***University Physics Volume II***

**Unit 1: Thermodynamics**

**Chapter 2: The Kinetic Theory of Gases**

**Conceptual Questions**

1. Two H2 molecules can react with one O2 molecule to produce two H2O molecules. How many moles of hydrogen molecules are needed to react with one mole of oxygen molecules?

Solution

2 moles, as that will contain twice as many molecules as the 1 mole of oxygen

1. Under what circumstances would you expect a gas to behave significantly differently than predicted by the ideal gas law?

Solution

sufficiently high pressure and low temperature that it’s close to liquefaction

1. A constant-volume gas thermometer contains a fixed amount of gas. What property of the gas is measured to indicate its temperature?

Solution

pressure

1. Inflate a balloon at room temperature. Leave the inflated balloon in the refrigerator overnight. What happens to the balloon, and why?

Solution

It shrinks and feels softer. The temperature decreased at a fixed amount of gas in the same, so the pressure and volume decreased.

1. In the last chapter, free convection was explained as the result of buoyant forces on hot fluids. Explain the upward motion of air in flames based on the ideal gas law.

Solution

The flame contains hot gas (heated by combustion). The pressure is still atmospheric pressure, in mechanical equilibrium with the air around it (or roughly so). The density of the hot gas is proportional to its number density *N*/*V* (neglecting the difference in composition between the gas in the flame and the surrounding air). At higher temperature than the surrounding air, the ideal gas law says that  is less than that of the surrounding air. Therefore the hot air has lower density than the surrounding air and is lifted by the buoyant force.

1. How is momentum related to the pressure exerted by a gas? Explain on the molecular level, considering the behavior of molecules.

Solution

The pressure of a gas is caused by the change in momentum of the molecules when they collide, as they exert a force equal to the change in momentum divided by the time between collisions.

1. If one kind of molecule has double the radius of another and eight times the mass, how do their mean free paths under the same conditions compare? How do their mean free times compare?

Solution

The mean free path is inversely proportional to the square of the radius, so it decreases by a factor of 4. The mean free time is proportional to the mean free path and inversely proportional to the rms speed, which in turn is inversely proportional to the square root of the mass. That gives a factor of  in the numerator, so the mean free time decreases by a factor of 

1. What is the average *velocity* of the air molecules in the room where you are right now?

Solution

0, though if students say they’re outside as they answer and give the wind velocity, that’s also correct. The velocity of a south wind is horizontally north.

1. Why do the atmospheres of Jupiter, Saturn, Uranus, and Neptune, which are much more massive and farther from the Sun than Earth is, contain large amounts of hydrogen and helium?

Solution

Since they’re more massive, their gravity is stronger, so the escape velocity from them is higher. Since they’re farther from the Sun, they’re colder, so the speeds of atmospheric molecules including hydrogen and helium are lower. The combination of those facts means that relatively few hydrogen and helium molecules have escaped from the outer planets.

1. Statistical mechanics says that in a gas maintained at a constant temperature through thermal contact with a bigger system (a “reservoir”) at that temperature, the fluctuations in internal energy are typically a fraction  of the internal energy. As a fraction of the total internal energy of a mole of gas, how big are the fluctuations in the internal energy? Are we justified in ignoring them?

Solution

For a mole, the fluctuations are on the order of  which is about . We’re certainly justified in ignoring that.

1. Which is more dangerous, a closet where tanks of nitrogen are stored, or one where tanks of carbon dioxide are stored?

Solution

One where nitrogen is stored, as excess CO2 will cause a feeling of suffocating, but excess nitrogen and insufficient oxygen will not.

1. Experimentally it appears that many polyatomic molecules’ vibrational degrees of freedom can contribute to some extent to their energy at room temperature. Would you expect that fact to increase or decrease their heat capacity from the value *R*? Explain.

Solution

Increase, since the heat capacity is proportional to the number of degrees of freedom.

1. One might think that the internal energy of diatomic gases is given by  Do diatomic gases near room temperature have more or less internal energy than that? *Hint:* Their internal energy includes the total energy added in raising the temperature from the boiling point (very low) to room temperature.

Solution

Less, because at lower temperatures their heat capacity was only 3*RT*/2.

