

Quiz 10 Standard 10 - Ford-Fulkerson Algorithm

Due Date TODO
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Quiz Code (enter in Canvas to get access to the LaTeX template) **ASIIO**

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Instructions

- You may either type your work using this template, or you may handwrite your work and embed it as an image in this template. **If you choose to handwrite your work, the image must be legible, and oriented so that we do not have to rotate our screens to grade your work.** We have included some helpful LaTeX commands for including and rotating images commented out near the end of the LaTeX template.
- You should submit your work through the **class Gradescope page** only. Please submit one PDF file, compiled using this LaTeX template.
- You may not need a full page for your solutions; pagebreaks are there to help Gradescope automatically find where each problem is. Even if you do not attempt every problem, please submit this document with no fewer pages than the blank template (or Gradescope has issues with it).
- You **may not collaborate with other students. Copying from any source is an Honor Code violation. Furthermore, all submissions must be in your own words and reflect your understanding of the material.** If there is any confusion about this policy, it is your responsibility to clarify before the due date.
- Posting to **any** service including, but not limited to Chegg, Discord, Reddit, StackExchange, etc., for help on an assignment is a violation of the Honor Code.
- You **must** virtually sign the Honor Code (see Section). Failure to do so will result in your assignment not being graded.

Honor Code (Make Sure to Virtually Sign)

Problem HC. • My submission is in my own words and reflects my understanding of the material.

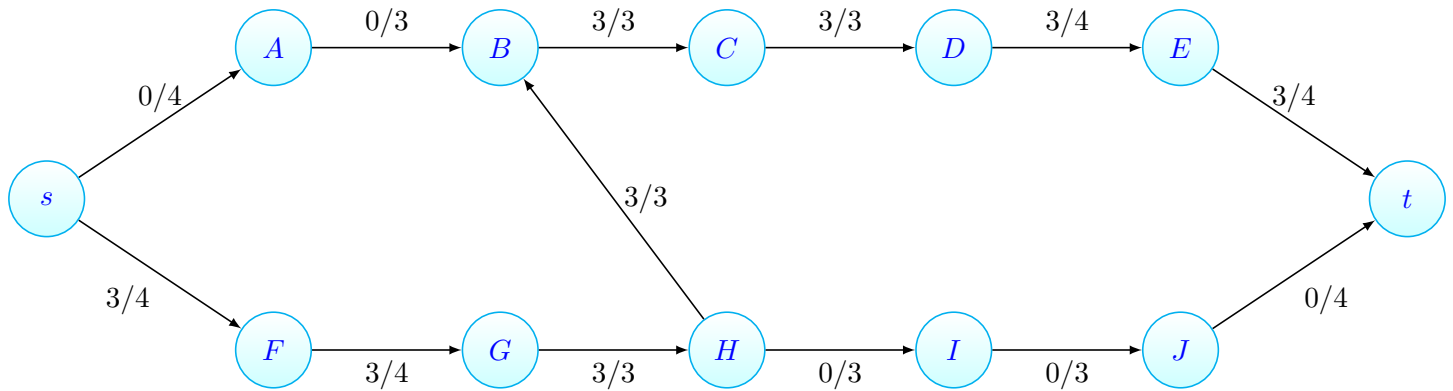
- Any collaborations and external sources have been clearly cited in this document.
- I have not posted to external services including, but not limited to Chegg, Reddit, StackExchange, etc.
- I have neither copied nor provided others solutions they can copy.

Agreed (I agree to the above, Blake Raphael).

□

10 Standard 10: Ford–Fulkerson algorithm (4 points)

Problem 10. For Problem 11, consider the following flow network.



