### Sensitivity Analysis Toolbox for Dynare\*

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#### Abstract

The Sensitivity Analysis Toolbox for Dynare is a set of MATLAB routines for the analysis of DSGE models with global sensitivity analysis. The routines are thought to be used within the Dynare 6 environment.

**Keywords**: Stability Mapping, Reduced form solution, DSGE models, Monte Carlo filtering, Global Sensitivity Analysis.

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#### 1 Introduction

The Sensitivity Analysis Toolbox for Dynare is a collection of MATLAB routines implemented to answer the following questions: (i) Which is the domain of structural coefficients assuring the stability and determinacy of a DSGE model? (ii) Which parameters mostly drive the fit of, e.g., GDP and which the fit of inflation? Is there any conflict between the optimal fit of one observed series versus another one? (iii) How to represent in a direct, albeit approximated, form the relationship between structural parameters and the reduced form of a rational expectations model?

The discussion of the methodologies and their application is described in Ratto (2008).

#### 2 Use of the Toolbox

The Dynare parser now recognizes sensitivity analysis commands. The syntax is based on a single command:

```
sensitivity(option1=<opt1_val>,option2=<opt2_val>,...)
```

with a list of options described in the next section.

In order to work properly, the sensitivity analysis Toolbox does not need a Dynare estimation environment to be set up. Rather, sensitivity is the only command to run to make a sensitivity analysis on a DSGE model<sup>1</sup>.

<sup>&</sup>lt;sup>1</sup>Of course, when the user needs to perform the mapping of the fit with a posterior sample, a Bayesian estimation has to be performed beforehand

# 3 List of options

## 3.1 Sampling options

option name	default	description
Nsam	2048	Size of MC sample
ilptau	1	$1 = \text{use } LP_{\tau} \text{ quasi-Monte Carlo}$
		0 = use LHS Monte Carlo
pprior	1	1 = sample from prior distributions
		0 = sample from multivariate normal
		$N(\hat{\theta}, \Sigma), \hat{\theta}$ is posterior mode
		$\Sigma = H^{-1}$ , H is Hessian at the mode
<pre>prior_range</pre>	1	1 = sample  uniformly  from prior ranges
		0 = sample from prior distributions:
morris	0	0 = no Morris sampling for screening
		1 = Morris sampling for screening
morris_nliv	6	number of levels in Morris design
morris_ntra	20	number of trajectories in Morris design
ppost	0	0 = don't use Metropolis posterior sample
		1 = use Metropolis posterior sample: this
		overrides any other sampling option!
neighborhood_width		$\delta$ (real number> 0) uniform sample in the
		neighborhood of the posterior mode $\hat{\theta}$
		interval width: $\hat{\theta}(1 \pm \delta)$

### 3.2 Stability mapping

option name	default	description
stab	1	1 = perform stability mapping
		0 = no stability mapping is performed
load_stab	0	0 = generate a new sample
		1 = load a previously created sample
<pre>pvalue_corr</pre>	0.001	critical p-value for correlations $\rho$ in filtered samples:
		plot couples of parameters with
		p-value <pvalue_corr< td=""></pvalue_corr<>
pvalue_ks	0.001	critical p-value for Smirnov statistics $d$ :
		plot parameters with p-value <pvalue_ks< td=""></pvalue_ks<>
lik_init	1	1 = the model is stationary (unit roots are 'explosive')
		3 = the model has unit roots (unit roots are 'stable')

#### 3.3 Reduced form mapping

The mapping of the reduced form solution forces the use of samples from prior ranges or prior distributions, i.e.:

```
options_.opt_gsa.pprior=1;
options_.opt_gsa.ppost=0;
```

It uses 250 samples to optimize smoothing parameters and 1000 samples to compute the fit. The rest of the sample is used for out-of-sample validation.

