

→ Linked - List

↳ linear data structure where elements (called nodes) are stored in non-contiguous memory location.

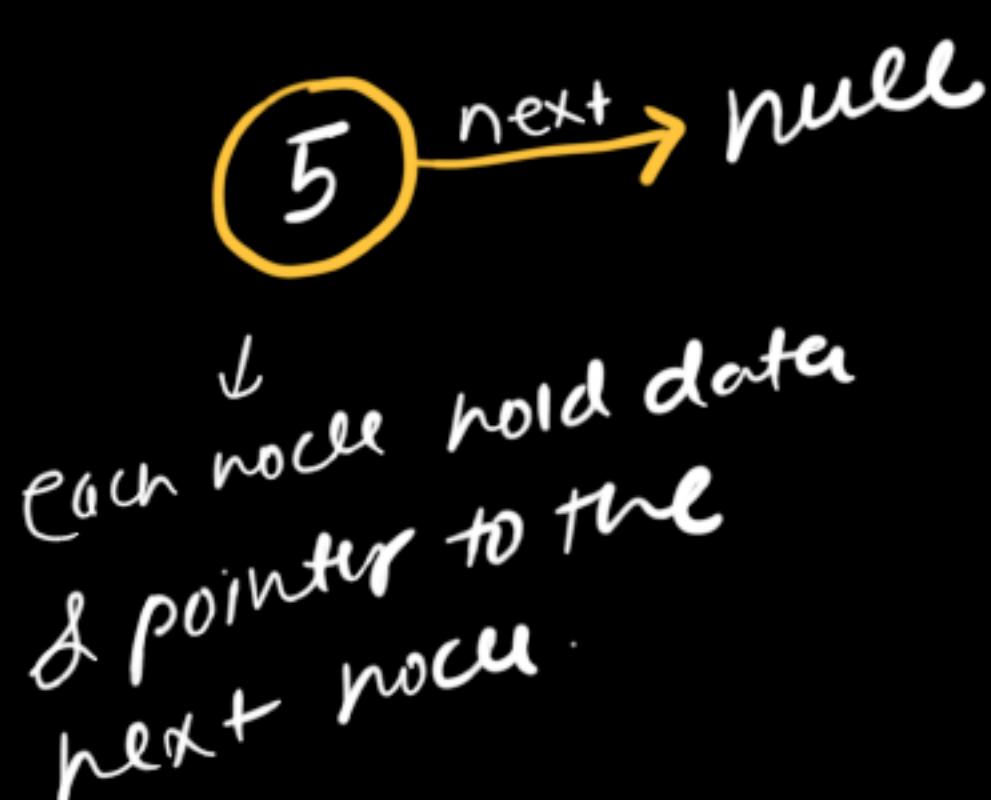
↳ Each Node contains :-

- ① Data → the value stored in the node
- ② Pointer (next) → a reference to the next node in the sequence.

→ Types of linked list :-

- ① Singly - LL : Node points to the next node only
- ② Doubly - LL : Nodes have pointers to both the next & previous node.
- ③ Circular - LL : The last node points back to the first node, can be singly or doubly.

→ Node - Structure



```
public class Node<T> {  
    public T data;  
    public Node<T> next;  
    Node(T data) {  
        this.data = data;  
        this.next = null;  
    }  
}
```

→ Time & space complexity

Insertion

- ↳ • addFirst
- addLast

with Head

$O(1)$

$O(N)$

with Tail

$O(1)$

$O(1)$

Deletion

- ↳ • deleteFirst
- deleteLast

$O(1)$

$O(N)$

$O(1)$

$O(N)$

$O(N)$

Searching / Traversing

$O(N)$

Insertion / deletion at

$O(N)$

$O(N)$

Index

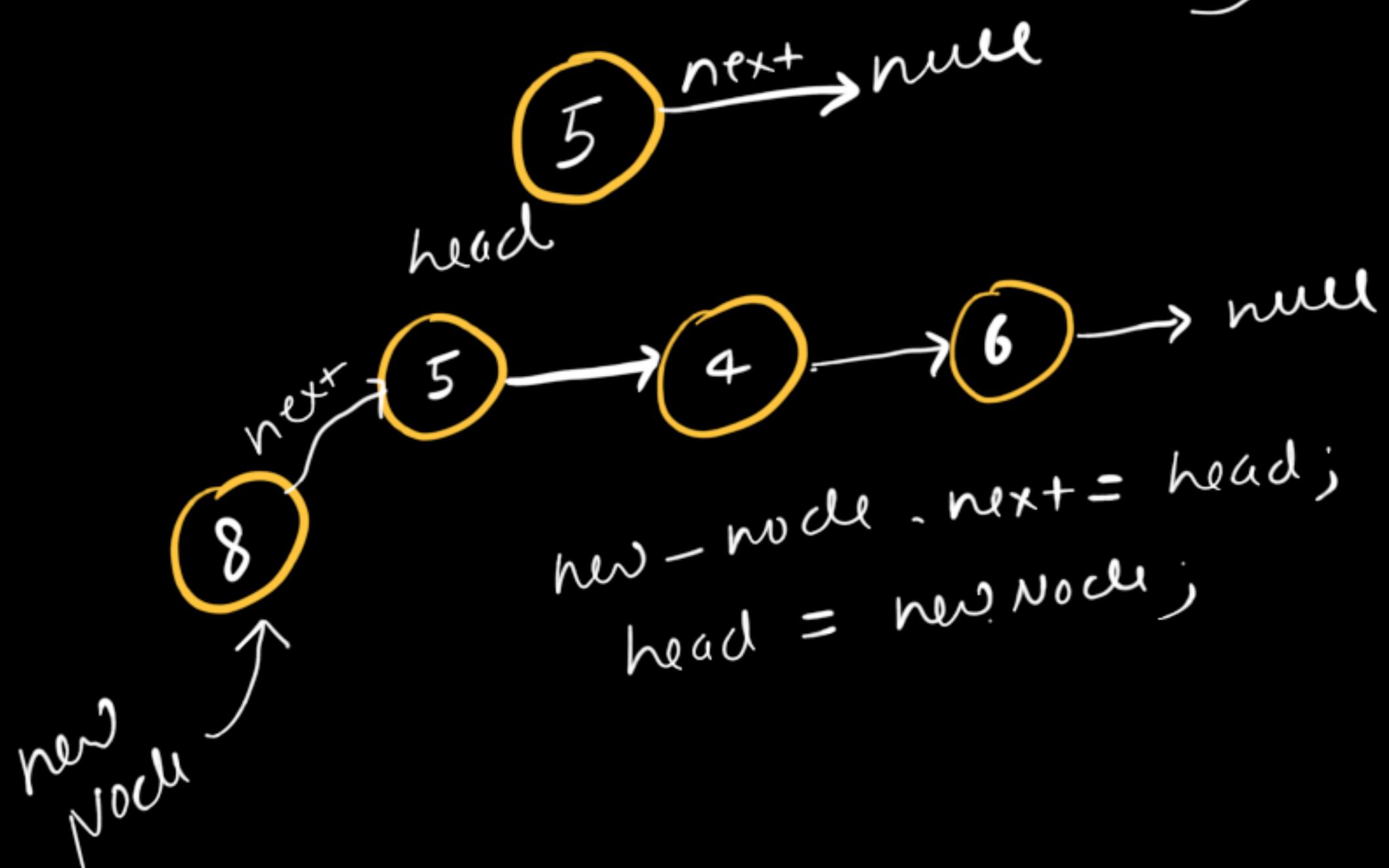
Space - complexity: $O(1)$

```
LLNode.java  
public class LLNode<T> { 8 usages new *  
    public T value;  
    public LLNode<T> next; 6 usages  
  
    public LLNode() { no usages new *  
    }  
  
    public LLNode(T value) { 3 usages new *  
        this.value = value;  
        this.next = null;  
    }  
  
    public LLNode(T value, LLNode<T> next) { no  
        this.value = value;  
        this.next = next;  
    }  
  
    public T getValue() { return value; }  
  
    public LLNode<T> getHead() { return next; }  
}
```

→ Inserion

• add First

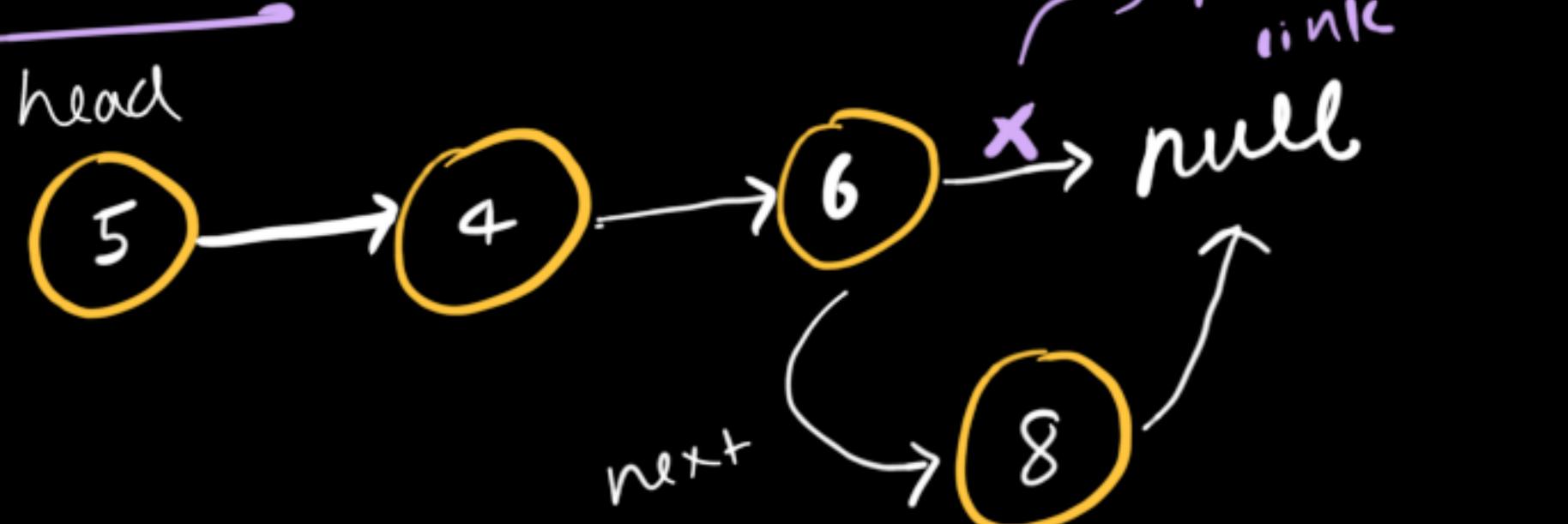
↳ Initially head is null



```
if (head == null) {  
    head = new Node(5);  
    return;  
}
```

```
LinkedList.java  
public void addFirst(T value) { 1 usage  ne  
    if (head == null) {  
        head = new LLNode<T>(value);  
        return;  
    }  
  
    LLNode<T> node = new LLNode<T>(value);  
    node.next = head;  
    head = node;  
}
```

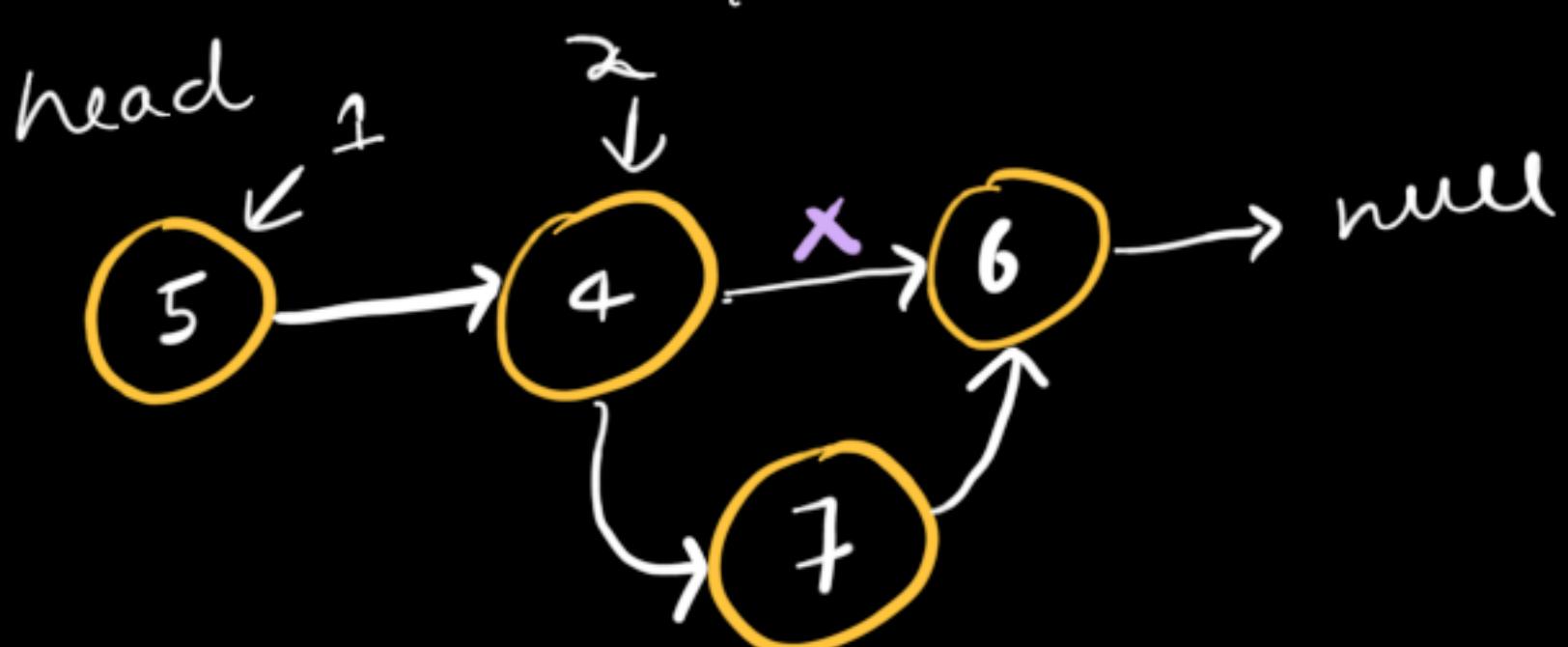
• add Last



• Traverse to the last node then,
last-node.next = new-node;

→ Insertion at index

index = 3, value = 7



• Traverse till index - 1

↳ Front-node = prev-node.next;
prev-node.next = new-node;
new-node.next = front-node;

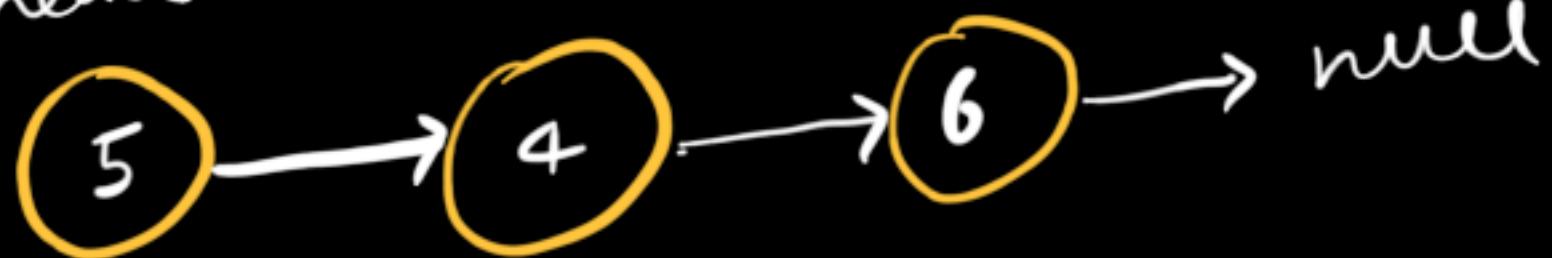
```
LinkedList.java  
public void addLast(T value) { 2 usagi  
    if (head == null) {  
        addFirst(value);  
        size++;  
        return;  
    }  
  
    LLNode<T> temp = head;  
    while (temp.next != null) {  
        temp = temp.next;  
    }  
    temp.next = new LLNode<T>(value);  
    size++;  
}
```

```
LinkedList.java  
public void insertAtIndex(int index, T value) {  
    if (index == 0) {  
        addFirst(value);  
        return;  
    }  
  
    if (index == this.size) {  
        addLast(value);  
        return;  
    }  
  
    LLNode<T> temp = head;  
    for (int i = 1; i < index; i++) {  
        temp = temp.next;  
    }  
  
    LLNode<T> front = temp.next;  
    LLNode<T> node = new LLNode<T>(value);  
    temp.next = node;  
    node.next = front;  
    size++;  
}
```

→ Deletion

- deleteFirst

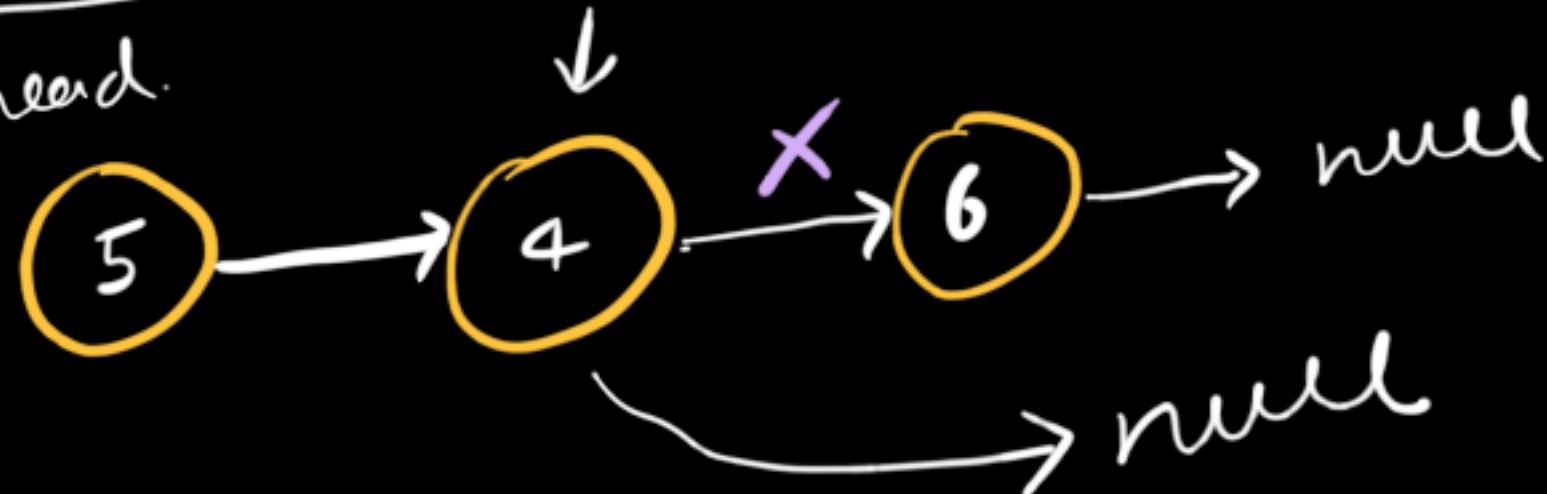
head



↳ $\text{head} = \text{head}.\text{next}$

- deleteLast

head



Traverse to second last node

↳ while ($\text{temp}.\text{next}.\text{next} \neq \text{null}$)

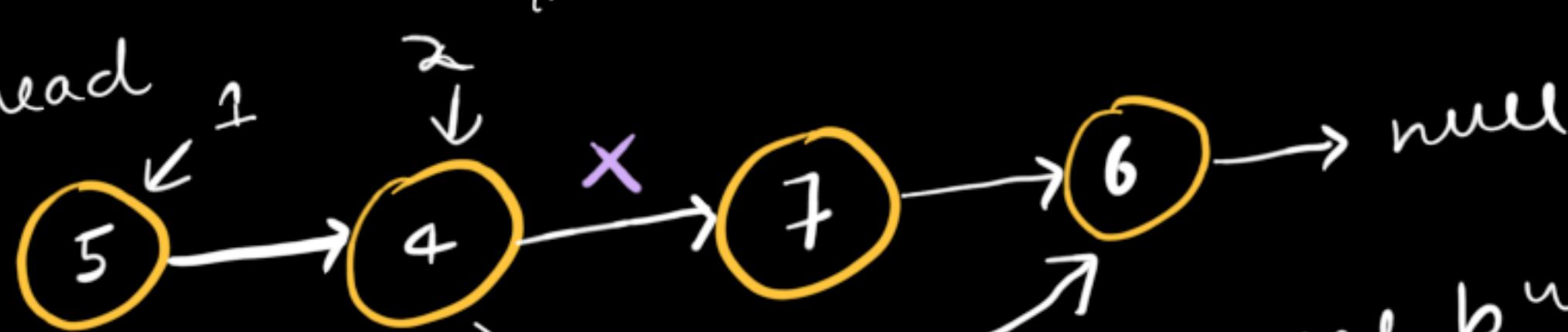
↳ + traverse

Second - Last - node. $\text{next} = \text{null}$,

→ deletion at index

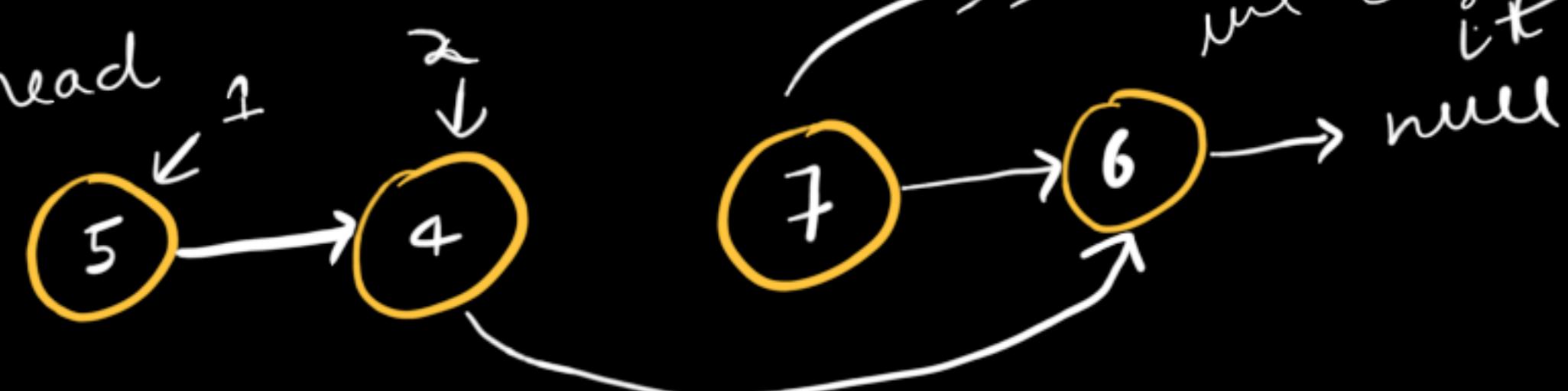
index = 3; value = 7

head



still there but
we cannot reach
it

head



- Traverse till index - 1

↳ Front-node = $\text{prev-node}.\text{next}$,
 $\text{del} = \text{prev-node}.\text{next}$,
 $\text{prev-node}.\text{next} = \text{null}$,
 return del ,

```

● ● ● LinkedList.java
public LLNode<T> deleteFirst() { 2 usages new
    if (head == null) {
        return null;
    }

    LLNode<T> temp = head;
    head = head.next;
    size--;
    return temp;
}

public LLNode<T> deleteLast() { 3 usages new
    if (head == null) {
        return null;
    }

    LLNode<T> temp = head;

    while (temp.next.next != null) {
        temp = temp.next;
    }

    LLNode<T> del = temp.next;
    temp.next = null;
    size--;
    return del;
}

public LLNode<T> deleteAtIndex(int index) {
    if (index == 0) {
        return deleteFirst();
    }

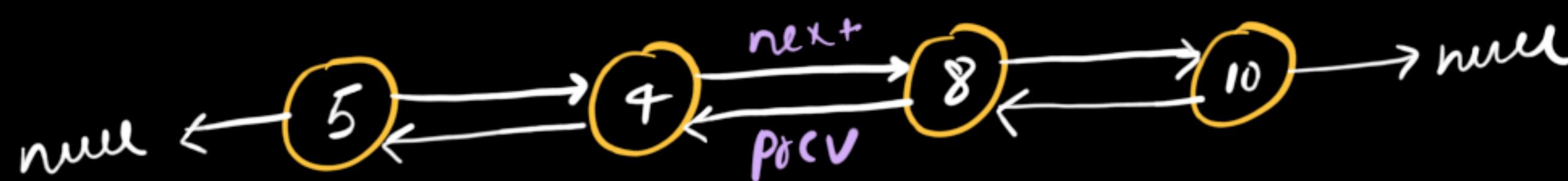
    if (index == this.size) {
        return deleteLast();
    }

    LLNode<T> temp = head;
    for (int i = 1; i < index; i++) {
        temp = temp.next;
    }

    LLNode<T> front = temp.next.next;
    LLNode<T> del = temp.next;
    temp.next = front;
    size--;
    return del;
}

```

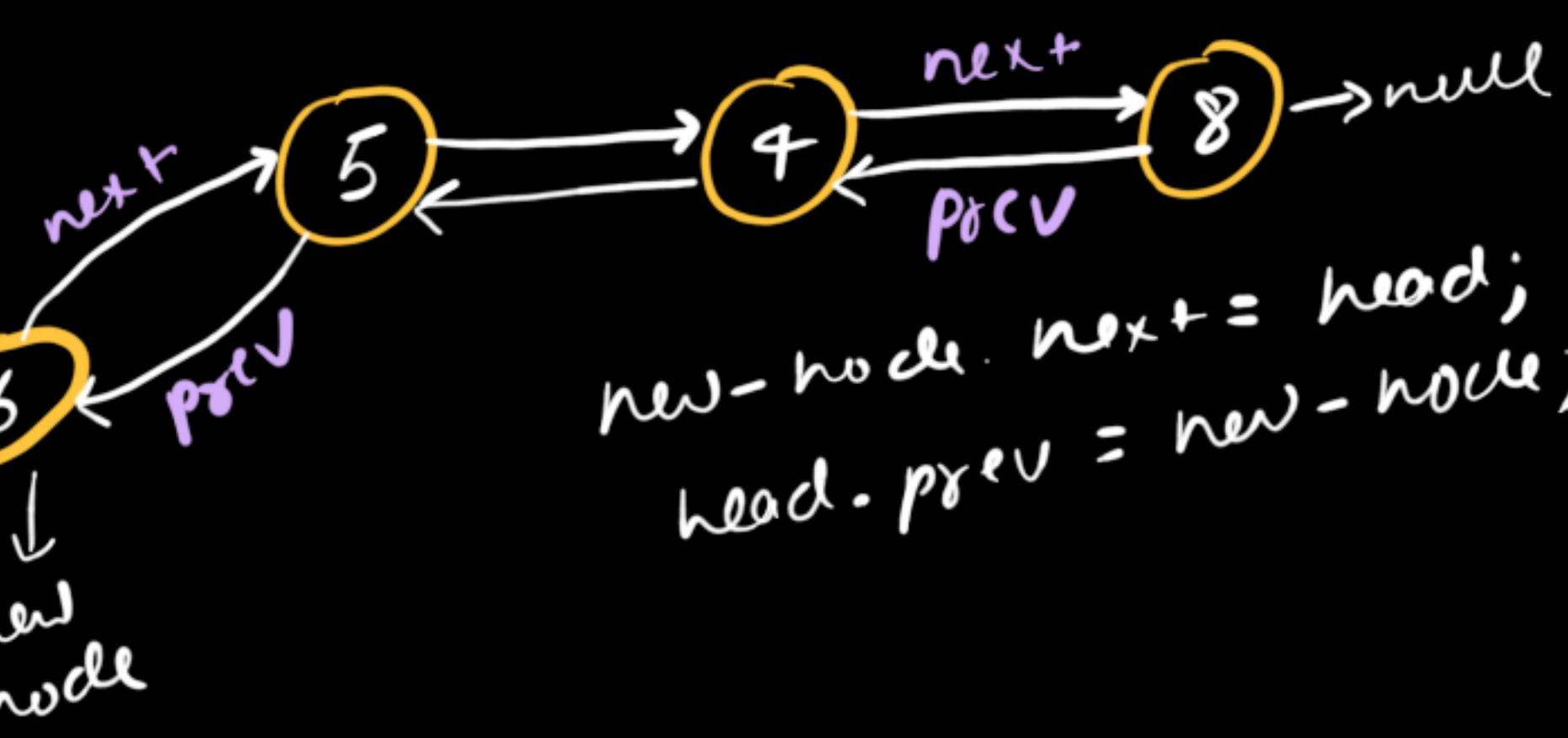
→ Doubly Linked List



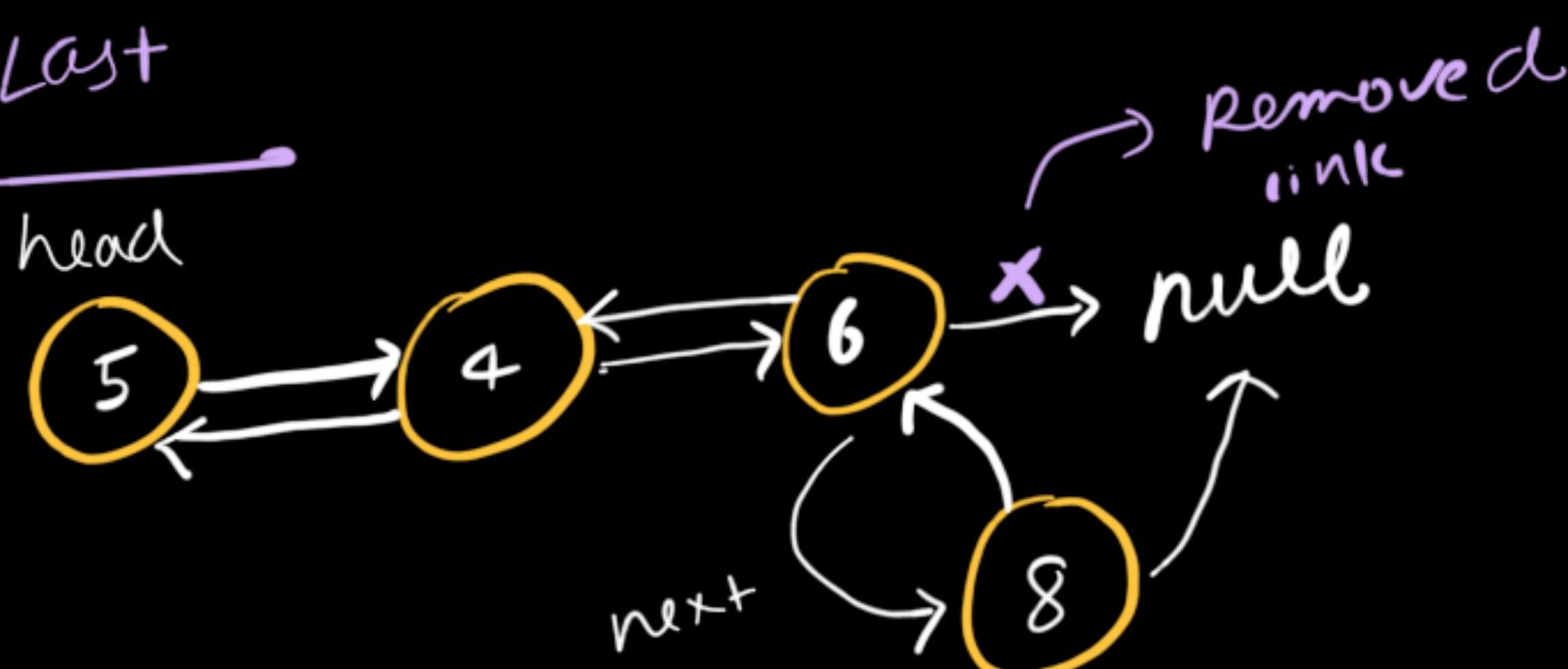
→ Insertion

• addFirst

↳ head is null initially.