1. You mix 5 moles of H2 at 300 K with 5 moles of He at 360 K in a perfectly insulated calorimeter. Is the final temperature higher or lower than 330 K?

Solution

lower; The hydrogen is diatomic, so it has a higher molar heat capacity, so its temperature changes less.

1. One cylinder contains helium gas and another contains krypton gas at the same temperature. Mark each of these statements true, false, or impossible to determine from the given information. (a) The rms speeds of atoms in the two gases are the same. (b) The average kinetic energies of atoms in the two gases are the same. (c) The internal energies of 1 mole of gas in each cylinder are the same. (d) The pressures in the two cylinders are the same.

Solution

a. false; b. true; c. true; d. true

1. Repeat the previous question if one gas is still helium but the other is changed to fluorine, .

Solution

a. false; b. true; c. false; d. true

1. An ideal gas is at a temperature of 300 K. To double the average speed of its molecules, what does the temperature need to be changed to?

Solution

1200 K

**Problems**

1. The gauge pressure in your car tires is  at a temperature of  when you drive it onto a ship in Los Angeles to be sent to Alaska. What is their gauge pressure on a night in Alaska when their temperature has dropped to ? Assume the tires have not gained or lost any air.

Solution

1.63 atm or 165 kPa

1. Suppose a gas-filled incandescent light bulb is manufactured so that the gas inside the bulb is at atmospheric pressure when the bulb has a temperature of . (a) Find the gauge pressure inside such a bulb when it is hot, assuming its average temperature is  (an approximation) and neglecting any change in volume due to thermal expansion or gas leaks. (b) The actual final pressure for the light bulb will be less than calculated in part (a) because the glass bulb will expand. Is this effect significant?

Solution

a. 0.137 atm; b.  Because of the expansion of the glass, . Multiplying by that factor does not make any significant difference.

1. People buying food in sealed bags at high elevations often notice that the bags are puffed up because the air inside has expanded. A bag of pretzels was packed at a pressure of 1.00 atm and a temperature of  When opened at a summer picnic in Santa Fe, New Mexico, at a temperature of  the volume of the air in the bag is 1.38 times its original volume. What is the pressure of the air?

Solution

0.749 atm

1. How many moles are there in (a) 0.0500 g of  gas  (b) 10.0 g of  gas  (c) How many molecules are present in each case?

Solution

a.  b. 0.227 mol; c.  molecules for the nitrogen,  molecules for the carbon dioxide

1. A cubic container of volume 2.00 L holds 0.500 mol of nitrogen gas at a temperature of  What is the net force due to the nitrogen on one wall of the container? Compare that force to the sample’s weight.

Solution

9830 N, far more than the sample’s weight, which is 0.137 N

1. Calculate the number of moles in the 2.00-L volume of air in the lungs of the average person. Note that the air is at  (body temperature) and that the total volume in the lungs is several times the amount inhaled in a typical breath as given in the example Calculating the Number of Molecules in a Cubic Meter of Gas.

Solution



1. An airplane passenger has  of air in his stomach just before the plane takes off from a sea-level airport. What volume will the air have at cruising altitude if cabin pressure drops to ?

Solution



1. A company advertises that it delivers helium at a gauge pressure of  in a cylinder of volume 43.8 L. How many balloons can be inflated to a volume of 4.00 L with that amount of helium? Assume the pressure inside the balloons is  and the temperature in the cylinder and the balloons is .

Solution



1. According to http://hyperphysics.phy-astr.gsu.edu/hbase/solar/venusenv.html, the atmosphere of Venus is approximately  and  by volume. On the surface, where the temperature is about 750 K and the pressure is about 90 atm, what is the density of the atmosphere?

Solution

According to the ideal gas law, the volume is proportional to the number of moles or molecules, so the percentages by volume are percentages by moles or molecules. Thus, the molar mass is . The ideal gas law says that the number of moles in a cubic meter is . The mass of that quantity of atmosphere is  so the density is .]

1. An expensive vacuum system can achieve a pressure as low as  at  How many molecules are there in a cubic centimeter at this pressure and temperature?

