

$$F = G \frac{m_1 m_2}{r^2}$$

To compare the gravitational force exerted on a baby by Jupiter and by the baby's mother when the baby is held close to the mother's chest, consider the ratio of forces. The baby's mass cancels:

$$\frac{F_J}{F_M} = \frac{M_J/r_J^2}{M_M/r_M^2} = \frac{M_J}{M_M} \left( \frac{r_M}{r_J} \right)^2$$

Assumed values:

$$M_M = 65 \text{ kg} \quad m_b = 3.5 \text{ kg} \quad r_M = 0.20 \text{ m}$$

$$M_J = 1.898 \times 10^{27} \text{ kg}$$

Earth-Jupiter distance:

$$r_J = 6.28 \times 10^{11} \text{ m} \quad (\text{closest})$$

$$r_J = 9.28 \times 10^{11} \text{ m} \quad (\text{farthest})$$

Mother-baby gravitational force:

$$F_M = G \frac{(65)(3.5)}{(0.20)^2} \approx 3.8 \times 10^{-7} \text{ N}$$

Jupiter-baby gravitational force:

Closest approach:

$$F_J = G \frac{(1.898 \times 10^{27})(3.5)}{(6.28 \times 10^{11})^2} \approx 1.1 \times 10^{-6} \text{ N}$$

Farthest separation:

$$F_J \approx 5.2 \times 10^{-7} \text{ N}$$

Force comparison:

$$\left. \frac{F_J}{F_M} \right|_{\text{closest}} \approx \frac{1.1 \times 10^{-6}}{3.8 \times 10^{-7}} \approx 2.9$$

$$\left. \frac{F_J}{F_M} \right|_{\text{farthest}} \approx \frac{5.2 \times 10^{-7}}{3.8 \times 10^{-7}} \approx 1.4$$