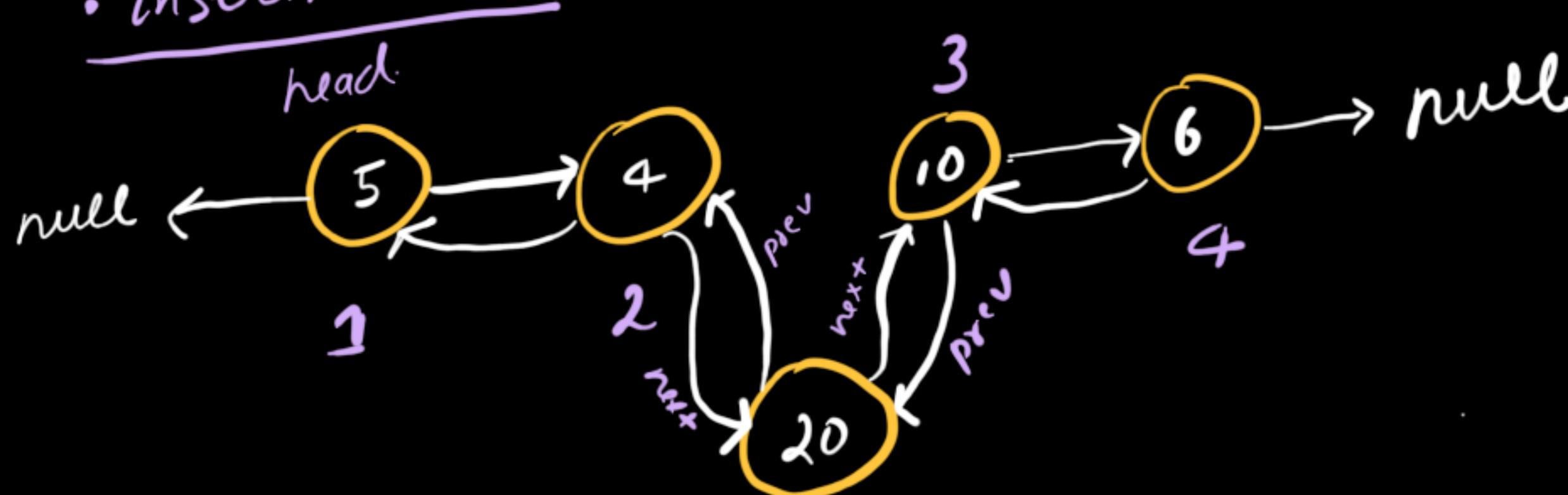
• addLast



• Traverse to the last Node then

last-node.next = new-node;
new-node.prev = last-node;

• insertAtIndex



front = temp.next;
new-node.next = front;
front.prev = new-node;
temp.next = new-node;
new-node.prev = temp;

```

●●● DoublyLinkedList.java
public void addFirst(T value) { 6 usages new *
    if (head == null) {
        head = new DLLNode<T>(value);
        size++;
        return;
    }

    DLLNode<T> temp = head;
    DLLNode<T> node = new DLLNode<>(value);
    node.next = temp;
    temp.prev = node;
    head = node;
    size++;
}

public void addLast(T value) { 3 usages new *
    if (head == null) {
        addFirst(value);
        return;
    }

    DLLNode<T> temp = head;
    while (temp.next != null) {
        temp = temp.next;
    }

    DLLNode<T> node = new DLLNode<>(value);
    temp.next = node;
    node.prev = temp;
    size++;
}

public void insertAtIndex(int index, T value) {
    if (index < 0 || index > size) return;
    if (index == 0) {
        addFirst(value);
        return;
    }

    if (index == this.size) {
        addLast(value);
        return;
    }

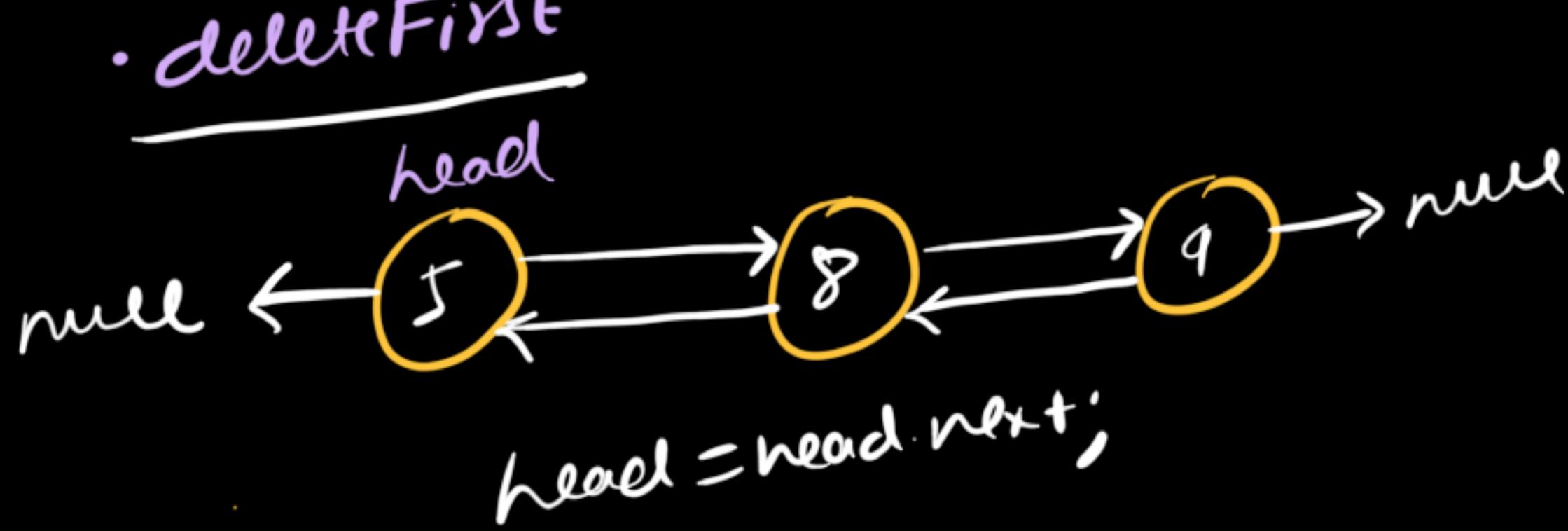
    DLLNode<T> temp = head;
    for (int i = 0; i < index - 1; i++) {
        temp = temp.next;
    }

    DLLNode<T> front = temp.next;
    DLLNode<T> node = new DLLNode<>(value);
    node.next = front;
    front.prev = node;
    temp.next = node;
    node.prev = temp;
    size++;
}

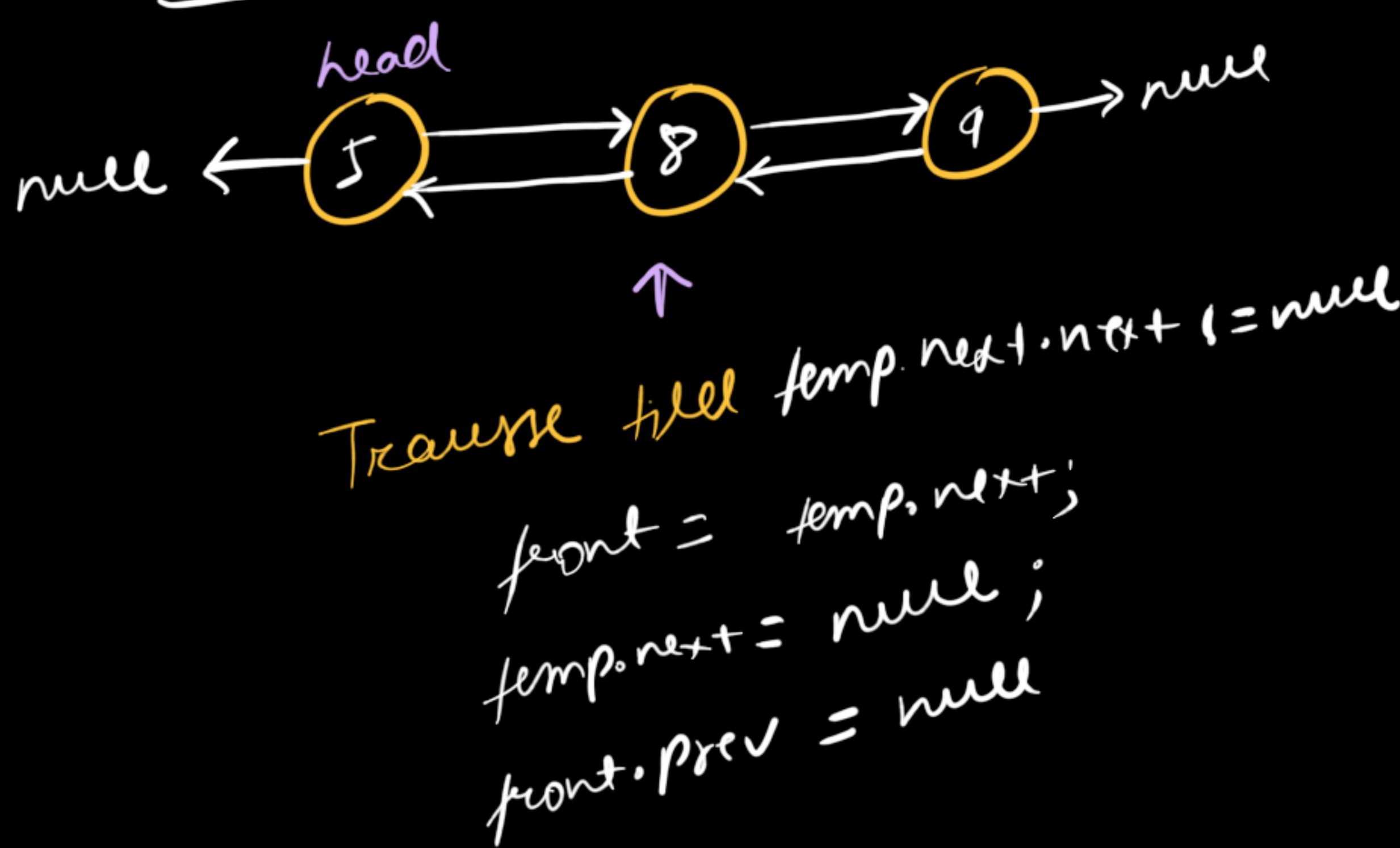
```

→ Deletion

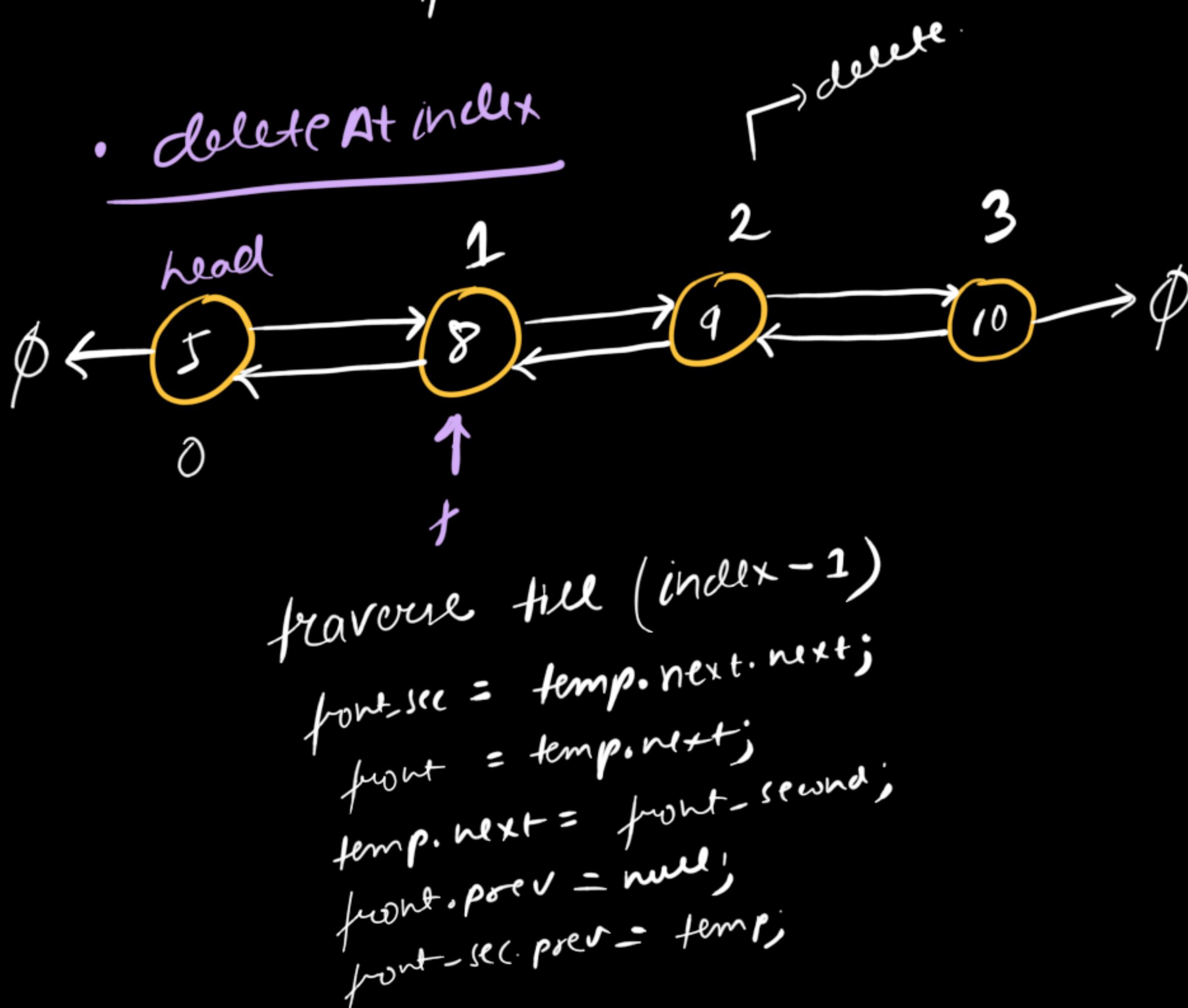
• deleteFirst



• deleteLast



• deleteAtIndex



```
DoublyLinkedList.java
public DLLNode<T> deleteFirst() { 2 usages new *
    if (head == null) return null;

    DLLNode<T> temp = head;
    head = head.next;

    if (head != null) head.prev = null;

    temp.next = null;
    size--;
    return temp;
}

public DLLNode<T> deleteLast() { 2 usages new *
    if (head == null) return null;

    if (head.next == null) {
        DLLNode<T> temp = head;
        head = null;
        size--;
        return temp;
    }

    DLLNode<T> temp = head;
    while (temp.next.next != null) {
        temp = temp.next;
    }

    DLLNode<T> del = temp.next;
    temp.next = null;
    del.prev = null;

    size--;
    return del;
}

public DLLNode<T> deleteAtIndex(int index) { 1 u
    if (index < 0 || index >= size) return null;

    if (index == 0) return deleteFirst();
    if (index == size - 1) return deleteLast();

    DLLNode<T> temp = head;
    for (int i = 0; i < index - 1; i++) {
        temp = temp.next;
    }

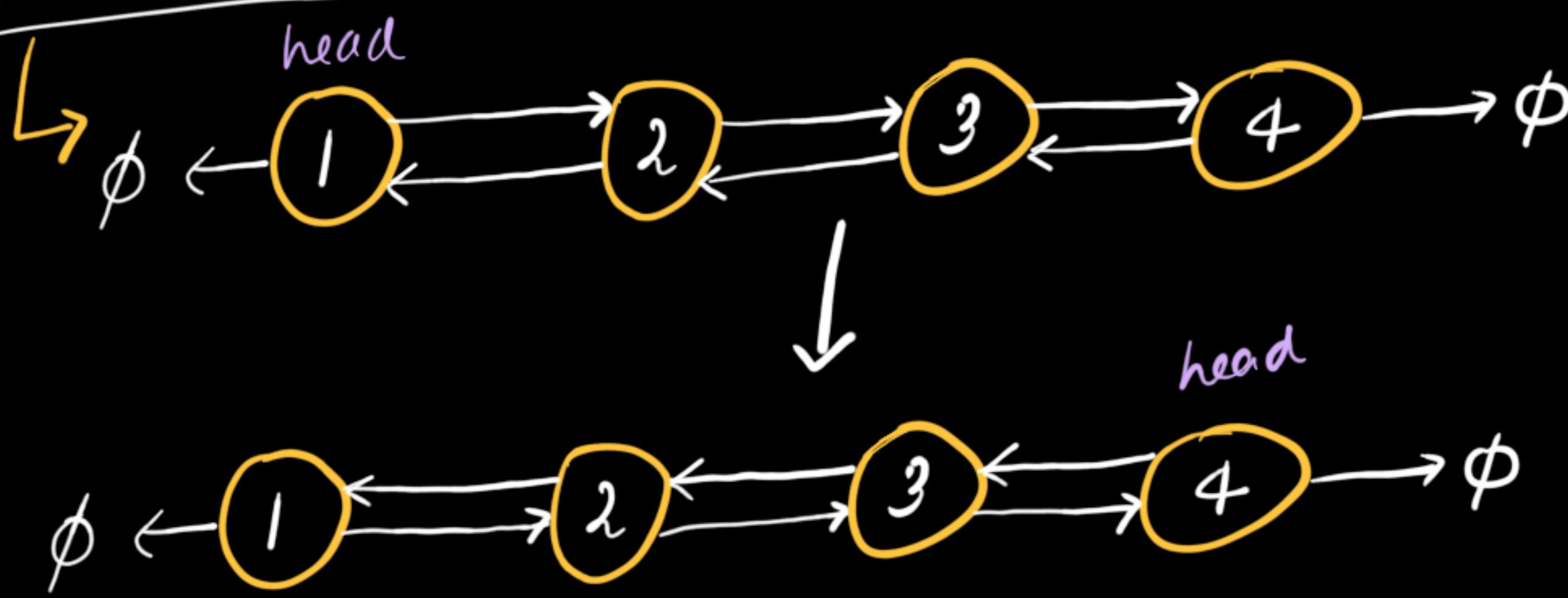
    DLLNode<T> del = temp.next;
    DLLNode<T> front = del.next;

    temp.next = front;
    if (front != null) front.prev = temp;

    del.prev = null;
    del.next = null;

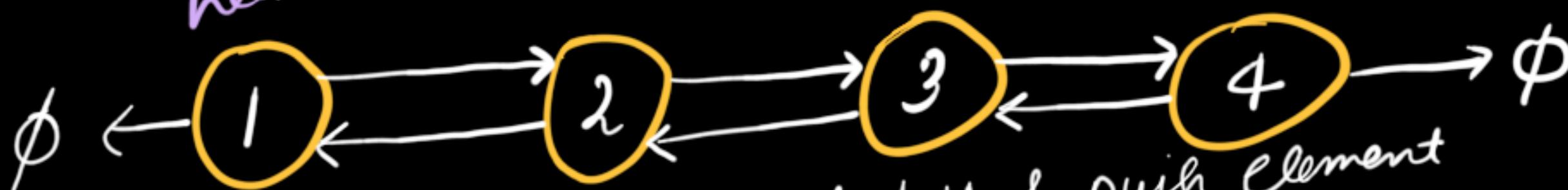
    size--;
    return del;
}
```

→ Reverse a doubly linked list



→ Approach-1

head.

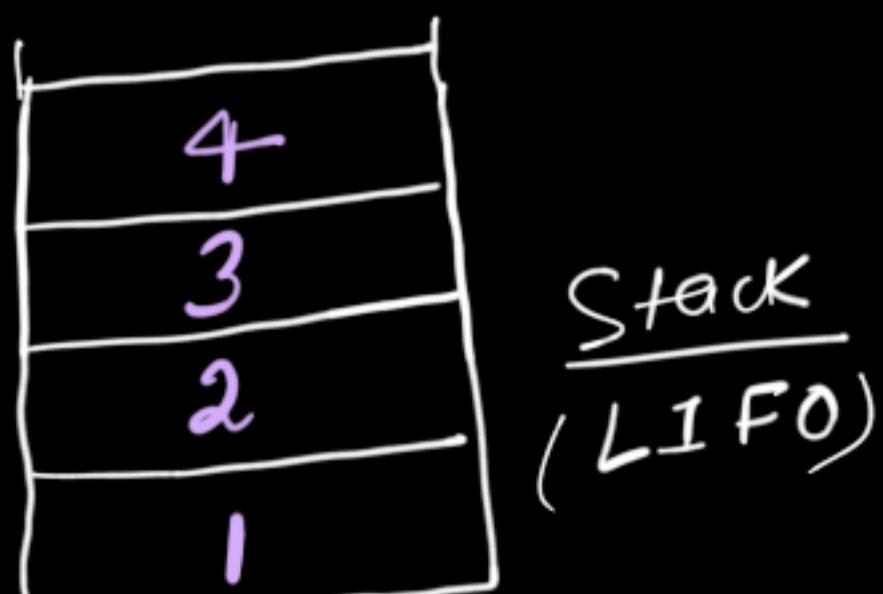


- we traverse the linked list & push element

in stack.

```
while (temp != null) {  
    stack.push(temp.value);  
    temp = temp.next;
```

}



- Again we start from head, update the value of each node by popping the stack.

temp = head

```
while (temp != null) { // !stack.isEmpty()  
    temp.value = stack.pop();  
    temp = temp.next;
```

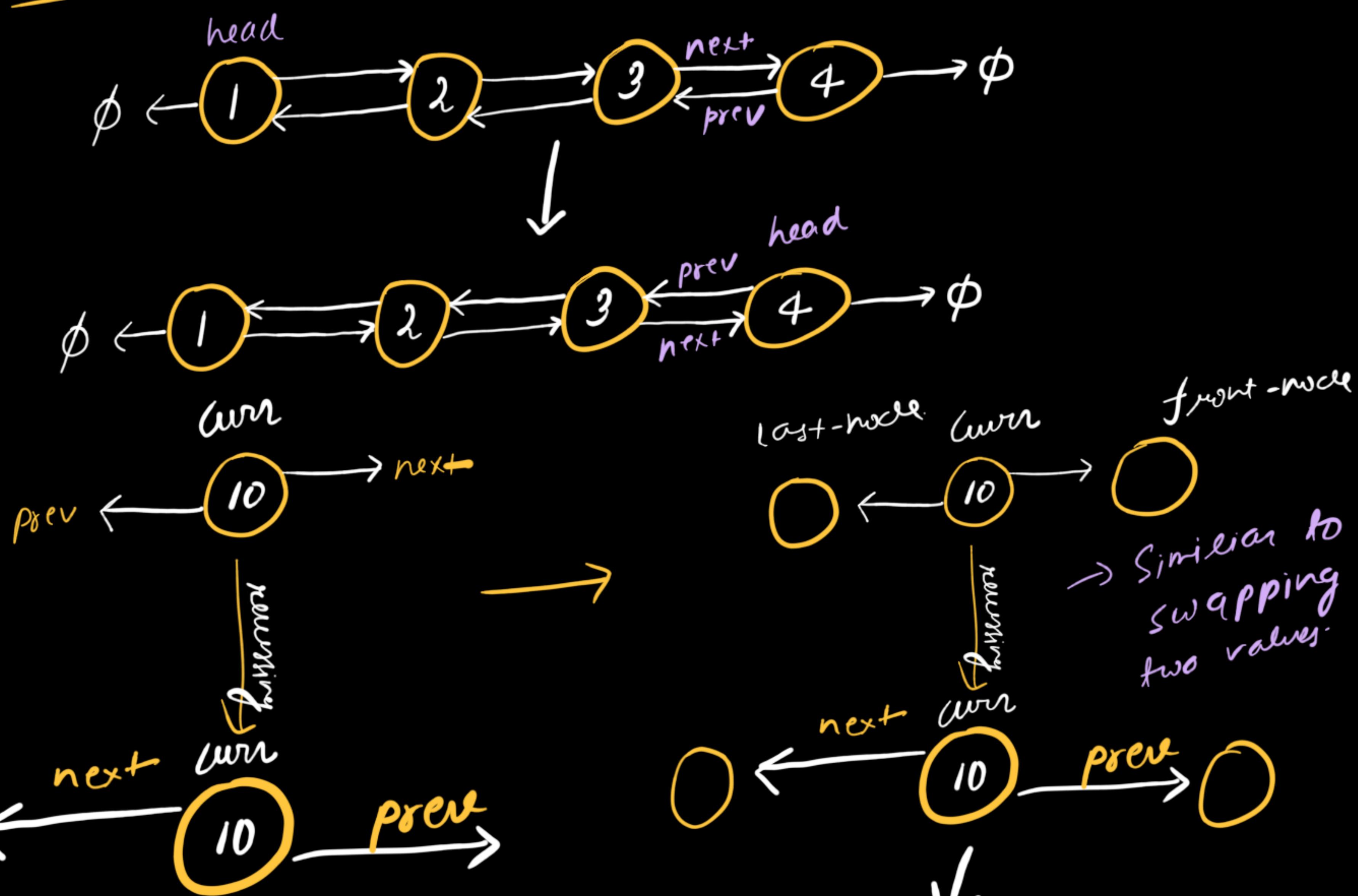
}

TC: O(2N)

SC: O(N)

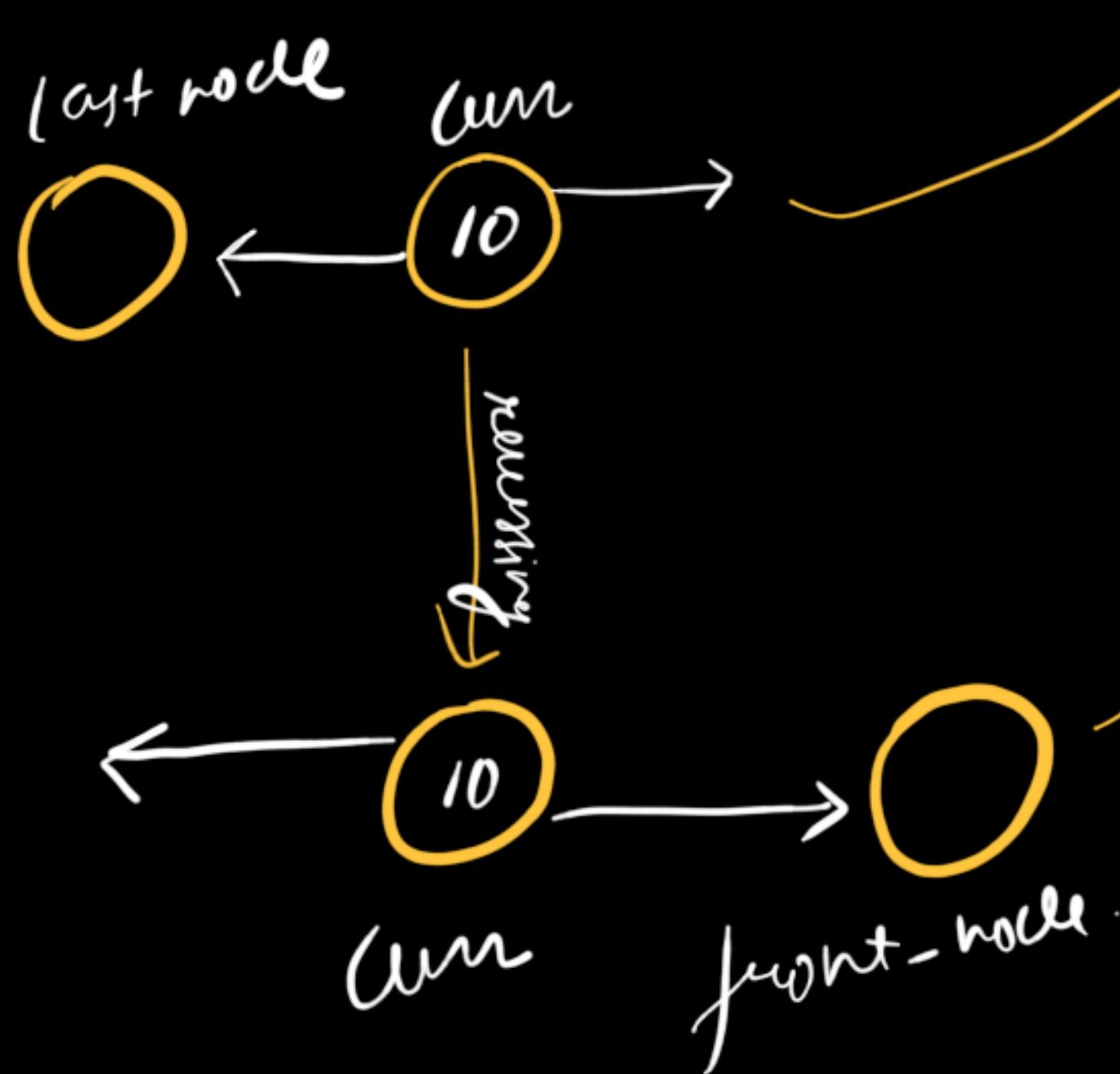
```
Part.java  
public static DLLNode<Integer> reverseDLL(DLLNode<Integer> head) {  
    if (head == null || head.next == null) {  
        return head;  
    }  
  
    Stack<Integer> stack = new Stack<>();  
    DLLNode<Integer> temp = head;  
  
    while (temp != null) {  
        stack.push(temp.value);  
        temp = temp.next;  
    }  
    temp = head;  
  
    while (!stack.isEmpty()) {  
        temp.value = stack.pop();  
        temp = temp.next;  
    }  
  
    return head;  
}
```

Approach - 2



This would need two variables to perform the operation.

But for swapping we need one.



last-node = curr · prev;
 curr · prev = curr · next;
 curr · next = last-node;

↓
 Similar to swapping
 we are taking a
 temp variable
 last-node.