Solution



1. The number density *N*/*V* of gas molecules at a certain location in the space above our planet is about 1.00 × 1011 m–3, and the pressure is  in this space. What is the temperature there?

Solution

199 K

1. A bicycle tire contains 2.00 L of gas at an absolute pressure of  and a temperature of . What will its pressure be if you let out an amount of air that has a volume of  at atmospheric pressure? Assume tire temperature and volume remain constant.

Solution

 6.86 atm

1. In a common demonstration, a bottle is heated and stoppered with a hard-boiled egg that’s a little bigger than the bottle’s neck. When the bottle is cooled, the pressure difference between inside and outside forces the egg into the bottle. Suppose the bottle has a volume of 0.500 L and the temperature inside it is raised to  while the pressure remains constant at 1.00 atm because the bottle is open. (a) How many moles of air are inside? (b) Now the egg is put in place, sealing the bottle. What is the gauge pressure inside after the air cools back to the ambient temperature of but before the egg is forced into the bottle?

Solution

a. 0.0172 mol; b. 

1. A high-pressure gas cylinder contains 50.0 L of toxic gas at a pressure of  and a temperature of . The cylinder is cooled to dry ice temperature  to reduce the leak rate and pressure so that it can be safely repaired. (a) What is the final pressure in the tank, assuming a negligible amount of gas leaks while being cooled and that there is no phase change? (b) What is the final pressure if one-tenth of the gas escapes? (c) To what temperature must the tank be cooled to reduce the pressure to 1.00 atm (assuming the gas does not change phase and that there is no leakage during cooling)? (d) Does cooling the tank as in part (c) appear to be a practical solution?

Solution

a.  b.  c. 2.15 K; d. no

1. Find the number of moles in 2.00 L of gas at  and under  of pressure.

Solution

57.9 mol

1. Calculate the depth to which Avogadro’s number of table tennis balls would cover Earth. Each ball has a diameter of 3.75 cm. Assume the space between balls adds an extra  to their volume and assume they are not crushed by their own weight.

Solution

40.7 km

1. (a) What is the gauge pressure in a  car tire containing 3.60 mol of gas in a 30.0-L volume? (b) What will its gauge pressure be if you add 1.00 L of gas originally at atmospheric pressure and ? Assume the temperature remains at  and the volume remains constant.

Solution

a. 1.94 atm; b. 1.97 atm

1. A person hits a tennis ball with a mass of 0.058 kg against a wall. The average component of the ball’s velocity perpendicular to the wall is 11 m/s, and the ball hits the wall every 2.1 s on average, rebounding with the opposite perpendicular velocity component. (a) What is the average force exerted on the wall? (b) If the part of the wall the person hits has an area of  what is the average pressure on that area?

Solution

a. 0.61 N; b. 0.20 Pa

1. A person is in a closed room (a racquetball court) with  hitting a ball  around at random without any pauses. The average kinetic energy of the ball is 2.30 J. (a) What is the average value of  Does it matter which direction you take to be *x*? (b) Applying the methods of this chapter, find the average pressure on the walls? (c) Aside from the presence of only one “molecule” in this problem, what is the main assumption in Pressure, Temperature, and RMS Speed that does not apply here?

Solution

a.  The choice of *x* doesn’t matter. b.  c. The assumption that gravity is negligible and the motion is isotropic.

1. Five bicyclists are riding at the following speeds: 5.4 m/s, 5.7 m/s, 5.8 m/s, 6.0 m/s, and 6.5 m/s. (a) What is their average speed? (b) What is their rms speed?

Solution

a. 5.88 m/s; b. 5.89 m/s

1. Some incandescent light bulbs are filled with argon gas. What is  for argon atoms near the filament, assuming their temperature is 2500 K?

Solution

1.25 × 103 m/s

1. Typical molecular speeds  are large, even at low temperatures. What is  for helium atoms at 5.00 K, less than one degree above helium’s liquefaction temperature?

Solution

177 m/s

1. What is the average kinetic energy in joules of hydrogen atoms on the  surface of the Sun? (b) What is the average kinetic energy of helium atoms in a region of the solar corona where the temperature is ?

Solution

a. 1.20 × 10–19 J; b. 1.24 × 10–17 J

1. What is the ratio of the average translational kinetic energy of a nitrogen molecule at a temperature of 300 K to the gravitational potential energy of a nitrogen-molecule−Earth system at the ceiling of a 3-m-tall room with respect to the same system with the molecule at the floor?

Solution

4.54 × 103

1. What is the total translational kinetic energy of the air molecules in a room of volume  if the pressure is 9.5 × 104 Pa (the room is at fairly high elevation) and the temperature is? Is any item of data unnecessary for the solution?

Solution

 Temperature is unnecessary.

1. The product of the pressure and volume of a sample of hydrogen gas at  is 80.0 J. (a) How many moles of hydrogen are present? (b) What is the average translational kinetic energy of the hydrogen molecules? (c) What is the value of the product of pressure and volume at 

Solution

a. 0.0352 mol; b.  c. 139 J

1. What is the gauge pressure inside a tank of  of compressed nitrogen with a volume of  if the rms speed is 514 m/s?

Solution

1.82 × 107 Pa

1. If the rms speed of oxygen molecules inside a refrigerator of volume  is 465 m/s, what is the partial pressure of the oxygen? There are 5.71 moles of oxygen in the refrigerator, and the molar mass of oxygen is 32.0 g/mol.

Solution

21.1 kPa

1. The escape velocity of any object from Earth is 11.1 km/s. At what temperature would oxygen molecules (molar mass is equal to 32.0 g/mol) have root-mean-square velocity  equal to Earth’s escape velocity of 11.1 km/s?

Solution



1. The escape velocity from the Moon is much smaller than that from the Earth, only 2.38 km/s. At what temperature would hydrogen molecules (molar mass is equal to 2.016 g/mol) have a root-mean-square velocity  equal to the Moon’s escape velocity?

Solution

458 K

1. Nuclear fusion, the energy source of the Sun, hydrogen bombs, and fusion reactors, occurs much more readily when the average kinetic energy of the atoms is high—that is, at high temperatures. Suppose you want the atoms in your fusion experiment to have average kinetic energies of . What temperature is needed?

Solution



1. Suppose that the typical speed  of carbon dioxide molecules (molar mass is 44.0 g/mol) in a flame is found to be 1350 m/s. What temperature does this indicate?

Solution



1. (a) Hydrogen molecules (molar mass is equal to 2.016 g/mol) have  equal to 193 m/s. What is the temperature? (b) Much of the gas near the Sun is atomic hydrogen (H rather than  Its temperature would have to be  for the rms speed  to equal the escape velocity from the Sun. What is that velocity?

Solution

a. 3.01 K; b. 

1. There are two important isotopes of uranium,  and ; these isotopes are nearly identical chemically but have different atomic masses. Only  is very useful in nuclear reactors. Separating the isotopes is called uranium enrichment (and is often in the news as of this writing, because of concerns that some countries are enriching uranium with the goal of making nuclear weapons.) One of the techniques for enrichment, gas diffusion, is based on the different molecular speeds of uranium hexafluoride gas, . (a) The molar masses of  and  are 349.0 g/mol and 352.0 g/mol, respectively. What is the ratio of their typical speeds ? (b) At what temperature would their typical speeds differ by 1.00 m/s? (c) Do your answers in this problem imply that this technique may be difficult?

Solution

a. 1.004; b. 764 K; c. This temperature is equivalent to , which is high but not impossible to achieve. Thus, this process is feasible. At this temperature, however, there may be other considerations that make the process difficult. (In general, uranium enrichment by gaseous diffusion is indeed difficult and requires many passes.)

1. The partial pressure of carbon dioxide in the lungs is about 470 Pa when the total pressure in the lungs is 1.0 atm. What percentage of the air molecules in the lungs is carbon dioxide? Compare your result to the percentage of carbon dioxide in the atmosphere, about 0.033%.

Solution

, 14 times the percentage in the atmosphere

1. Dry air consists of approximately  by mole, with trace amounts of other gases. A tank of compressed dry air has a volume of 1.76 cubic feet at a gauge pressure of 2200 pounds per square inch and a temperature of 293 K. How much oxygen does it contain in moles?

Solution

65 mol

1. (a) Using data from the previous problem, find the mass of nitrogen, oxygen, and argon in 1 mol of dry air. The molar mass of  is 28.0 g/mol, that of  is 32.0 g/mol, and that of argon is 39.9 g/mol. (b) Dry air is mixed with pentane  molar mass 72.2 g/mol), an important constituent of gasoline, in an air-fuel ratio of 15:1 by mass (roughly typical for car engines). Find the partial pressure of pentane in this mixture at an overall pressure of 1.00 atm.

Solution

a. 0.0218 kg nitrogen, 0.00672 kg oxygen, 0.000399 kg argon; b. 0.0260 atm

1. (a) Given that air is  oxygen, find the minimum atmospheric pressure that gives a relatively safe partial pressure of oxygen of 0.16 atm. (b) What is the minimum pressure that gives a partial pressure of oxygen above the quickly fatal level of 0.06 atm? (c) The air pressure at the summit of Mount Everest (8848 m) is 0.334 atm. Why have a few people climbed it without oxygen, while some who have tried, even though they had trained at high elevation, had to turn back?

Solution

a. 0.76 atm; b. 0.29 atm; c. The pressure there is barely above the quickly fatal level.

1. (a) If the partial pressure of water vapor is 8.05 torr, what is the dew point?  (b) On a warm day when the air temperature is  and the dew point is , what are the partial pressure of the water in the air and the relative humidity?

Solution

a. ; b. 3167 Pa, 

1. To give a helium atom nonzero angular momentum requires about 21.2 eV of energy (that is, 21.2 eV is the difference between the energies of the lowest-energy or ground state and the lowest-energy state with angular momentum). The electron-volt or eV is defined as  Find the temperature *T* where this amount of energy equals  Does this explain why we can ignore the rotational energy of helium for most purposes? (The results for other monatomic gases, and for diatomic gases rotating around the axis connecting the two atoms, have comparable orders of magnitude.)

Solution

; Yes, that’s an impractically high temperature.

1. (a) How much heat must be added to raise the temperature of 1.5 mol of air from  to  at constant volume? Assume air is completely diatomic. (b) Repeat the problem for the same number of moles of xenon, Xe.

Solution

a. 249 J; b. 150 J

1. A sealed, rigid container of 0.560 mol of an unknown ideal gas at a temperature of  is cooled to . In the process, 980 J of heat are removed from the gas. Is the gas monatomic, diatomic, or polyatomic?

Solution

polyatomic

1. A sample of neon gas (Ne, molar mass  at a temperature of  is put into a steel container of mass 47.2 g that’s at a temperature of . The final temperature is (No heat is exchanged with the surroundings, and you can neglect any change in the volume of the container.) What is the mass of the sample of neon?

Solution

0.415 kg

1. A steel container of mass 135 g contains 24.0 g of ammonia, NH3, which has a molar mass of 17.0 g/mol. The container and gas are in equilibrium at . How much heat has to be removed to reach a temperature of ? Ignore the change in volume of the steel.

Solution



1. A sealed room has a volume of . It’s filled with air, which may be assumed to be diatomic, at a temperature of  and a pressure of 9.83 × 104 Pa. A 1.00-kg block of ice at its melting point is placed in the room. Assume the walls of the room transfer no heat. What is the equilibrium temperature?

Solution



1. Heliox, a mixture of helium and oxygen, is sometimes given to hospital patients who have trouble breathing, because the low mass of helium makes it easier to breathe than air. Suppose helium at  is mixed with oxygen at  to make a mixture that is  helium by mole. What is the final temperature? Ignore any heat flow to or from the surroundings, and assume the final volume is the sum of the initial volumes.

Solution



1. Professional divers sometimes use heliox, consisting of  helium and  oxygen by mole. Suppose a perfectly rigid scuba tank with a volume of 11 L contains heliox at an absolute pressure of  at a temperature of . (a) How many moles of helium and how many moles of oxygen are in the tank? (b) The diver goes down to a point where the sea temperature is  while using a negligible amount of the mixture. As the gas in the tank reaches this new temperature, how much heat is removed from it?

Solution

a. 72 mol He and 19 mol ; b. 

1. In car racing, one advantage of mixing liquid nitrous oxide (N2O) with air is that the boiling of the “nitrous” absorbs latent heat of vaporization and thus cools the air and ultimately the fuel-air mixture, allowing more fuel-air mixture to go into each cylinder. As a very rough look at this process, suppose 1.0 mol of nitrous oxide gas at its boiling point, , is mixed with 4.0 mol of air (assumed diatomic) at . What is the final temperature of the mixture? Use the measured heat capacity of N2O at , which is . (The primary advantage of nitrous oxide is that it consists of 1/3 oxygen, which is more than air contains, so it supplies more oxygen to burn the fuel. Another advantage is that its decomposition into nitrogen and oxygen releases energy in the cylinder.)

Solution



1. In a sample of hydrogen sulfide  at a temperature of 3.00 × 102 K, estimate the ratio of the number of molecules that have speeds very close to  to the number that have speeds very close to 

Solution

22.5

1. Using the approximation  for small **, estimate the fraction of nitrogen molecules at a temperature of  that have speeds between 290 m/s and 291 m/s.

Solution

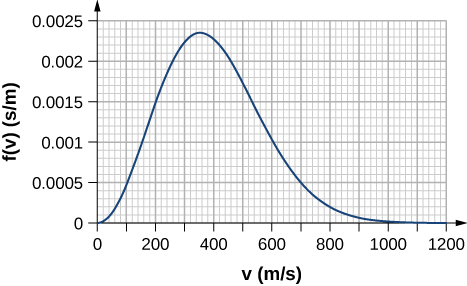
0.00157

1. Using the method of the preceding problem, estimate the fraction of nitric oxide (NO) molecules at a temperature of 250 K that have energies between  and.

Solution

0.00602

1. By counting squares in the following figure, estimate the fraction of argon atoms at  that have speeds between 600 m/s and 800 m/s. The curve is correctly normalized. The value of a square is its length as measured on the *x*-axis times its height as measured on the *y*-axis, with the units given on those axes.



Solution

About 0.072. Answers may vary slightly. A more accurate answer is 0.074.

1. Using a numerical integration method such as Simpson’s rule, find the fraction of molecules in a sample of oxygen gas at a temperature of 250 K that have speeds between 100 m/s and 150 m/s. The molar mass of oxygen () is 32.0 g/mol. A precision to two significant digits is enough.

Solution

0.034

1. Find (a) the most probable speed, (b) the average speed, and (c) the rms speed for nitrogen molecules at 295 K.

Solution

a. 419 m/s; b. 472 m/s; c. 513 m/s

1. Repeat the preceding problem for nitrogen molecules at 2950 K.

Solution

a.  b.  c. 

1. At what temperature is the average speed of carbon dioxide molecules  510 m/s?

Solution

541 K

1. The most probable speed for molecules of a gas at 296 K is 263 m/s. What is the molar mass of the gas? (You might like to figure out what the gas is likely to be.)

Solution

70.9 g/mol (The gas might be 

1. a) At what temperature do oxygen molecules have the same average speed as helium atoms  have at 300 K? b) What is the answer to the same question about most probable speeds? c) What is the answer to the same question about rms speeds?

Solution

2400 K for all three parts

**Additional Problems**

1. In the deep space between galaxies, the density of molecules (which are mostly single atoms) can be as low as 106 atoms/m3, and the temperature is a frigid 2.7 K. What is the pressure? (b) What volume (in ) is occupied by 1 mol of gas? (c) If this volume is a cube, what is the length of its sides in kilometers?

Solution

a.  b.  c. 800 km

1. (a) Find the density in SI units of air at a pressure of 1.00 atm and a temperature of , assuming that air is 78% N2, 21% O2, and 1% Ar, (b) Find the density of the atmosphere on Venus, assuming that it’s 96% CO2 and 4% N2, with a temperature of 737 K and a pressure of 92.0 atm.

Solution

a. ; b. 

1. The air inside a hot-air balloon has a temperature of 370 K and a pressure of 101.3 kPa, the same as that of the air outside. Using the composition of air as 78% N2, 21% O2, and 1% Ar, find the density of the air inside the balloon.

Solution



1. When an air bubble rises from the bottom to the top of a freshwater lake, its volume increases by . If the temperatures at the bottom and the top of the lake are 4.0 and 10 , respectively, how deep is the lake?

Solution

7.9 m

1. (a) Use the ideal gas equation to estimate the temperature at which 1.00 kg of steam (molar mass ) at a pressure of  occupies a volume of . (b) The van der Waals constants for water are  and . Use the Van der Waals equation of state to estimate the temperature under the same conditions. (c) The actual temperature is 779 K. Which estimate is better?

Solution

a. 715 K; b. 726 K; c. The Van der Waals estimate is better but definitely not perfect.

1. One process for decaffeinating coffee uses carbon dioxide  at a molar density of about  and a temperature of about . (a) Is CO2 a solid, liquid, gas, or supercritical fluid under those conditions? (b) The van der Waals constants for carbon dioxide are  and  Using the van der Waals equation, estimate the pressure of  at that temperature and density.

Solution

a. supercritical fluid; b. 

1. On a winter day when the air temperature is , the relative humidity is . Outside air comes inside and is heated to a room temperature of . What is the relative humidity of the air inside the room. (Does this problem show why inside air is so dry in winter?)

Solution

; yes, that’s very dry.

1. On a warm day when the air temperature is , a metal can is slowly cooled by adding bits of ice to liquid water in it. Condensation first appears when the can reaches . What is the relative humidity of the air?

Solution



1. (a) People often think of humid air as “heavy.” Compare the densities of air with  relative humidity and  relative humidity when both are at 1 atm and . Assume that the dry air is an ideal gas composed of molecules with a molar mass of 29.0 g/mol and the moist air is the same gas mixed with water vapor. (b) As discussed in the chapter on the applications of Newton’s laws, the air resistance felt by projectiles such as baseballs and golf balls is approximately , where  is the mass density of the air, *A* is the cross-sectional area of the projectile, and *C* is the projectile’s drag coefficient. For a fixed air pressure, describe qualitatively how the range of a projectile changes with the relative humidity. (c) When a thunderstorm is coming, usually the humidity is high and the air pressure is low. Do those conditions give an advantage or disadvantage to home-run hitters?

Solution

a. dry air:  humid air:  b. increased humidity decreases air resistance and increases range; c. an advantage

1. The mean free path for helium at a certain temperature and pressure is  The radius of a helium atom can be taken as . What is the measure of the density of helium under those conditions (a) in molecules per cubic meter and (b) in moles per cubic meter?

Solution

a.  b. 

1. The mean free path for methane at a temperature of 269 K and a pressure of  is Find the effective radius *r* of the methane molecule.

Solution



1. In the chapter on fluid mechanics, Bernoulli’s equation for the flow of incompressible fluids was explained in terms of changes affecting a small volume *dV* of fluid. Such volumes are a fundamental idea in the study of the flow of compressible fluids such as gases as well. For the equations of hydrodynamics to apply, the mean free path must be much less than the linear size of such a volume,  For air in the stratosphere at a temperature of 220 K and a pressure of 5.8 kPa, how big should *a* be for it to be 100 times the mean free path? Take the effective radius of air molecules to be  which is roughly correct for N2.

Solution

8.2 mm

1. Find the total number of collisions between molecules in 1.00 s in 1.00 L of nitrogen gas at standard temperature and pressure (, 1.00 atm). Use  as the effective radius of a nitrogen molecule. (The number of collisions per second is the reciprocal of the collision time.) Keep in mind that each collision involves two molecules, so if one molecule collides once in a certain period of time, the collision of the molecule it hit cannot be counted.

Solution



1. (a) Estimate the specific heat capacity of sodium from the Law of Dulong and Petit. The molar mass of sodium is 23.0 g/mol. (b) What is the percent error of your estimate from the known value, ?

Solution

a. ; b. 

1. A sealed, perfectly insulated container contains 0.630 mol of air at  and an iron stirring bar of mass 40.0 g. The stirring bar is magnetically driven to a kinetic energy of 50.0 J and allowed to slow down by air resistance. What is the equilibrium temperature?

