

Multiclass classification with neural networks

Softmax regression

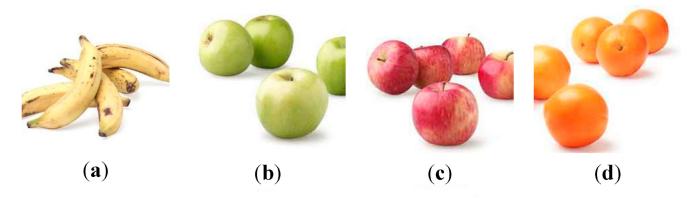
Filippo Biscarini Senior Scientist CNR, Milan (Italy) Nelson Nazzicari Research fellow CREA, Lodi (Italy)











From: Wang et al., 2015 (Entropy)

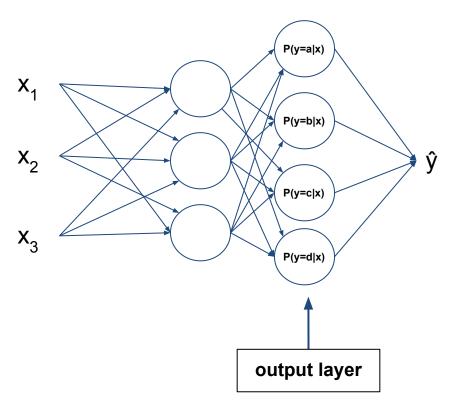
- **more than two classes** to recognize
- in this case, 4 classes: bananas, green apples, red apples, oranges
- need to extend logistic regression to estimating the probabilities of samples to belong to each of the four classes











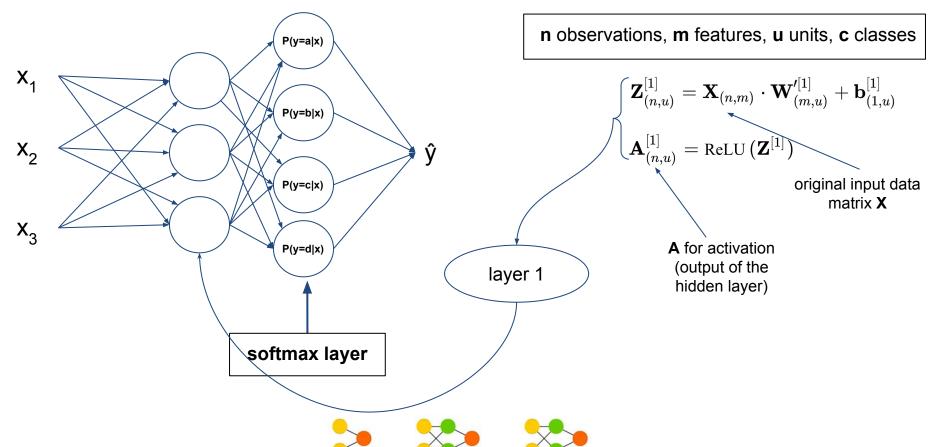
- the output layer has now 4 nodes (instead of just one as in binary classification)
- the activation function is now the softmax function
- this is why the output layer is also called the softmax layer, and multiclass classification is called softmax regression



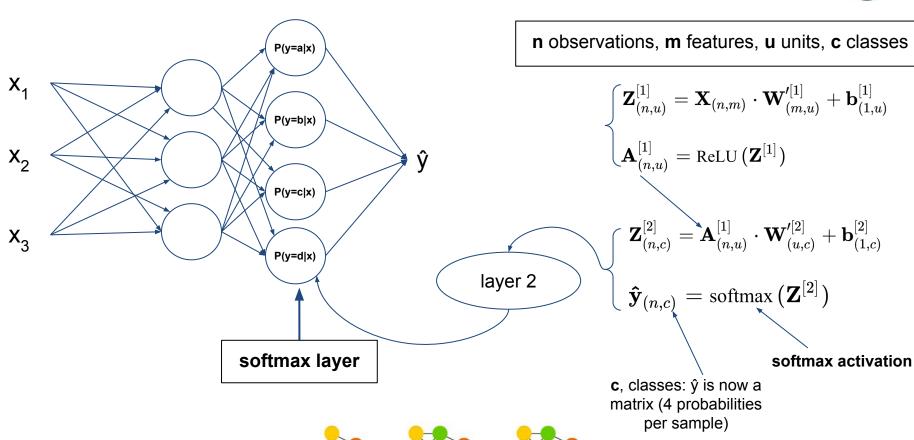




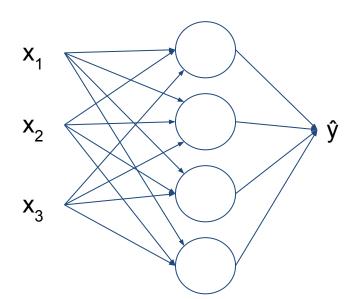












- as we did for binary classification, we can also represent softmax regression with no hidden layers
- this would essentially reduce to multinomial logistic regression, with no neural networks involved
- we'll see this implementation in the ipynb file
 4c, part 1







Loss function for softmax regression



$$L(\hat{y},y) = -\left(y \cdot \log\left(\hat{y}
ight) + (1-y) \cdot \log\left(1-\hat{y}
ight)
ight) ullet$$

loss function for logistic regression

$$L(\hat{y},y) = -\sum_{j=1}^{c} y_j \cdot \log\left(\hat{y_j}
ight)$$
 — loss function for softmax regression

- generalization of the loss function for logistic regression over c classes
- you then sum up the loss for each sample and divide by the number of samples →
 cost function for the entire dataset







Loss function for softmax regression



$$L(\hat{y},y) = -\left(y \cdot \log\left(\hat{y}
ight) + (1-y) \cdot \log\left(1-\hat{y}
ight)
ight) leftarrow 0$$

loss function for logistic regression

$$L(\hat{\mathbf{y}},\mathbf{y}) = -\sum_{j=1}^{c} y_j \cdot \log\left(\hat{y_j}
ight)$$
 —

loss function for softmax regression

these are actually vectors of length c (number of classes)!









- demonstration 04c
- exercise 04c.1 (multiclass logistic regression)

→ code_04c_keras_multiclass_classification.ipynb







Neural networks models: recap



- exercise 04d.1 (write your own code)

→ code_04d_neural_networks_exercise.ipynb