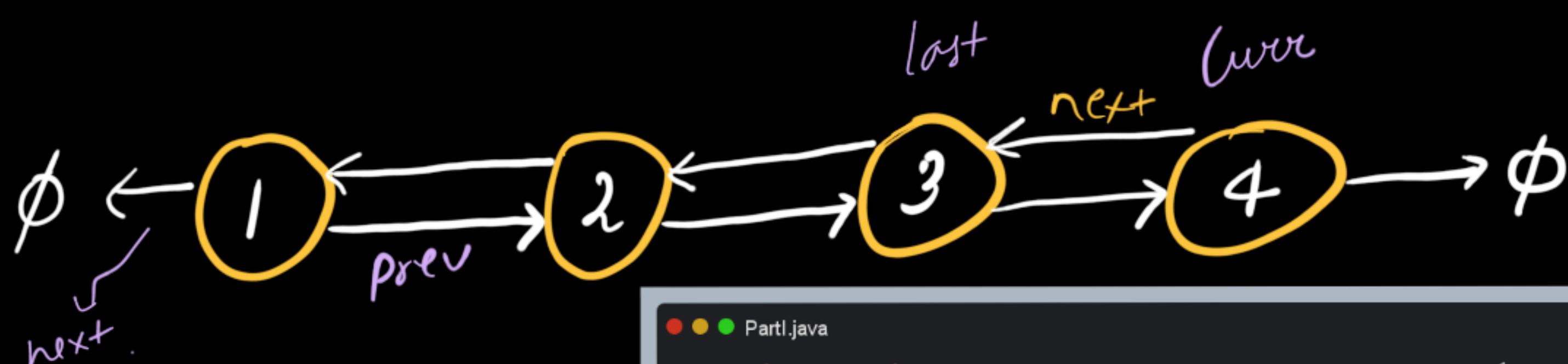
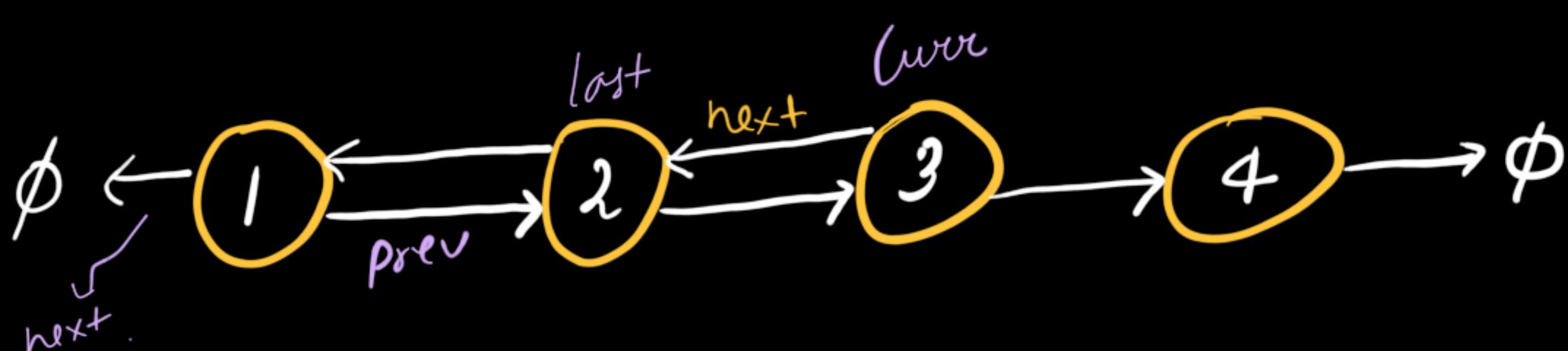
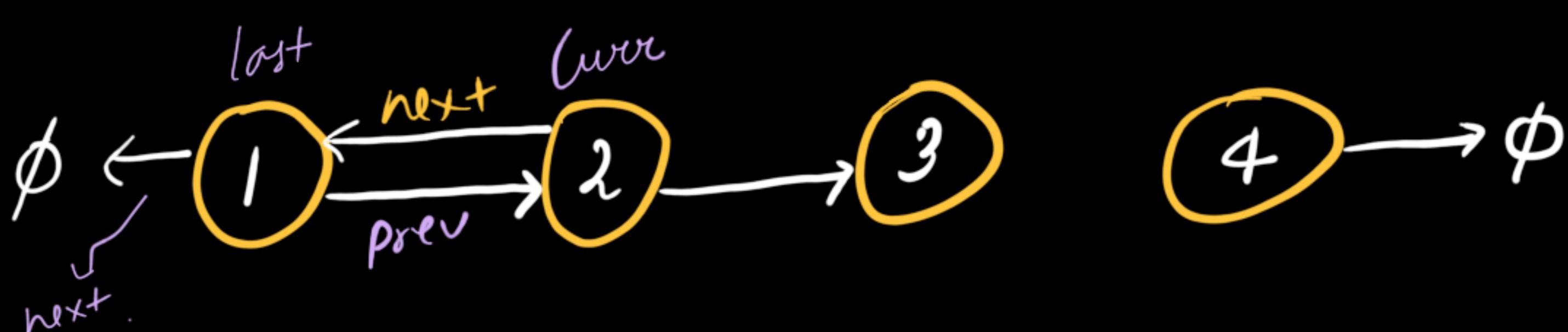
$\text{last_node} = \text{curr} \cdot \text{prev}$,

$\text{curr} \cdot \text{prev} = \text{curr} \cdot \text{next}$;

$\text{curr} \cdot \text{next} = \text{last_node}$;

$\text{curr} = \text{curr} \cdot \text{prev}$;

to move forward since
next become previous
& prev become next



$\text{new_head} = \text{last} \cdot \text{prev};$

TC: $O(N)$

SC: $O(1)$

```

PartI.java
public static DLLNode<Integer> reverseDLLOpt(DLLNode<Integer> head) {
    if (head == null || head.next == null) {
        return head;
    }
    DLLNode<Integer> last = null;
    DLLNode<Integer> curr = head;

    while (curr != null){
        last = curr.prev;
        curr.prev = curr.next;
        curr.next = last;

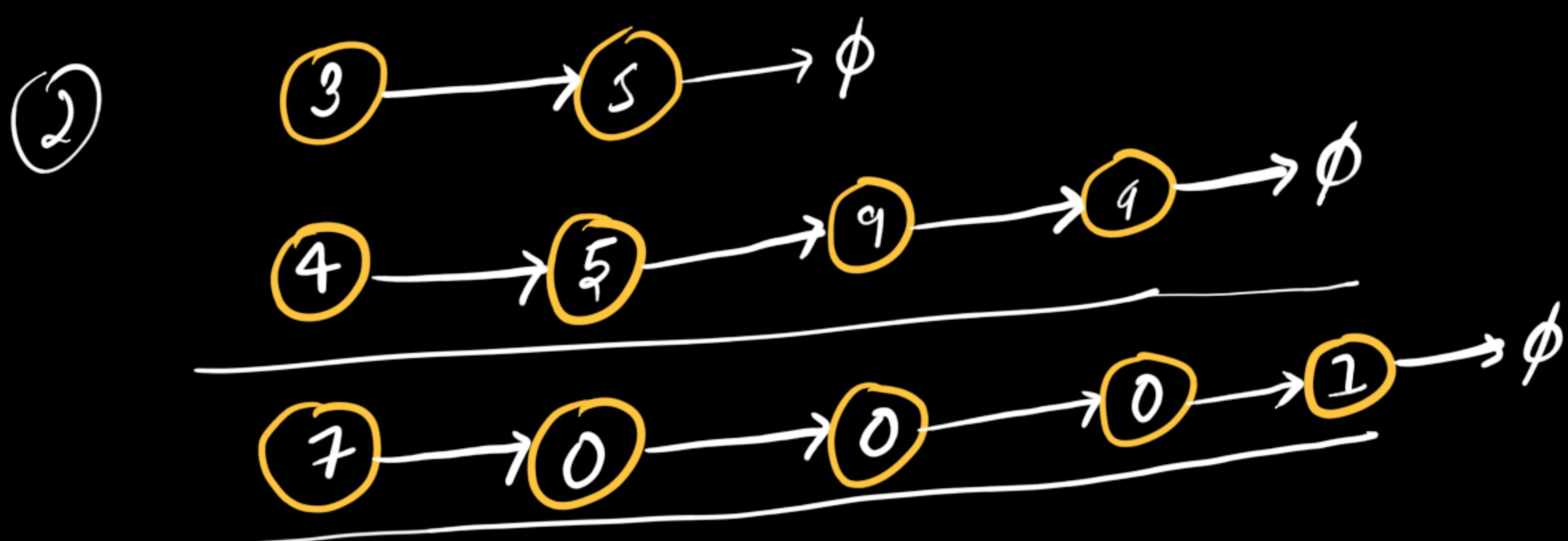
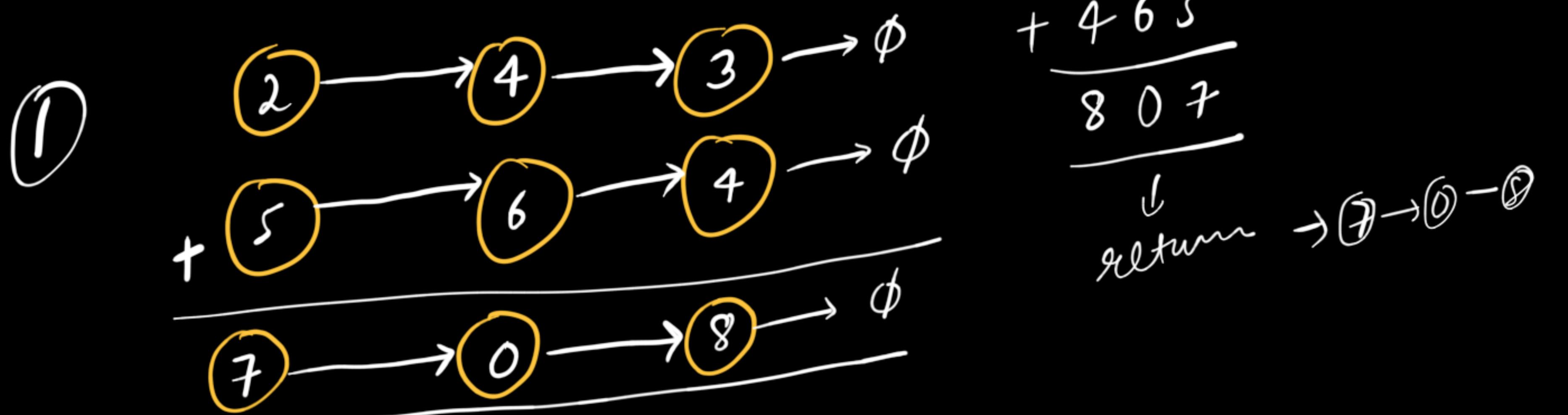
        curr = curr.prev;
    }
    head = last.prev;
}

return head;
}

```

→ Add two numbers

- ↳ Given two linked list $l1$ & $l2$, return sum of these two list in a new linked list.
- The digits are stored in reverse order.



→ Dummy node approach

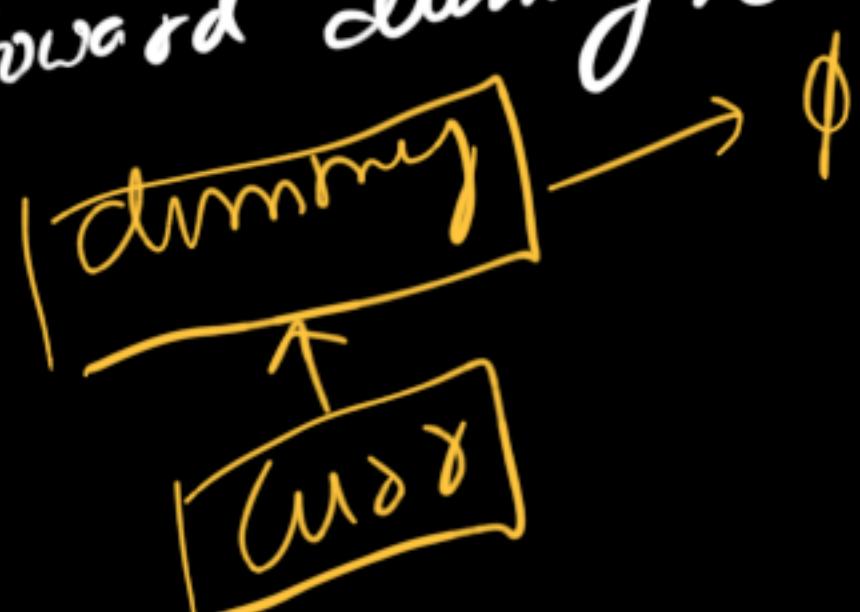
↳ common linked list pattern used to simplify operations like insertion, merging, addition etc.

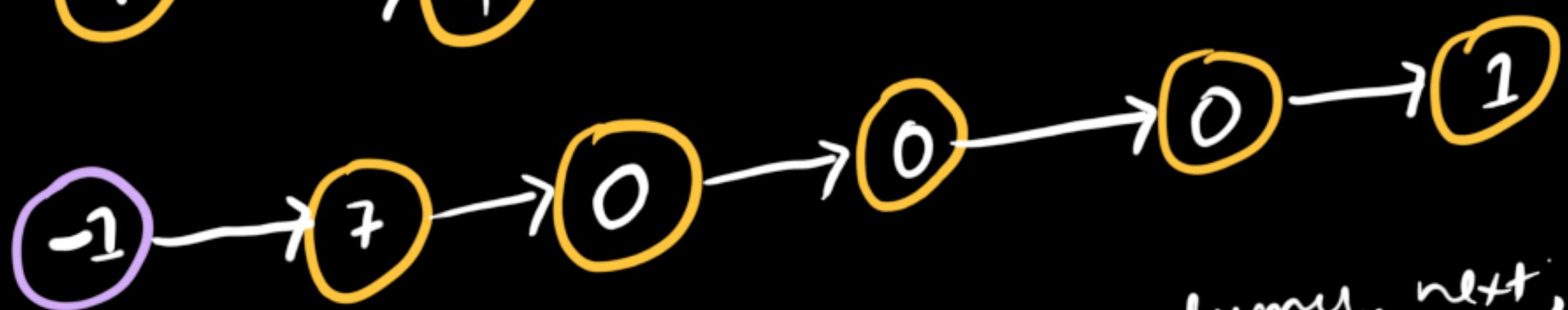
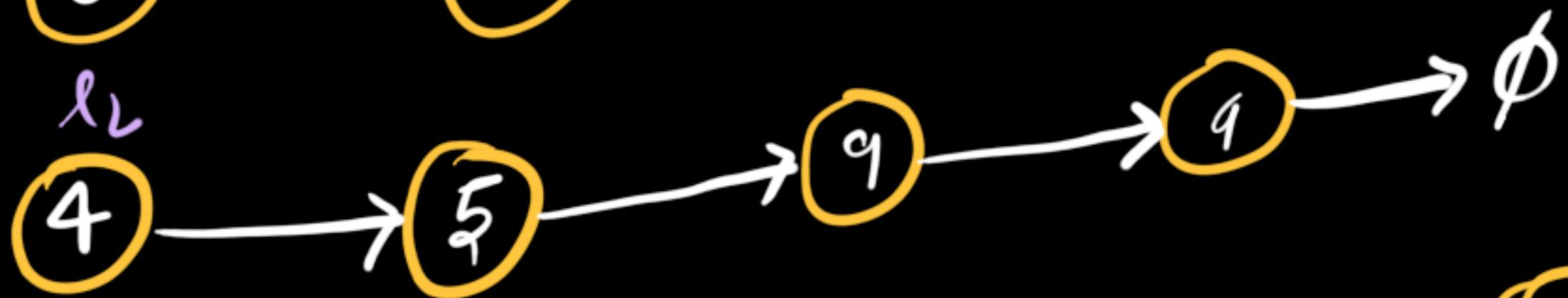
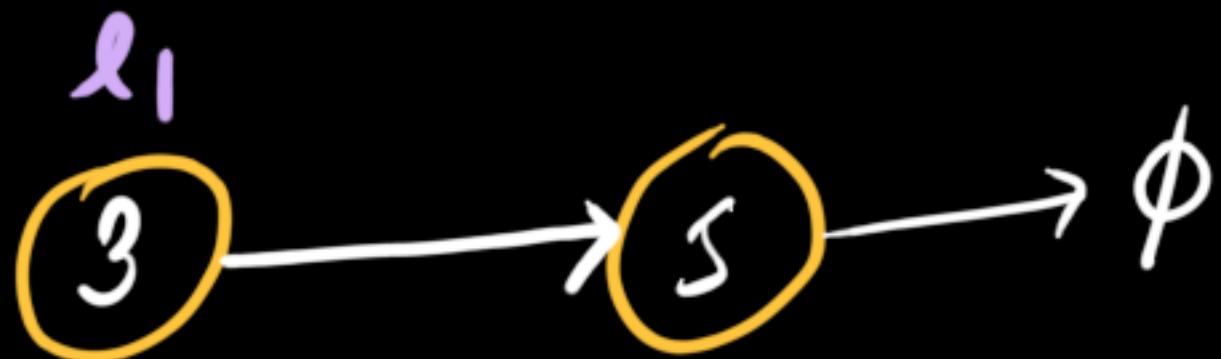
↳ helps by avoiding special handling for the head of the list.

↳ Benefits:

- No edge-case for first-node
- Avoid checking ($head == \text{null}$)
- makes code more readable.

- Initially,
 - A dummy node $\rightarrow -1 \rightarrow \emptyset$
 - carry value (0)
 - current node pointing toward dummy node.





dummy
node

\hookrightarrow new head = dummy.next;

```
carry = 0; temp = dummy
while (l1 != null || l2 != null) {
    int sum = carry;
    if (l1 != null) {
        sum += l1.value;
        l1 = l1.next;
    }
    if (l2 != null) {
        sum += l2.value;
        l2 = l2.next;
    }
    temp.next = new Node(sum % 10);
    carry = sum / 10;
    temp = temp.next;
}
if (carry != 0) {
    temp.next = new Node(carry);
}
return dummy.next;
```

```
PartII.java
public static LLNode<Integer> addTwoNumbers(LLNode<Integer> l1, LLNode<Integer> l2) {
    if (l1 == null && l2 == null) return null;
    if (l1 == null) return l2;
    if (l2 == null) return l1;

    LLNode<Integer> dummy = new LLNode<>(value: -1);
    LLNode<Integer> temp = dummy;
    int carry = 0;

    while (l1 != null || l2 != null) {
        int sum = carry;
        if (l1 != null) {
            sum += l1.value;
            l1 = l1.next;
        }

        if (l2 != null) {
            sum += l2.value;
            l2 = l2.next;
        }

        temp.next = new LLNode<>(value: sum % 10);
        carry = sum / 10;
        temp = temp.next;
    }

    if (carry != 0) {
        temp.next = new LLNode<>(carry);
    }

    return dummy.next;
}
```

Carry = 0
7 2 1

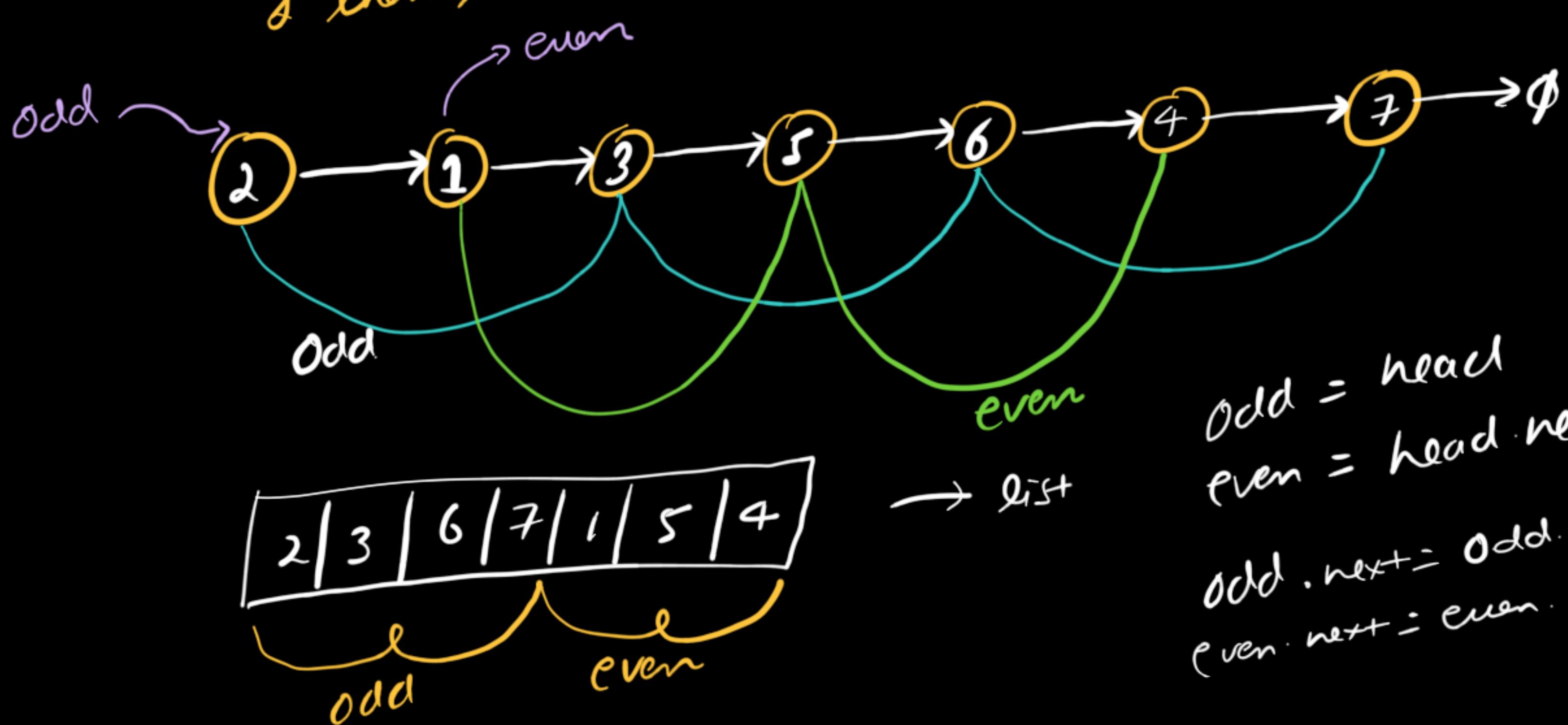
TC: $O(N)$
SC: $O(N)$
 \hookrightarrow but only
for output

\hookrightarrow
return dummy.next;

if (carry remain even after
finishing both list, just add
a new node with value
(carry))

→ Odd - Even Linked List

↳ Given the head of the linked list, group all the node with odd indices together followed by even indices, & then return the reordered list.



→ Approach - 1

↳ Take a list & traverse on odd indices
add it to the list & then traverse at even indices & then add it to the list
• After building list, iterate over it & override the value.



↳ For odd length linked list,
(odd.next != null) condition
will hit & it will miss
flat value, so we make
another check if (odd != null)
add it to the list
↓
Same goes for even part

TC: $O(2N)$

SC: $O(N)$

```
PartIII.java
public static LLNode<Integer> oddEvenList(LLNode<Integer> head) {
    if (head == null || head.next == null) {
        return head;
    }

    List<Integer> list = new ArrayList<>();

    LLNode<Integer> odd = head;
    LLNode<Integer> even = head.next;

    while (odd != null && odd.next != null){
        list.add(odd.value);
        odd = odd.next.next;
    }
    if (odd != null) list.add(odd.value);

    while (even != null && even.next != null){
        list.add(even.value);
        even = even.next.next;
    }
    if (even != null) list.add(even.value);

    LLNode<Integer> temp = head;

    int index = 0;
    while (temp != null){
        temp.value = list.get(index);
        index++;
        temp = temp.next;
    }

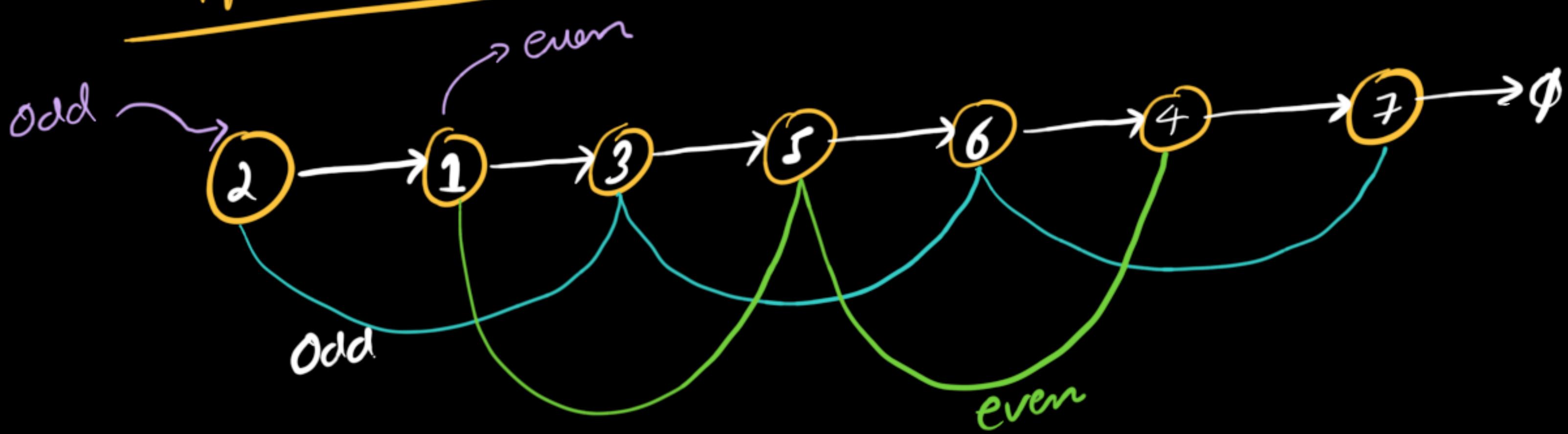
    return head;
}
```

$O(N/2)$

$O(N/2)$

$O(N)$

→ Approach - 2

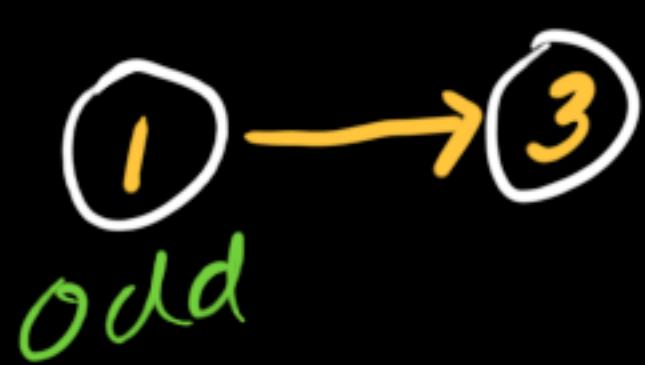


Links:

$\text{odd}.\text{next} = \text{odd}.\text{next}.\text{next}$; \exists connecting links
 $\text{even}.\text{next} = \text{even}.\text{next}.\text{next}$;

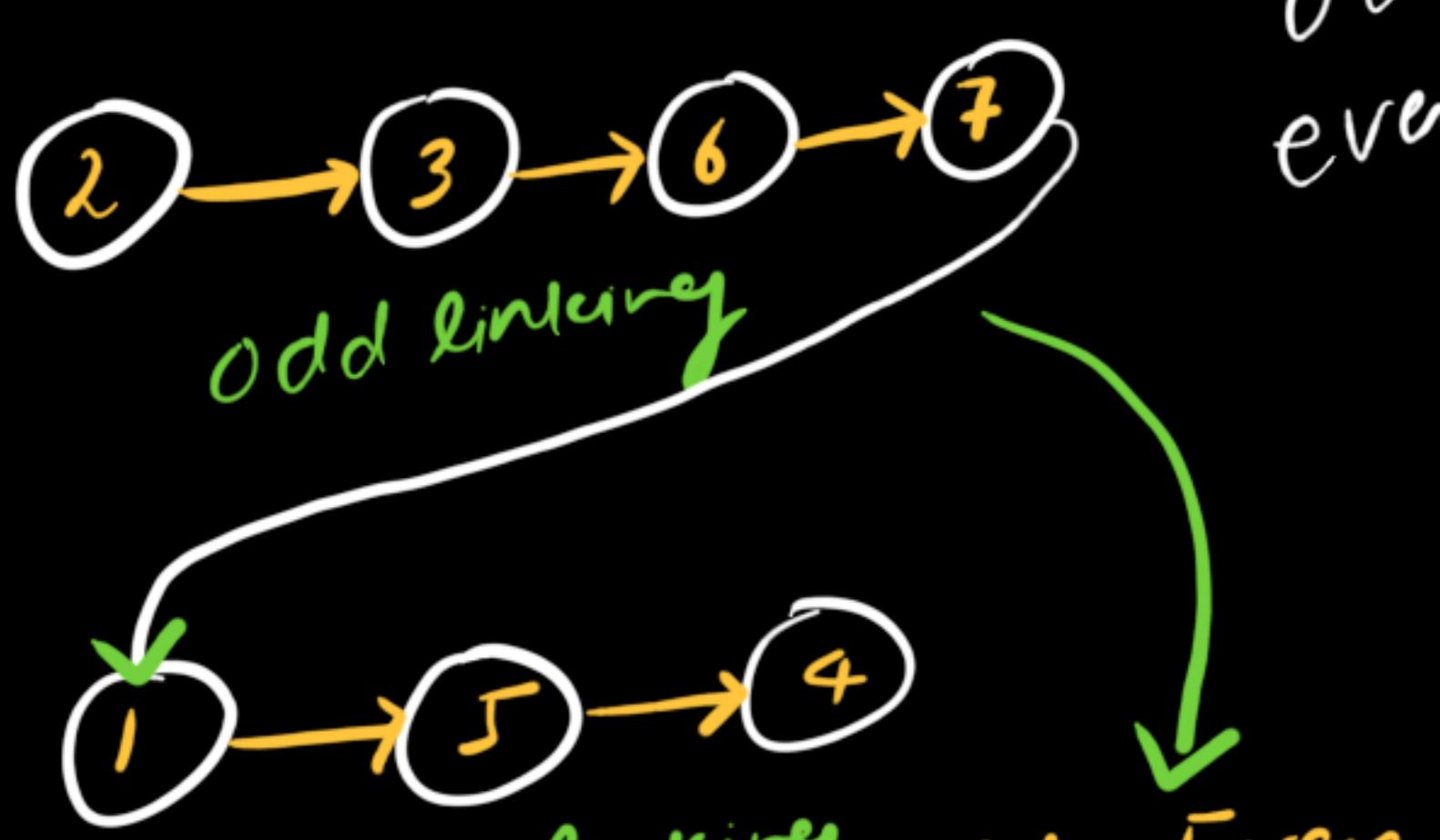
Now after connecting odd & even link to the
next odd & even node.

↳ To keep on performing these operation
we need to move to next odd & even
node.



↳ After performing above linking
operation, the new odd & even :-

$\text{odd} = \text{odd}.\text{next}$;
 $\text{even} = \text{even}.\text{next}$;



To connect them odd-Even
part we need to keep
reference to first even
node & then:-

$\text{odd}.\text{next} = \text{first-even-node}$;

```

PartIII.java
public static LLNode<Integer> oddEvenListOpt(LLNode<Integer> head) {
    if (head == null || head.next == null) {
        return head;
    }

    LLNode<Integer> odd = head;
    LLNode<Integer> even = head.next;
    LLNode<Integer> evenHead = head.next;

    while (even != null && even.next != null){
        odd.next = odd.next.next;
        even.next = even.next.next;

        odd = odd.next;
        even = even.next;
    }

    odd.next = evenHead;
    return head;
}

```

Tc: O(N)
Sc: O(1)

→ Sort 0's, 1's & 2's list
↳ sort the linked list containing 0's, 1's & 2's

→ Approach - 1

- ① Count the frequency of 0's, 1's & 2's
- ② Iterate over the linked list & override the value.

① Overwrite 0
Until count 0
is != 0.

② Overwrite 1
Until count 1
is != 0

③ Overwrite 2
Until count 2
is != 0

Tc: O(2N)
Sc: O(1)

```
PartIV.java
public static LLNode<Integer> sortList(LLNode<Integer> head) {
    int count0 = 0;
    int count1 = 0;
    int count2 = 0;

    LLNode<Integer> temp = head;

    while (temp != null){
        if (temp.value == 0) count0++;
        else if (temp.value == 1) count1++;
        else count2++;

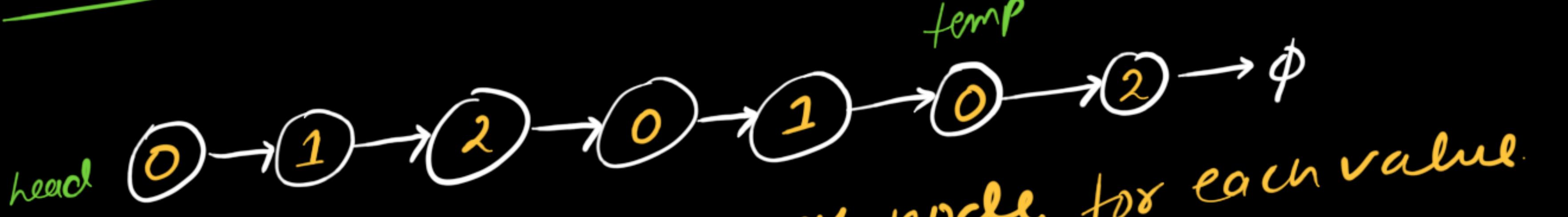
        temp = temp.next;
    }

    temp = head;

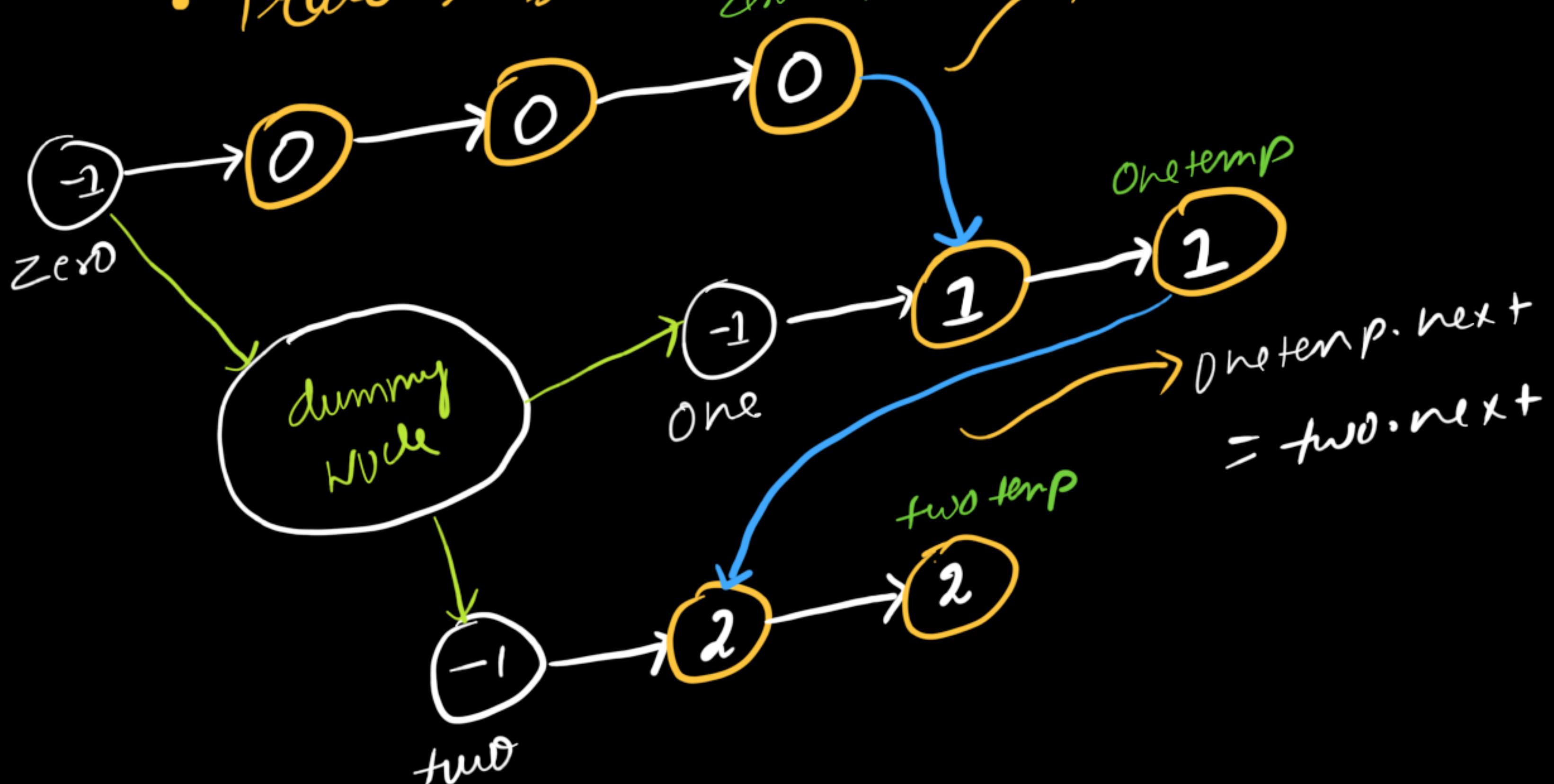
    while (temp != null){
        if (count0 != 0) {
            temp.value = 0;
            count0--;
        } else if (count1 != 0) {
            temp.value = 1;
            count1--;
        } else {
            temp.value = 2;
            count2--;
        }
        temp = temp.next;
    }

    return head;
}
```

→ Approach-2



- Create three dummy nodes for each value.
- Traverse & connect to each node (0, 1, 2)



Edge-Cases

① What if there are only 0's & 2's?

↳ check if $\text{ones}.\text{next} \neq \text{null}$
 ↳ if null, point
 0's to 2's else
 point 0's to one's.

i.e. if $\text{ones}.\text{next} \neq \text{null}$
 $\text{tempZero}.\text{next} = \text{ones}.\text{next}$
 } else {
 $\text{tempZero}.\text{next} = \text{two}.\text{next}$

} $\text{tempTwo}.\text{next}$ will always

② last of tempTwo will always
 point to null.
 $\text{tempTwo}.\text{next} = \text{null}$

TC: $O(N)$
 SC: $O(1)$

```

PartIV.java
public static LLNode<Integer> sortListOpt(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;
    ↳ dummy node
    LLNode<Integer> zeroes = new LLNode<>(-1);
    LLNode<Integer> ones = new LLNode<>(-1);
    LLNode<Integer> twos = new LLNode<>(-1);

    LLNode<Integer> tempZero = zeroes;
    LLNode<Integer> tempOne = ones;
    LLNode<Integer> tempTwo = twos;

    LLNode<Integer> temp = head;

    while (temp != null) {
        if (temp.value == 0) {
            tempZero.next = temp;
            tempZero = tempZero.next;
        } else if (temp.value == 1) {
            tempOne.next = temp;
            tempOne = tempOne.next;
        } else {
            tempTwo.next = temp;
            tempTwo = tempTwo.next;
        }
        temp = temp.next;
    }

    // Break the last node
    tempTwo.next = null;

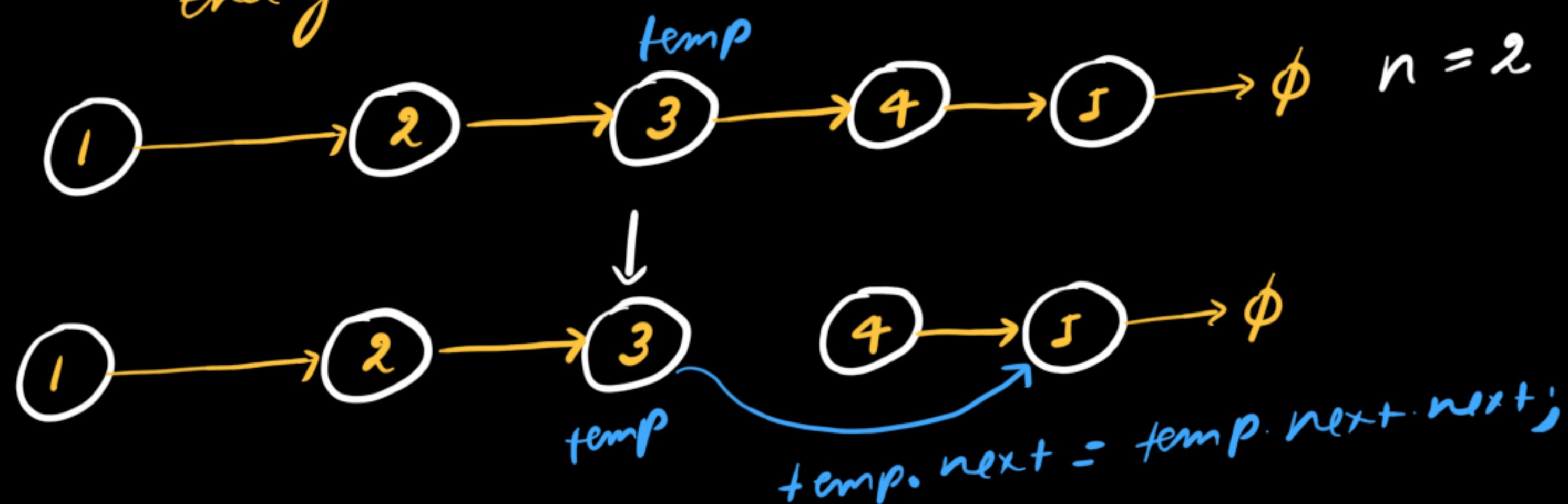
    // Connect 0s → 1s → 2s
    tempZero.next = ones.next != null ? ones.next : twos.next;
    tempOne.next = twos.next;

    return zeroes.next;
}

```

→ Remove n^{th} node from list

↳ Given the head of a linked list, remove n^{th} node from the end of the list & return its head.



→ Approach - 1

① Find the length of the list & iterate till
(length - $n-1$)

② perform *temp.next = temp.next.next;*

③ Edge case:
↳ what if length of the ll == n ?
↳ return head.next;

TC: $O(1 \cdot \text{len}) + O(\text{len} - n)$
SC: $O(1)$

```
PartV.java
public LLNode<Integer> removeNthFromEnd(LLNode<Integer> head, int n) {
    int length = len(head);

    if (n == length) {
        return head.next;
    }

    LLNode<Integer> temp = head;
    for (int i = 0; i < length - n - 1; i++) {
        temp = temp.next;
    }

    temp.next = temp.next.next;
    return head;
}

public static int len(LLNode<Integer> head) { 1 usage new *
    int len = 0;
    LLNode<Integer> temp = head;
    while (temp != null) {
        len++;
        temp = temp.next;
    }
    return len;
}
```

→ Approach-2

↳ How can we reach just before n^{th} node?

↳ Imagine there are two racers P_1 & P_2 .
 $P_1 \rightarrow$ cheats & run n steps before the race starts.
 $P_2 \rightarrow$ runs when race start.

- The relative gap between P_1 & P_2 is n initially. P_2

- Now both racers run at equal pace i.e 1 step

↳ Let P_2 takes x steps, so P_2 also takes x steps.

$$\text{so, } \text{pos}(P_1) + x = L \quad \text{---(2)}$$

$$\text{pos}(P_2) = x \quad \text{---(3)}$$

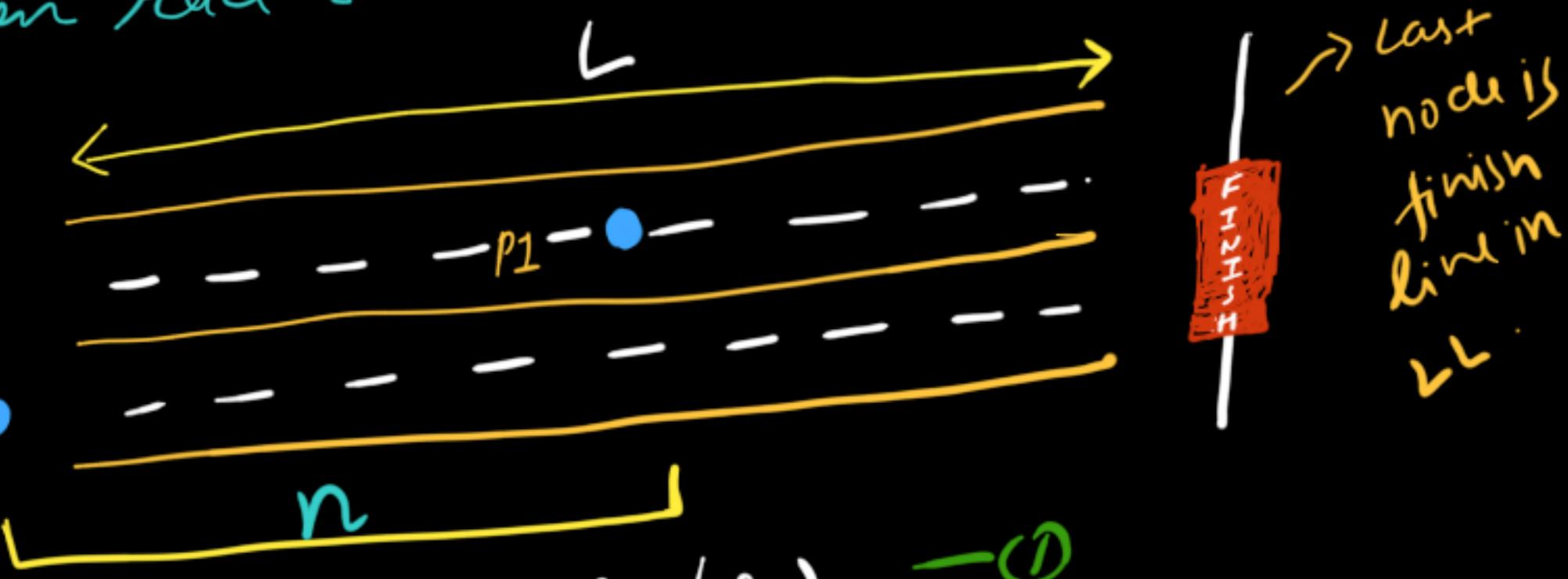
$$\text{pos}(P_1) + \text{pos}(P_2) = L \quad \text{---(2) \& (3)}$$

$$\text{pos}(P_2) = L - \text{pos}(P_1) \rightarrow (1)$$

$$\text{pos}(P_2) = L - n + \text{pos}(P_1) \quad \left\{ \begin{array}{l} \text{pos}(P_1) = 0, \text{ initially} \\ \text{pos}(P_2) = L - n \end{array} \right.$$

$$\boxed{\text{pos}(P_2) = L - n}$$

- When P_1 finishes the race, P_2 is at $(L - n)$ i.e exactly before the n^{th} node.

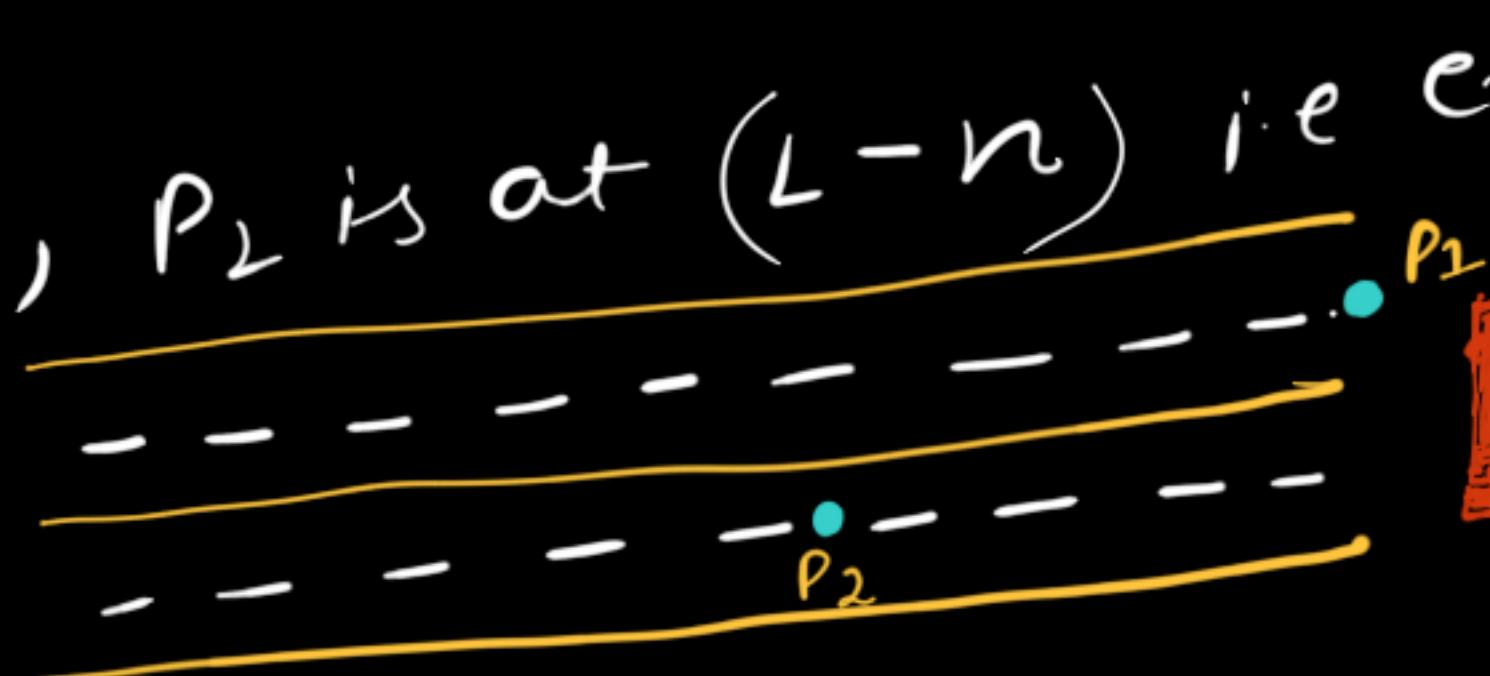


$$\text{pos}(P_1) = n + \text{pos}(P_2) \quad \text{---(1)}$$

↳ Initially P_1 is at 0

$$\text{pos}(P_1) + x = L \quad \text{---(2)}$$

$$\text{pos}(P_2) = x \quad \text{---(3)}$$



```

PartV.java

public static LLNode<Integer> removeNthFromEndOpt(LLNode<Integer> head, int n) {
    if (head == null) return null;
    LLNode<Integer> fast = head;
    LLNode<Integer> slow = head;

    for (int i = 0; i < n; i++) {
        fast = fast.next;
    }

    // when length == n i.e FAST becomes null, and we are req to delete first node
    if (fast == null) return head.next;

    while (fast.next != null){
        slow = slow.next;
        fast = fast.next;
    }

    slow.next = slow.next.next;
    return head;
}

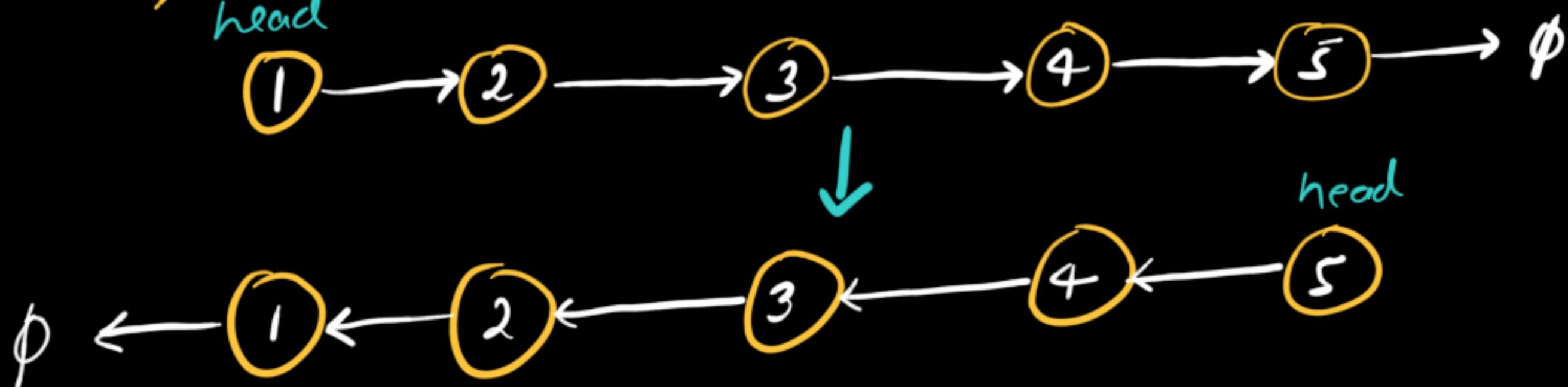
```

$T_C: O(N)$

$S_C: O(1)$

→ Reverse a Linked List

Given the head of linked list, reverse & return the head of linked list.



→ Approach-1

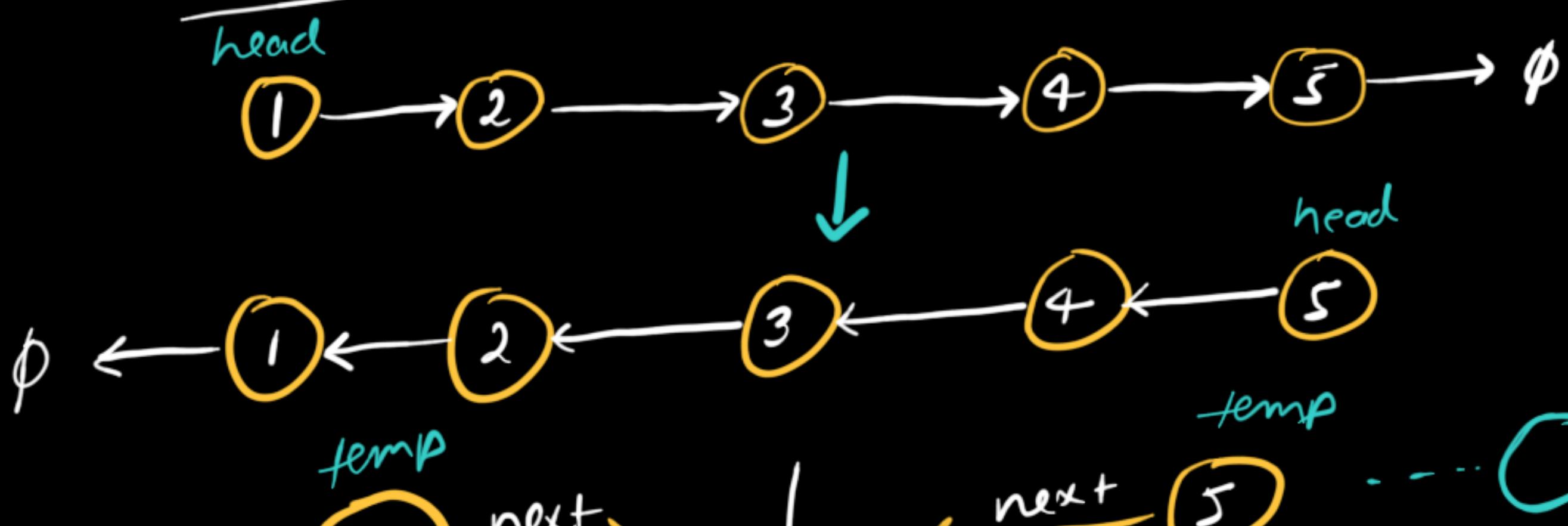
① Use stack, push element into stack

② Again, iterate from start, & override the value of temp by popping off from the stack

$Tc: O(2N)$: $Sc: O(N)$

→ Approach-2

• Iteratively



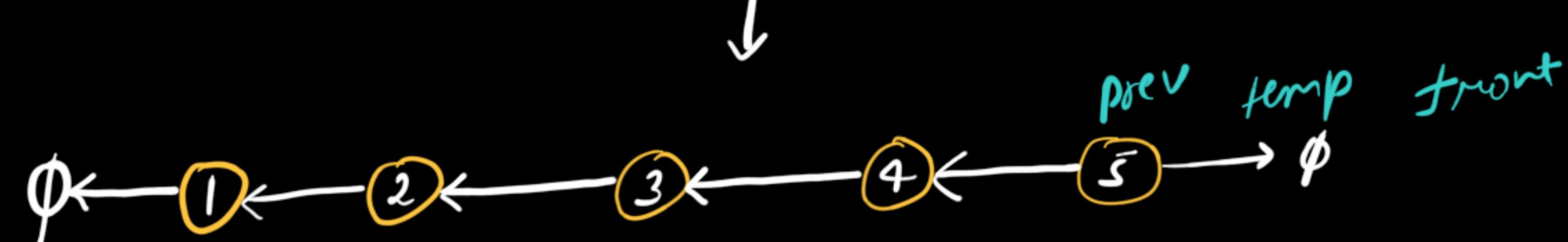
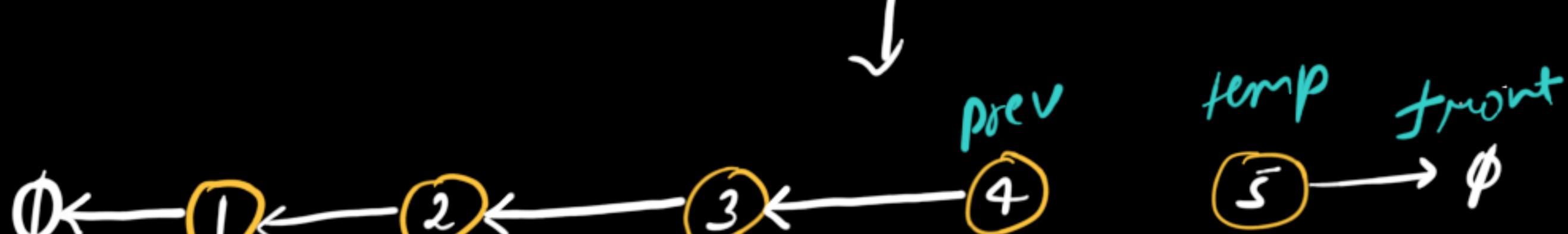
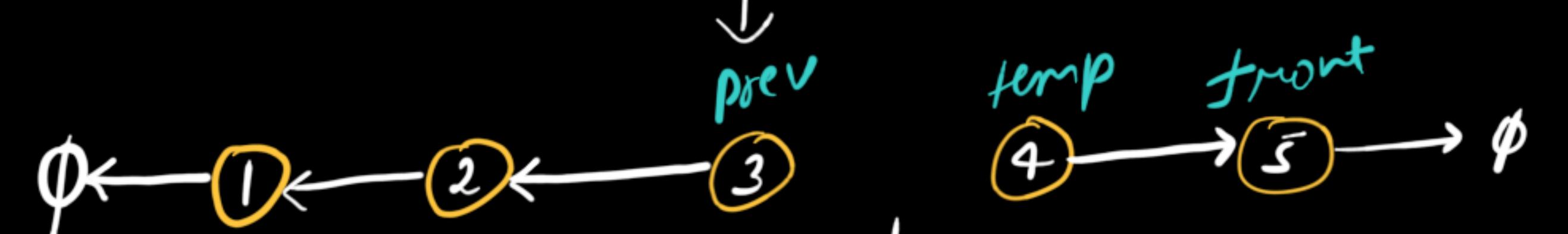
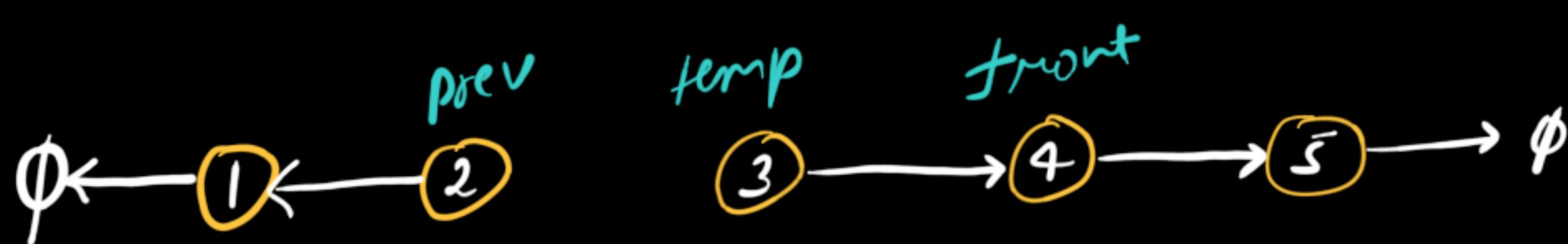
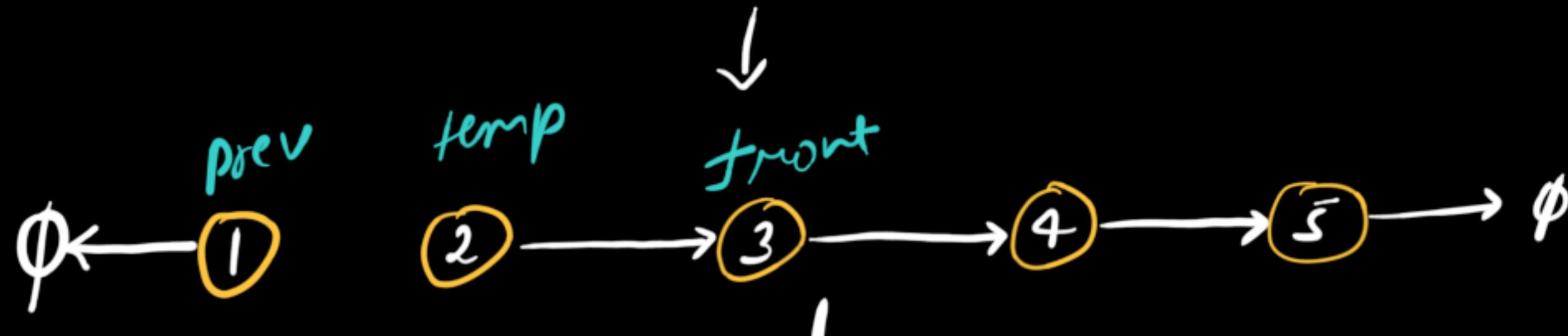
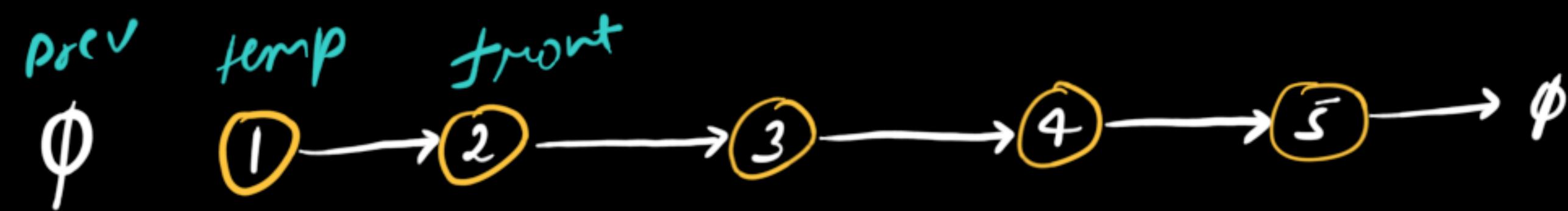
- Again to reconnect front node to prev node, we need to store prev node.

pseudocode:

```

prev=null, temp=head
while (temp!=null) {
    front = temp.next;
    temp.next = prev;
    prev = temp;
    temp = front;
}
    
```

- To move to next node we need to store front node.



- When temp reaches null, our linked list is reversed & new head is prev.

PartVI.java

```
public static LLNode<Integer> reverseListOpt(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;

    LLNode<Integer> temp = head;
    LLNode<Integer> prev = null;

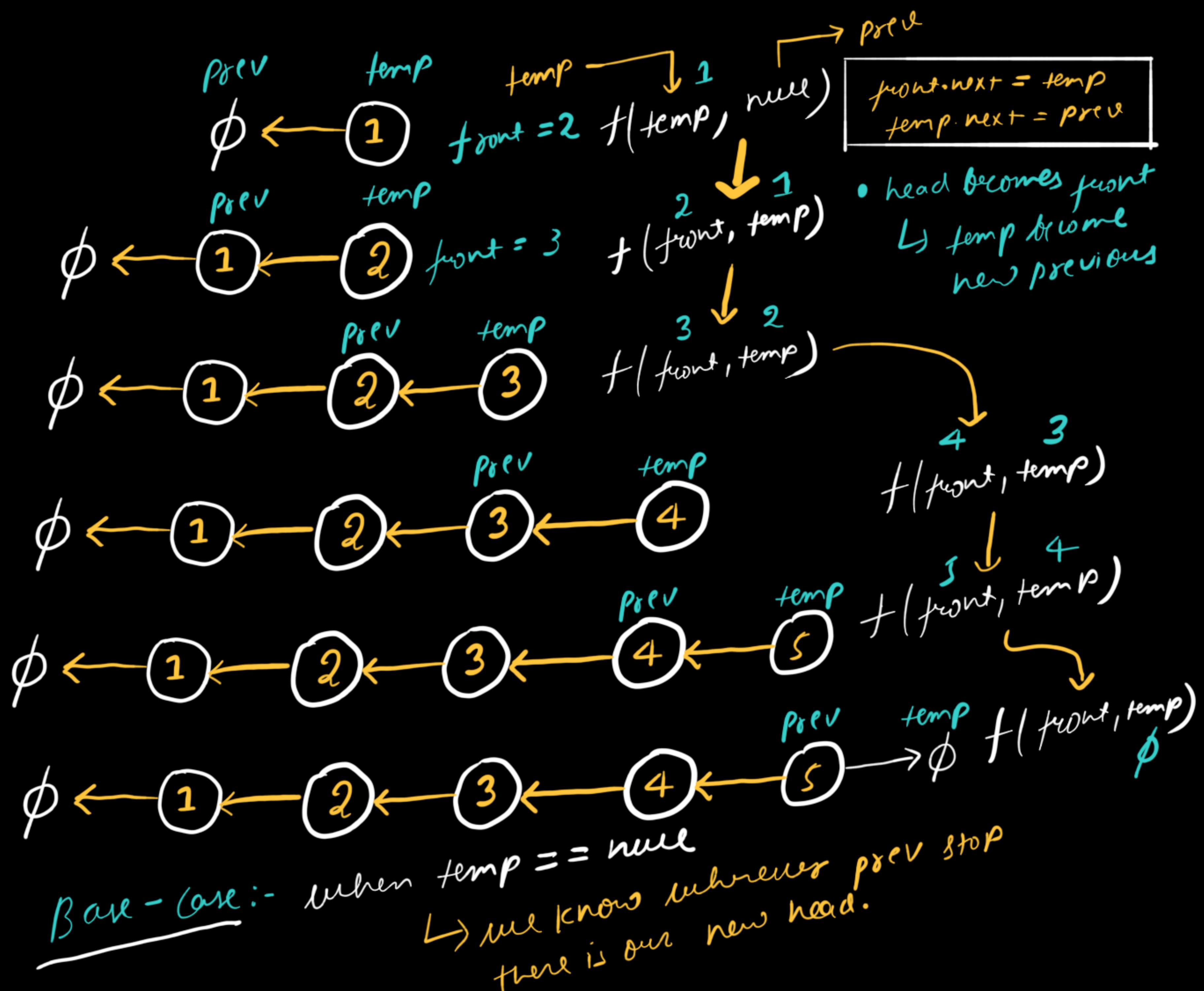
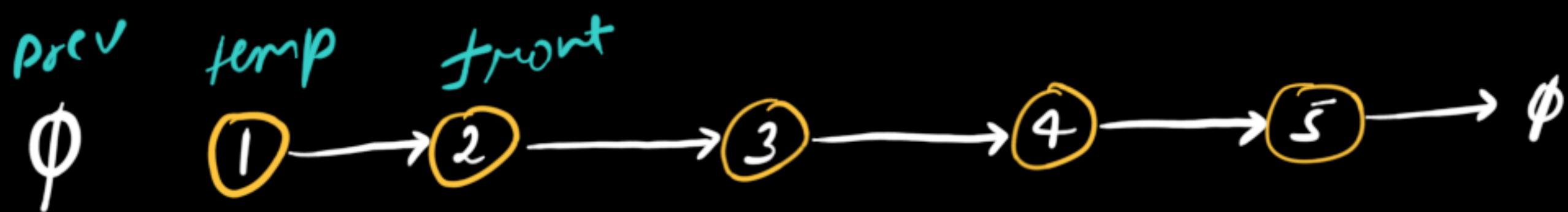
    while (temp != null){
        LLNode<Integer> front = temp.next;
        temp.next = prev;
        prev = temp;
        temp = front;
    }

    return prev;
}
```

$Tc: O(N)$

$Sc: O(1)$

→ Recursive
↳ only two variables are changing externally
① temp ② prev



```
PartVI.java
public static LLNode<Integer> reverseListOptRecur(LLNode<Integer> temp, LLNode<Integer> prev) {
    if (temp == null) {
        return prev;
    }

    LLNode<Integer> front = temp.next;
    temp.next = prev;

    return reverseListOptRecur(front, temp);
}
```

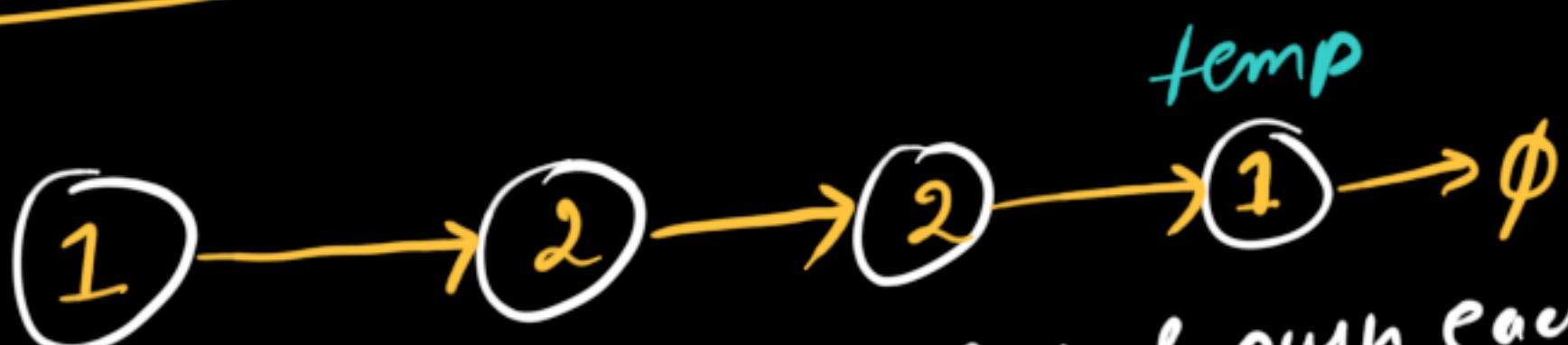
TC: $O(N)$ ↗ stack space
SC: $O(N)$ ↗ stack space

→ Check if linked list is palindrome
↳ given the head of the linked list, return true if "is palindrome".

head



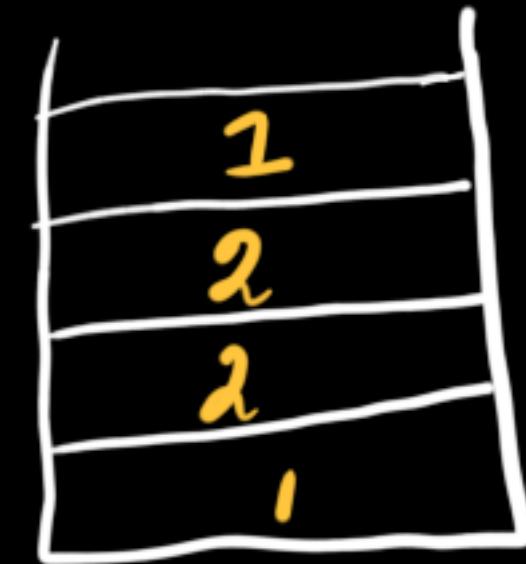
→ Approach - 1



(1) iterate over linked list & push each element in stack

(2) now again iterate from head, & compare the value of each node by popping off the stack.

Tc: $O(2N)$ SC: $O(N)$



Stack

→ Approach - 2

head



- if we somehow divide these linked list into two list, & then reverse the 2nd divided list, then we can compare each node, if \neq we return false else true.



head



head

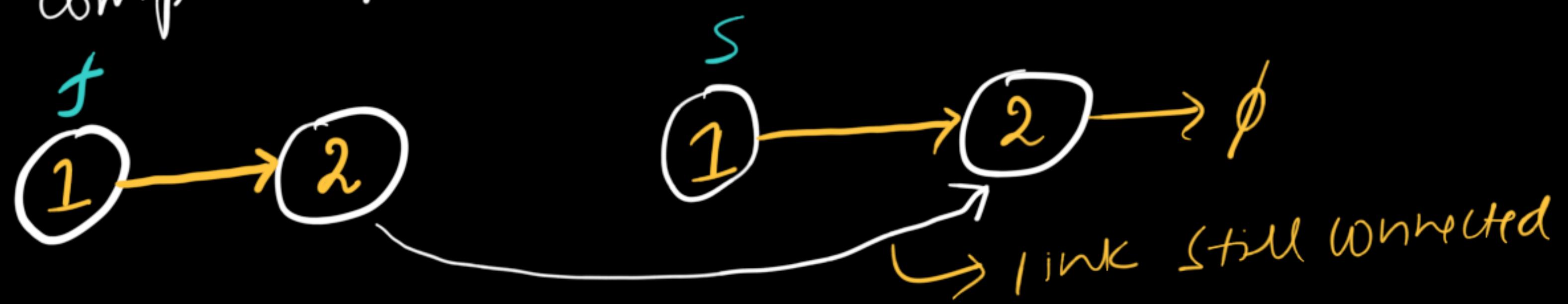


↓ Reverse



→ link still connected

- Now if we put two pointer f & s , compare & keep on moving



```
while (s != null) {
    if (f.value != s.value) {
        return false;
    }
}
```

```
f = f.next;
s = s.next;
```

```
}
```

return true.

~~* Always restore original list.~~

do not distort the original linked list.

TC: $O(2N)$

SC: $O(1)$

```
PartVII.java
public static boolean isPalindromeOpt(LLNode<Integer> head) { 1 usage
    LLNode<Integer> mid = getMid(head);
    LLNode<Integer> r = reverseListOpt(mid);

    LLNode<Integer> f = head;
    LLNode<Integer> s = r;

    while (s != null) {
        if (!f.value.equals(s.value)) {
            reverseListOpt(r); // restore original list
            return false;
        }

        f = f.next;
        s = s.next;
    }
    reverseListOpt(r); // restore original list
    return true;
}

@Contract(value = "null -> null", pure = true)
private static LLNode<Integer> getMid(LLNode<Integer> head) { 1 usage
    if (head == null || head.next == null) return head;

    LLNode<Integer> slow = head;
    LLNode<Integer> fast = head;

    while (fast != null && fast.next != null) {
        slow = slow.next;
        fast = fast.next.next;
    }

    return slow;
}

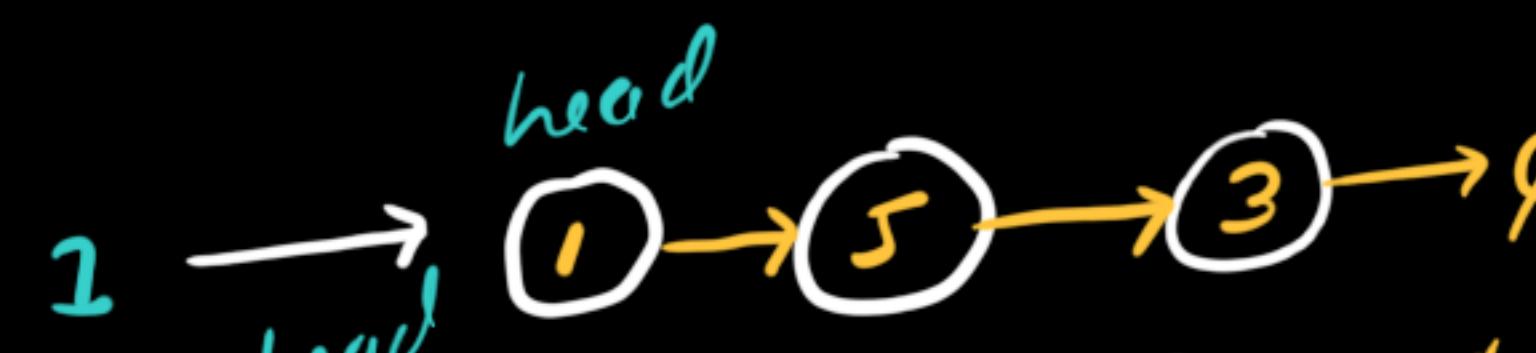
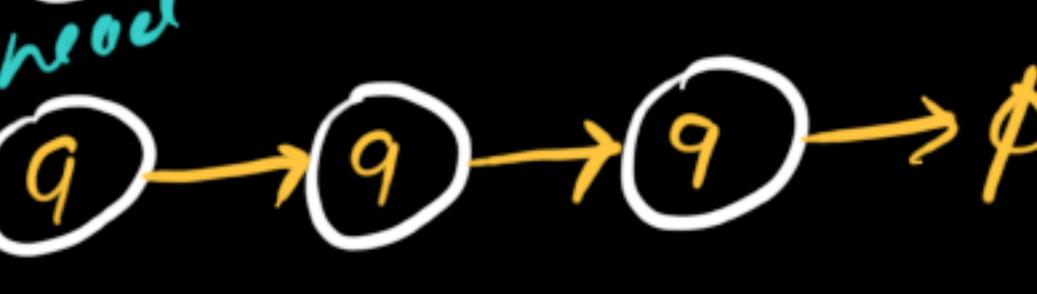
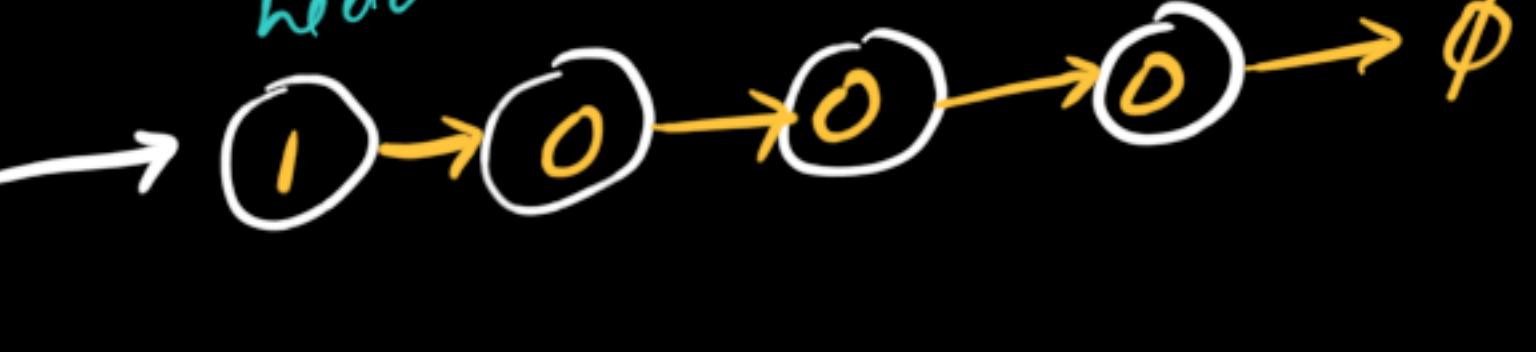
@Contract("null -> null")
private static LLNode<Integer> reverseListOpt(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;

    LLNode<Integer> temp = head;
    LLNode<Integer> prev = null;

    while (temp != null) {
        LLNode<Integer> front = temp.next;
        temp.next = prev;
        prev = temp;
        temp = front;
    }

    return prev;
}
```

→ Add 1 to the linked list
 ↳ Given +ve integer represented in the form of singly linked list.
 ↳ Add one to the number i.e. increment the given number by one.

Ex-1:  \rightarrow 
Ex-2:  \rightarrow 

→ Approach-1

(1) Reverse the LL \rightarrow

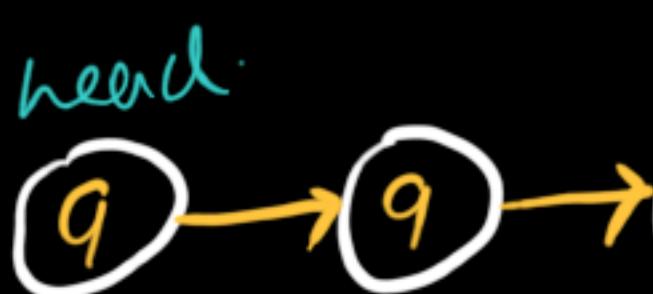


(2) Add 1 to it \rightarrow



(3) Again reverse the LL \rightarrow



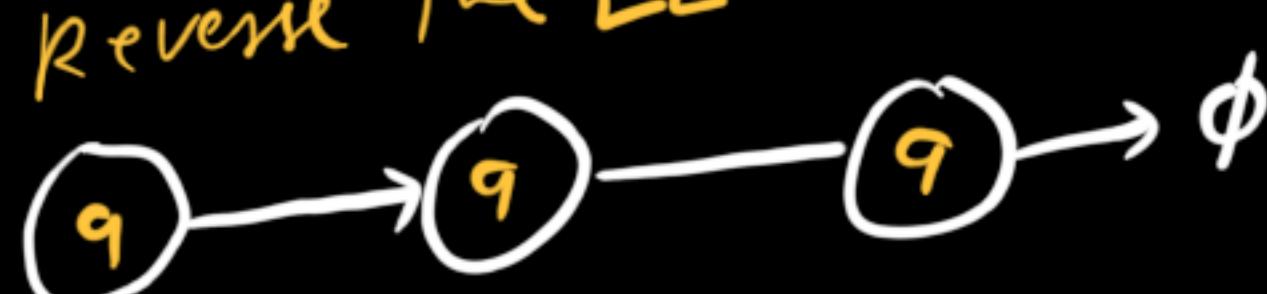
(4) what if?  \rightarrow $\phi + 1$

if (carry == 0) \rightarrow

In this case we need to add one more node to first.

break;
 ↳ we don't need to perform further operation

↳ (1) Reverse the LL



(2) Add 1 to it

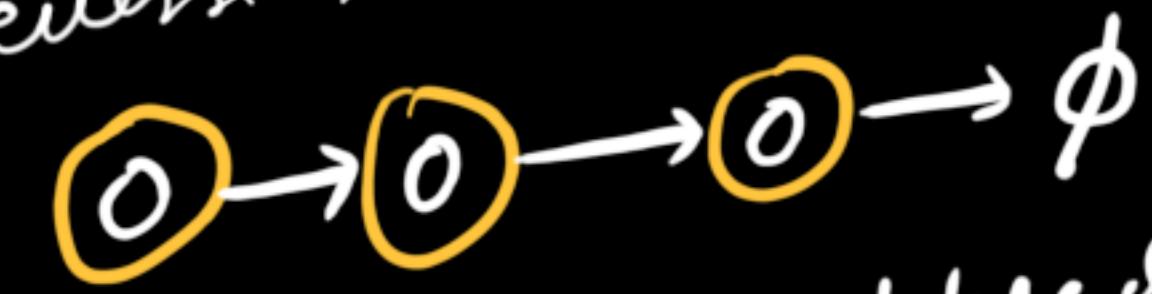


Carry 1 1 1



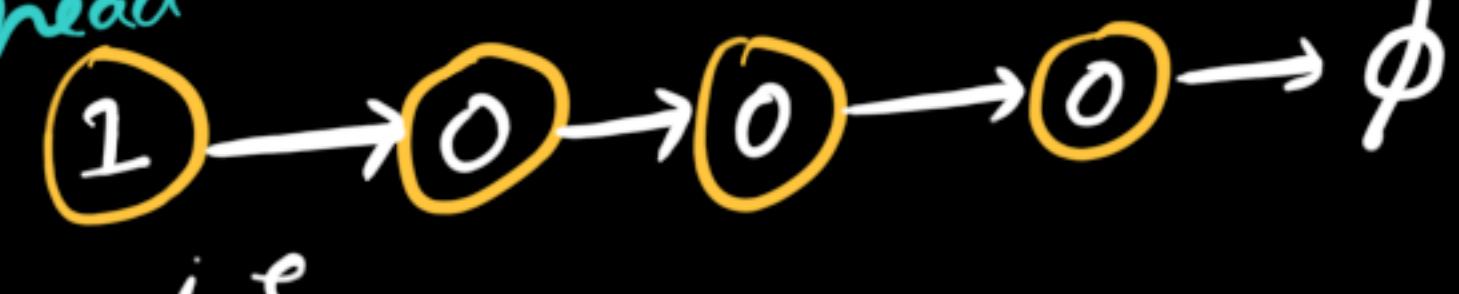
(3) carry = 1 & temp is at null

↳ (1) Reverse the LL



(2) Add 1 carry node at head

head



i.e.

New-node = new Node(carry)

new-node.next = head;

head = new-node.

```
PartVIII.java
public static LLNode<Integer> addOne(LLNode<Integer> head) {
    head = reverseListOpt(head);
    LLNode<Integer> temp = head;
    int carry = 1;

    while (temp != null) {
        int sum = temp.value + carry;
        temp.value = sum % 10;
        carry = sum / 10;

        if (carry == 0) break;
        temp = temp.next;
    }

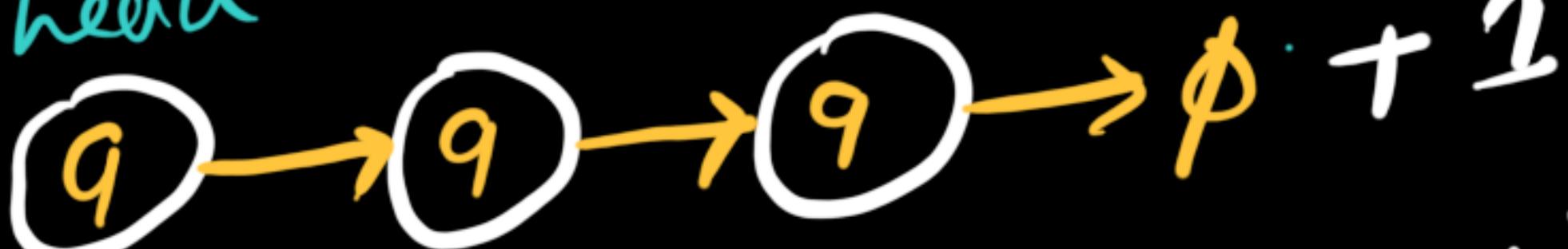
    head = reverseListOpt(head);

    if (carry > 0) {
        LLNode<Integer> c = new LLNode<>(carry);
        c.next = head;
        head = c;
    }
}

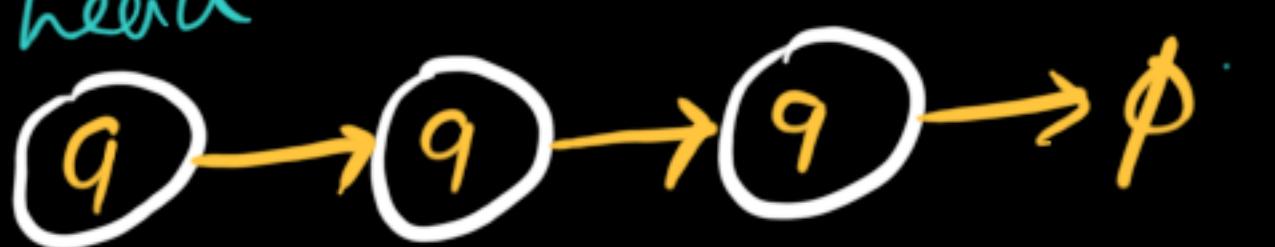
return head;
}
TC: O(3N)
SC: O(1)
```

→ Approach-2 → can we do it in single pass
↳ use recursion

head:



head



f(head)

Base-case:



↳ head == null?

↳ return 1

head



f(head.next)

head



f(head.next)

head



f(head.next)

head



f(head)



f(head.next)



f(head.next.next)



f(head.next.next.next)



f(head.next.next.next.next)

head

new head will
be the carry node

Still carry = 1
if (carry != 0)
add new node
at head.

head.value = sum % 10
carry = sum / 10

{ sum = head.val +
carry }
(2)

head

PartVIII.java

```
public static LLNode<Integer> add1(LLNode<Integer> head){
```

```
    int carry = addOneOpt(head);
```

```
    if (carry > 0){
```

```
        LLNode<Integer> c = new LLNode<Integer>(carry);
```

```
        c.next = head;
```

```
        head = c;
```

```
}
```

```
    return head;
```

```
}
```

```
private static int addOneOpt(LLNode<Integer> head) { 2 us
```

```
    if (head == null) return 1;
```

```
    int carry = addOneOpt(head.next);
```

```
    int sum = head.value + carry;
```

```
    head.value = sum % 10;
```

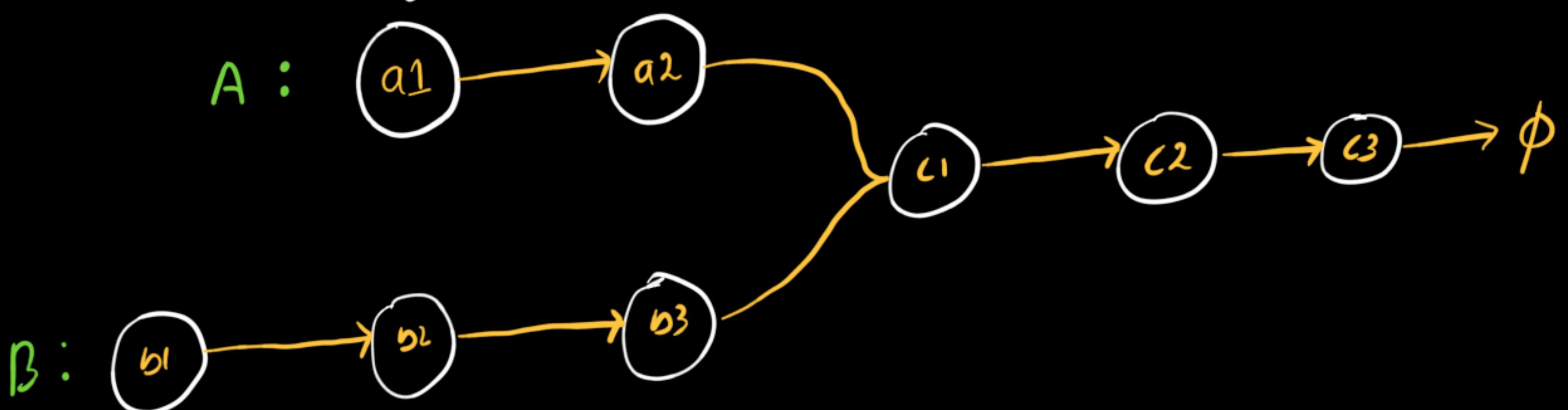
```
    return sum / 10;
```

```
}
```

Tc : O(N)

Sc : O(N)

→ Intersection of two linked list



→ Approach - 1

- we can add one of the linked list in SET
- then traverse the second list, & the moment we find a node already in set i.e our intersection point.

```

PartIX.java
public static @Nullable LLNode<Integer> getIntersectionNode(LLNode<Integer> headA, LLNode<Integer> headB) {
    Set<LLNode<Integer>> set = new HashSet<>();
    LLNode<Integer> ll = headA;

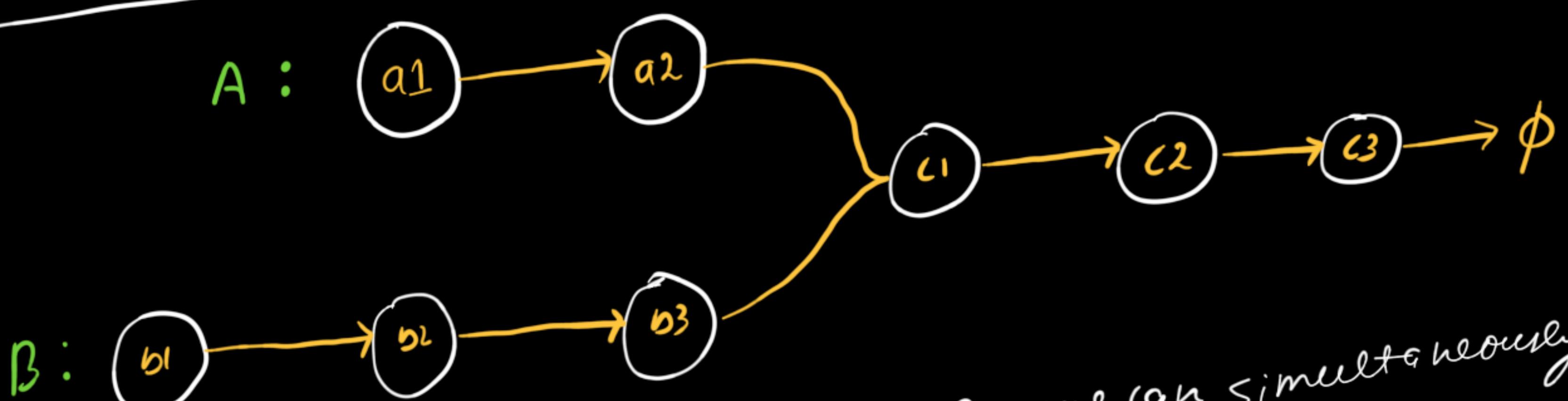
    while (ll != null) {
        set.add(ll);
        ll = ll.next;
    }
    LLNode<Integer> temp = headB;

    while (temp != null) {
        if (set.contains(temp)) {
            return temp;
        }
        temp = temp.next;
    }
    return null;
}

```

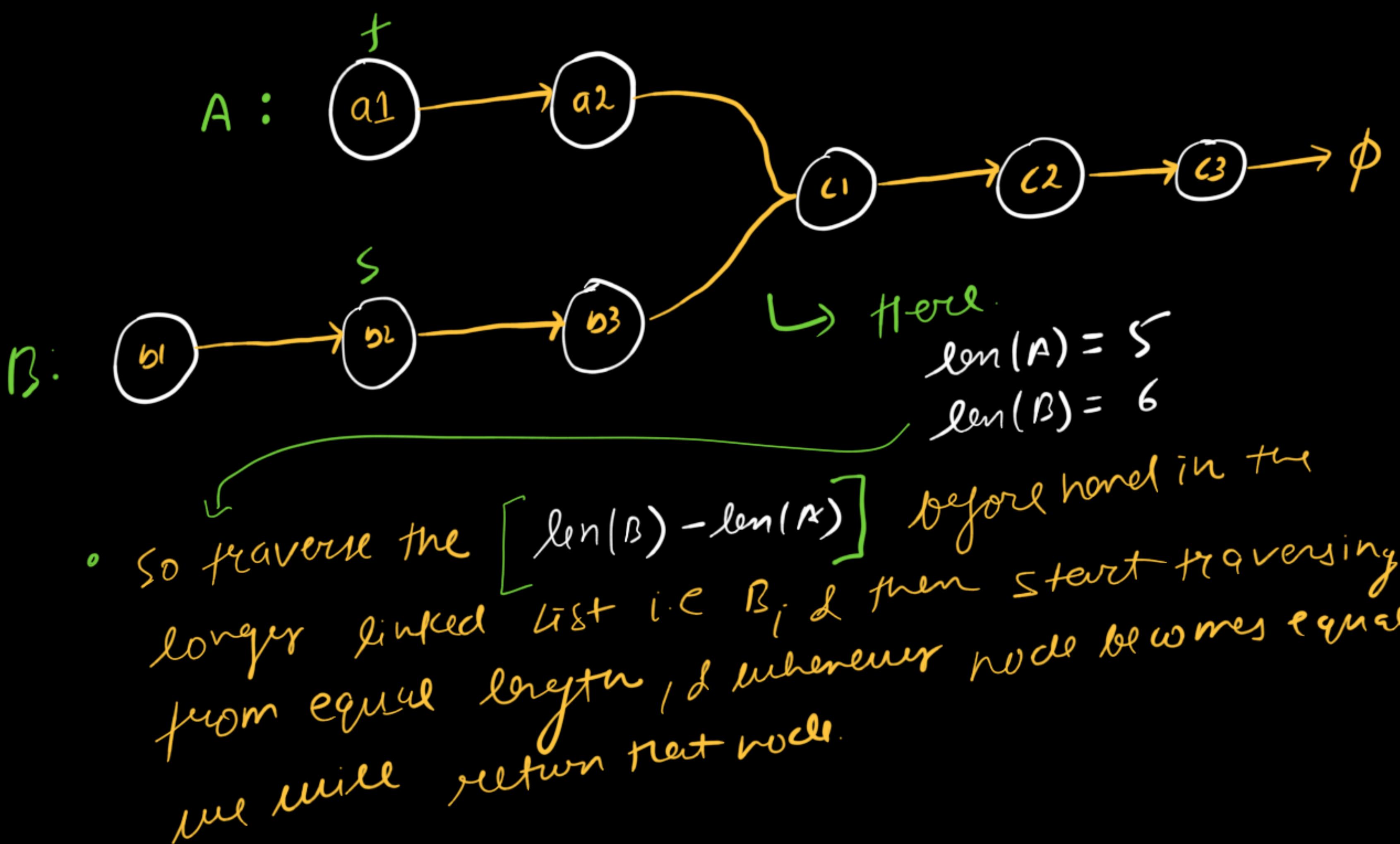
$O(l_1)$ \rightarrow length of 1st LL
 $O(l_2)$ \rightarrow length of 2nd LL
 $T.C: O(l_1 + l_2)$
 $S.C: O(l_1)$

→ Approach - 2



- ① if length of A == length of B, we can simultaneously traverse & if we find common value i.e our intersection point.

- ② what if $\text{len}(A) > \text{len}(B)$ || $\text{len}(A) < \text{len}(B)$?
- ↳ traverse the length difference in longer part of the LL & then traverse & find the intersection point.



```

PartIX.java
public static LLNode<Integer> getInter(LLNode<Integer> a, LLNode<Integer> b) { 1 us;
    if (a == null || b == null) return null;
    int lenOfA = getLen(a);
    int lenOfB = getLen(b);          O(a+b)

    if (lenOfA > lenOfB) {
        int diff = lenOfA - lenOfB;      O(b-a)
        while (diff-- > 0) a = a.next;
    } else {
        int diff = lenOfB - lenOfA;
        while (diff-- > 0) b = b.next;
    }
    return intersection(a, b);      O(min(a,b))
}

@Contract(...)
private static LLNode<Integer> intersection(LLNode<Integer> f, LLNode<Integer> s) {

    while (f != null && s != null) {
        if (f == s) {
            return f;
        }
        f = f.next;
        s = s.next;
    }
    return null;
}

@Contract(pure = true)
private static int getLen(LLNode<Integer> head) { 2 usages new *
    int len = 0;

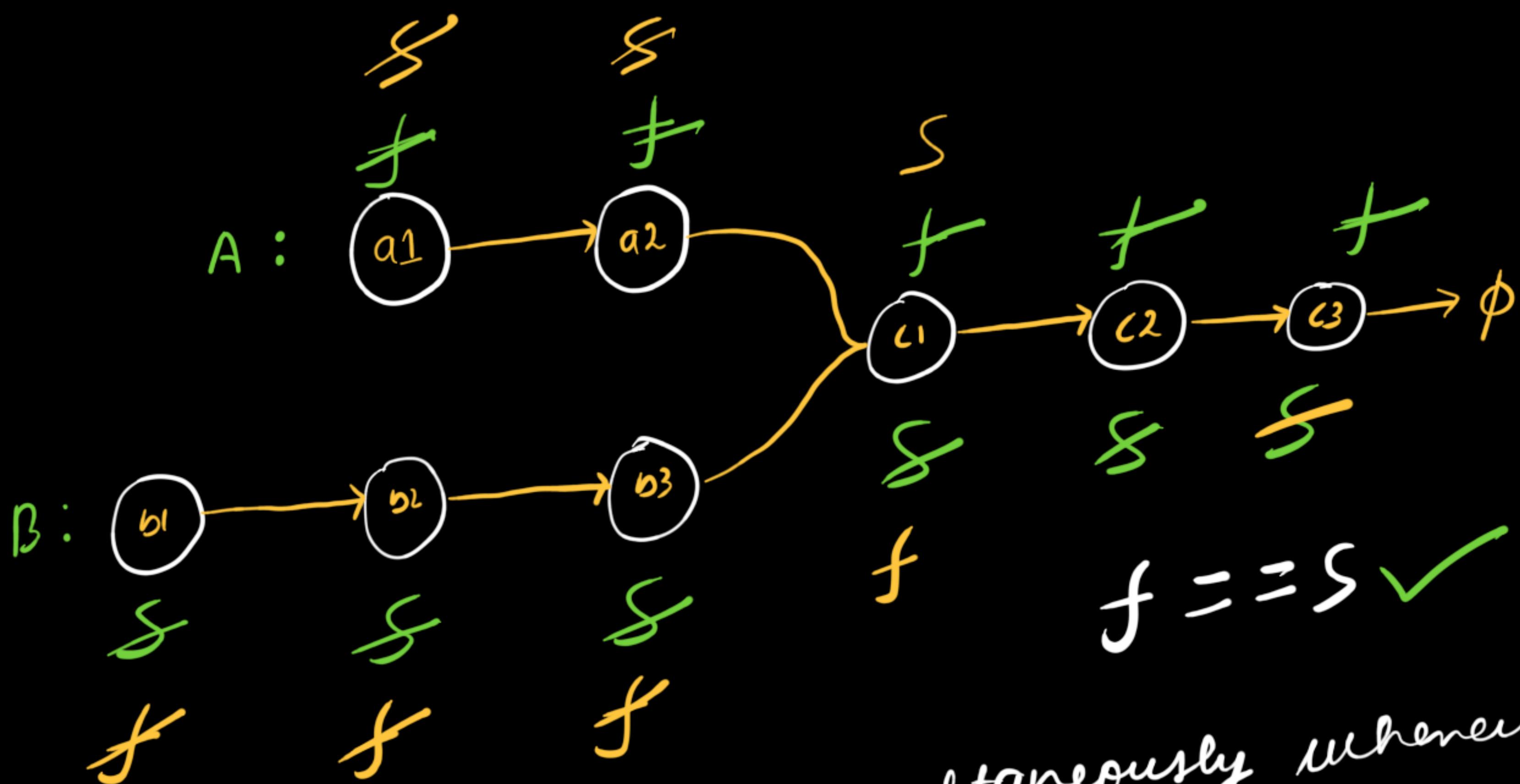
    LLNode<Integer> temp = head;
    while (temp != null) {
        len++;
        temp = temp.next;
    }

    return len;
}

