Quiz 2 Standard 2 - BFS/DFS

Due Date ....TODO
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Quiz Code (enter in Canvas to get access to the LaTeX template) .... **CVDFO**

Contents

Instructions

- You may either type your work using this template, or you may handwrite your work and embed it as an image in this template. **If you choose to handwrite your work, the image must be legible, and oriented so that we do not have to rotate our screens to grade your work.** We have included some helpful LaTeX commands for including and rotating images commented out near the end of the LaTeX template.

- You should submit your work through the **class Canvas page** only. Please submit one PDF file, compiled using this LaTeX template.

- You may not need a full page for your solutions; pagebreaks are there to help Gradescope automatically find where each problem is. Even if you do not attempt every problem, please submit this document with no fewer pages than the blank template (or Gradescope has issues with it).

- You **may not collaborate with other students**. **Copying from any source is an Honor Code violation. Furthermore, all submissions must be in your own words and reflect your understanding of the material.** If there is any confusion about this policy, it is your responsibility to clarify before the due date.

- Posting to **any** service including, but not limited to Chegg, Discord, Reddit, StackExchange, etc., for help on an assignment is a violation of the Honor Code.

- You **must** virtually sign the Honor Code (see Section). Failure to do so will result in your assignment not being graded.

Honor Code (Make Sure to Virtually Sign)

Problem HC.
- My submission is in my own words and reflects my understanding of the material.

- Any collaborations and external sources have been clearly cited in this document.

- I have not posted to external services including, but not limited to Chegg, Reddit, StackExchange, etc.

- I have neither copied nor provided others solutions they can copy.

Agreed (I agree to the following, Blake Raphael). □

2   Standard 2 BFS/DFS

Problem 2. A *simple $s \to t$ path* in a graph G is a path in G starting at s, ending at t, and never visiting the same vertex twice. Using the graph $G(V, E)$ below and vertices $s, t \in V(G)$, find a path that (i) starts at s and ends at t, (ii) that DFS traverses, and (iii) is neither a shortest path nor a longest simple path. Detail the execution of DFS (list the contents of the stack at each step, and which vertex it pops off the stack). Additionally, show (a) the final $s \to t$ path it finds, (b) show a shorter $s \to t$ path, and (c) a longer simple $s \to t$ path.
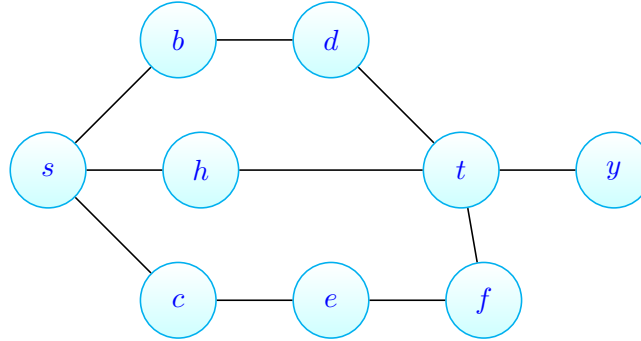

Proof. DFS will start at node s. It will then exploit the first child node, b. While exploiting this node, it will search to node d and finally to node t. This completes DFS traversal path from $s \to t$. We do not pop any nodes from the stack in this example, because in DFS we only pop to "go back" to visit unexplored nodes down a branch. The following table shows a path that traverses s to t that DFS finds and that is neither the shortest path nor the longest, simple path.
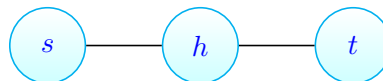
Table 1: DFS Traversal and Stack Contents

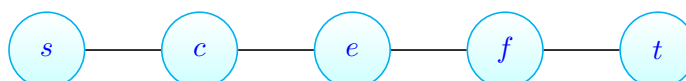| Step	Stack Contents
1	s
2	b, s
3	d, b, s
4	t, d, b, s

(a) Here is the final path DFS finds:
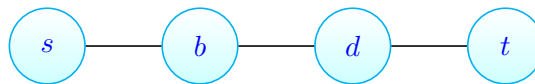
(b) Here is a shorter $s \to t$ path:

(c) Here is a longer, simple $s \to t$ path: