

# From logistic regression to neural networks

Binary classification problems

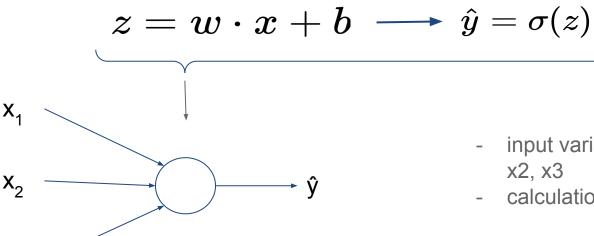
Filippo Biscarini Senior Scientist CNR, Milan (Italy) Nelson Nazzicari Research fellow CREA, Lodi (Italy)











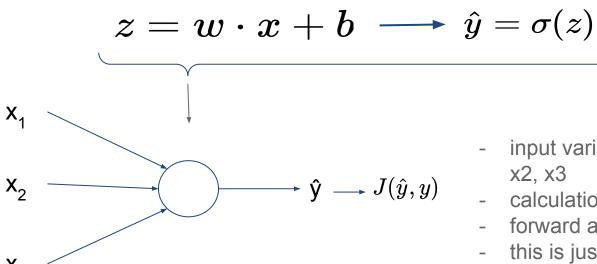
- input variables (features): x1,
  x2, x3
- calculations in the unit/neuron











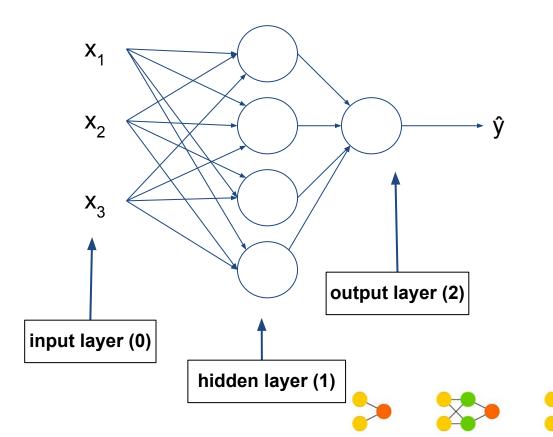
- input variables (features): x1,
  x2, x3
- calculations in the unit/neuron
- forward and back propagation
- this is just one single neuron!





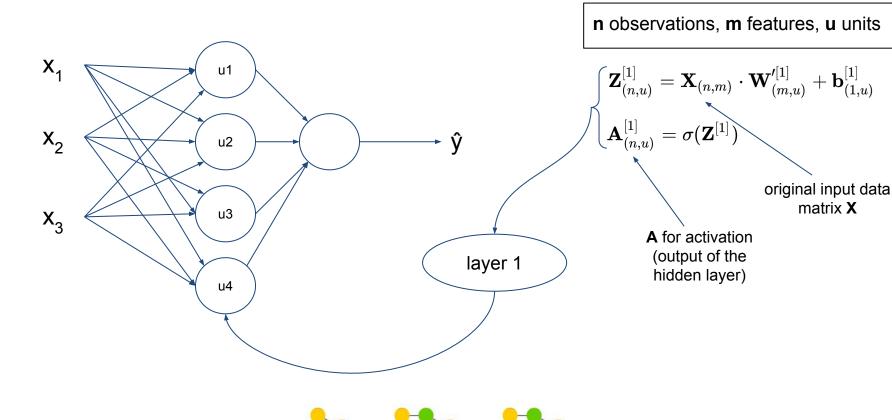




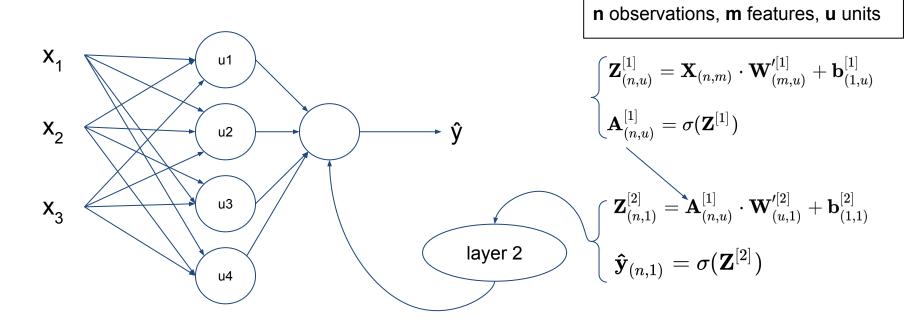


- <u>two layers</u>:
  - 1 hidden layer, 4 nodes
  - 1 output layer, 1 node
- logistic regression is performed in each node
- each node in the hidden layer receives all input variables
- the node in the output layer receives all outputs (activations) from the hidden layer nodes















#### Take away messages



- You can build a neural network (NN) for binary classification
- NNs are logistic regression repeated several times! → n. of nodes/units, n. of layers
- probably a bit of an overkill to use NNs in place of a simple logistic regression model → used for illustration
- however, when you have many observations and many features (big data), NN will do the job









## Let's go deep

### From NNs to deep learning

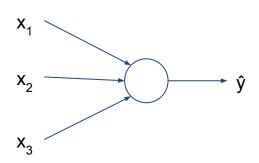
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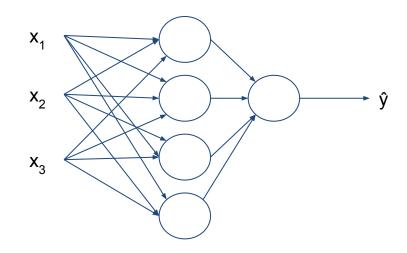








logistic regression (1 layer)



shallow NN (2 layers)

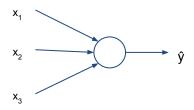


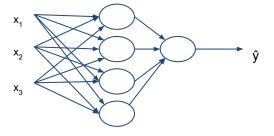






- we had a (cursory) look at the calculations involved in neural networks models
- Lots of details, but it's not a black box!