```

TC: $O(a+b+b-f+min(a,b))$
TC: $O(2b+min(a,b))$
SC: $O(1)$

→ Approach-3



1) Traverse both list simultaneously whenever one list reaches null switch to the second list, & vice versa At one point they will intersect & we will return the node.

```
PartIX.java
public static LLNode<Integer> interOpt(LLNode<Integer> a , LLNode<Integer> b){
    if (a == null || b == null) return null;
    LLNode<Integer> f = a;
    LLNode<Integer> s = b;

    while (f != s){
        f = f == null ? b : f.next;
        s = s == null ? a : s.next;
    }

    return f;
}
```

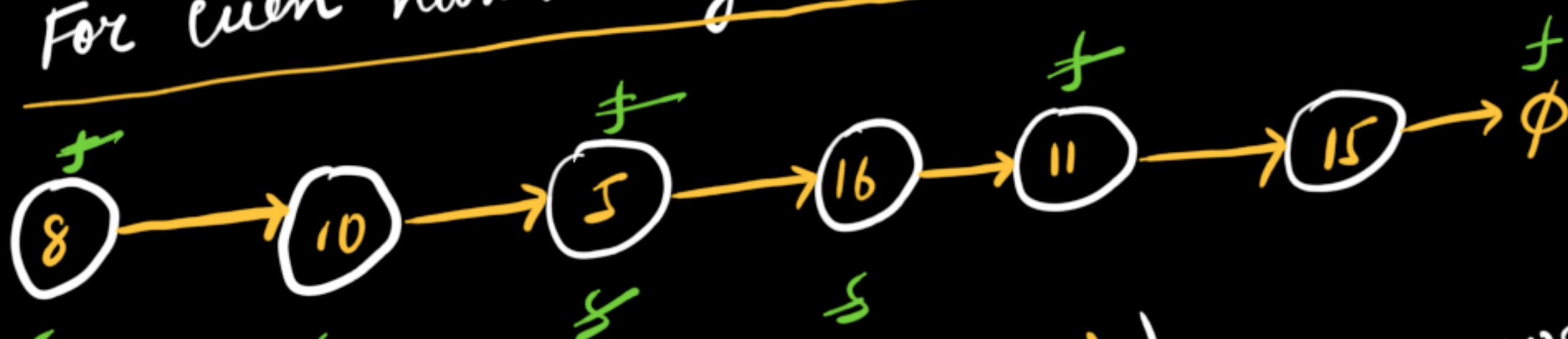
TC: $O(N)$

SC: $O(1)$

- Find middle of the linked list (Tortoise & 1)
- Given the head of the singly linked list, return the middle node.
- For odd number of nodes
-
- $slow = slow.next;$
 $fast = fast.next.next;$

- when ($fast.next \neq null$)
↳ slow is the middle node

- For even numbers of Nodes



- while ($fast \neq null$)
↳ slow is the middle node

PartX.java

```
public static LLNode<Integer> middleNode(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;

    LLNode<Integer> fast = head;
    LLNode<Integer> slow = head;

    while (fast != null && fast.next != null){
        slow = slow.next;
        fast = fast.next.next;
    }

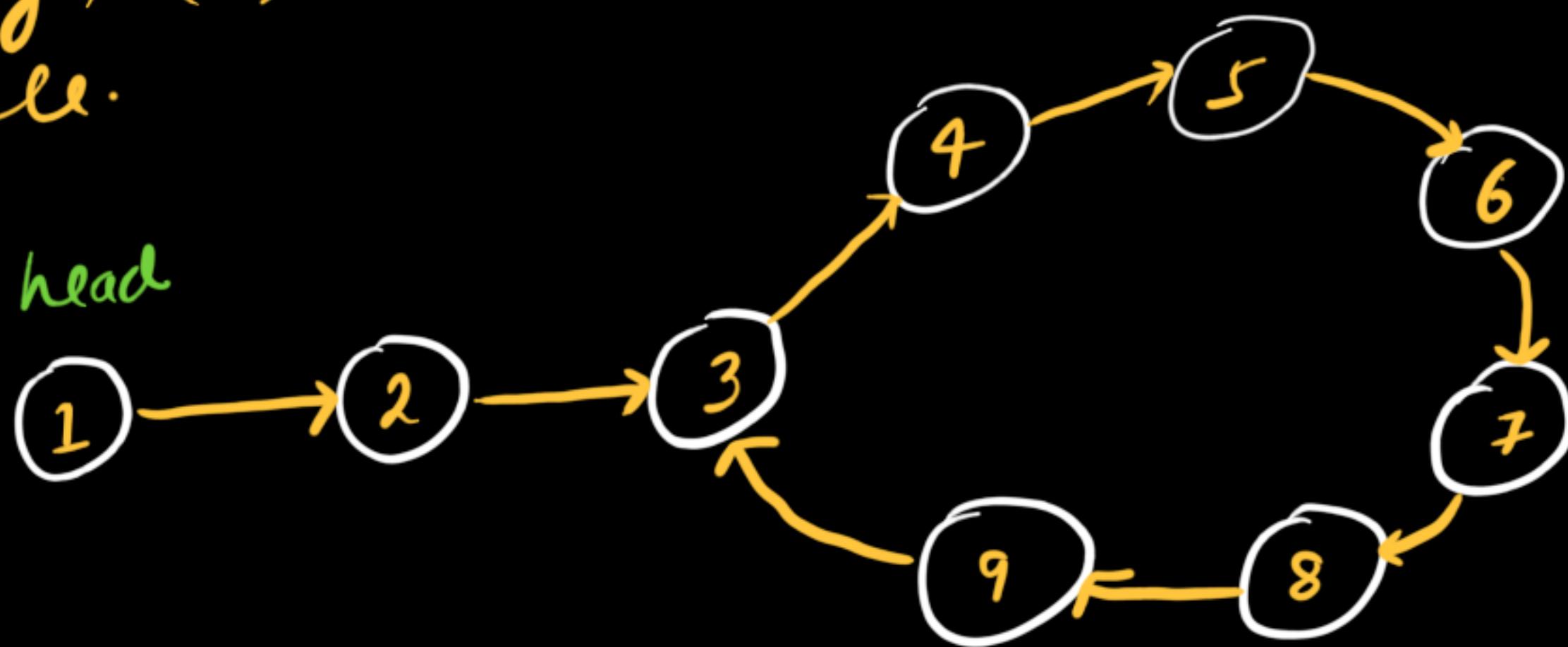
    return slow;
}
```

TC: $O(N/2)$

SC: $O(1)$

→ Detect a Loop or cycle in linked list

↳ Given head of the linked list, return true if it contain a cycle.



→ Approach-1

↳ we set to check if new node being inserted is already visited or not? ↳ does have cycle.

↳ if visited → return true
!visited → return false.

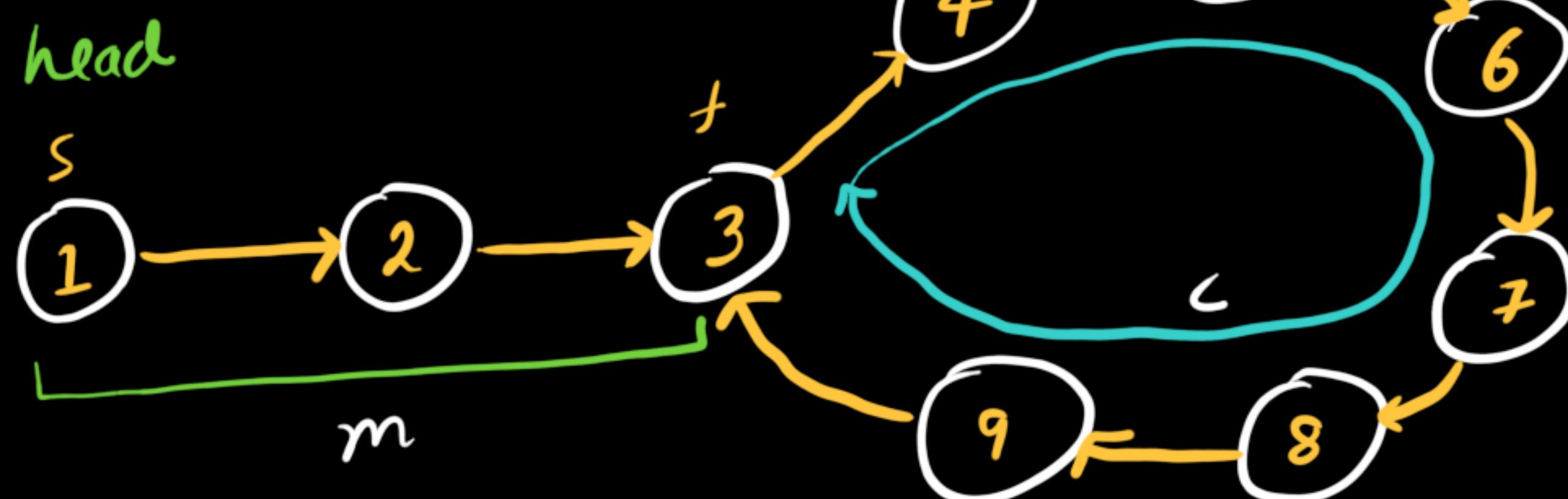
PartXI.java

```
public static boolean containsCycle(LLNode<Integer> head) {  
    if (head == null || head.next == null) return false;  
  
    Set<LLNode<Integer>> set = new HashSet<>();  
    LLNode<Integer> temp = head;  
  
    while (temp != null) {  
        if (set.contains(temp)) return true;  
        else set.add(temp);  
        temp = temp.next;  
    }  
    return false;  
}
```

$Tc: O(N)$

$Sc: O(N)$

→ Approach-2



m = number of nodes before the cycle starts

c = length of the cycle

s = slow pointer moves one step i.e. $\{ \text{slow} = \text{slow}.next \}$

f = fast pointer moves two steps i.e. $\{ \text{fast} = \text{fast}.next.next \}$

$$\boxed{f = 2s} \quad \textcircled{1}$$

- They both started at head. The distance travelled by both pointers must differ by a multiple of the cycle length (since once inside the cycle, any multiple of c brings you back to the same position)

$$\boxed{f - s = nc} \quad \textcircled{2} \quad \text{for } n \geq 1$$

Putting $\textcircled{1}$ in $\textcircled{2}$,

$$2s - s = nc$$

$$\boxed{s = nc}$$

- slow pointer has moved nc steps
- fast pointer has moved $2nc$ steps

→ Interpretation

- out of nc steps, the first m steps are before the cycle begins.
- The remaining $(nc - m)$ steps are within the cycle.

TC: $O(N/2)$

SC: $O(1)$

```
PartXI.java
public static boolean containsCycleOpt(LLNode<Integer> head) {
    if (head == null || head.next == null) return false;

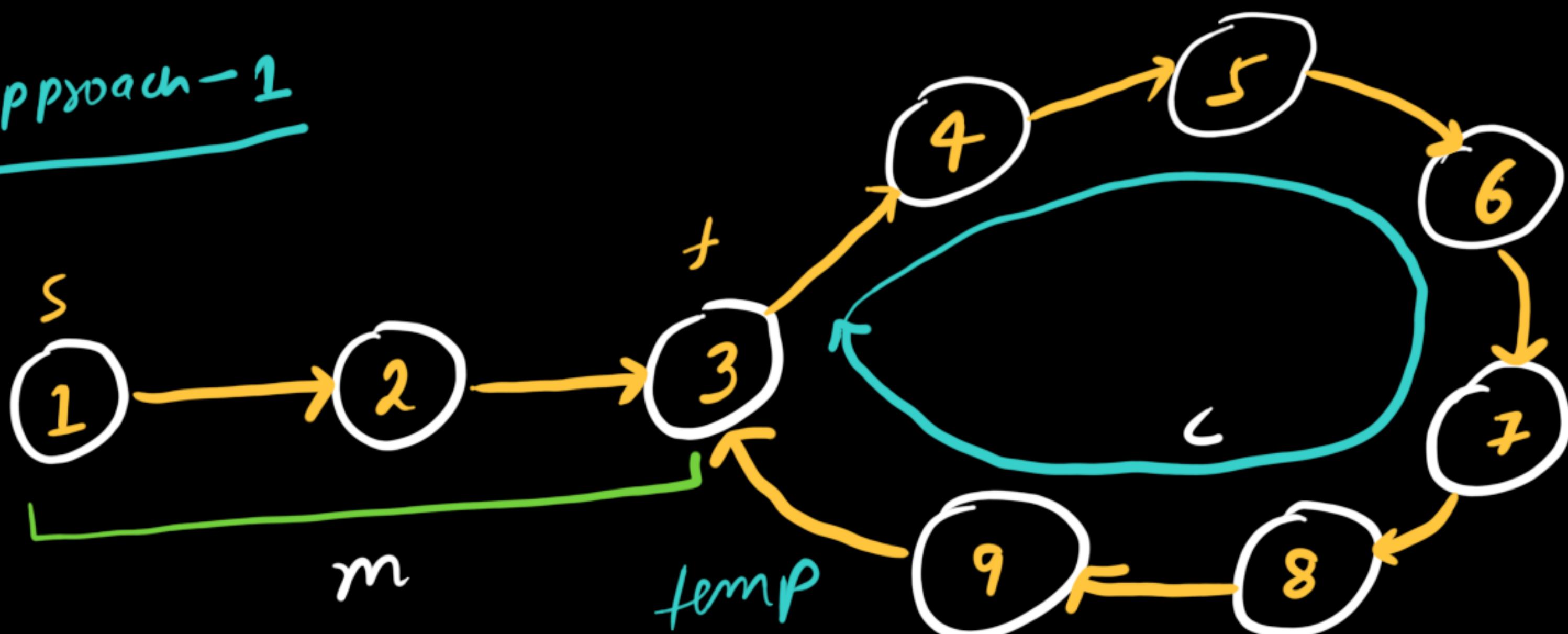
    LLNode<Integer> slow = head;
    LLNode<Integer> fast = head;

    while (fast != null && fast.next != null) {
        slow = slow.next;
        fast = fast.next.next;

        if (slow == fast) return true;
    }
    return false;
}
```

→ Find the length of the loop in LinkedList

→ Approach-1



Count = 0

1	(9, 9)
2	(18, 18)
3	(7, 7)
4	(6, 6)
5	(5, 5)
6	(4, 4)
7	(3, 3)
8	(2, 2)
9	(1, 1)

<Node, count>

Again we reach at
Node → ③ so
length of the
linked list is

len = current - count -
map.get(temp)

```
PartXII.java
public static int lengthOfLL(LLNode<Integer> head) {    no
    if (head == null || head.next == null) return 0;

    Map<LLNode<Integer>, Integer> map = new HashMap<>();
    LLNode<Integer> temp = head;
    int count = 0;

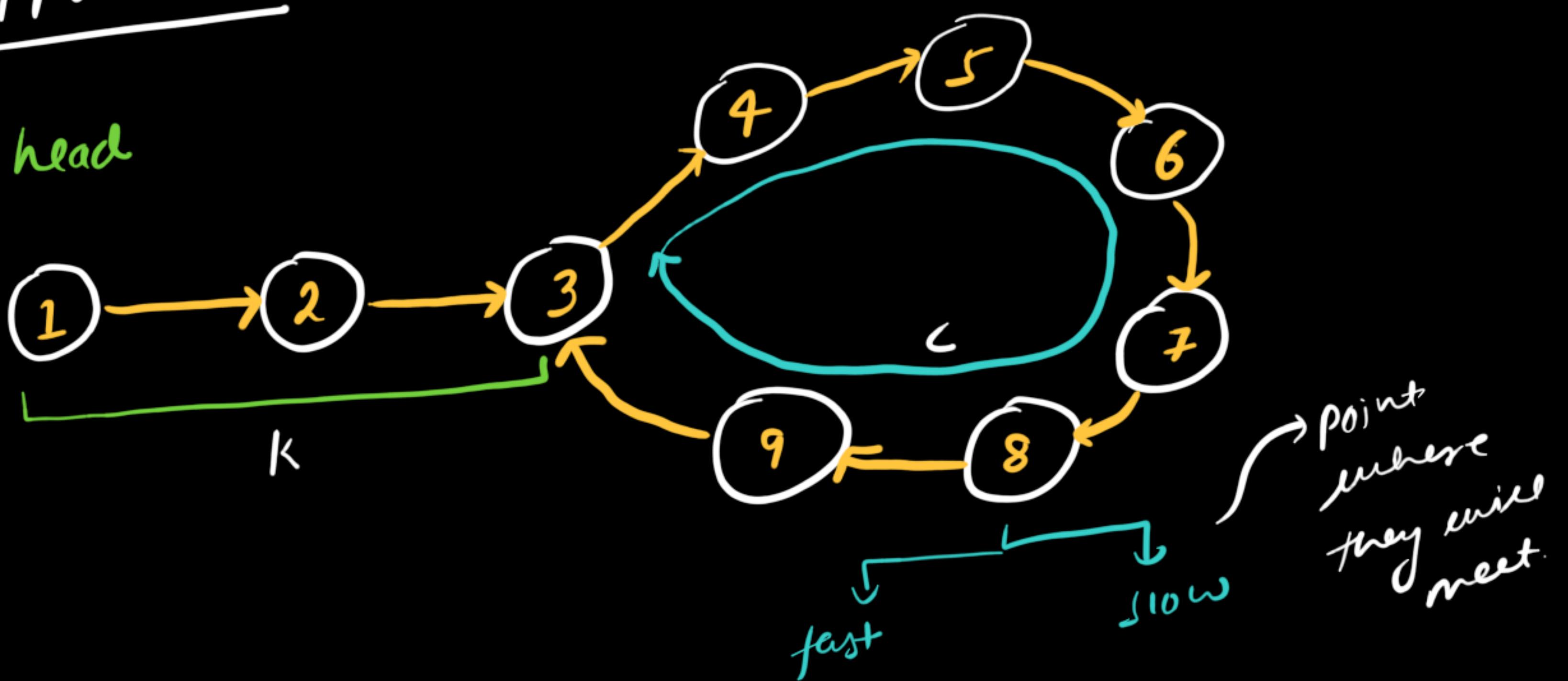
    while (temp != null) {
        if (map.containsKey(temp)) {
            return count - map.get(temp);
        }
        map.put(temp, count);
        temp = temp.next;
        count++;
    }
    return 0;
}
```

TC: O(N)

SC: O(N)

→ Approach-2

head



① Find the point where both pointers fast & slow meets.

② Now again iterate through the cycle, while fast again doesn't meet the slow keep counting.

↳ Initially both fast & slow will be equal, so move fast by 1 & then start the iteration by keeping a count variable, keep on incrementing until fast reaches slow.

Tc: $O(K+c) + O(1) \approx O(N)$

Sc: $O(1)$

```
PartXII.java
public static int lengthOfLLOpt(LLNode<Integer> head) { 1 usage new
    if (head == null || head.next == null) return 0;

    LLNode<Integer> slow = head;
    LLNode<Integer> fast = head;

    while (fast != null && fast.next != null) {
        slow = slow.next;
        fast = fast.next.next;

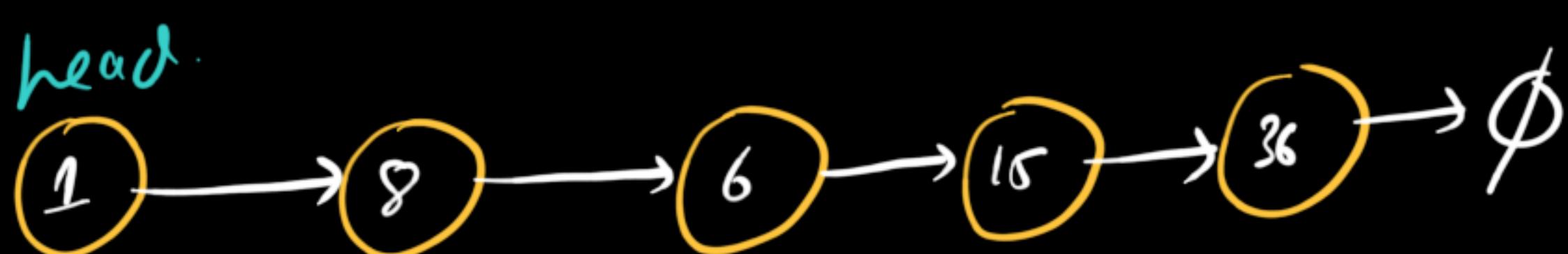
        if (slow == fast) { O(K+c)
            return len(slow, fast);
        }
    }
    return 0;
}

private static int len(LLNode<Integer> slow, LLNode<Integer> fast) {
    int count = 1;
    fast = fast.next;

    while (slow != fast){ no of nodes before cycle starts
        count++;
        fast = fast.next;
    }
    return count;
}
```

$O(c)$ ↳ length of the cycle.

→ delete middle node of the linked list



→ Approach-1

- Find the length of the linked list & divide it by two
- traverse one time less than the $(\text{len}/2)$
- $\text{current-node.next} = \text{current.next.next}$

$$\begin{aligned} \text{TC: } & O(N) + O(N/2) \\ \text{SC: } & O(1) \end{aligned}$$

→ Approach-2

- Apply tortoise & hare algorithm to find middle node.
- Keep a prev node before the middle node.
 - ↳ $\text{prev.next} = \text{slow.next}$,

```
PartXIII.java

public static LLNode<Integer> deleteMiddle(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;

    LLNode<Integer> prev = null;
    LLNode<Integer> slow = head;
    LLNode<Integer> fast = head;

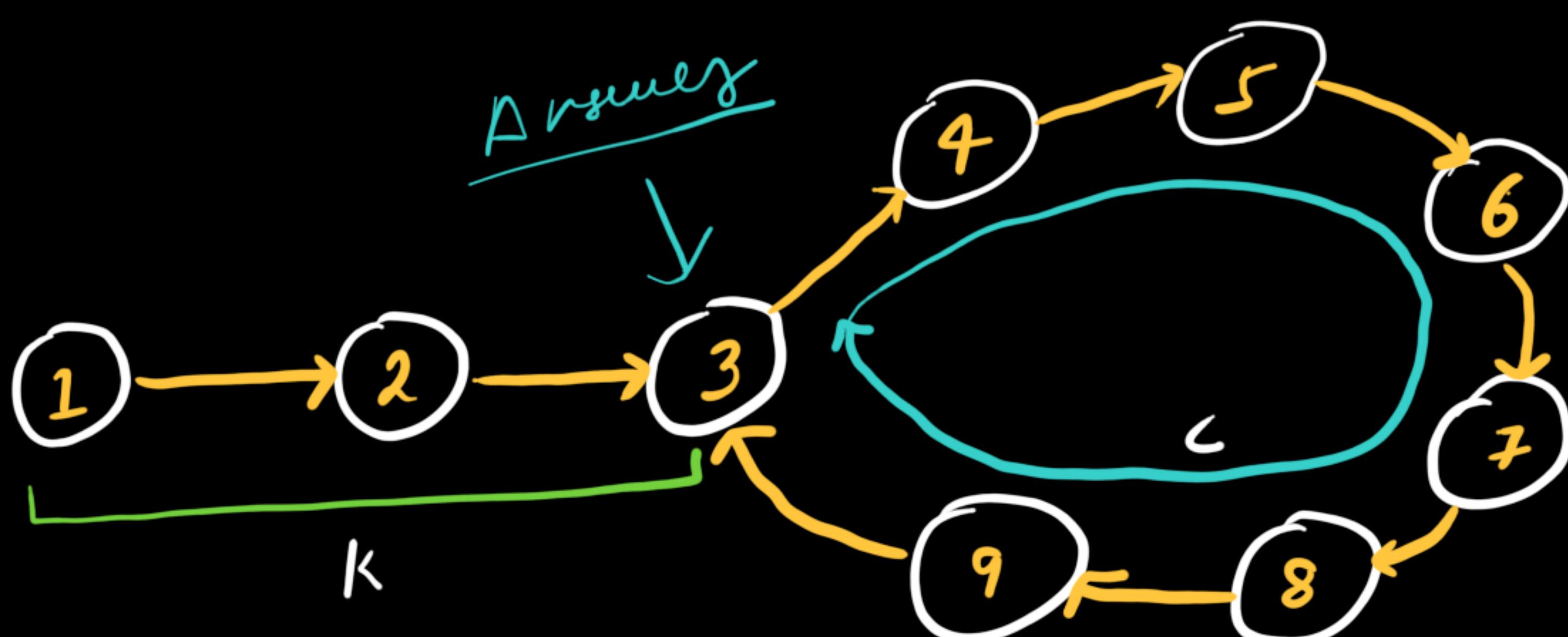
    while (fast != null && fast.next != null){
        prev = slow;
        slow = slow.next;
        fast = fast.next.next;
    }

    prev.next = slow.next;
    return head;
}
```

$$\text{TC: } O(N/2)$$

$$\text{SC: } O(1)$$

→ Find Start of a cycle in LL



→ Approach - 1

- Use set data structure whenever we encounter the same node, we simply return that node.

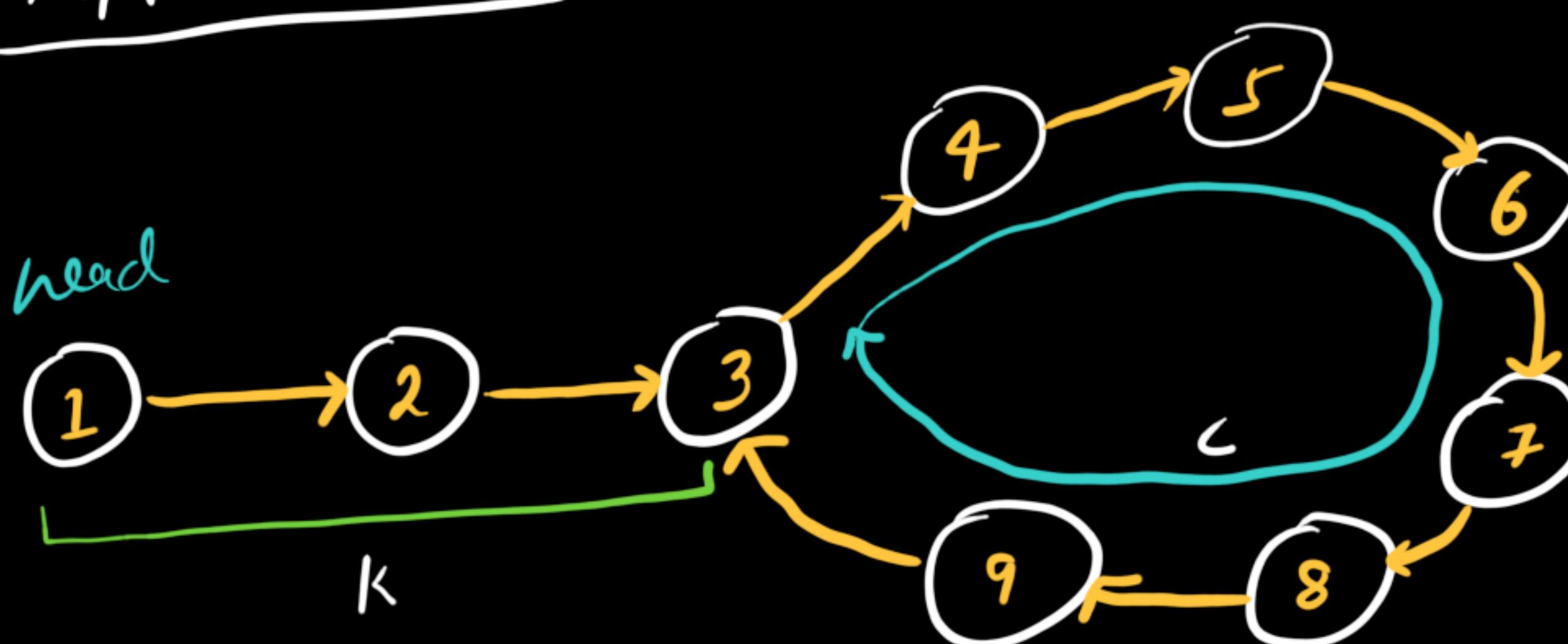
```
PartXIV.java
public static LLNode<Integer> startOfCycle(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;

    Set<LLNode<Integer>> set = new HashSet<>();
    LLNode<Integer> temp = head;

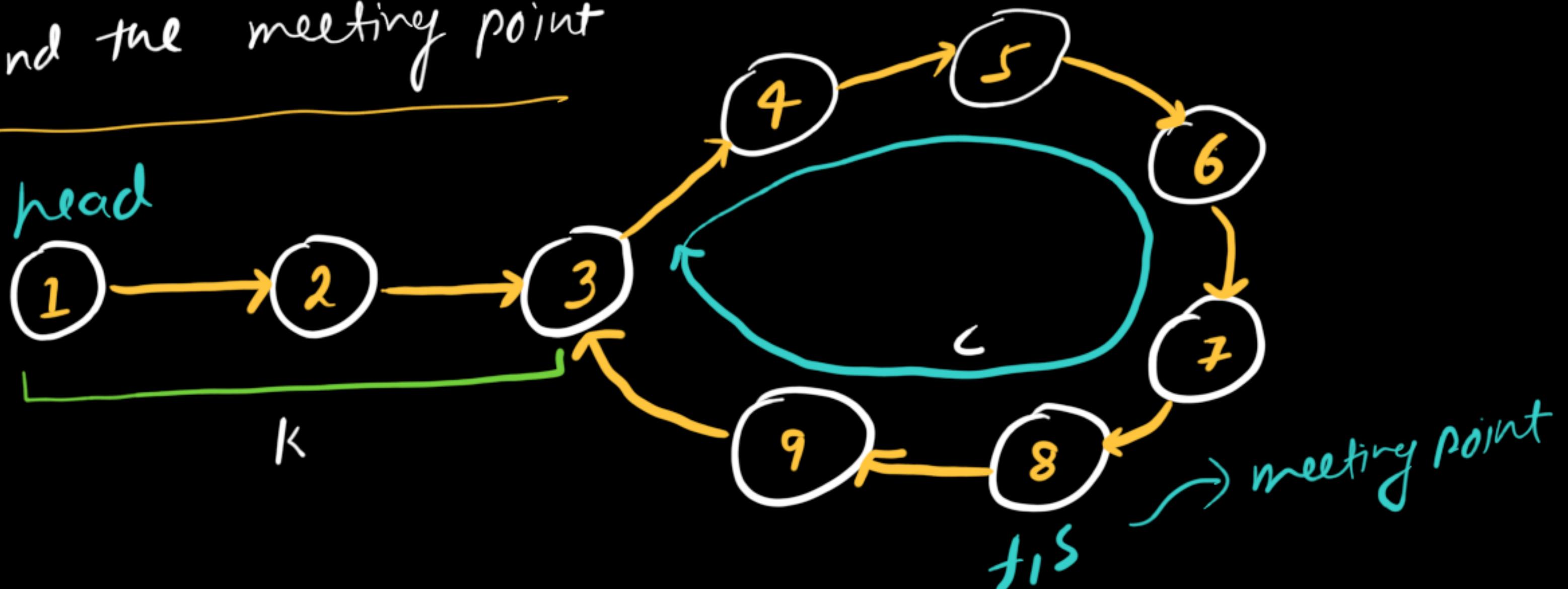
    while (temp != null) {
        if (set.contains(temp)) {
            return temp;
        }
        set.add(temp);
        temp = temp.next;
    }
    return null;
}
```

$TC: O(N)$
 $SC: O(N)$

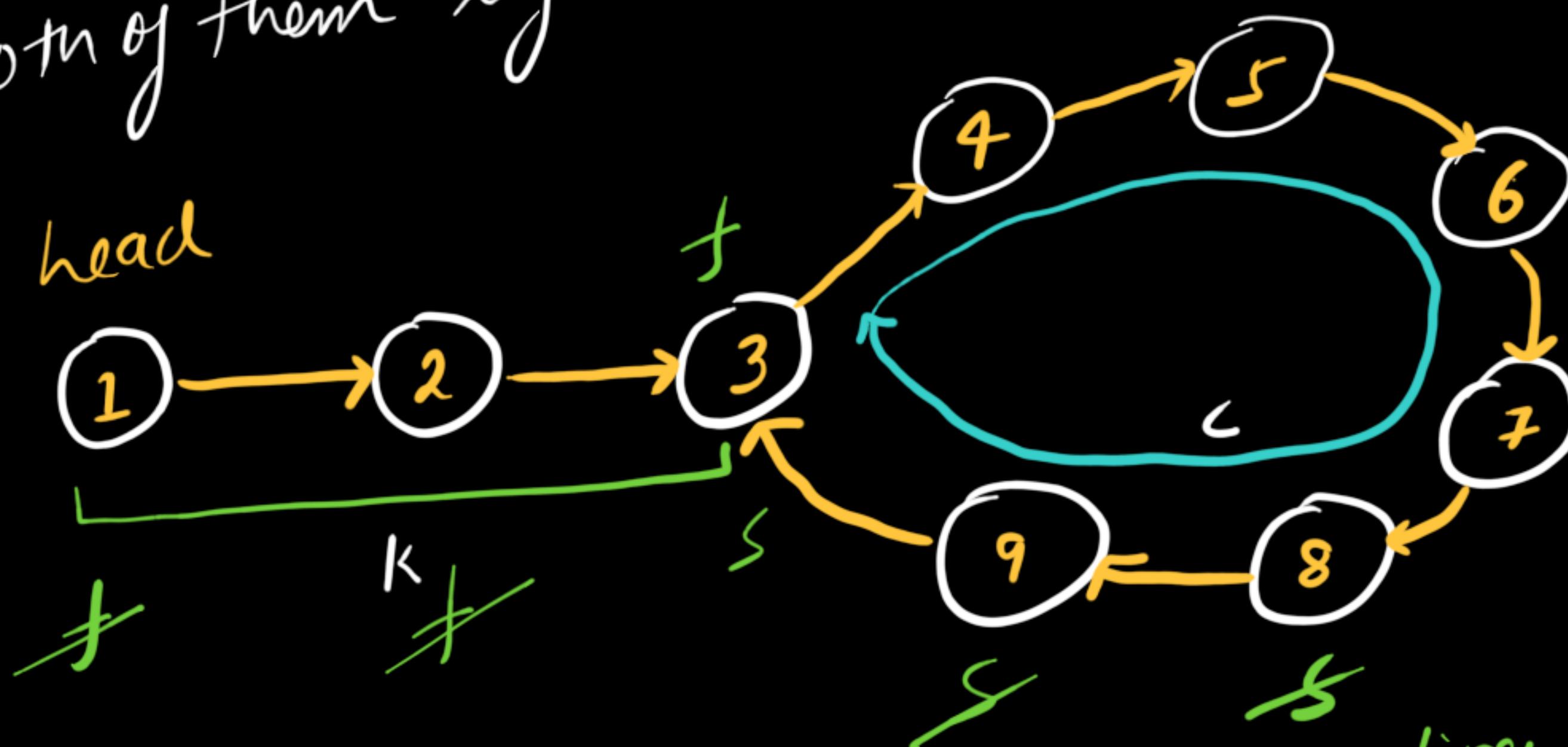
→ Approach - 2



① Find the meeting point



② Reset one of the pointers to head & then traverse both of them by one step.



