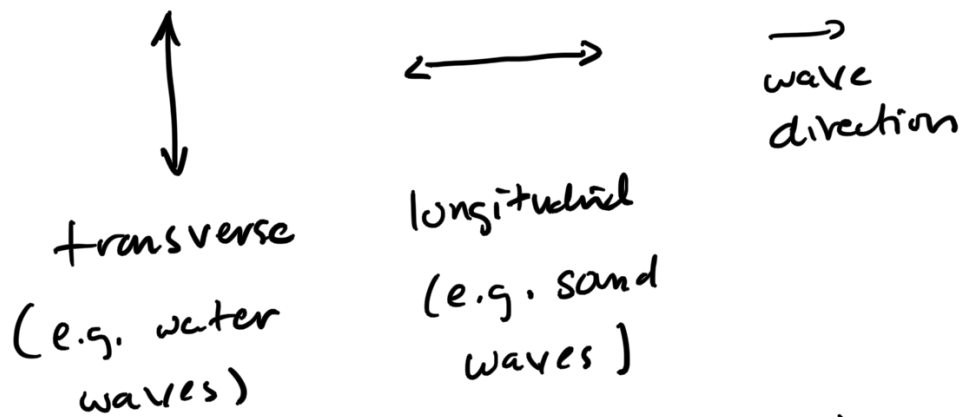
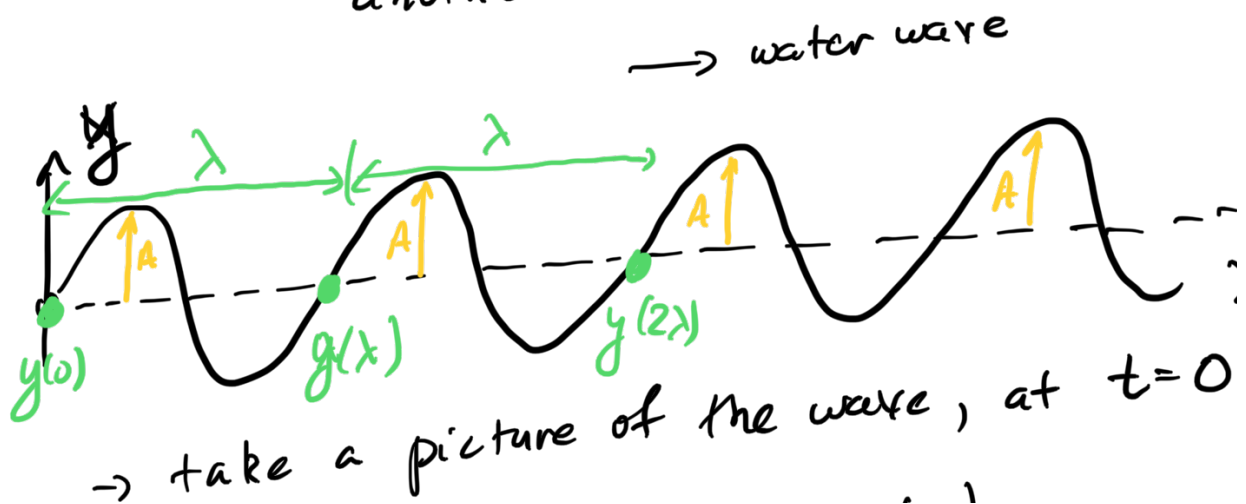


Waves

- normal waves are disturbances of a medium (the material in which the wave travels)
- the molecules of the material are actually moving.



- energy travels from one place to another.



$$y = A \sin(kx + \phi)$$

\uparrow Amplitude \uparrow wave number \uparrow phase

(i) the sin function goes between +1 and -1 \therefore
 y goes between $+A$ and $-A$.

(ii) the sin function repeats every 360° , or
 every 2π radians.

$$y(0) = A \sin(\phi)$$

$$y(\lambda) = A \sin(k\lambda + \phi) = y(0)$$

$$\therefore k\lambda = 2\pi$$

$$k = 2\pi/\lambda$$

$$y = A \sin\left(\frac{2\pi x}{\lambda} + \phi\right)$$

\uparrow
wave length.

