

## Topics for Test 1

### 1. Systems of linear equations

- homogeneous and non-homogeneous
- echelon form
- leading variables and free variables
- Finding all solutions using Gauss' algorithm
- parameterized solutions

### 2. Matrices

- addition and scalar multiplication
- echelon and reduced echelon form

### 3. Vectors in $\mathbb{R}^2$ and $\mathbb{R}^3$

- magnitude and direction
- addition and scalar product
- parallel vectors
- dot product and perpendicularity
- parameterized equations
- lines
- planes and normal vectors
- subspaces
- linear combinations and span

### 4. Abstract Vector Spaces

- definition
- examples
- linear combinations and span
- subspaces
- checking if subsets are closed under addition or scalar multiplication.