↳ They will meet at the starting point of the cycle; return any one of them

Tc: O(N)

Sc: O(1)

```
PartXIV.java
public static LLNode<Integer> startOfCycleOpt(LLNode<Integer> head){
    if (head == null || head.next == null) return head;

    LLNode<Integer> slow = head;
    LLNode<Integer> fast = head;

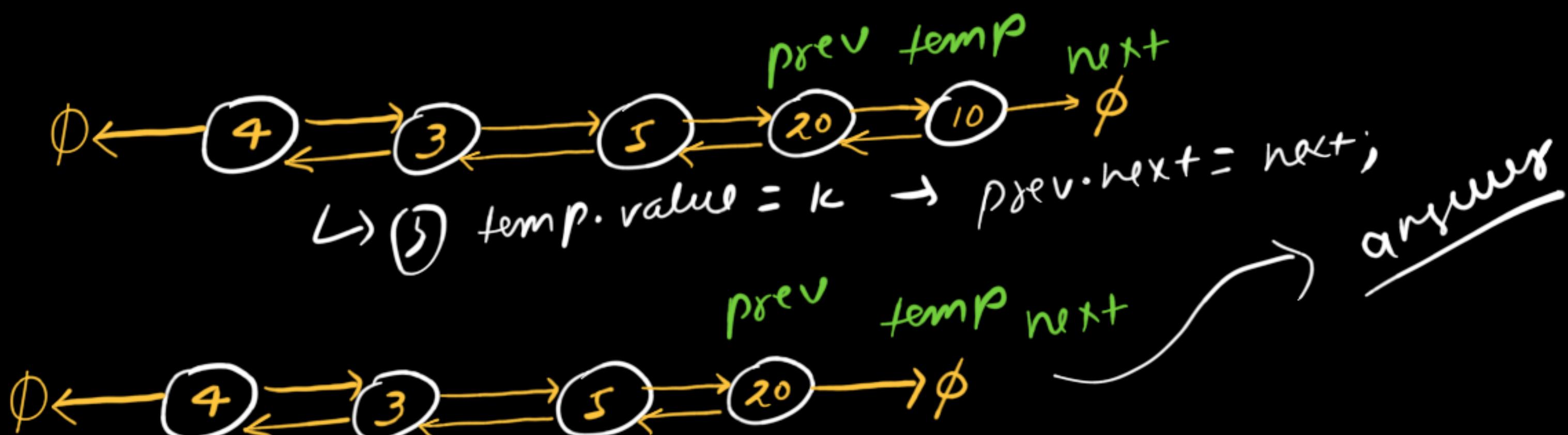
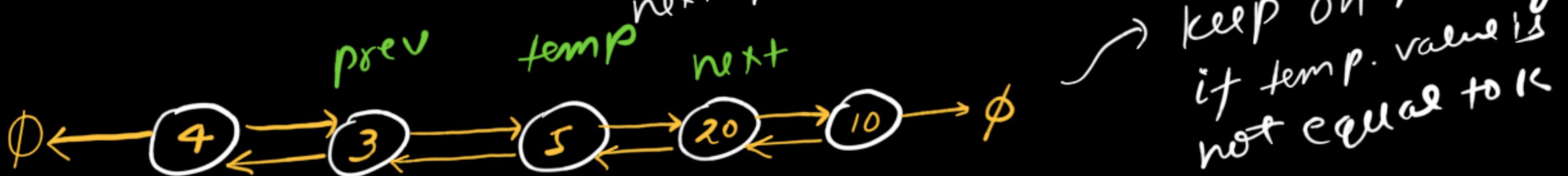
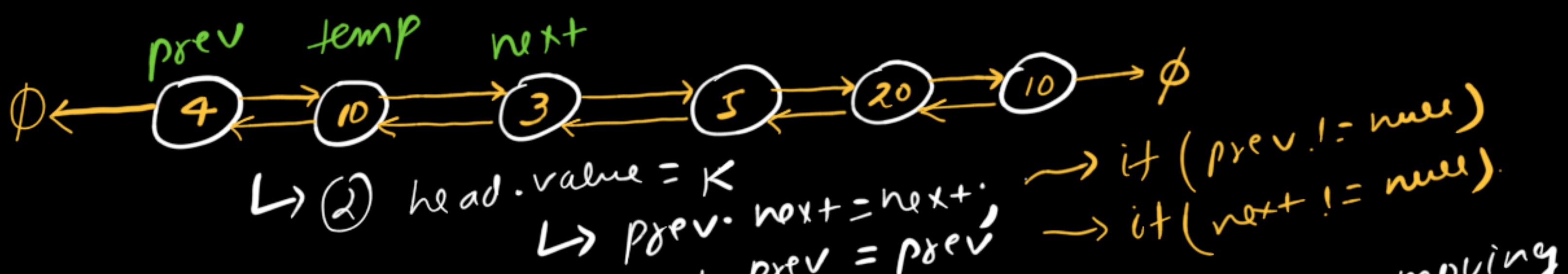
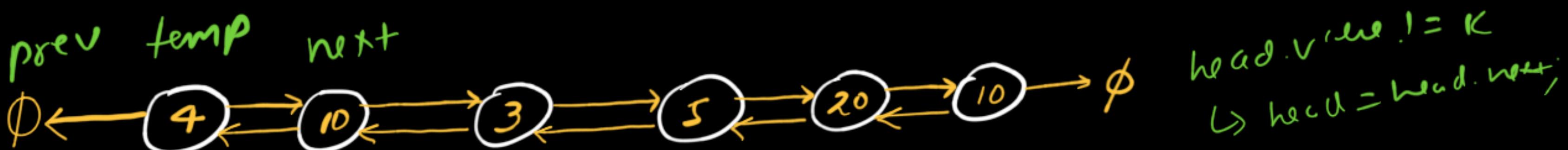
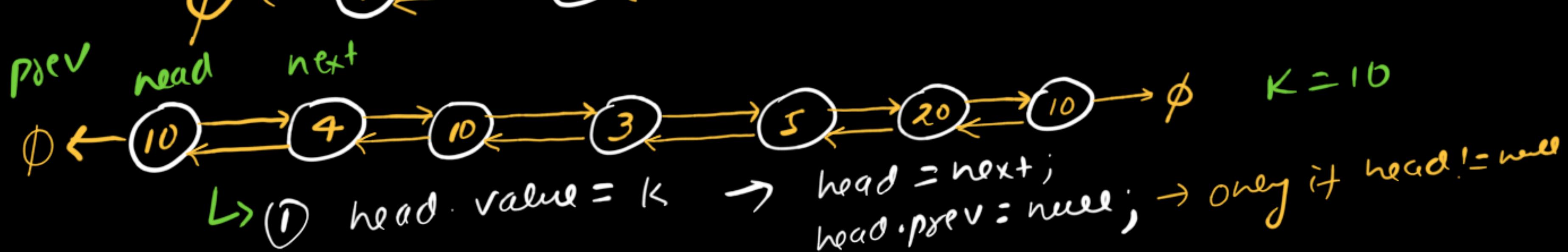
    while (fast != null && fast.next != null){
        slow = slow.next;
        fast = fast.next.next;

        if (slow == fast) break;
    }

    fast = head;

    while (slow != fast){
        slow = slow.next;
        fast = fast.next;
    }
    return fast;
}
```

→ Delete all occurrences of a key in a DLL



$T_C: O(N)$

$SC: O(1)$

```
PartXV.java
public static DLLNode<Integer> deleteAllOccurrences(DLLNode<Integer> head, int k) {
    if (head == null) return null;

    DLLNode<Integer> temp = head;

    while (temp != null) {
        if (temp.value.equals(k)) {
            DLLNode<Integer> prev = temp.prev;
            DLLNode<Integer> next = temp.next;

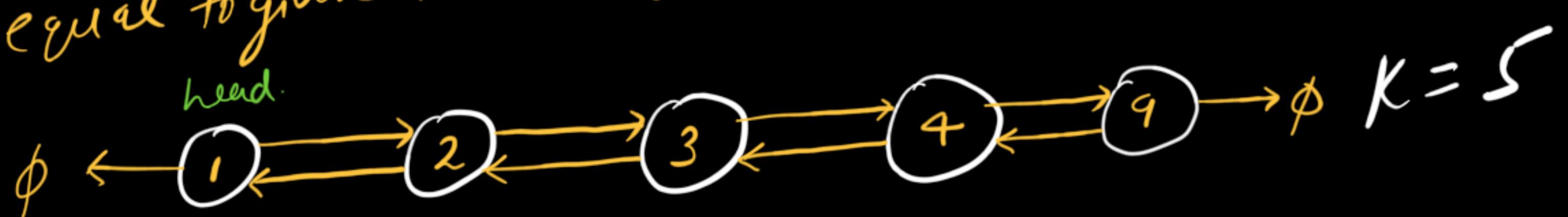
            if (temp == head) {
                head = next;
                if (head != null) head.prev = null;
            } else {
                if (prev != null) prev.next = next;
                if (next != null) next.prev = prev;
            }

            temp = next;
        } else {
            temp = temp.next;
        }
    }

    return head;
}
```

→ Find pairs with given sum in sorted DLL

Given sorted doubly linked list of positive distinct elements, the task is to find pairs in a doubly-linked list whose sum is equal to given value target.



→ Approach-1

- iterate over the doubly linked list & check each time if $t \cdot \text{value} + s \cdot \text{value} \leq k$, add it to the data structure

TC: $O(N^2)$

SC: $O(1)$

```
PartXVI.java
public static @NotNull List<Integer[]> findPair(DLLNode<Integer> head, int k) {
    DLLNode<Integer> temp = head;
    List<Integer[]> ans = new ArrayList<>();

    while (temp != null){
        DLLNode<Integer> s = temp.next;

        while (s != null && temp.value + s.value <= k){
            if (temp.value + s.value == k){
                ans.add(new Integer[]{temp.value, s.value});
            }
            s = s.next;
        }
        temp = temp.next;
    }
    return ans;
}
```

→ Approach-2

- insert node value as key & temp node as value in hashmap.
- $\text{target} = k - \text{temp.value}$, if target is present inside map, then we have one of our pair.

```
PartXVI.java
public static @NotNull List<Integer[]> findPairBetter(DLLNode<Integer> head, int k) {
    DLLNode<Integer> temp = head;
    Map<Integer, DLLNode<Integer>> map = new HashMap<>();
    List<Integer[]> ans = new ArrayList<>();

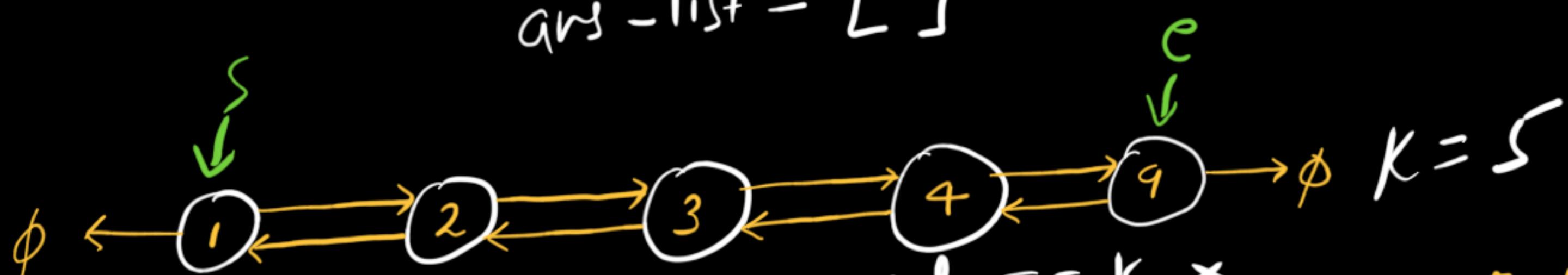
    while (temp != null) {
        Integer target = k - temp.value;
        if (map.containsKey(target)) {
            ans.add(new Integer[]{temp.value, target});
        }
        map.put(temp.value, temp);
        temp = temp.next;
    }
    return ans;
}
```

TC: $O(N)$
SC: $O(N)$

→ Approach-3

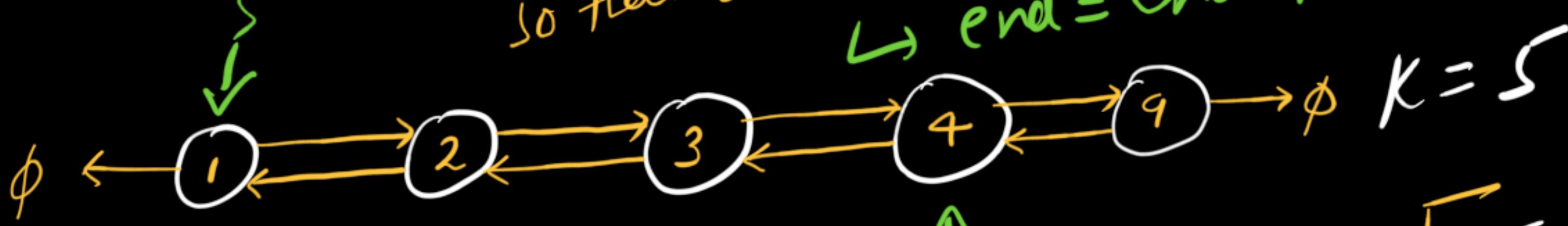
- Since array is sorted we can take advantage of its properties.

$\text{ans-list} = []$



$\hookrightarrow \text{sum} = s.\text{val} + e.\text{val} == K \times$

- If $\text{sum} > K$, we need to decrement e pointer.
So that overall sum decreases.

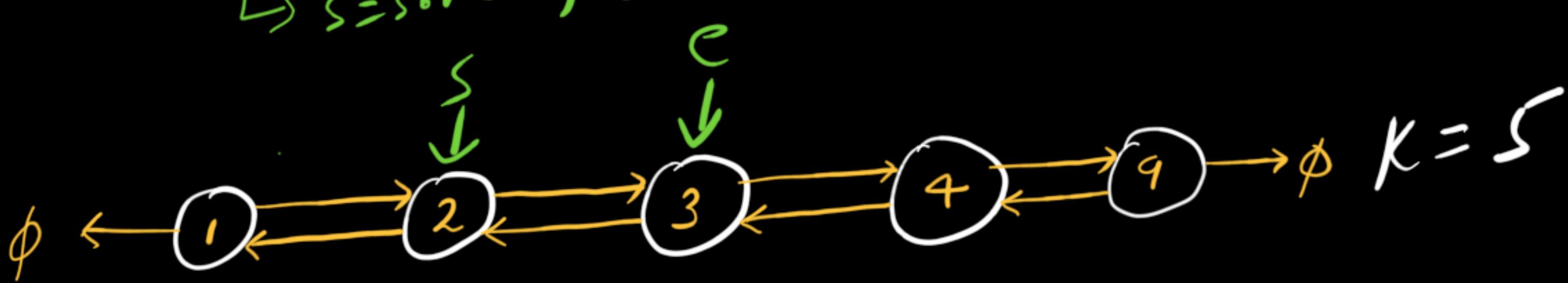


$\hookrightarrow \text{end} = \text{end.prev}$

$\hookrightarrow \text{sum} = s.\text{val} + e.\text{val} == K$ $\text{ans-list} = [[1, 4]]$

- $\text{sum} = s.\text{val} + e.\text{val} == K$

$\hookrightarrow s = s.\text{next}$, $\text{end} = \text{end.prev}$



$\hookrightarrow s = s.\text{next}$, $\text{end} = \text{end.prev}$ $\text{ans} = [[1, 4], [2, 3]]$

TC: $O(N)$
SC: $O(1)$

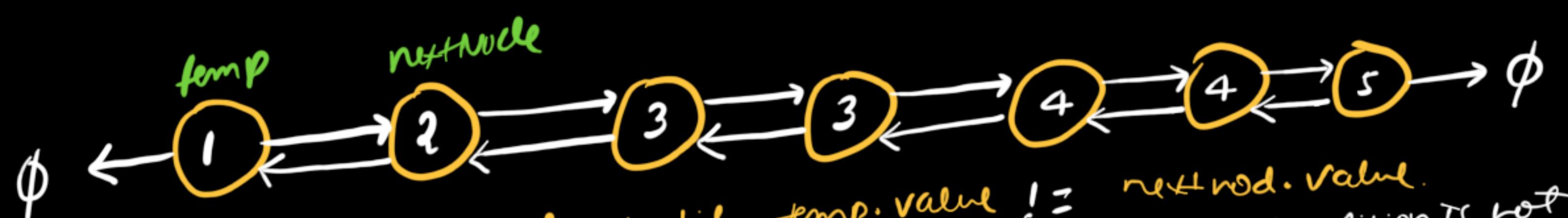
```
PartXVI.java
public static @NotNull List<Integer[]> findPairOpt(DLLNode<Integer> head, int k) {
    DLLNode<Integer> start = head;
    DLLNode<Integer> end = head;
    List<Integer[]> ans = new ArrayList<>();

    while (end.next != null) end = end.next;

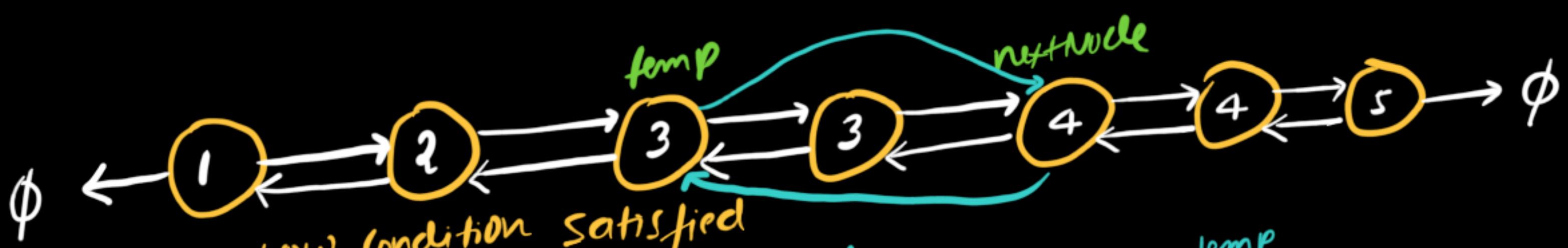
    while (start.value < end.value) {
        int sum = start.value + end.value;

        if (sum == k){
            ans.add(new Integer[]{start.value, end.value});
            start = start.next;
            end = end.prev;
        }
        else if (sum > k){
            end = end.prev;
        }
        else start = start.next;
    }
    return ans;
}
```

→ Remove duplicates from sorted DLL

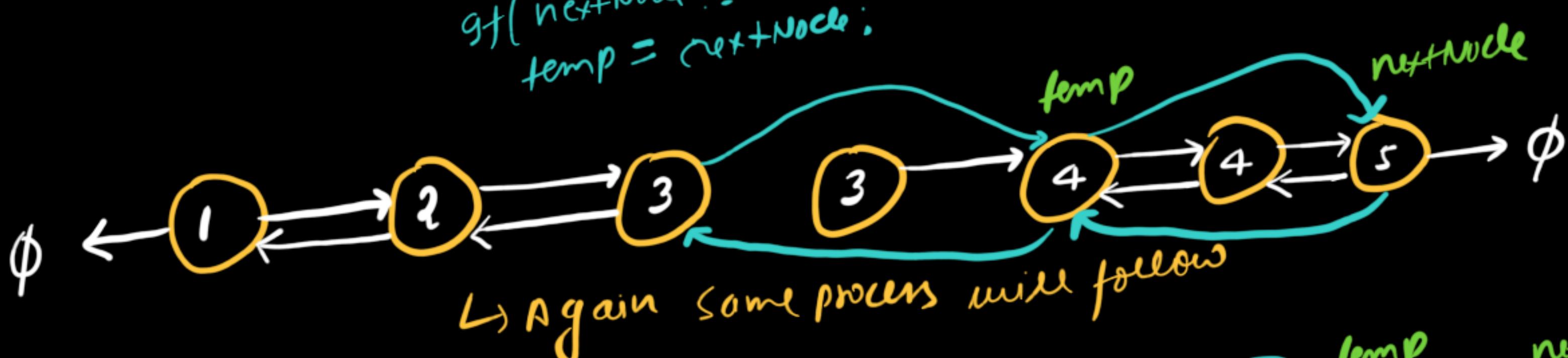


- move nextNode until temp.value != nextNode.value.
- move nextNode one by one until this condition is not satisfied.

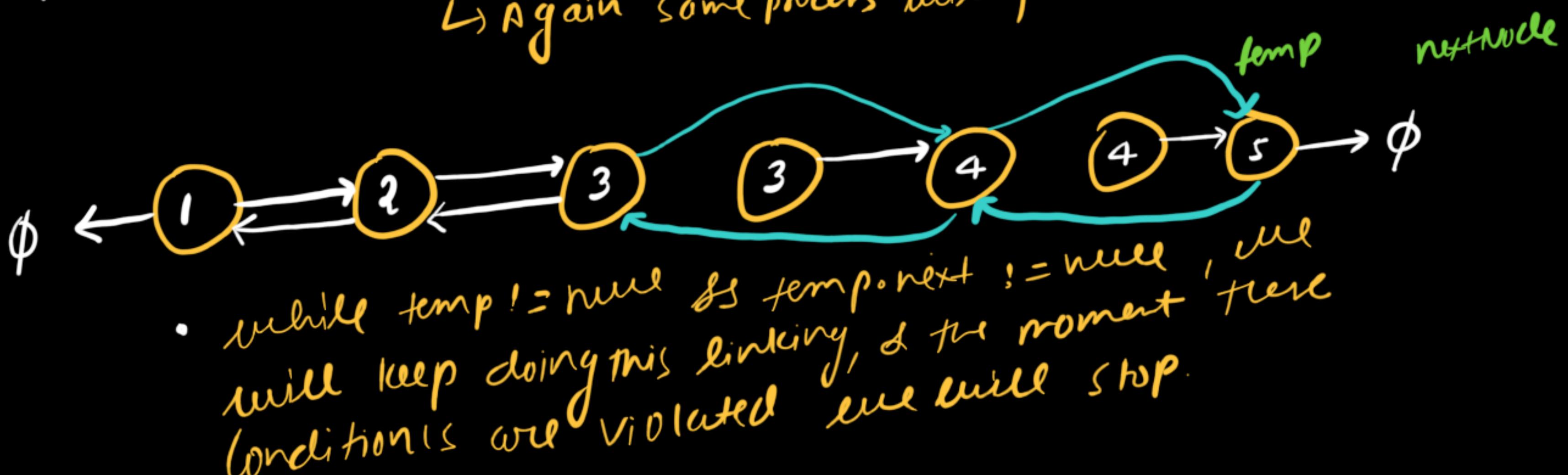


- Now condition satisfied

temp.next = nextNode;
if(nextNode != null) nextNode.prev = temp
temp = nextNode;



↳ Again same process will follow



- while temp != null & temp.next != null, we will keep doing this linking, & the moment this condition is violated we will stop.

```
PartXVII.java
public static DLLNode<Integer> removeDuplicates(DLLNode<Integer> head){
    if (head == null || head.next == null) return head;

    DLLNode<Integer> temp = head;

    while (temp != null && temp.next != null){
        DLLNode<Integer> nextNode = temp.next;

        while (nextNode != null && nextNode.value.equals(temp.value)){
            nextNode = nextNode.next;
        }

        temp.next = nextNode;
        if (nextNode != null) nextNode.prev = temp;
        temp = temp.next;
    }

    return head;
}
```

Tc : O(N)

Sc : O(1)

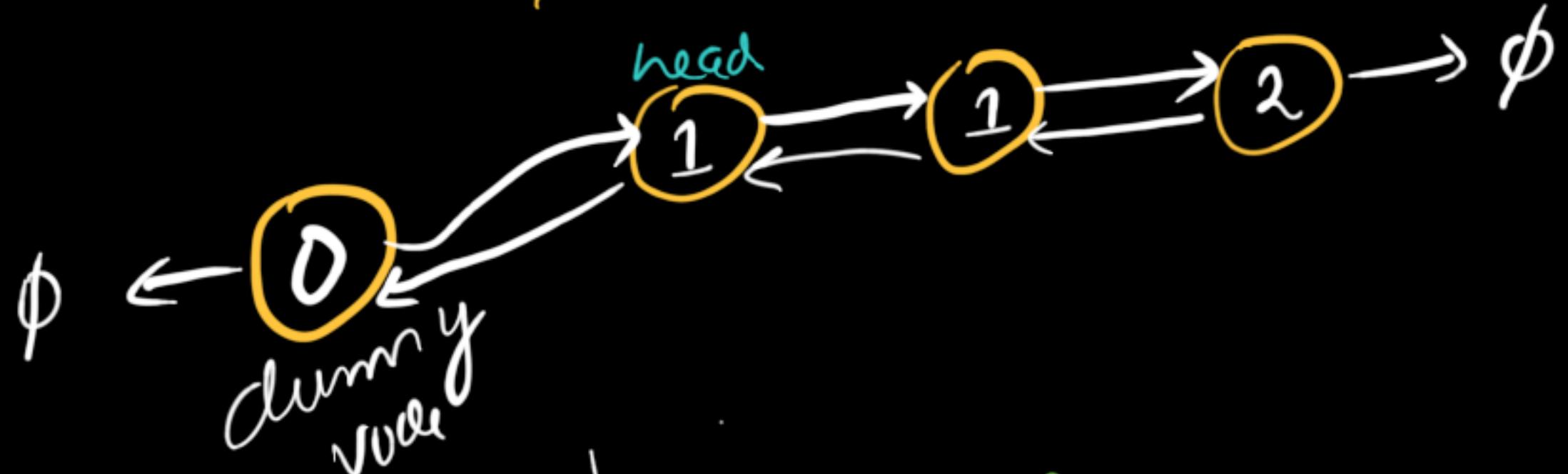
→ Follow up:

→ What if we have to remove all nodes that have duplicate numbers, leaving only distinct numbers from the original list.

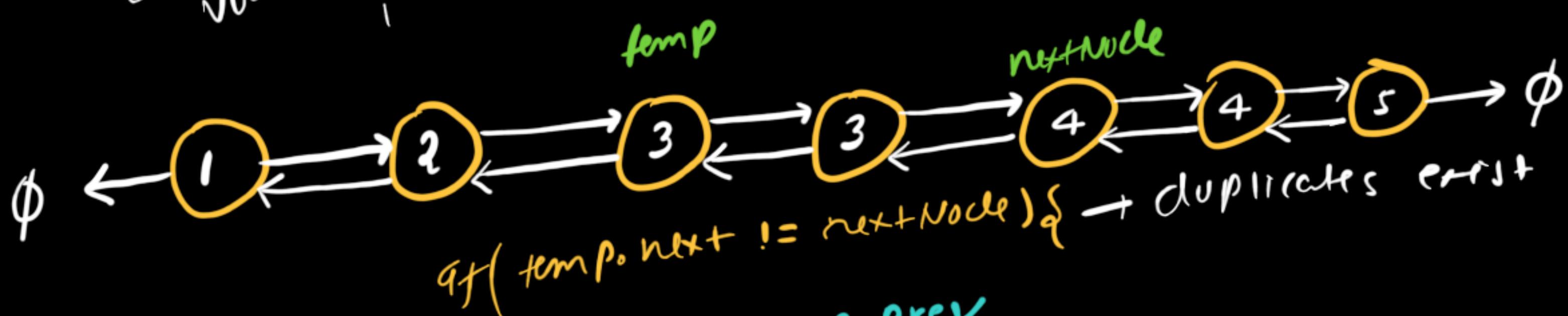
① What if head may get removed?



