

# HW 9: Signed Binary Arithmetic

For each of the  $\langle X, Y \rangle$  pairs in the table below:

- Convert  $X$  and  $Y \rightarrow$  binary
- Compute  $X + Y$  (the 8-bit **sum**)
- Compute  $\bar{Y}$  (the 2's complement of  $Y$ )
- Compute  $X - Y \equiv X + \bar{Y}$  (the 8-bit **difference**)
- Indicate the signs of  $X$ ,  $Y$ ,  $X + Y$ ,  $\bar{Y}$ , and  $X - Y$
- Convert  $X + Y$ ,  $\bar{Y}$ , and  $X - Y \rightarrow$  hexadecimal
- Indicate condition flag (**z**, **n**, **c**, **v**) values for  $X + Y$ ,  $X - Y$
- Which (if either) of  $X + Y$  and  $X - Y \rightarrow$  is honest?

Where  $\langle X, Y \rangle =$

- |                                 |                                 |
|---------------------------------|---------------------------------|
| 1) $\langle 0x4F, 0x6D \rangle$ | 2) $\langle 0xB3, 0x17 \rangle$ |
| 3) $\langle 0xA3, 0x95 \rangle$ | 4) $\langle 0x6E, 0x3A \rangle$ |

# Signed Arithmetic Example X1

**X**

0x8C

**Y**

0x6F

**X + Y**

**~Y**

**X - Y**

# Signed Arithmetic: X1 a)

**X**

**Y**

**X + Y**

**~Y**

**X - Y**

**0x8C**

**0x6F**

**10001100**

**01101111**

# Signed Arithmetic: X1 b)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
<b>0x8C</b>	<b>0x6F</b>			
10001100	01101111	10001100 01101111 <u>          </u> 01111011		

# Signed Arithmetic: X1 c)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
<b>0x8C</b>	<b>0x6F</b>			
10001100	01101111	10001100 <u>01101111</u> 011111011	<u>01101111</u> 10010000 <u>00000001</u> 10010001	

# Signed Arithmetic: X1 d)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
<b>0x8C</b>	<b>0x6F</b>			
10001100	01101111	10001100 <u>01101111</u> 011111011	<u>01101111</u> 10010000 <u>00000001</u> 10010001	10001100 <u>10010001</u> 100011101

# Signed Arithmetic: X1 e)

X	Y	X + Y	$\sim Y$	X - Y
0x8C	0x6F			
10001100	01101111	10001100 <u>01101111</u> 011111011	<u>01101111</u> 10010000 <u>00000001</u> 10010001	10001100 <u>10010001</u> 100011101

# Signed Arithmetic: X1 f)

X	Y	X + Y	~Y	X - Y
0x8C	0x6F			
10001100	01101111	10001100 <u>01101111</u> 011111011	<u>01101111</u> 10010000 <u>00000001</u> 10010001	10001100 <u>10010001</u> 100011101
		0xFB	0x91	0x1D



# Signed Arithmetic: X1

X	Y	X + Y	~Y	X - Y
0x8C	0x6F			
10001100	01101111	<div>10001100 01101111 ----- 01111011</div>	<div>01101111 10010000 00000001 ----- 10010001</div>	<div>10001100 10010001 ----- 10001101</div>
		0xFB	0x91	0x1D
		no overflow		overflow

# Signed Arithmetic: X1 g)

X	Y	X + Y	~Y	X - Y
0x8C	0x6F			
10001100	01101111	<div>10001100</div> <div>01101111</div> <hr/> <div>011111011</div>	<div>01101111</div> <hr/> <div>10010000</div> <div>00000001</div> <hr/> <div>10010001</div>	<div>10001100</div> <div>10010001</div> <hr/> <div>100011101</div>
		0xFB	0x91	0x1D
		zncv		zncv

# Signed Arithmetic: X1 h)

X	Y	X + Y	~Y	X - Y
0x8C	0x6F			
10001100	01101111	<div> <div>10001100</div> <div>01101111</div> <hr/> <div>011111011</div> </div>	<div> <div>01101111</div> <hr/> <div>10010000</div> <div>00000001</div> <hr/> <div>10010001</div> </div>	<div> <div>10001100</div> <div>10010001</div> <hr/> <div>100011101</div> </div>
		0xFB	0x91	0x1D
		<div> <div>zncv</div> </div>		<div> <div>zncv</div> </div>
		honest		deceptive

# Signed Arithmetic: X1 i)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
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**0x8C**

**0x6F**

10001100

01101111

10001100  
 01101111  
 -----  
 00001100  
 01111011

01101111  
 10010000  
 00000001  
 -----  
 10010001

10001100  
 10010001  
 -----  
 10001101

**0xFB**

**0x91**

**0x1D**

— —  
 zncv

(s) honest  
 (u) honest

—  
 zncv

(s) deceptive  
 (u) honest

# Signed Arithmetic: X2 i)

X	Y	X + Y	~Y	X - Y
0x54	0xF3			
01010100	11110011	<div> <div>01010100</div> <div>11110011</div> <hr/> <div>11110000</div> <div>101000111</div> </div>	<div> <div>11110011</div> <hr/> <div>00001100</div> <div>00000001</div> <hr/> <div>00001101</div> </div>	<div> <div>01010100</div> <div>00001101</div> <hr/> <div>00110001</div> </div>
		0x47	0x0D	0x61
		<div> <div>zncv</div> </div>		<div> <div>zncv</div> </div>
		(s) honest (u) deceptive		(s) honest (u) deceptive

# Signed Arithmetic: X3 i)

X	Y	X + Y	~Y	X - Y
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0x9E

0xCC

10011110

11001100

1	0	0	1	1	1	0	0
1	0	0	1	1	1	0	0
1	0	1	1	0	1	0	1

1	1	0	0	1	1	0	0
0	0	1	1	0	0	1	1
0	0	0	0	0	0	0	1
0	0	1	1	0	1	0	0

1	0	0	1	1	1	0	0
0	0	1	1	0	1	0	0
0	1	1	0	1	0	0	1

0x6A

0x34

0xD2

zncv

(s) honest  
(u) deceptive

zncv

(s) honest  
(u) deceptive

# Signed Arithmetic Example: X4

**X**

0x5A

**Y**

0x5A

**X + Y**

**~Y**

**X - Y**

# Signed Arithmetic: X4 a)

**X**

**Y**

**X + Y**

**~Y**

**X - Y**

**0x5A**

**0x5A**

**01011010**

**01011010**



# Signed Arithmetic: X4 b)

**X**

**Y**

**X + Y**

**~Y**

**X - Y**

**0x5A**

**0x5A**

01011010

01011010

01011010

01011010

0 1 0 1 1 0 1 0

010110100

# Signed Arithmetic: X4 c)

**X**

**Y**

**X + Y**

**~Y**

**X - Y**

**0x5A**

**0x5A**

01011010

01011010

01011010

01011010

01011010

10100101

0 1 0 1 1 0 1 0

00000001

**0**10110100

10100110

# Signed Arithmetic: X4 d)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
<b>0x5A</b>	<b>0x5A</b>			
01011010	01011010	01011010 <u>01011010</u>	<u>01011010</u> 10100101	01011010 10100110
		0 1 0 1 1 0 1 0	<u>00000001</u>	1 1 1 1 1 1 1 0
		<b>0</b> 10110100	10100110	<b>1</b> 11101000

# Signed Arithmetic: X4 e)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
<b>0x5A</b>	<b>0x5A</b>			
01011010	01011010	01011010 <u>01011010</u>	<u>01011010</u> 10100101 <u>00000001</u>	01011010 <b>10100110</b>
		0 1 0 1 1 0 1 0 <b>010110100</b>	<b>10100110</b>	1 1 1 1 1 1 1 0 <b>111101000</b>