option name	default	description
redform	0	0 = don't prepare MC sample of
		reduced form matrices
		1 = prepare MC sample of
		reduced form matrices
$load\_redform$	0	0 = estimate the mapping of
		reduced form model
		1 = load previously estimated mapping
$logtrans\_redform$	0	0 = use raw entries
		1 = use log-transformed entries
${\tt threshold\_redform}$		[] = don't filter MC entries
		of reduced form coefficients
		[max max] = analyse filtered
		entries within the range [max max]
${\tt ksstat\_redform}$	0.001	critical p-value for Smirnov statistics d
		when threshold_redform is active
		plot parameters with p-value <ksstat_redform< td=""></ksstat_redform<>
alpha2_redform	0	critical p-value for correlation $\rho$
		when threshold_redform is active
		plot couples of parameters with
		p-value <alpha2_redform< td=""></alpha2_redform<>
namendo	()	list of endogenous variables
	:	jolly character to indicate ALL endogenous
namlagendo	()	list of lagged endogenous variables:
		analyse entries [namendo×namlagendo]
	<b>:</b>	jolly character to indicate ALL endogenous
namexo	()	list of exogenous variables:
		analyse entries [namendo×namexo]
	:	jolly character to indicate ALL exogenous

One can also load a previously estimated mapping with a new MC sample, to look at the forecast for the new MC sample.

#### 3.4 Mapping the fit

The RMSE analysis can be performed with different types of sampling options:

- 1. when pprior=1 and ppost=0, the Toolbox analyses the RMSE's for the MC sample obtained by sampling parameters from their prior distributions (or prior ranges): this analysis provides some hints about what parameter drives the fit of which observed series, prior to the full estimation;
- 2. when pprior=0 and ppost=0, the Toolbox analyses the RMSE's for a multivariate normal MC sample, with covariance matrix based on the inverse Hessian at the optimum: this analysis is useful when ML estimation is done (i.e. no Bayesian estimation);
- 3. when ppost=1 the Toolbox analyses the RMSE's for the posterior sample obtained by Dynare's Metropolis procedure.

The use of cases 2. and 3. require an estimation step beforehand! To facilitate the sensitivity analysis after estimation, the sensitivity command also allows to indicate some options of estimation. These are:

- datafile
- diffuse\_filter
- mode\_file
- first\_obs
- lik\_init
- nobs
- prefilter
- presample
- loglinear

option name	default	description
rmse	0	0 = no RMSE analysis
		1 = do RMSE analysis
load_rmse	0	0 = make a new RMSE analysis
		1 = load previous RMSE analysis
lik_only	0	0 = compute RMSE's for all observed series
		1 = compute only likelihood and posterior
var_rmse	varobs	list of observed series to be considered
pfilt_rmse	0.1	filtering threshold for RMSE's: default it to
		filter the best 10% for each observed series
istart_rmse	1	start computing RMSE's from istart_rmse:
		use 2 to avoid big initial error
alpha_rmse	0.001	p-value for Smirnov statistics $d$ :
		plot parameters with p-value <alpha_rmse< td=""></alpha_rmse<>
alpha2_rmse	0	p-value for correlation $\rho$
_		plot couples of parameters with p-value <alpha2_rmse< td=""></alpha2_rmse<>

#### 3.5 Screening analysis

The screening analysis does not require any additional options with respect to those listed in the 'Sampling options': morris, morris\_nliv, morris\_ntra. The Toolbox performs all the analyses required and displays results.

### 3.6 Identification analysis

Setting the option identification=1, an identification analysis based on theoretical moments is performed. Sensitivity plots are provided that allow to infer which parameters are most likely to be less identifiable.

option name	default	description
identification	0	0 = no identification analysis
		1 = performs identification analysis:
		this forces redform=0 and default morris=1
morris	1	1 = Screening analysis (Type II error)
		2 = Analytic derivatives (Iskrev, 2010, 2011)
morris_nliv	6	number of levels in Morris design
morris_ntra	20	number of trajectories in Morris design

For example, the following commands in the Dynare model file

```
sensitivity(identification=1, morris=2);
```

trigger the identification analysis using Iskrev (2010, 2011), jointly with the mapping of the acceptable region.