Solution



1. Find the ratio  for hydrogen gas  at a temperature of 77.0 K.

Solution

 or about 1.10

1. **Unreasonable results**. (a) Find the temperature of 0.360 kg of water, modeled as an ideal gas, at a pressure of  if it has a volume of . (b) What is unreasonable about this answer? How could you get a better answer?

Solution

a. 374 K, or ; b. As the water is just above its boiling point, the ideal gas law doesn’t apply. The van der Waals equation would work better. (Looking the answer up in “steam tables” would work even better.)

1. **Unreasonable results**. (a) Find the average speed of hydrogen sulfide, , molecules at a temperature of 250 K. Its molar mass is 31.4 g/mol (b) The result isn’t *very* unreasonable, but why is it less reliable than those for, say, neon or nitrogen?

Solution

a. 411 m/s; b. According to the following table, the *CV* of H2S is significantly different from the theoretical value, so the ideal gas model does not describe it very well at room temperature and pressure, and the Maxwell-Boltzmann speed distribution for ideal gases may not hold very well, even less well at a lower temperature.

|  |  |
| --- | --- |
| Gas | *CV*/R at 25 °C and 1 atm |
| Ar | 1.50 |
| He | 1.50 |
| Ne | 1.50 |
| CO | 2.50 |
|  | 2.47 |
|  | 2.50 |
|  | 2.53 |
|  | 2.8 |
|  | 3.48 |
|  | 3.13 |
|  | 3.66 |

**Challenge Problems**

1. An airtight dispenser for drinking water is 25 cm × 10 cm in horizontal dimensions and 20 cm tall. It has a tap of negligible volume that opens at the level of the bottom of the dispenser. Initially, it contains water to a level 3.0 cm from the top and air at the ambient pressure, 1.00 atm, from there to the top. When the tap is opened, water will flow out until the gauge pressure at the bottom of the dispenser, and thus at the opening of the tap, is 0. What volume of water flows out? Assume the temperature is constant, the dispenser is perfectly rigid, and the water has a constant density of 1000 kg/m3.

Solution

Let *h* be the new distance of the water surface from the top of the dispenser. Then the depth of the water is .The gauge pressure  is given by  At constant *T*, the air pressure is inversely proportional to the volume, and as the cross-sectional area of the container is uniform, the volume of the air is proportional to the height of the air space. Thus, . The additional pressure due to the water is  Then, we have to solve  Multiplying by *h* gives a quadratic equation whose solution is 0.0305 m (as well as a negative solution, which is irrelevant). Thus, the water level is reduced by only 0.5 mm (independent of the horizontal dimensions of the dispenser). The volume poured out is that change in depth times the cross-sectional area of the dispenser, which is  or 12.5 mL. (Now you have to let some air in to get more water out.)

1. Eight bumper cars, each with a mass of 322 kg, are running in a room 21.0 m long and 13.0 m wide. They have no drivers, so they just bounce around on their own. The rms speed of the cars is 2.50 m/s. Repeating the arguments of Pressure, Temperature, and RMS Speed find the average force per unit length (analogous to pressure) that the cars exert on the walls.

Solution

29.5 N/m

1. Verify that 

Solution

To find the *v* that maximizes *f*(*v*), we set  and solve for *v*:

**,

**,

**.

We take the derivative by using the product rule. The speed that solves the equation is .

**,

**,



1. Verify the normalization equation  In doing the integral, first make the substitution  This “scaling” transformation gives you all features of the answer except for the integral, which is a dimensionless numerical factor. You’ll need the formula

**

to find the numerical factor and verify the normalization.

Solution

Substituting  and  gives



1. Verify that  Make the same scaling transformation as in the preceding problem.

Solution

We need

**

We can do that integral by parts.

**.

The first term is 0. The integral on the right side is easily evaluated by substitution.

**

We finally have 

1. Verify that 

Solution

Making the scaling transformation as in the previous problems, we find that

**

As in the previous problem, we integrate by parts:

**

Again, the first term is 0, and we were given in an earlier problem that the integral in the second term equals  We now have

**

Taking the square root of both sides gives the desired result: 

This file is copyright 2016, Rice University. All Rights Reserved.