# Signed Arithmetic: X4 f)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
<b>0x5A</b>	<b>0x5A</b>			
01011010	01011010	01011010 <u>01011010</u>	<u>01011010</u> 10100101 <u>00000001</u>	01011010 <b>10100110</b>
		0 1 0 1 1 0 1 0 <b>010110100</b>	<b>10100110</b>	1 1 1 1 1 1 1 0 <b>111101000</b>
		<b>0xB4</b>	<b>0xA6</b>	<b>0x00</b>

# Signed Arithmetic: X4

X	Y	X + Y	~Y	X - Y
0x5A	0x5A			
01011010	01011010	<div>01011010 01011010 ----- 010110100</div>	<div>01011010 10100101 ----- 10100110</div>	<div>01011010 10100110 ----- 111101000</div>
		0 1 0 1 1 0 1 0	0 0 0 0 0 0 0 1	1 1 1 1 1 1 1 0
		0xB4	0xA6	0x00
		oVerflow		no oVerflow

# Signed Arithmetic: X4

X	Y	X + Y	~Y	X - Y
0x5A	0x5A			
01011010	01011010	01011010 <u>01011010</u> 0 1 0 1 1 0 1 0 010110100	<u>01011010</u> 10100101 00000001 10100110	01011010 10100110 1 1 1 1 1 1 0 111101000
		0xB4	0xA6	0x00
		oVerflow		no oVerflow

# Signed Arithmetic: X4

X	Y	X + Y	~Y	X - Y
0x5A	0x5A			
01011010	01011010	<div>01011010 01011010 ----- 010110100</div>	<div>01011010 10100101 ----- 10100110</div>	<div>01011010 10100110 ----- 111101000</div>
		0 1 0 1 1 0 1 0	0 0 0 0 0 0 0 1	1 1 1 1 1 1 1 0
		0xB4	0xA6	0x00
		oVerflow		no oVerflow



# Signed Arithmetic: X4 g)

X	Y	X + Y	~Y	X - Y
0x5A	0x5A			
01011010	01011010	<div>01011010 01011010 ----- 010110100</div>	<div>01011010 10100101 ----- 10100110</div>	<div>01011010 10100110 ----- 111101000</div>
		0 1 0 1 1 0 1 0	0 0 0 0 0 0 0 1	1 1 1 1 1 1 1 0
		0xB4	0xA6	0x00
		zncv		zncv

# Signed Arithmetic: X4 h)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
<b>0x5A</b>	<b>0x5A</b>			
01011010	01011010	<div>01011010</div> <div>01011010</div> <hr/> <div>01011010</div> <div>01011010</div> <hr/> <div>01011010</div>	<div>01011010</div> <div>10100101</div> <hr/> <div>00000001</div> <div>10100110</div> <hr/> <div>10100110</div>	<div>01011010</div> <div>10100110</div> <hr/> <div>11110100</div> <div>11110100</div> <hr/> <div>11110100</div>
		<b>0xB4</b>	<b>0xA6</b>	<b>0x00</b>
		<div>zncv</div> <div>(s) deceptive</div>		<div>zncv</div> <div>(s) honest</div>

# Signed Arithmetic: X4 i)

<b>X</b>	<b>Y</b>	<b>X + Y</b>	<b>~Y</b>	<b>X - Y</b>
0x5A	0x5A			
01011010	01011010	<div style="border-left: 2px solid red; padding-left: 5px;">           01011010            01011010  <hr/> <span style="border: 1px solid red; padding: 0 2px;">0</span><span style="border: 1px solid red; padding: 0 2px;">1</span>011010            010110100         </div>	<div style="border-top: 1px solid black; padding-top: 5px;">           01011010            10100101            00000001  <hr/>           10100110         </div>	<div style="border-left: 2px solid green; padding-left: 5px;">           01011010            10100110  <hr/> <span style="border: 1px solid blue; padding: 0 2px;">1</span><span style="border: 1px solid blue; padding: 0 2px;">1</span>111110            111101000         </div>
		0xB4	0xA6	0x00
		$\overline{\text{zncv}}$ (s) deceptive (u) honest		$\overline{\text{zncv}}$ (s) honest (u) honest