#### 4 Directory structure

Sensitivity analysis results are saved on the hard-disk of the computer. The Toolbox uses a dedicated folder called GSA, located in

<Dynare\_file>\GSA,

where <Dynare\_file>.mod is the name of the Dynare model file.

#### 4.1 Binary data files

A set of binary data files is saved in the GSA folder:

- <Dynare\_file>\_prior.mat: this file stores information about the analyses
   performed sampling from the prior ranges, i.e. pprior=1 and ppost=0;
- <Dynare\_file>\_mc.mat: this file stores information about the analyses performed sampling from multivariate normal, i.e. pprior=0 and ppost=0;
- <Dynare\_file>\_post.mat: this file stores information about analyses performed using the Metropolis posterior sample, i.e. ppost=1.
- <Dynare\_file>\_prior\_\*.mat: these files store the filtered and smoothed
   variables for the prior MC sample, generated when doing RMSE anal ysis (pprior=1 and ppost=0);
- <Dynare\_file>\_mc\_\*.mat: these files store the filtered and smoothed variables for the multivariate normal MC sample, generated when doing
  RMSE analysis (pprior=0 and ppost=0).

#### 4.2 Stability analysis

Figure files <Dynare\_file>\_prior\_\*.fig store results for the stability mapping from prior MC samples:

- <Dynare\_file>\_prior\_stab\_SA\_\*.fig: plots of the Smirnov test analyses
   confronting the CDF of the sample fulfilling Blanchard-Kahn conditions
   with the CDF of the rest of the sample;
- <Dynare\_file>\_prior\_stab\_indet\_SA\_\*.fig: plots of the Smirnov test
   analyses confronting the CDF of the sample producing indeterminacy
   with the CDF of the original prior sample;

- <Dynare\_file>\_prior\_stab\_unst\_SA\_\*.fig: plots of the Smirnov test analyses confronting the CDF of the sample producing unstable (explosive roots) behaviour with the CDF of the original prior sample;
- <Dynare\_file>\_prior\_stable\_corr\_\*.fig: plots of bivariate projections
   of the sample fulfilling Blanchard-Kahn conditions;
- <Dynare\_file>\_prior\_indeterm\_corr\_\*.fig: plots of bivariate projections of the sample producing indeterminacy;
- <Dynare\_file>\_prior\_unstable\_corr\_\*.fig: plots of bivariate projections of the sample producing instability;
- <Dynare\_file>\_prior\_unacceptable\_corr\_\*.fig: plots of bivariate projections of the sample producing unacceptable solutions, i.e. either
  instability or indeterminacy or the solution could not be found (e.g.
  the steady state solution could not be found by the solver).

Similar conventions apply for <Dynare\_file>\_mc\_\*.fig files, obtained when samples from multivariate normal are used.

#### 4.3 RMSE analysis

Figure files <Dynare\_file>\_rmse\_\*.fig store results for the RMSE analysis.

- <Dynare\_file>\_rmse\_mc\*.fig: save results for the analysis using multivariate normal MC samples;
- <Dynare\_file>\_rmse\_post\*.fig: save results for the analysis using Metropolis posterior samples.

The following types of figures are saved (we show prior sample to fix ideas, but the same conventions are used for multivariate normal and posterior):

- <Dynare\_file>\_rmse\_prior\_\*.fig: for each parameter, plots the CDF's
   corresponding to the best 10% RMES's of each observed series;
- <Dynare\_file>\_rmse\_prior\_dens\_\*.fig: for each parameter, plots the
   pdf's corresponding to the best 10% RMES's of each observed series;
- <Dynare\_file>\_rmse\_prior\_<name of observedseries>\_corr\_\*.fig: for
  each observed series plots the bi-dimensional projections of samples
  with the best 10% RMSE's, when the correlation is significant;