Now, image sitting at $x=0$, and allow time to pass.

$$y_0(t) = A \sin(\omega t + \phi)$$

Again, the sin function repeats every 2π radians, or every T seconds.

$$\therefore \omega = \frac{2\pi}{T}$$

$$y_0(t) = A \sin\left(\frac{2\pi t}{T} + \phi\right)$$

Putting these two things together, we can write:

$$y(x, t) = A \sin\left(\frac{2\pi x}{\lambda} - \frac{2\pi t}{T} + \phi\right)$$

amplitude phase

0

λ wavelength T period

Recall :

distance = speed \times time.

$$\therefore \text{speed} = \frac{\text{distance}}{\text{time}}$$

$$v_{\text{wave}} = \frac{\lambda}{T}$$

Define

$$\text{frequency} = \frac{1}{T}$$

$$\therefore v_{\text{wave}} = f \cdot \lambda$$

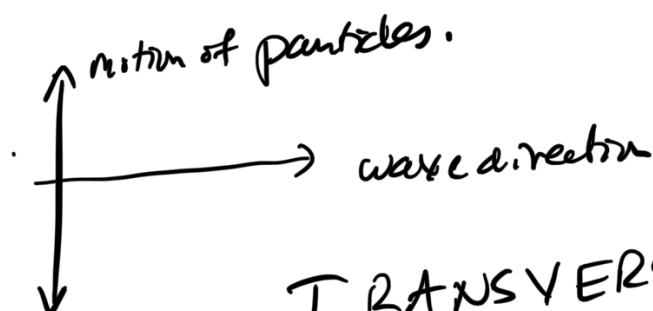
\uparrow
a constant for
a given medium at
a given pressure, temperature.

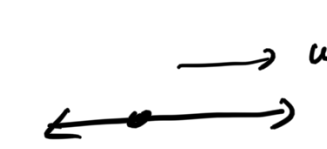
① A wave is traveling in a constant medium.

∴ the wave is going to travel at a constant speed.

② amplitude, wavelength, phase,
(A) (λ) (ϕ)

frequency, period, medium
(f) (T) ↑
the material

④ 
TRANSVERSE wave

⑤ 
LONGITUDINAL WAVE

$$\textcircled{6} \quad f = 80 \text{ Hz}$$

$$= \frac{1}{5} = \text{s}^{-1}$$

$$f = \frac{1}{T} \quad \therefore T = \frac{1}{f}$$

$$= \frac{1}{80 \text{ Hz}}$$

$$= 0.0125 \text{ s}$$

$\textcircled{9}$ What type of "waves" do not have a physical medium?

LIGHT WAVES!

(Electromagnetic waves/radiation)

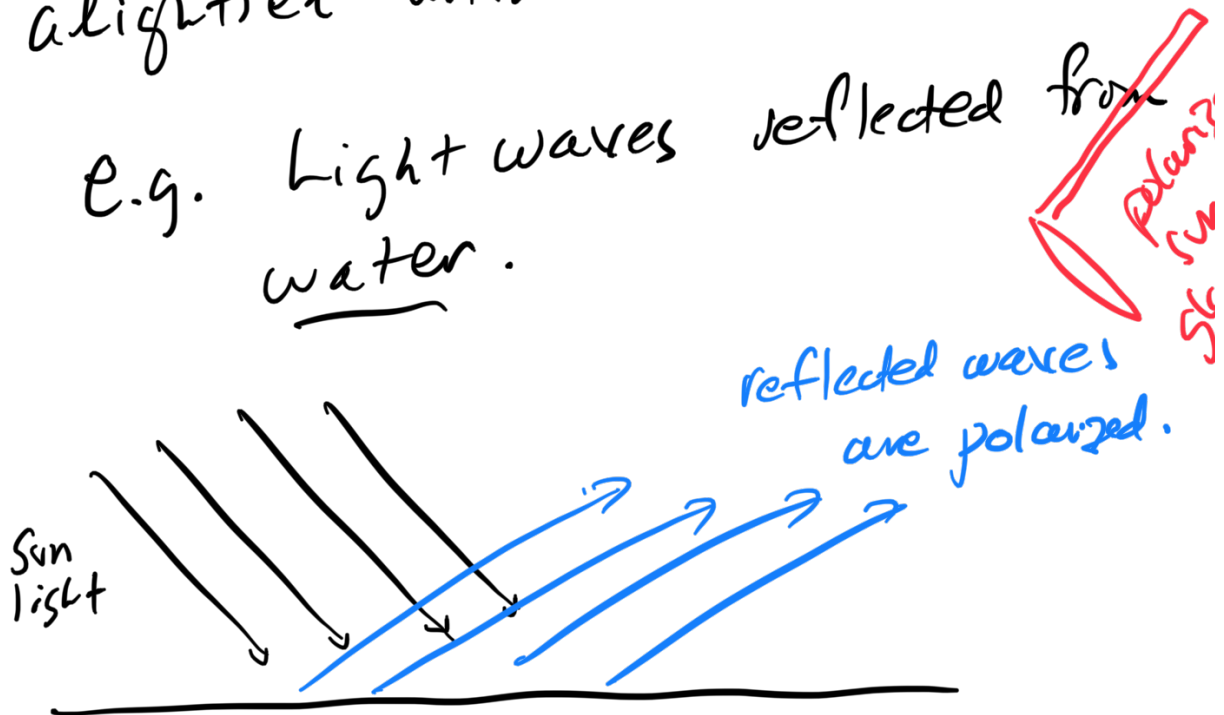
$\textcircled{3}$ Light waves can be polarized.

