10)", :NOT_NULL
end</pre>
```

We need to note that this is the clustered key, provide the column descriptions for the key, and the column descriptions for the non-key ("row") fields. It's necessary to ask innodb\_space to load this class with the following additional arguments:

```
-r -r ./simple_t_btree_describer.rb -d SimpleTBTreeDescriber
```

#### Look at the record contents

The root page (which is a leaf page) in this example can be dumped using the **page-dump** mode and providing the page number for the root page:

```
$ innodb_space -f t_btree.ibd -r ./simple_t_btree_describer.rb -d SimpleTBTreeDes
```

Aside from some parts of this output we've looked at before, it will now print a "records:" section with the following structure per record:

```
{:format=>:compact,
 :offset=>125.
 :header=>
  {:next=>157,
    :type=>:conventional,
   :heap_number=>2,
   :n owned=>0
   :min_rec=>false,
   :deleted=>false
    :field_nulls=>nil,
    :field_lengths=>[0, 0, 0, 0],
    :field_externs=>[false, false, false, false]},
 :next=>157
 :type=>:clustered,
:key=>[{:name=>"i",
                         :type=>"INT", :value=>0, :extern=>nil}],
 :transaction_id=>"0000000f4745",
 :roll_pointer=>
 f:is_insert=>true, :rseg_id=>8, :undo_log=>{:page=>312, :offset=>272}},
:row=>[{:name=>"s", :type=>"CHAR(10)", :value=>"A", :extern=>nil}]}
```

This should align with the above detailed illustration perfectly, as I've copied most of the information from this example for accuracy. Note the following aspects:

- The :format being :compact indicates that the record is the new "compact" format in Barracuda format tables (as opposed to "redundant" in Antelope tables).
- The :key listed in the output is an array of key fields for the index, and :row is an array of non-key fields.
- The :transaction\_id and :roll\_pointer fields are internal fields for MVCC included in each record, since this is a clustered key (the PRIMARY KEY).
- The :next field within the :header hash is a relative offset (32) which must be added to
  the current record offset (125) to yield the actual offset of the next record (157). For convenience this calculated offset is included as :next in the record hash.

#### Recurse the index

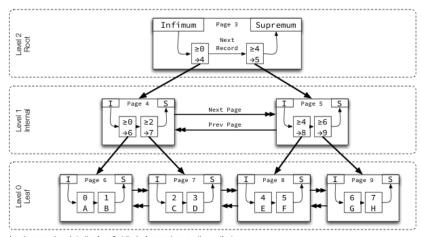
A nice and simple output of recursing the entire index can be achieved with the **index-recurse** mode, but since this is still a single-page index, the output will be very short:

```
$ innodb_space -f t_btree.ibd -r ./simple_t_btree_describer.rb -d SimpleTBTreeDes
RECORD: (i=0) -> (s=B)
RECORD: (i=2) -> (s=C)
```

# Building a non-trivial index tree

A multi-level index tree (overly simplified) in InnoDB looks like:

# **B+Tree Structure**



Levels are numbered starting from 0 at the leaf pages, incrementing up the tree.

Pages on each level are doubly-linked with previous and next pointers in ascending order by key.

Records within a page are singly-linked with a next pointer in ascending order by key.

Infirmum represents a value lower than any key on the page, and is always the first record in the singly-linked list of records.

Supremum represents a value higher than any key on the page, and is always the last record in the singly-linked list of records.

Non-leaf pages contain the minimum key of the child page and the child page number, called a "node pointer".

As previously described, all pages at each level are doubly-linked to each other, and within each page, records are singly-linked in ascending order. Non-leaf pages contain "pointers" (containing the child page number) rather than non-key row data.

If we use the simpler table schema with 1 million rows created in A quick introduction to innodb\_ruby, the tree structure looks a little more interesting:

```
$ innodb_space -f t.ibd -r ./simple_t_describer.rb -d SimpleTDescriber -p 3 index
ROOT NODE #3: 2 records, 26 bytes
NODE POINTER RECORD >= (i=252) -> #36
  INTERNAL NODE #36: 1117 records, 14521 bytes
NODE POINTER RECORD >= (i=252) -> #4
     LEAF NODE #4: 446 records, 9812 bytes
        RECORD: (i=1) -> ()
RECORD: (i=2) -> ()
RECORD: (i=3) -> ()
        RECORD: (i=4) \rightarrow ()
<many lines omitted>
     NODE POINTER RECORD >= (i=447) -> #1676
     LEAF NODE #1676: 444 records, 9768 bytes
RECORD: (i=447) -> ()
RECORD: (i=448) -> ()
        RECORD: (i=449) -> ()
RECORD: (i=450) -> ()
<many lines omitted>
     NODE POINTER RECORD >= (i=891) -> #771
     LEAF NODE #771: 512 records, 11264 bytes
        RECORD: (i=891) -> ()
        RECORD: (i=892) -> ()
        RECORD:
                  (i=893) -> ()
        RECORD: (i=894)
```

This is a three-level index tree, which can be seen by the ROOT, INTERNAL, LEAF lines above. We can see that some pages are completely full, with 468 records consuming almost 15 KiB of the

16 KiB page.

Looking at a non-leaf page (page 36, in the above output) using the page-dump mode, records look slightly different than the leaf pages shown previously:

```
$ innodb_space -f t.ibd -r ./simple_t_describer.rb -d SimpleTDescriber -p 36 page
{:format=>:compact,
 :offset=>125,
 :header=>
  {:next=>11877,
   :type=>:node_pointer.
   :heap_number=>2,
   :n_owned=>0,
   :min_rec=>true
   :deleted=>false
   :field_nulls=>nil
   :field_lengths=>[0]
   :field_externs=>[false]},
 :next=>11877
 itype=>:clustered,
:key=>[{:name=>"i", :type=>"INT UNSIGNED", :value=>252, :extern=>nil}],
 :child_page_number=>4}
```

The :key array is present, although it represents the minimum key rather than an exact key, and no :row is present, as a :child\_page\_number takes its place.

# The root page is a bit special

Since the root page is allocated when the index is first created, and that page number is stored in the data dictionary, the root page can never relocated or removed. Once the root page fills up, it will need to be split, forming a small tree of a root page plus two leaf pages.

However, the root page itself can't actually *be* split, since it cannot be relocated. Instead, a new, empty page is allocated, the records in the root are moved there (the root is "raised" a level), and *that* new page is split into two. The root page then does not need to be split again until the level immediately below it has enough pages that the root becomes full of child page pointers (called "node pointers"), which in practice often means several hundred to more than a thousand.

# B+Tree levels and increasing tree depth

As an example of the efficiency of B+Tree indexes, assume perfect record packing (every page full, which will never quite happen in practice, but is useful for discussion). A B+Tree index in InnoDB for the simple table in the examples above will be able to store 468 records per leaf page, or 1203 records per non-leaf page. The index tree can then be a *maximum* of the following sizes at the given tree heights:

Height	Non-leaf pages	Leaf pages	Rows	Size in bytes
1	0	1	468	16.0 KiB
2	1	1203	> 563 thousand	18.8 MiB
3	1204	1447209	> 677 million	22.1 GiB
4	1448413	1740992427	> 814 billion	25.9 TiB

As you can imagine, most tables with sensible PRIMARY KEY definitions are 2-3 levels, with some achieving 4 levels. Using an excessively large PRIMARY KEY can cause the B+Tree to be much less efficient, however, since primary key values must be stored in the non-leaf pages. This can drastically inflate the size of the records in non-leaf pages, meaning many fewer of those records fit in each non-leaf page, making the whole structure less efficient.

#### What's next?

Next we'll take a look at the page directory structure in INDEX pages which mentioned several times already, and then look at how to search efficiently within InnoDB indexes.

#### Share this:





#### Related

The basics of InnoDB space file layout

In "InnoDB"

oDB index pages

In "InnoDB"

The physical structure of Inn- The physical structure of records in InnoDB

In "InnoDB"

Posted on January 10, 2013 by Jeremy Cole. This entry was posted in InnoDB, MySQL. Bookmark the permalink

# 13 thoughts on "B+Tree index structures in InnoDB"



### **Daegeun Kim**

January 10, 2013 at 09:28

Reblogged this on **Dani's Notes** and commented:

B+Tree index structures in InnoDB

Reply



## he dengcheng

January 10, 2013 at 18:31

Hi, Cole

As i learned, Max\_Trx\_Id in the index page is only used for coverage index scan, so it is valid only on the secondary index, in primary index, it's useless.

Reply



# he dengcheng

January 10, 2013 at 19:44

Hi, Cole

I've fully learned the B+Tree Detailed Page Structure, I think i know all the attributes but two: Order and Min\_rec in the user record, what's these two attributes means? or where i can find these two attributes in the innodb source code?

Look forward to your reply! Thanks!

Reply



#### **Jeremy Cole**

January 10, 2013 at 21:58

He:

Order is quite simple: It's the order the record was inserted into the heap. Infimum is always Order: 0, Supremum is always Order: 1, and user records end up incrementing from there. Check for rec\_get\_heap\_no\_new function and REC\_NEW\_HEAP\_NO define.

Min\_Rec is a true/false flag which is set on the lowest-key record at any non-leaf level. I'm not sure of its actual purpose. Check for rec\_get\_info\_bits/rec\_set\_info\_bits\_new functions and REC\_INFO\_MIN\_REC\_FLAG define.

#### Reply



# he dengcheng

- January 10, 2013 at 23:18

Thanks for your reply, i am clear now:)

For Order, i named it heap\_no, which is used to identify a record in the page, row lock is locked on this number.

For Min\_Rec, i am also puzzled. I'll see the source for its actual purpose.

I am also write some documents on InnoDB Index Structure, Page Structure, Row Format, and Operations on these structures(Insert/Update/Delete/Purge/SMO), unfortunately in chinese. Keeping in touch.



# **Jeremy Cole**

- January 11, 2013 at 08:07

He: It may be that I should rename "Order" to "Heap Number" in my documentation. I believe the term "Order" came from some (very incomplete) InnoDB documentation that I referenced, but it is not used at all in the InnoDB source code. So that may be unnecessarily confusing.



#### l ei I i

- February 4, 2014 at 13:55

Thanks for this great post. It helps the beginner like me to well understand MySQL.

Reply



#### Eric Liu

- February 5, 2014 at 09:04

Hi, Cole

I am trying to follow the example you give, but it seems there are some typos:

 $\$  innodb\_space -f t.ibd -r ./simple\_t\_describer.rb -d SimpleTDescriber -p 3 index-recurse should be

\$ innodb\_space -f t.ibd -r ./simple\_t\_btree\_describer.rb -d SimpleTBTreeDescriber -p 3 index-recurse

 $\$  innodb\_space -f t.ibd -r ./simple\_t\_describer.rb -d SimpleTDescriber -p 36 page-dump should be

\$ innodb\_space -f t.ibd -r ./ simple\_t\_btree\_describer.rb -d SimpleTBTreeDescriber -p 36 page-dump

Not guite sure about the above...Maybe I missed something.

But thank you so much for the great article. It helps a lot to understand how the B+tree works.

Reply



# **Jeremy Cole**

- February 5, 2014 at 09:37

Eric,

Actually the commands are correct. Sorry for the confusion — those examples refer to the describer and the table structure discussed previously in  $\underline{A}$  quick introduction to innodb\_ruby.

Regards,

Jeremy

Reply



#### **Jeremy Cole**

- February 5, 2014 at 09:39

I added some clarifications to the post.

Reply



# Eric Liu

- February 6, 2014 at 08:21

Thank you for the quick reply! Got it now!



# Yunyoung

- June 11, 2014 at 19:23

I have a question about "NULL" value. Could you let me know where is the NULL value stored in leaf node of secondary index?

Reply



#### Ivan

- January 13, 2015 at 01:51

Hi Cole,

I tried to create an index in MySQL using phpmyadmin. When I look at the index info, it shows the index has been created using BTREE. Is this B+Tree likely you described on this page? Or it is just B Tree. Many thanks

Reply

# What do you think?

Enter your comment here...

Blog at WordPress.com.