

ENGR 2910  
HOMEWORK 10 SOLUTIONS

①  $v = 0$  at  $t = -\frac{2}{3}\pi$   
and increasing at  $80,000 \text{ V/s}$

a)  $v(t) = 80 \cos(\omega t + \phi)$

$$\frac{dv(t)}{dt} = -80\omega \sin(\omega t + \phi)$$

when  $\cos(\ ) = 0 \Rightarrow \sin(\ ) = 1$

$$\Rightarrow 80\omega = 80,000 \text{ or } \boxed{\omega = 1000 \text{ rad/s}}$$

b)  $f = \frac{\omega}{2\pi} = 159.155 \text{ Hz}$

$$T = \frac{1}{f} = 6.28 \text{ ms}$$

$$\frac{-\frac{2}{3}\pi}{6.28} = -0.3335 \Rightarrow \phi = -90 - (-0.3335)(360) = 30^\circ$$

$$\boxed{v = 80 \cos(1000t + 30^\circ)}$$

② a)  $f = 50,000$

$$\omega = 2\pi f = 314,159 \text{ rad/s}$$

b)  $I = \frac{V}{Z_C} = \frac{10 \times 10^{-3} \angle 0^\circ}{(1/j\omega C)} = j\omega C (10 \times 10^{-3}) \angle 0^\circ$   
 $= (10 \times 10^{-3})\omega C \angle 90^\circ$

$$\boxed{\phi = 90^\circ}$$

c)  $I_m = 628.32 \mu\text{A} = 10 \times 10^{-3} \omega C$

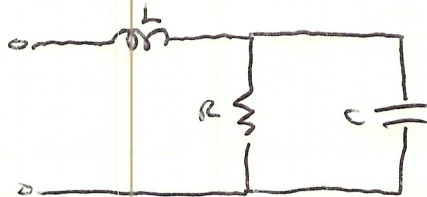
$$\frac{1}{\omega C} = \frac{10 \times 10^{-3}}{628.32 \times 10^{-6}} = 15.92 \Omega \quad \text{REACTANCE} \quad \boxed{X_C = -15.92 \Omega}$$

d)  $C = \frac{1}{(15.92)\omega} = \frac{1}{(15.92)(314,159)} = 0.2 \mu\text{F}$

e)  $Z_C = \frac{1}{j\omega C} = \frac{-j}{\omega C} = -j 15.92 \Omega$



③



$$\begin{aligned} C &= 25 \times 10^{-8} \text{ F} \\ L &= 160 \times 10^{-6} \text{ H} \\ R &= 100 \text{ } \Omega \end{aligned}$$

$$\begin{aligned} \text{a) } Z_{\text{eq}} &= Z_L + Z_R \parallel Z_C \\ &= j\omega L + \left( R \parallel \frac{-j}{\omega C} \right) \\ &= j\omega L + \left( \frac{1}{\frac{1}{R} + \frac{\omega C}{-j}} \right) \\ &= j\omega L + \left( \frac{1}{\frac{-j + \omega C R}{-jR}} \right) \\ &= j\omega L + \frac{-jR}{-j + \omega C R} \\ &= j\omega L + \frac{-jR(\omega C R + j)}{\omega^2 C^2 R^2 + 1} \end{aligned}$$