- a. Specify an augmenting path (from s to t). No explanation needed, just specify the path. (0.5 points)

Answer. $s \rightarrow F \rightarrow G \rightarrow H \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow t$

□

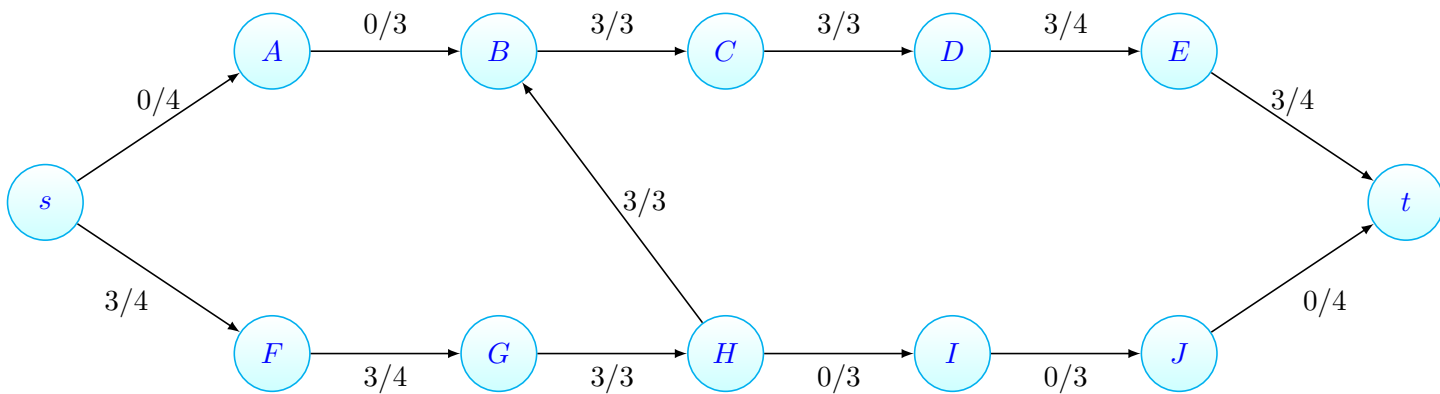
- b. What is the maximum amount of flow you can push along your augmenting path? Clearly specify what calculation you do to figure this out, and write out your work/calculation. (1 points)

Answer. There cannot be anymore flow pushed through this path because all of edges are at capacity. I used the minimum capacity of the edges that are a part of the augmenting path. We have 0 more flow capacity at 4 different edges: $G \rightarrow H$, $H \rightarrow B$, $B \rightarrow C$, and $C \rightarrow D$, so we cannot push anymore flow

□

- c. Push the amount of flow from part (b) along the path you found in part (a), and draw the updated flow network here. (0.5 points)

Answer. Here is the updated graph:



□

- d. Calculate the value of the flow in your answer to part (c). Fill in the blanks (and add additional lines below as needed). (1 points)

Proof. The value of the flow is the sum of the flows on the following edges: 24

The flow on edge $s \rightarrow F$ is 3

The flow on edge $F \rightarrow G$ is 3

The flow on edge $G \rightarrow H$ is 3

The flow on edge $H \rightarrow B$ is 3

The flow on edge $B \rightarrow C$ is 3

The flow on edge $D \rightarrow E$ is 3

The flow on edge $E \rightarrow t$ is 3

Therefore the total flow value is the sum of the above, which is 24. □

- e. (i) Specify the cut *corresponding to your flow* (this is not just any cut with the same value as your flow—there is a specific procedure for finding the cut corresponding to your flow, see, e.g., Levet Section 5.4). (ii) Calculate the value of the cut. Specify where your numbers are coming from and what calculation you are doing. Show your work. (1 points)

Proof. The cut that corresponds to the flow will be $\{F, G\}$. The value of my cut is 3. The calculation I am doing is using the capacity of all the edges included in our flow, which is only one edge with capacity 3. My numbers are coming from the following: We can push 1 more unit of flow from $F \rightarrow G$, so we add G to our cut with F . Because we cannot push any more flow from $G \rightarrow H$, we end our cut at G . □