In normal light, The direction of "oscillation" is random (unpolarized)

" oscillation.

For polarized light, the oscillation direction is not random. It is aligned with some axis.

e.g. Light waves reflected from water.



The only questions we have left are ⑦ + ⑧.

Two waves

$$y_1 = A_1 \sin(2\pi f_1 t)$$

$$y_2 = A_2 \sin(2\pi f_2 t)$$

$$\begin{aligned} y_{\text{total}} &= y_1 + y_2 \\ &= A_1 \sin(2\pi f_1 t) + A_2 \sin(2\pi f_2 t) \end{aligned}$$

↓ math

$$= (A_1 + A_2) \sin\left(2\pi\left(\frac{f_1 + f_2}{2}\right)t\right) \times \cos\left(2\pi\left(\frac{f_1 - f_2}{2}\right)t\right)$$

Beat frequency

$$= |f_1 - f_2|$$

$$= |81 \text{ Hz} - 50 \text{ Hz}| = 31 \text{ Hz}$$

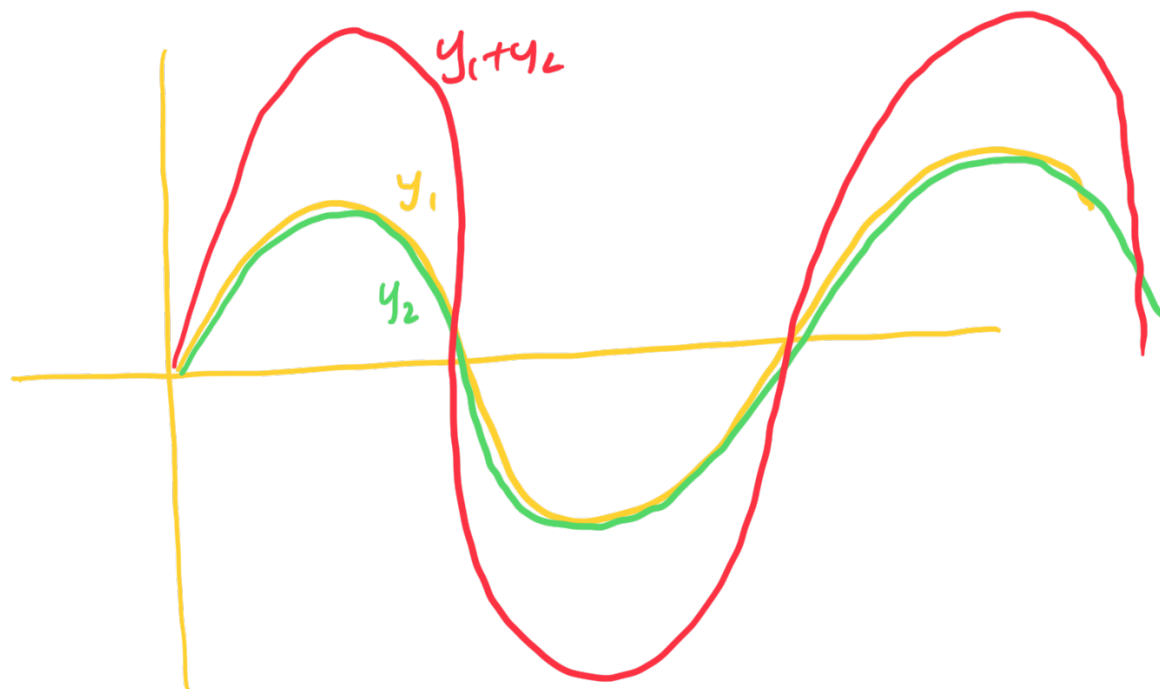
Combining two waves of the
same frequency:

$$y_1 = A \sin(2\pi ft + \phi_1)$$

$$y_2 = A \sin(2\pi ft + \phi_2)$$

$$y = y_1 + y_2$$

Case 1 $\phi_1 = \phi_2 = 0^\circ$

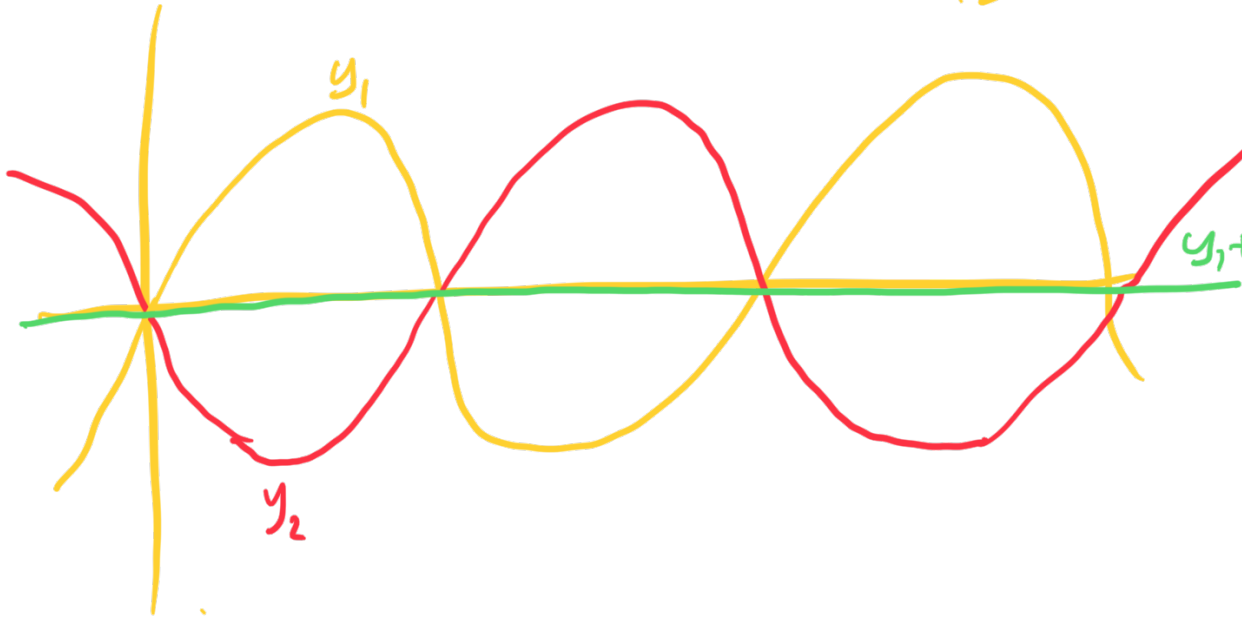


... produce a bigger

- waves combine to produce a wave.

CONSTRUCTIVE interference

Case 2: $\phi_1 = 0^\circ$
 $\phi_2 = 180^\circ$



→ waves combine and cancel each other out!

DESTRUCTIVE interference!