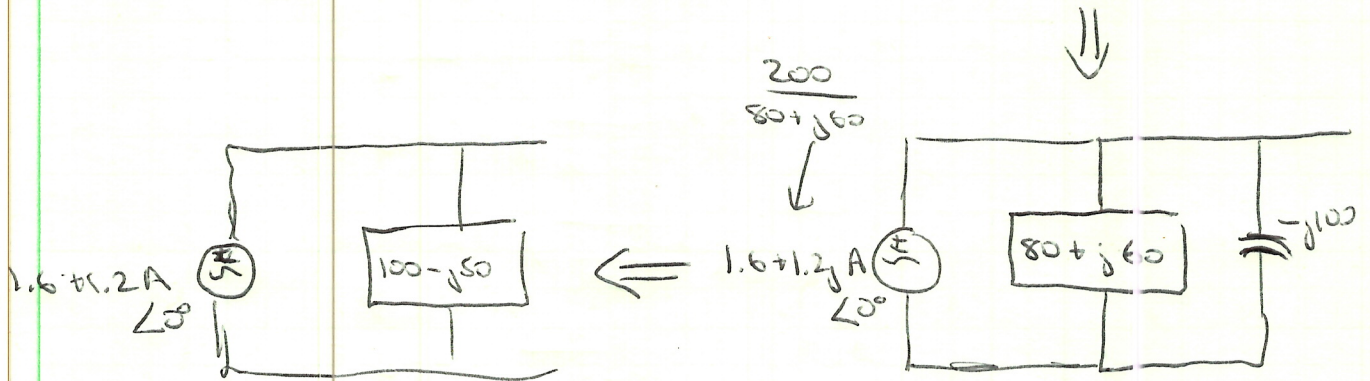
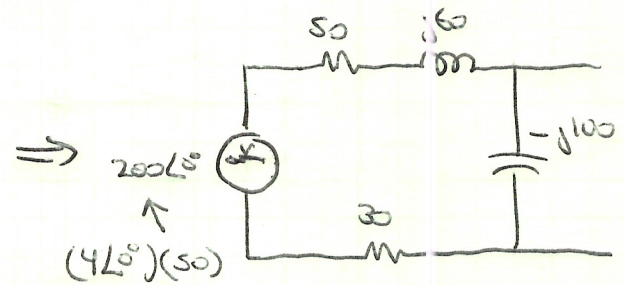
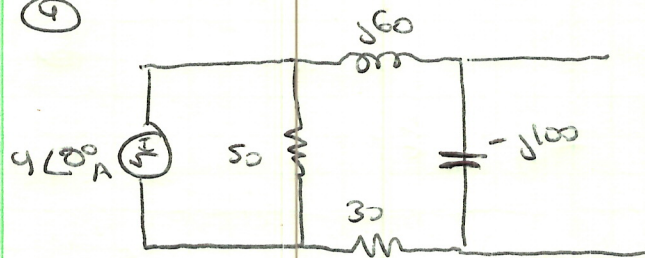
$$\text{Im}\{Z_{\text{eq}}\} = \omega L - \frac{\omega C R^2}{\omega^2 C^2 R^2 + 1} = 0$$

$$\Rightarrow \omega^2 = \frac{(CR^2/L) - 1}{C^2 R^2} = 900 \times 10^8$$

$$\boxed{\omega = 300 \times 10^3 \text{ rad/s}}$$

$$\text{b) } Z_{\text{eq}}(300k) = j(48) + \frac{(100)(-j133)}{100 - j133} = 64.2$$

④



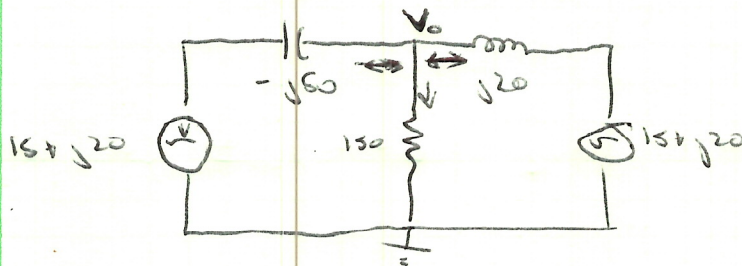
⑤  $Z_L = j\omega L = j20$

$Z_C = \frac{-j}{\omega C} = -j50$

$v_{q1}(t) = 25 \cos(400t + 143.13^\circ) = 25 \cos(400t + 53.13^\circ)$

$V_{q1} = 25 \angle 53.13^\circ = 15 + j20 \text{ V}$

$V_{q2} = 15.03 \angle 33.69^\circ = 15 + j20 \text{ V}$



KCL:  $\frac{(15 + j20) - V_o}{-j50} + \frac{(15 + j20) - V_o}{j20} = \frac{V_o}{150}$

$V_o = 15 \angle 30^\circ$

$v_o(t) = 15 \cos(400t) \text{ V}$