P 5.2 [a] Let the value of the voltage source be v_s :

$$\frac{v_n - v_s}{10,000} + \frac{v_n - v_o}{40,000} = 0.$$

But $v_n = v_p = 0$. Therefore,

$$v_o = -\frac{40,000}{10,000} v_s = -4v_s.$$

When $v_s = -6 \text{ V}$, $v_o = -4(-6) = 24 \text{ V}$; saturates at $v_o = 15 \text{ V}$.

When
$$v_s = -3.5 \text{ V}$$
, $v_o = -4(-3.5) = 14 \text{ V}$.

When
$$v_s = -1.25 \text{ V}$$
, $v_o = -4(-1.25) = 5 \text{ V}$.

When
$$v_s = 1 \text{ V}$$
, $v_o = -4(1) = -4 \text{ V}$.

When
$$v_s = 2.4 \text{ V}$$
, $v_o = -4(2.4) = -9.6 \text{ V}$.

When $v_s = 5.4 \text{ V}$, $v_o = -4(5.4) = -21.6 \text{ V}$; saturates at $v_o = -15 \text{ V}$.

[b]
$$-4v_s = 15$$
 so $v_s = \frac{15}{-4} = -3.75$ V;

$$-4v_s = -15$$
 so $v_s = \frac{-15}{-4} = 3.75$ V.

The range of source voltages that avoids saturation is -3.75 V $\leq v_s \leq 3.75$ V.

$${\rm P~5.4}~~\frac{v_{\rm b}-v_{\rm a}}{20} + \frac{v_{\rm b}-v_{o}}{100} = 0, ~~{\rm therefore}~~v_{o} = 6v_{\rm b} - 5v_{\rm a}.$$

[a]
$$v_{\rm a} = 4 \text{ V}$$
, $v_{\rm b} = 0 \text{ V}$, $v_o = -16 \text{ V}$ (sat).

[b]
$$v_a = 2 \text{ V}, \quad v_b = 0 \text{ V}, \quad v_o = -10 \text{ V}.$$

[c]
$$v_a = 2 \text{ V}, \quad v_b = 1 \text{ V}, \quad v_o = -4 \text{ V}.$$

$$[{\bf d}] \ v_{\rm a} = 1 \ {\rm V}, \qquad v_{\rm b} = 2 \ {\rm V}, \qquad v_o = 7 \ {\rm V}.$$

[e] If
$$v_{\rm b} = 1.6\,$$
 V, $v_o = 9.6 - 5v_{\rm a} = \pm 16;$

$$\therefore$$
 -1.25 < v_a < 5.12 V.

P 5.5 [a]
$$i_a = \frac{240 \times 10^{-3}}{8000} = 30 \,\mu\text{A}.$$

[b]
$$\frac{0 - v_{\rm a}}{60,000} = i_{\rm a}$$
 so $v_{\rm a} = -60,000i_{\rm a} = -1.8$ V.

[c]
$$\frac{v_{\rm a}}{60,000} + \frac{v_{\rm a}}{40,000} + \frac{v_{\rm a} - v_{\rm o}}{30,000} = 0;$$

$$v_0 = 2.25v_a = -4.05 \text{ V}.$$

[d]
$$i_{\rm o} = \frac{-v_{\rm o}}{20,000} + \frac{v_{\rm a} - v_{\rm o}}{30,000} = 277.5 \,\mu\text{A}.$$

P 5.6
$$v_p = \frac{5000}{5000 + 10,000}(6) = 2 \text{ V} = v_n;$$

$$\frac{v_n+5}{3000} + \frac{v_n-v_o}{6000} = 0;$$

$$2(2+5) + (2-v_o) = 0;$$

$$v_o = 16 \text{ V}.$$

$$i_{\rm L} = \frac{v_o}{8000} = \frac{16}{8000} = 2000 \times 10^{-6};$$

$$i_{\rm L}=2$$
 mA.

P 5.7 Since the current into the inverting input terminal of an ideal op-amp is zero, the voltage across the $3.3 \,\mathrm{M}\Omega$ resistor, positive on the left, is $(3.3 \times 10^6)(2.5 \times 10^{-6})$ or 8.25 V. Therefore the voltmeter reads -8.25 V.

P 5.12 [a] This circuit is an example of an inverting summing amplifier.

[b]
$$v_o = -\frac{220}{33}v_a - \frac{220}{22}v_b - \frac{220}{80}v_c = -8 + 15 - 11 = -4 \text{ V}.$$

[c]
$$v_o = -19 - 10v_b = \pm 6$$
;

$$v_b = -1.3 \text{ V}$$
 when $v_o = -6 \text{ V}$;
 $v_b = -2.5 \text{ V}$ when $v_o = 6 \text{ V}$;

$$\therefore$$
 -2.5 V $\leq v_{\rm b} \leq -1.3$ V.

P 5.17 [a]
$$\frac{8-4}{40,000} + \frac{8-9}{22,000} + \frac{8-13}{100,000} + \frac{8}{352,000} + \frac{8-v_0}{R_f} = 0;$$
 $\frac{8-v_o}{R_f} = -2.7272 \times 10^{-5}$ so $R_f = \frac{8-v_o}{-2.727 \times 10^{-5}}.$

For
$$v_o = 15 \text{ V}$$
, $R_f = 256.7 \text{ k}\Omega$;

For $v_o = -15$ V, $R_f < 0$ so this solution is not possible.

[b]
$$i_o = -(i_f + i_{10k}) = -\left[\frac{15 - 8}{256.7 \times 10^3} + \frac{15}{10,000}\right] = -1527 \,\mu \text{ A}.$$

P 5.14
$$v_o = -\left[\frac{R_f}{3000}(0.15) + \frac{R_f}{5000}(0.1) + \frac{R_f}{25,000}(0.25)\right];$$

$$-6 = -8 \times 10^{-5} R_f; \qquad R_f = 75 \,\mathrm{k}\Omega; \qquad \therefore \quad 0 \le R_f \le 75 \,\mathrm{k}\Omega.$$

P 5.31 [a]

$$v_a$$
 v_b
 v_b
 v_b
 v_c
 v_b
 v_c
 v_c
 v_d
 $v_p \ge 20k\Omega$

$$\frac{v_p}{20,000} + \frac{v_p - v_c}{30,000} + \frac{v_p - v_d}{20,000} = 0;$$

$$\therefore 8v_p = 2v_c + 3v_d = 8v_n.$$

$$\frac{v_n - v_a}{20,000} + \frac{v_n - v_b}{18,000} + \frac{v_n - v_o}{180,000} = 0;$$

$$\begin{array}{rcl} \therefore & v_o & = & 20v_n - 9v_{\rm a} - 10v_{\rm b} \\ \\ & = & 20[(1/4)v_{\rm c} + (3/8)v_{\rm d}] - 9v_{\rm a} - 10v_{\rm b} \\ \\ & = & 20(0.75 + 1.5) - 9(1) - 10(2) = 16 \text{ V}. \end{array}$$

[b]
$$v_o = 5v_c + 30 - 9 - 20 = 5v_c + 1;$$

$$\pm 20 = 5v_{\rm c} + 1;$$

:.
$$v_{\rm b} = -4.2 \text{ V}$$
 and $v_{\rm b} = 3.8 \text{ V}$;

$$\therefore$$
 -4.2 V $\leq v_{\rm b} \leq 3.8$ V.