



① Let's go this path:  $R_L = \frac{4.5V}{25mA} = 180\Omega = R_L$

and for  $i < 25mA$ ,  $R_L > 180\Omega$ .

Under full load

$$V = 13.8 \left( \frac{R_2 / 180}{R_1 + R_2 / 180} \right) = 4.5V \quad (1)$$

$$\text{And no load: } 13.8 \left( \frac{R_2}{R_1 + R_2} \right) = 5.1V \quad (2)$$

2 eqns w/ 2 unknowns

Invert them:

$$\frac{R_1 + x}{x} = \frac{13.8}{4.5} = 3.07 \rightarrow R_1 + x = 3.07x \rightarrow R_1 = 2.07x = 2.07(R_2 / 180\Omega)$$

$$\frac{R_1 + R_2}{R_2} = \frac{13.8}{5.1} = 2.71 \rightarrow R_1 + R_2 = 2.71 R_2 \rightarrow R_1 = 1.71 R_2$$

$$\Rightarrow 1.71 R_2 = 2.07 \left( \frac{R_2 \cdot 180}{R_2 + 180} \right) \rightarrow R_2 + 180 = \frac{2.07}{1.71} \cdot 180 = 218 \rightarrow R_2 = 38\Omega$$

$$R_1 = 1.71 R_2 = 65.9\Omega = R_1$$

③ Power: No load,  $R_{TOT} = R_1 + R_2 = (38 + 65.9)\Omega = 103\Omega$ ,  $P = \frac{V^2}{R} = \frac{13.8^2}{103} = 1.85W$   
With load  $R_{TOT} = R_1 + R_2 / 180 = 65.9 + \frac{38 \cdot 180}{38 + 180} = 96.4\Omega \rightarrow P = 1.98W$

Efficiency =  $\frac{\text{power to load}}{\text{total power}} \cdot 100\% = \frac{(4.5V)^2 / 180\Omega}{1.98W} = \frac{113mW}{2W} = 5.6\%$  efficient

④ To get  $25mA = I_E = h_{FE} \cdot I_B \rightarrow I_B = \frac{25mA}{100} = 250\mu A$ . So 2 extremes:

$$i = 0 @ V = 5.1 + 0.6 = 5.7V \quad (1)$$

$$I = 250\mu A @ V = 4.5 + 0.6 = 5.1V \quad (2)$$

$$Z_L = \frac{5.1V}{250\mu A} = 20.4K\Omega$$

(1)  $13.8 \left( \frac{R_2}{R_1 + R_2} \right) = 5.7 \rightarrow R_1 + R_2 = \frac{13.8}{5.7} R_2 \rightarrow R_1 = 1.42 R_2$

(2)  $13.8 \left( \frac{R_2 / 20.4K}{R_1 + R_2 / 20.4K} \right) = 5.1 \rightarrow R_1 + x = 2.71 \rightarrow R_1 = 1.71 \frac{R_2 / 20.4K}{R_2 + 20.4K} = 1.42 R_2$

$$\Rightarrow 24.5K = R_2 + 20.4K \rightarrow R_2 = 4.11K\Omega \quad R_1 = 5.83K\Omega$$

⑥ No load power  $P = \frac{V^2}{(R_1 + R_2)} = \frac{13.8^2}{(4.11K + 5.83K)} = \boxed{19.2\text{mW}}$   
 What about the transistor?  $R_L = \infty \Rightarrow I_c = 0 \Rightarrow I_B = 0 \Rightarrow I_c = 0$ , ...  
 its turned off.

⑦ When  $R_L = 180\Omega$ , drawing 25mA, 250mA comes from  $I_B$  and the rest comes from  $I_c$ . We've shown that the base-emitter- $R_L = 180\Omega$  series combination =  $20.4\Omega$   $\rightarrow$  Power through that part of the circuit is  $P = \frac{V^2}{(R_1 + R_2 + 20.4\Omega)} = \frac{13.8^2}{(5.83K + \frac{4.11K \cdot 20.4K}{4.11K + 20.4K})} = \boxed{20.6\text{mW}}$

But the majority of power comes through  $I_c$ :  $P = VI = 13.8 \cdot (25\text{mA} - 250\mu\text{A}) = \boxed{342\text{mW}}$

So total power = 363mW

The transistor will dissipate  $P = V_{CE} I_c = (13.8 - 4.5)(25\text{mA}) = \boxed{233\text{mW}}$

The load power = 113mW (#4)  $\Rightarrow$

Efficiency =  $\frac{113\text{mW}}{363\text{mW}} \cdot 100\% = \boxed{31\%}$ , 5.5 times more efficient than the passive circuit