

Compilers (CS31003)

Lecture 06

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A grammar

$G = \langle T, N, S, P \rangle$ is a (context-free) grammar where:

T	:	Set of terminal symbols
N	:	Set of non-terminal symbols
S	:	$S \in N$ is the start symbol
P	:	Set of production rules

Every production rule is of the form: $A \rightarrow \alpha$, where $A \in N$ and $\alpha \in (N \cup T)^*$.

Symbol convention:

a, b, c, \dots	Lower case letters at the beginning of alphabet	$\in T$
x, y, z, \dots	Lower case letters at the end of alphabet	$\in T^+$
A, B, C, \dots	Upper case letters at the beginning of alphabet	$\in N$
X, Y, Z, \dots	Upper case letters at the end of alphabet	$\in (N \cup T)$
$\alpha, \beta, \gamma, \dots$	Greek letters	$\in (N \cup T)^*$

A grammar

- * $G_1 = (\{E\}, \{+, *, (,), \text{Id}\}, P_1, E)$
- * $P_1 \quad E \rightarrow E + E \mid E * E \mid (E) \mid \text{Id}$

Id+Id

Left most derivation:

unambiguous grammar

$E \rightarrow E + E \rightarrow \text{Id} + E \rightarrow \text{Id} + \text{Id}$

Right most derivation

$E \rightarrow E + E \rightarrow E + \text{Id} \rightarrow \text{Id} + \text{Id}$

A grammar

- * $G_1 = (\{E\}, \{+, *, (,), \text{Id}\}, P_1, E)$
- * $P_1 \quad E \rightarrow E + E \mid E * E \mid (E) \mid \text{Id}$

Id*Id+Id

ambiguous grammar

Left most derivation:

$E \rightarrow E + E \rightarrow E * E + E \rightarrow \text{Id} * E + E \rightarrow \text{Id} * \text{Id} + E \rightarrow \text{Id} * \text{Id} + \text{Id}$

$E \rightarrow E * E \rightarrow \text{Id} * E \rightarrow \text{Id} * E + E \rightarrow \text{Id} * \text{Id} + E \rightarrow \text{Id} * \text{Id} + \text{Id}$

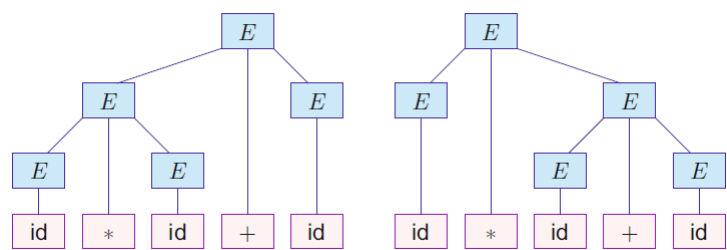
Right most derivation

$E \rightarrow E * E \rightarrow E * E + E \rightarrow E * E + \text{Id} \rightarrow E * \text{Id} + \text{Id} \rightarrow \text{Id} * \text{Id} + \text{Id}$

$E \rightarrow E + E \rightarrow E + \text{Id} \rightarrow E * E + \text{Id} \rightarrow E * \text{Id} + \text{Id} \rightarrow \text{Id} * \text{Id} + \text{Id}$

A grammar

- * $G_1 = (\{E\}, \{+, *, (,), Id\}, P_1, E)$
 - * $P_1 \quad E \rightarrow E + E \mid E * E \mid (E) \mid Id$
- ambiguous grammar



Two grammars

- $G_0 = (\{E, T, F\}, \{+, *, (,), Id\}, P_0, E)$
 - $P_0 \quad E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E) \mid Id$
-
- * $G_1 = (\{E\}, \{+, *, (,), Id\}, P_1, E)$
 - * $P_1 \quad E \rightarrow E + E \mid E * E \mid (E) \mid Id$

Parsing Fundamentals

Derivation	Parsing	Parser	Remarks
Left-most	Top-Down	Predictive: Recursive Descent, LL(1)	No Ambiguity No Left-recursion Tool: Antlr
Right-most	Bottom-Up	Shift-Reduce: SLR, LALR(1), LR(1)	Ambiguity okay Left-recursion okay Tool: YACC, Bison

Recursive Descent Parser

$S \rightarrow c A d$
 $A \rightarrow ab \mid a$

```

int main() {
    l = getchar();
    S(); // S is a start symbol

    // Here l is lookahead. If l = $, it represents the end of the string
    if (l == '$')
        printf("Parsing Successful");
    else printf("Error");
}

S() { // Definition of S, as per the given production
    match('c');
    A();
    match('d');
}

A() { // Definition of A as per the given production
    match('a');
    if (l == 'b') { // Look-ahead for decision
        match('b');
    }
}

match(char t) { // Match function - matches and consumes
    if (l == t) { l = getchar();
    }
    else printf("Error");
}

```

Check with: $cad\$$ ($S \Rightarrow cAd \Rightarrow cad$), $cabd\$$ ($S \Rightarrow cAd \Rightarrow cabd$), $caad\$$

Recursive Descent Parser

$$\begin{array}{lcl} S & \rightarrow & c A d \\ A & \rightarrow & aAb \mid a \end{array}$$

```
int main() {
    l = getchar();
    S(); // S is a start symbol.

    // Here l is lookahead. if l = $, it represents the end of the string
    if (l == '$')
        printf("Parsing Successful");
    else printf("Error");
}

S() { // Definition of S, as per the given production
    match('c');
    A();
    match('d');
}

A() { // Definition of A as per the given production
    match('a');
    if (l == 'a') { // Look-ahead for decision
        A();
        match('b');
    }
}

match(char t) { // Match function - matches and consumes
    if (l == t) { l = getchar();
    }
    else printf("Error");
}

}

Check with: cad$ (S ⇒ cAd ⇒ cad), cabd$, caabd$ (S ⇒ cAd ⇒ caAbd ⇒ caabd)
```

Recursive Descent Parser

$$\begin{array}{lcl} E & \rightarrow & a E' \\ E' & \rightarrow & + a E' \mid \epsilon \end{array}$$

```
int main() {
    l = getchar();
    E(); // E is a start symbol.
    // Here l is lookahead. If l = $, it represents the end of the string
    if (l == '$') printf("Parsing Successful");
    else printf("Error");
}

E() { // Definition of E, as per the given production
    match('a');
    E'();
}

E'() { // Definition of E' as per the given production
    if (l == '+') { // Look-ahead for decision
        match('+');
        match('a');
        E'();
    }
    else return (); // epsilon production
}

match(char t) { // Match function - matches and consumes
    if (l == t) { l = getchar();
    }
    else printf("Error");
}

}

Check with: a$ (E ⇒ aE' ⇒ a), a+a$ (E ⇒ aE' ⇒ a + aE' ⇒ a + a), a+a+a$ (E ⇒ aE' ⇒ a + aE' ⇒ a + a + aE' ⇒ a + a + a)
```

Recursive Descent Parser

$$E \rightarrow E + E \mid a$$

```
int main() {
    l = getchar();
    E(); // E is a start symbol.

    // Here l is lookahead. if l = $, it represents the end of the string
    if (l == '$')
        printf("Parsing Successful");
    else printf("Error");
}

E() { // Definition of E as per the given production
    if (l == 'a') { // Terminate ? -- Look-ahead does not work
        match('a');
    }

    E();          // Call ?
    match('+');
    E();
}

match(char t) { // Match function - matches and consumes
    if (l == t) { l = getchar();
    }
    else printf("Error");
}

Check with: a+a$, a+a+a$
```