- <Dynare\_file>\_rmse\_prior\_lnlik\*.fig: for each observed series, plots in red the CDF of the log-likelihood corresponding to the best 10% RMSE's, in green the CDF of the rest of the sample and in blue the CDF of the full sample; this allows to see the presence of some idiosyncratic behaviour;
- <Dynare\_file>\_rmse\_prior\_lnpost\*.fig: for each observed series, plots
   in red the CDF of the log-posterior corresponding to the best 10%
   RMSE's, in green the CDF of the rest of the sample and in blue the
   CDF of the full sample; this allows to see idiosyncratic behaviour;
- <Dynare\_file>\_rmse\_prior\_lnprior\*.fig: for each observed series, plots
   in red the CDF of the log-prior corresponding to the best 10% RMSE's,
   in green the CDF of the rest of the sample and in blue the CDF of the
   full sample; this allows to see idiosyncratic behaviour;
- <Dynare\_file>\_rmse\_prior\_lik\_SA\_\*.fig: when lik\_only=1, this shows
  the Smirnov tests for the filtering of the best 10% log-likelihood values;
- <Dynare\_file>\_rmse\_prior\_post\_SA\_\*.fig: when lik\_only=1, this shows
  the Smirnov test for the filtering of the best 10% log-posterior values.

#### 4.4 Reduced form mapping

In the case of the mapping of the reduced form solution, synthetic figures are saved in the \GSA folder:

- <Dynare\_file>\_redform\_<endo name>\_vs\_lags\_\*.fig: shows bar charts
   of the sensitivity indices for the ten most important parameters driv ing the reduced form coefficients of the selected endogenous variables
   (namendo) versus lagged endogenous variables (namlagendo); suffix log
   indicates the results for log-transformed entries;
- <Dynare\_file>\_redform\_<endo name>\_vs\_shocks\_\*.fig: shows bar charts
   of the sensitivity indices for the ten most important parameters driv ing the reduced form coefficients of the selected endogenous variables
   (namendo) versus exogenous variables (namexo); suffix log indicates the
   results for log-transformed entries;
- <Dynare\_file>\_redform\_GSA(\_log).fig: shows bar chart of all sensitivity indices for each parameter: this allows to notice parameters that
  have a minor effect for any of the reduced form coefficients,

Detailed results of the analyses are shown in the subfolder \GSA\redform\_stab, where the detailed results of the estimation of the single functional relationships between parameters  $\theta$  and reduced form coefficient are stored in separate directories named as:

<namendo>\_vs\_<namlagendo>: for the entries of the transition matrix;

<namendo>\_vs\_<namexo>: for entries of the matrix of the shocks.

Moreover, analyses for log-transformed entries are denoted with the following suffixes (y denotes the generic reduced form coefficient):

```
log: y^* = \log(y);
minuslog: y^* = \log(-y);
logsquared: y^* = \log(y^2) for symmetric fat tails;
logskew: y^* = \log(|y + \lambda|) for asymmetric fat tails.
```

The optimal type of transformation is automatically selected without the need of any user's intervention.

#### 4.5 Screening analysis

The results of the screening analysis with Morris sampling design are stored in the subfolder \GSA\SCREEN. The data file <Dynare\_file>\_prior stores all the information of the analysis (Morris sample, reduced form coefficients, etc.).

Screening analysis merely concerns reduced form coefficients. Similar synthetic bar charts as for the reduced form analysis with MC samples are saved:

- <Dynare\_file>\_redform\_<endo name>\_vs\_lags\_\*.fig: shows bar charts
   of the elementary effect tests for the ten most important parameters
   driving the reduced form coefficients of the selected endogenous variables (namendo) versus lagged endogenous variables (namlagendo);
- <Dynare\_file>\_redform\_<endo name>\_vs\_shocks\_\*.fig: shows bar charts
   of the elementary effect tests for the ten most important parameters
   driving the reduced form coefficients of the selected endogenous variables (namendo) versus exogenous variables (namexo);
- <Dynare\_file>\_redform\_screen.fig: shows bar chart of all elementary
   effect tests for each parameter: this allows to identify parameters that
   have a minor effect for any of the reduced form coefficients.

### References

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