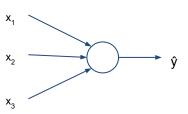
- we had a (cursory) look at the calculations involved in neural networks models
- Lots of details, but it's not a black box!
- however, when you go deep (more layers), the magic gets back in the play!

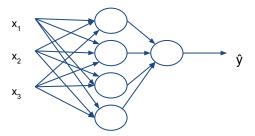


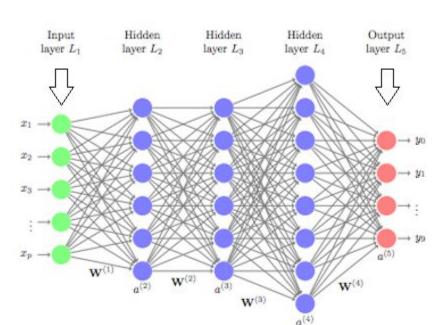
















- 4 layers ("deep" NN)
- n. of layers in a deep learning model: hyperparameter to tune (one of many)

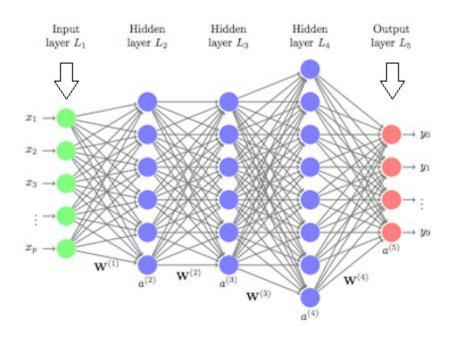






#### Layers matter!





Source: University of Cincinnati

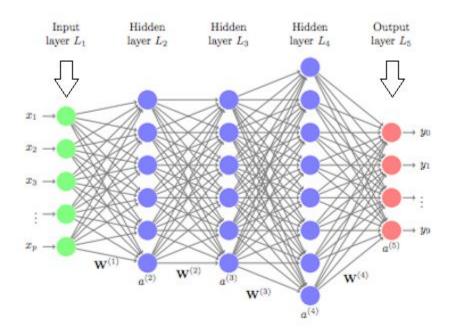
- 4 layers ("deep" NN)
- n. of layers in a deep learning model: hyperparameter to tune (one of many)
- research in the Al/machine learning communities has shown that there are functions that deep NN can learn which can not be learnt by shallower models







#### Forward propagation



Source: University of Cincinnati



- L: n. of layers (l in 1 to L)
- X: matrix of input features  $\rightarrow$   $A^{[0]}$

$$egin{aligned} \mathbf{Z}^{[l]} &= \mathbf{A}^{[l-1]} \cdot \mathbf{W}'^{[l]} + \mathbf{b}^{[l]} \ \mathbf{A}^{[l]} &= g^{[l]}(\mathbf{Z}^{[l]}) \end{aligned}$$

- for each layer
- iterate over n. of layers (unavoidable for loop)







#### **Compositional representation**

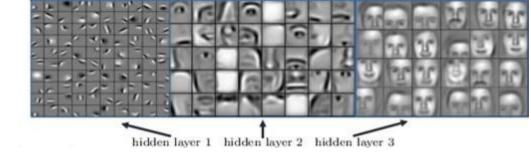


- why do deep NNs work better?
- each layer focuses on one representation of the data
- representations are then combined to get the final result → compositional representation

#### Simplified example from face recognition:

- Layer 1 → edges
- Layer 2 → pieces of faces
- Layer 3 → pieces











#### **Compositional representation**



- works also with other types of data
- e.g. speech recognition: i) high/low soundwaves; ii) combinations of soundwaves into phonemes; iii) combination of phonemes into words; iv) from words to sentences
- relatively simple functions of the input data in the first layers → progressively more complex functions of the data in the later layers







#### **Depth vs width**



- deep learning works by stacking together multiple (many) hidden layers with relatively few nodes
- alternatively, one could use a shallow but very wide (many nodes) neural network
- depth is more efficient than width: shallow NN require exponentially more hidden units (nodes) compared to deep NN:
  - e.g.: XOR of x features (x<sub>1</sub> XOR x<sub>2</sub> XOR ... XOR x<sub>n</sub>)
  - deep NN → O(log(n))
  - wide  $NN \rightarrow O(2^n)$







#### **Hyperparameters**



- we saw that there are many ingredients that make up a deep learning model (and many still yet to come) → deep learning has many hyperparameters:
  - learning rate α
  - n. of hidden layers
  - n. of nodes (total, each layer)
  - activation function
  - and many more (mini-batch size, NN architecture, regularization etc.)
- to be fine-tuned (→ cross-validation)







#### **Neural networks models**



- demonstration 04b

→ code\_04b\_keras\_shallow\_neural\_networks.ipynb