• To remove head, connect dummy node to the head



`dummy = new Node(0);
dummy.next = head;
head.prev = dummy;`



`prevNode = temp.prev;
prevNode.next = nextNode;
if (nextNode != null) nextNode.prev = prevNode;
temp = nextNode`

`} else {
 temp = temp.next;`

`temp = temp.next;`

`}`

```
PartXVII.java
public static DLLNode<Integer> removeDuplicatesII(DLLNode<Integer> head) {
    if (head == null || head.next == null) return head;

    DLLNode<Integer> dummy = new DLLNode<>( value: 0 );
    dummy.next = head;
    head.prev = dummy;

    DLLNode<Integer> temp = head;

    while (temp != null) {
        DLLNode<Integer> nextNode = temp.next;

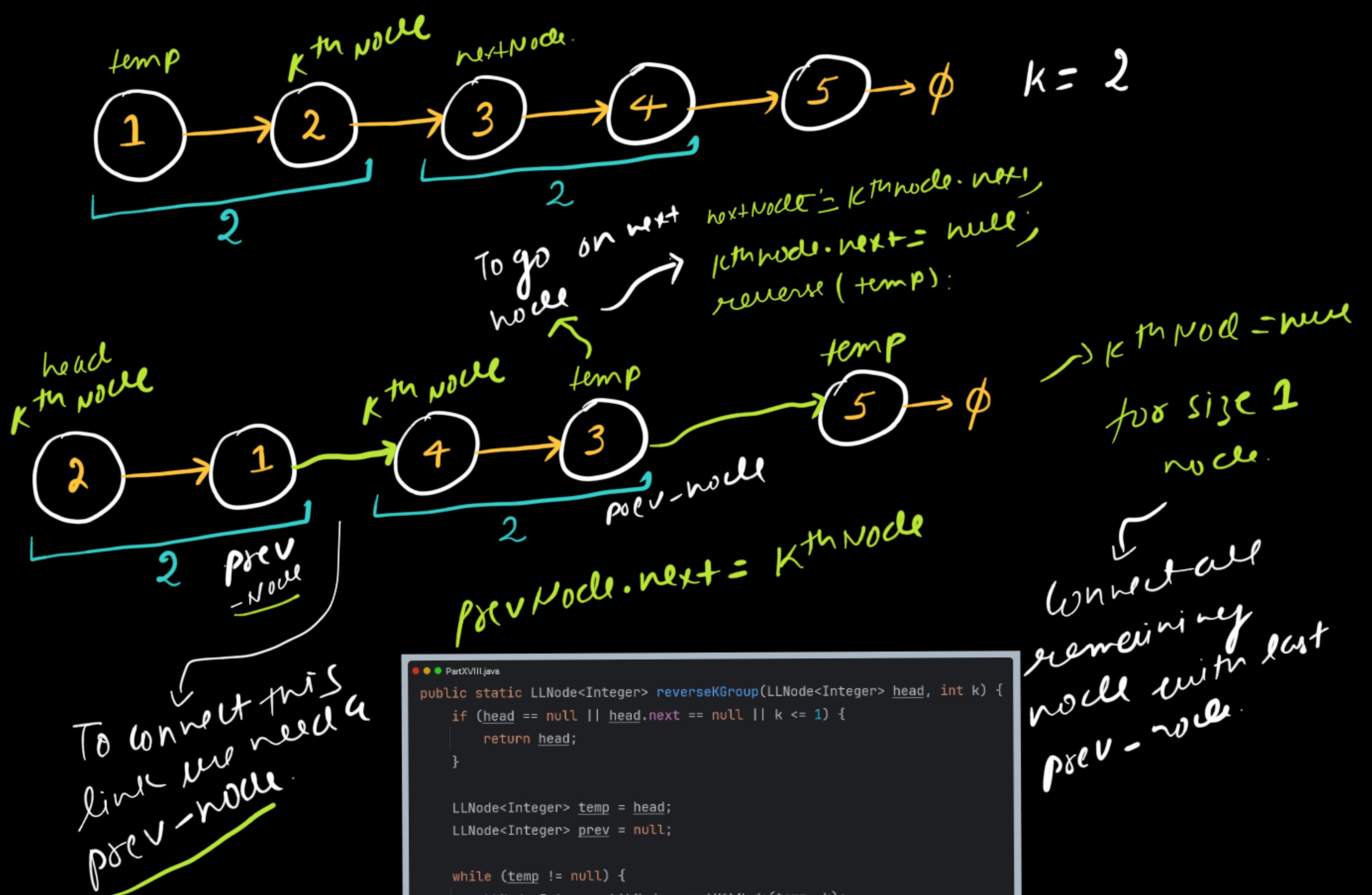
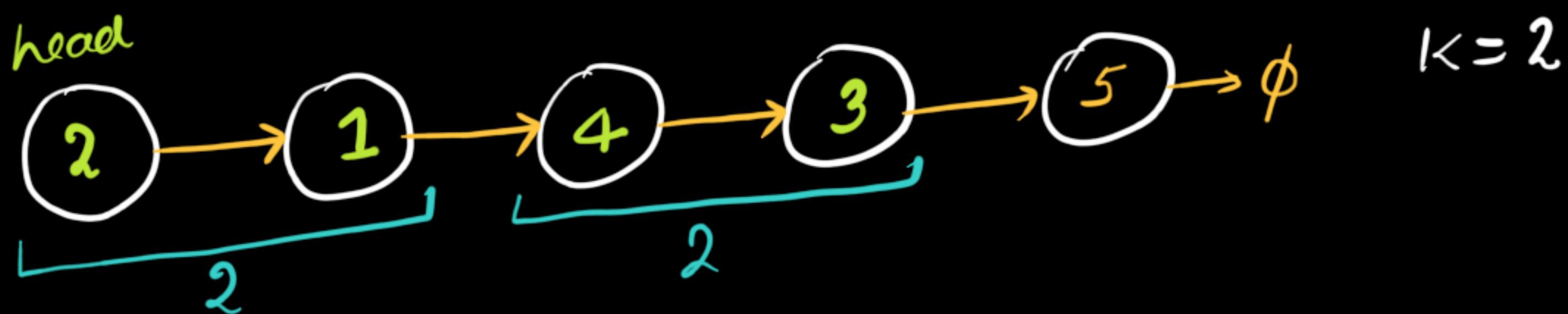
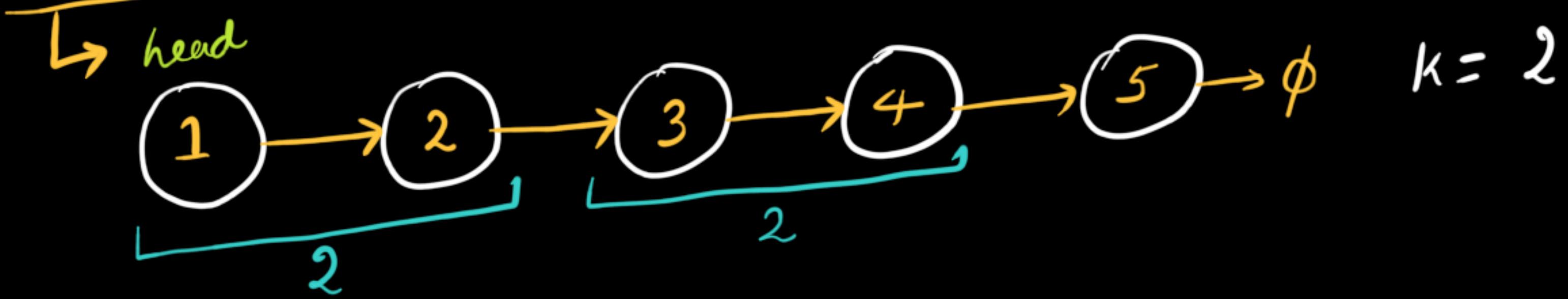
        while (nextNode != null && nextNode.value.equals(temp.value)) {
            nextNode = nextNode.next;
        }

        if (temp.next != nextNode){ // duplicates detected
            DLLNode<Integer> prevNode = temp.prev;
            prevNode.next = nextNode;
            if (nextNode != null) nextNode.prev = temp;
            temp = nextNode;
        }
        else temp = temp.next; // no duplicates
    }
    return head;
}
```

TC: O(N)

SC: O(1)

→ Reverse nodes in k-group



TC: $O(n/k) * O(k)$
 Outer loop for finding k^{th} node

SC: $O(1)$

```

••• PartXVIII.java
public static LLNode<Integer> reverseKGroup(LLNode<Integer> head, int k) {
    if (head == null || head.next == null || k <= 1) {
        return head;
    }

    LLNode<Integer> temp = head;
    LLNode<Integer> prev = null;

    while (temp != null) {
        LLNode<Integer> kthNode = getKthNode(temp, k);
        if (kthNode == null) {
            // connect remainder if less than k nodes left
            if (prev != null) prev.next = temp;
            break;
        }

        LLNode<Integer> nextNode = kthNode.next;
        kthNode.next = null;

        LLNode<Integer> reversedHead = reverseListOpt(temp);

        if (temp == head) head = reversedHead;
        else prev.next = reversedHead;

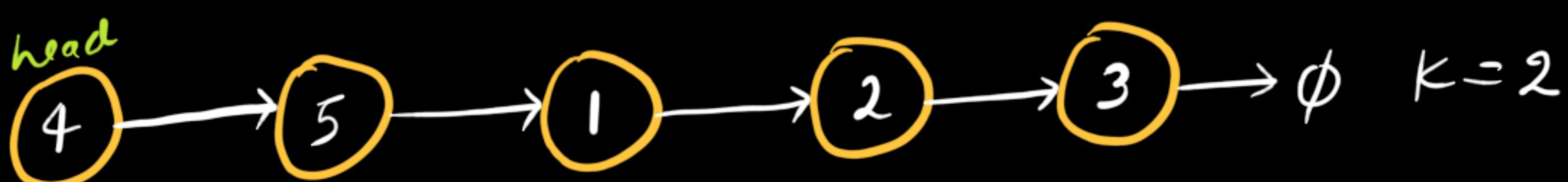
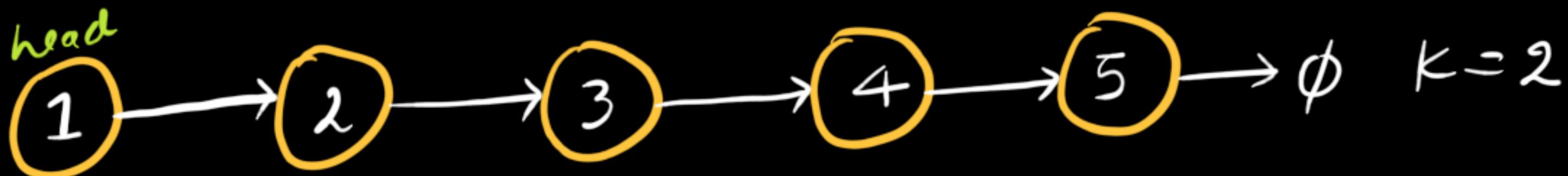
        // temp becomes the tail of the reversed group
        prev = temp;
        temp = nextNode;
    }

    return head;
}

@Contract(pure = true)
private static LLNode<Integer> getKthNode(LLNode<Integer> head, int k) {
    LLNode<Integer> temp = head;
    while (--k > 0 && temp != null) {
        temp = temp.next;
    }
    return temp;
}

```

→ Rotate a list



Steps:

- Count length & point the tail to head to form circle.



- traverse $(len - k)$ nodes i.e $(5 - 2) = 3$ nodes



$new\ head = temp.next$
 $temp.next = null;$

our list is reversed
now

$Tc: O(n)$

$Sc: O(1)$

```

PartXIX.java
public static LLNode<Integer> rotate(LLNode<Integer> head, int k) {
    if (head == null || head.next == null) return head;

    int len = 1;
    LLNode<Integer> temp = head;

    while (temp.next != null) {
        len++;
        temp = temp.next;
    }
    temp.next = head;

    k = k % len;

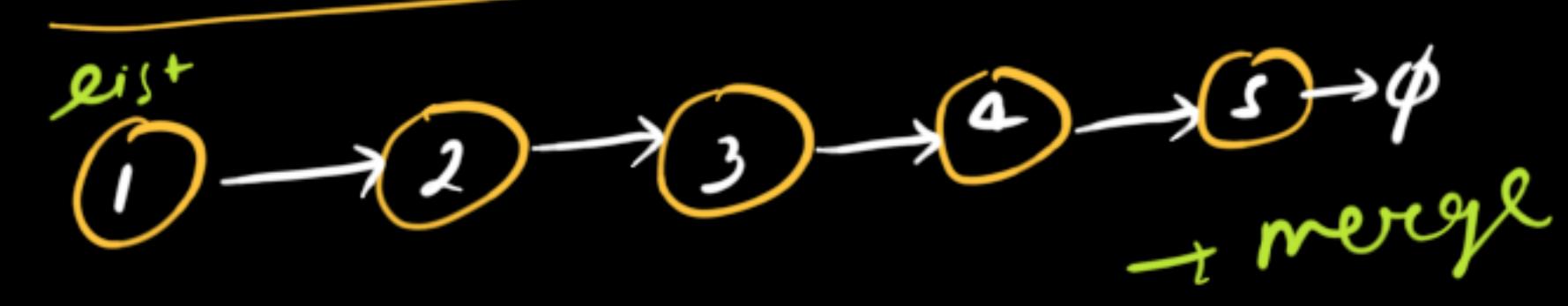
    if (k == 0) {
        temp.next = null;
        return head;
    }
    int diff = len - k;
    temp = head;

    while (temp != null && --diff > 0) {
        temp = temp.next;
    }
    LLNode<Integer> nextHead = temp.next;
    temp.next = null;

    return nextHead;
}

```

→ merge two sorted list



while (list₁ != null & list₂ != null) {

```
if (list1.val ≥ list2.val) {  
    dummy.next = list2;  
    list2 = list2.next;
```

```
} else {  
    dummy.next = list1;  
    list1 = list1.next;
```

```
}  
dummy = dummy.next;
```

}

if any list reaches null, & any
pointer is not at null connect
that list later.

dummy.next = list₁ != null ? list₁ : list₂;

PartXX.java

```
public static LLNode<Integer> mergeTwoLists(LLNode<Integer> list1, LLNode<Integer> list2) {  
    if (list1 == null) return list2;  
    if (list2 == null) return list1;  
  
    return merge(list1, list2);  
}
```

```
private static LLNode<Integer> merge(LLNode<Integer> list1, LLNode<Integer> list2) { 1 usage  
    LLNode<Integer> newList = new LLNode<~> (value: 0);  
    LLNode<Integer> temp = newList;
```

```
    while (list1 != null && list2 != null) {  
        if (list1.value ≥ list2.value) {  
            temp.next = list2;  
            list2 = list2.next;  
        } else {  
            temp.next = list1;  
            list1 = list1.next;  
        }  
        temp = temp.next;  
    }
```

```
    temp.next = list1 != null ? list1 : list2;  
    return newList.next;
```

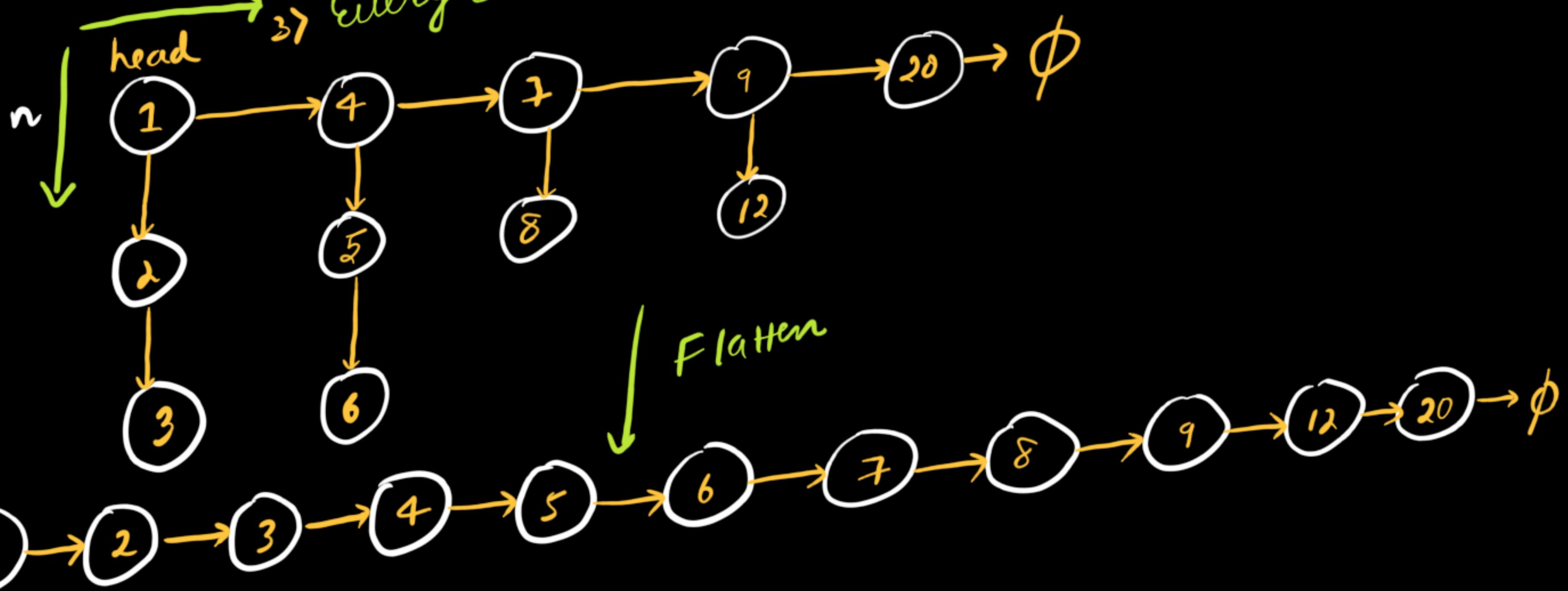
TC: O(n+m)

SC: O(1)

↓
other than a single
node

→ Flatten a linked list

- Given a linked list containing n head nodes, where every node in the linked list contains two pointers:
 - $\text{next} \rightarrow$ points to the next node in the list
 - $\text{child} \rightarrow$ points to a linked list where the current node is head



→ Approach - 1

- Traverse through child & next pointer and add it in array list.
- Sort the array list.
- Convert the sorted list into a flattened linked list.

```

PartXXI.java

public static Node flattenLinkedList(Node head) { 1 usage new *
    if (head == null || (head.next == null && head.child == null)) {
        return head;
    }

    Node temp = head;
    List<Integer> list = new ArrayList<>();
    while (temp != null) {
        Node childTemp = temp;

        while (childTemp != null) {
            list.add(childTemp.data);           O(mxn)
            childTemp = childTemp.child;
        }
        temp = temp.next;
    }
    Collections.sort(list);           O(mxn log(mxn))
    return convert(list);
}

private static @Nullable Node convert(@NotNull List<Integer> ls) { 1
    if (ls.isEmpty()) return null;

    Node dummy = new Node(data: -1);
    Node temp = dummy;

    for (int e : ls) {               O(mxn)
        temp.next = new Node(e);
        temp = temp.next;
    }
    return dummy.next;
}

```

$$TC = 2 \times O(m \times n) + m \times n \log(m \times n)$$

$$TC = mxn(2 + \log(m \times n))$$

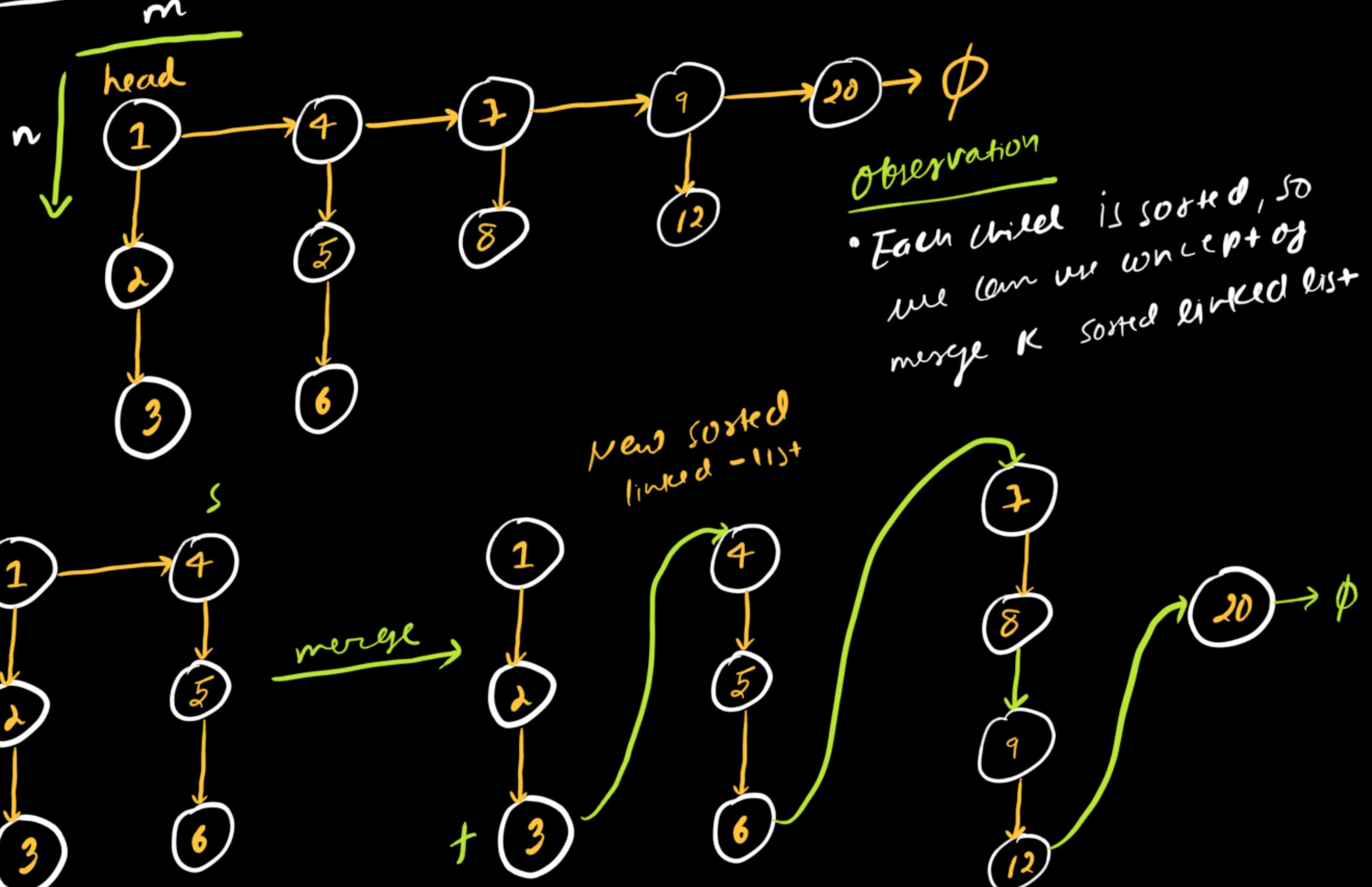
$$TC = (mxn) \log(m \times n)$$

SC: $O(m \times n)$

$m = \text{no. of nodes using next pointer}$

$n = \text{no. of nodes using child pointer}$

→ Approach-2



- Recursively traverse to the last list

↓
Pass the current head &
returned merged head to
the merge function

↑ length of horizontal chain

$$TC: m \times (m+n) \quad \{ m = n \}$$

$$= m \times (2N) \approx 2MN$$

SC: $O(N)$
↳ Recursive stack space

```

PartXXI.java

public static Node flattenLinkedListOpt(Node head) {
    if (head == null || head.next == null){
        return head;
    }

    Node mergedHead = flattenLinkedListOpt(head.next);
    head.next = null; // break the horizontal chain

    return merge(head, mergedHead);
}

private static Node merge(Node list1, Node list2) {
    Node dummy = new Node(data: 0);
    Node temp = dummy;

    while (list1 != null && list2 != null) {
        if (list1.data <= list2.data) {
            temp.child = list1;
            list1 = list1.child;
        } else {
            temp.child = list2;
            list2 = list2.child;
        }
        temp = temp.child;
    }

    temp.child = (list1 != null) ? list1 : list2;

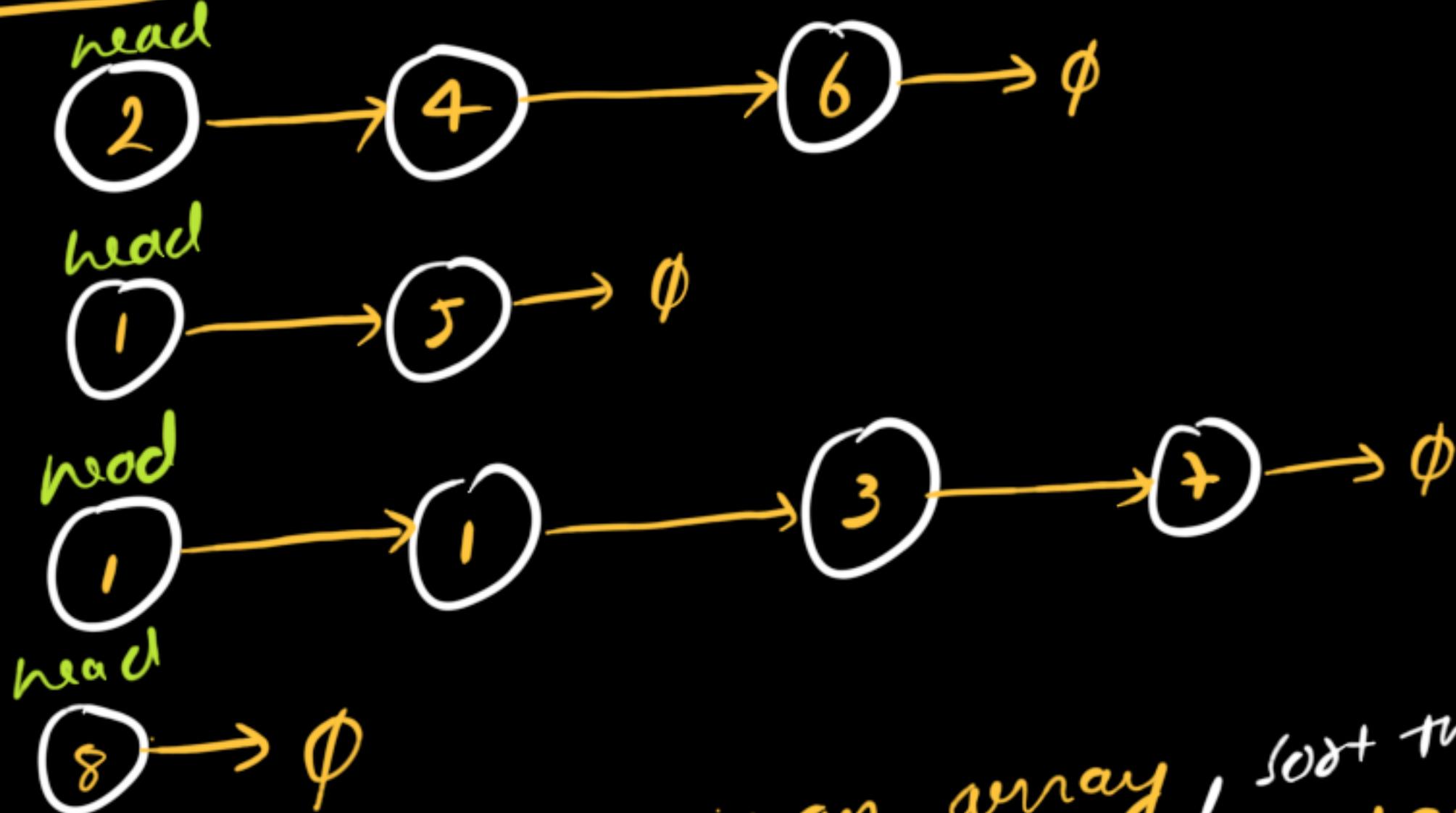
    return dummy.child;
}

```

$TC: O(m+n)$

→ Merge K sorted linked list

→ Approach-1



- Traverse & store them in an array, sort them
with the linked list from the sorted array

- Traverse & Sort
 - Again build the linked list from τ_k

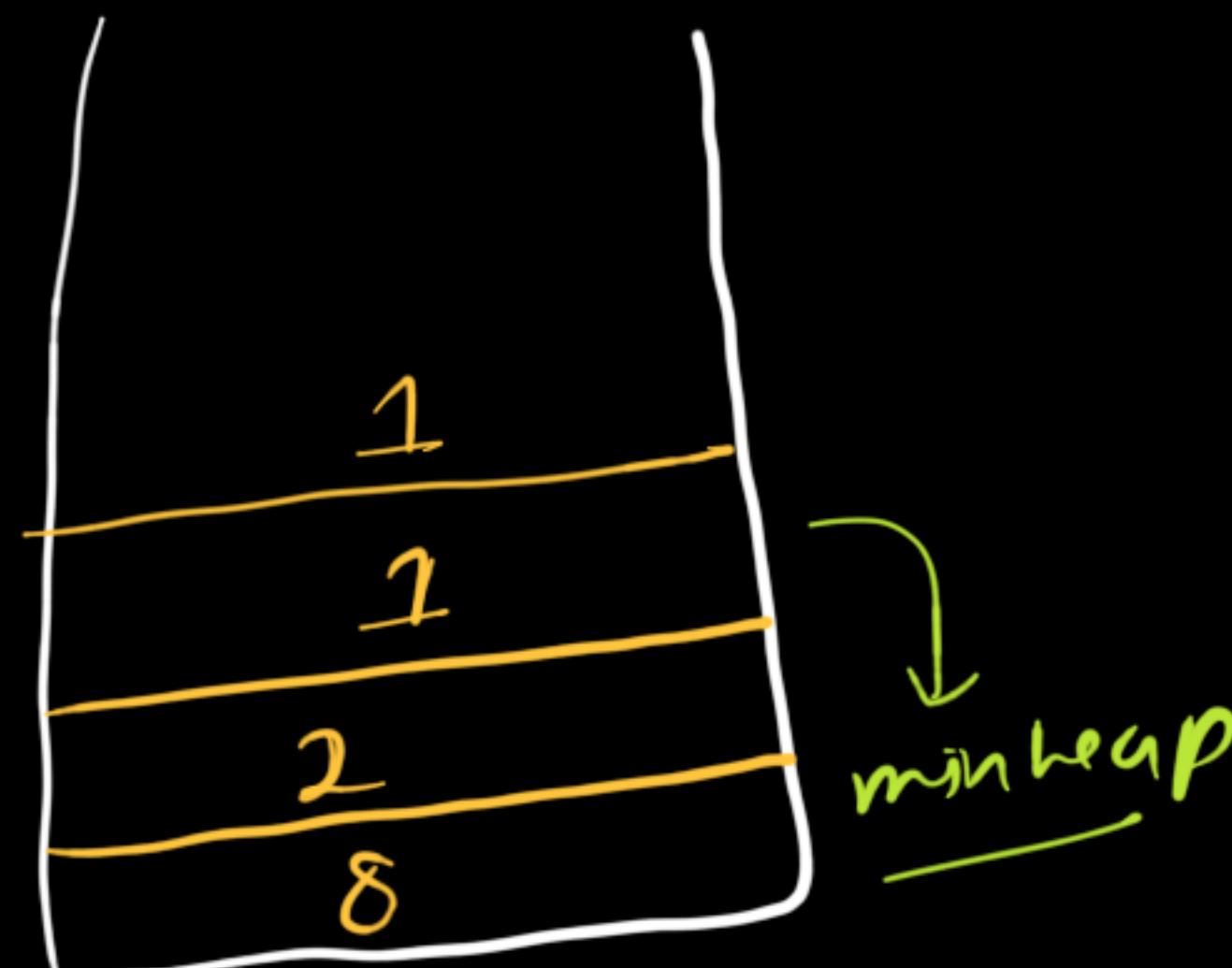
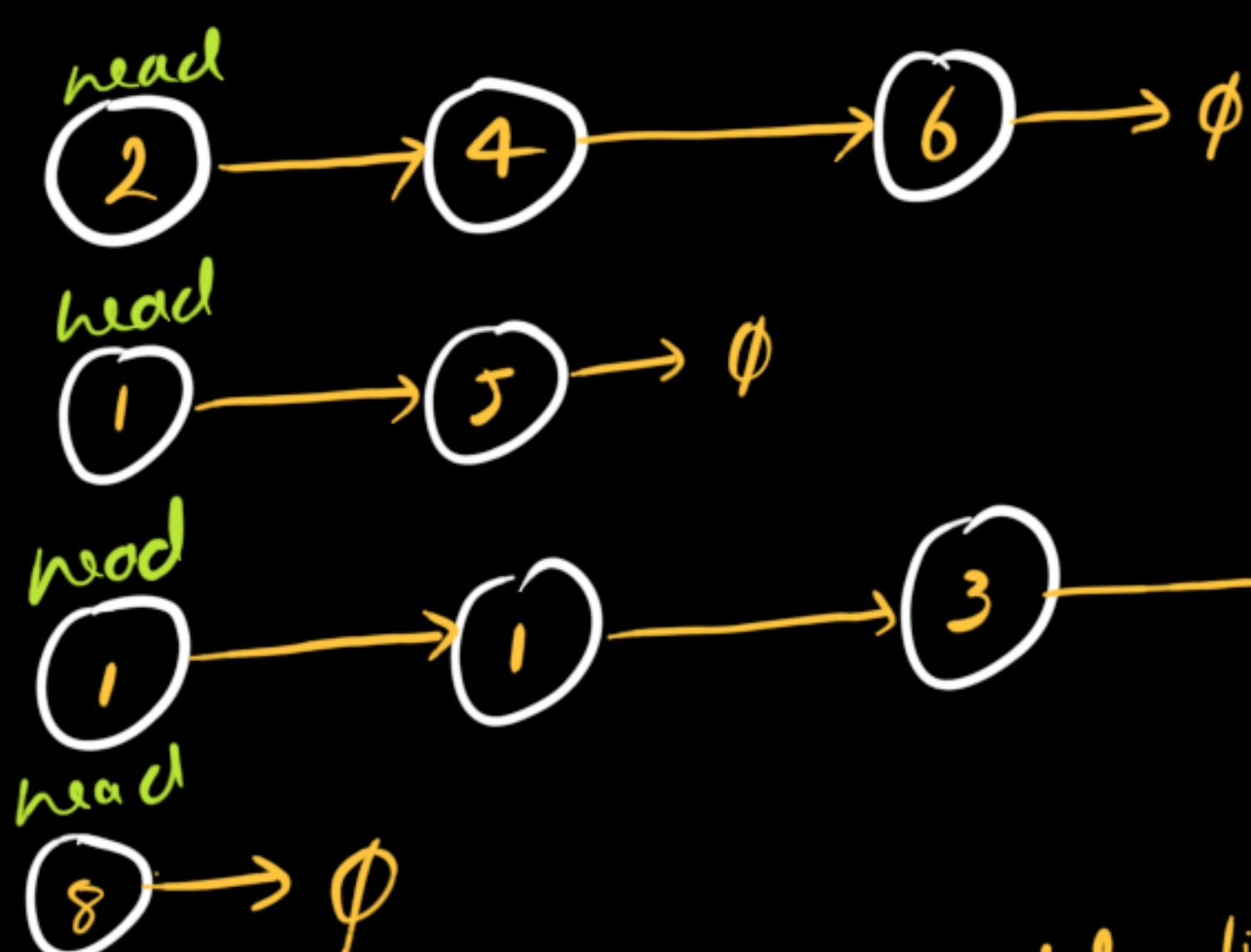
Total: $O(N \times K) + O(N \times K \log(N \times K)) + O(N \times K)$

TC: OLR ↓
no of LL given
Each LL
Name length
p.e.

$\mathcal{O}(N \times m)$

(Nxm) for storing the result.

→ Approach-2



- ① Insert the head of all linked list $\text{PQ} \leftarrow \text{Node}_1$

② Create a dummy node $\text{dummy} \rightarrow \phi$

③ Pop off minimum node from priority queue i.e 1
 Insert the popped off node to the dummy.next

④ Whether the popped node $\text{next} = \text{null}$

⑤ Check if the popped node $\text{next} \rightarrow \text{insert next to the PQ}$

⑥ Keep doing this until PQ is empty

```

XXII.java
public static @Nullable LLNode<Integer> mergeKLists(LLNode<Integer> @NotNull [] lists) {

    if (lists.length == 0) return null;

    PriorityQueue<LLNode<Integer>> pq = new PriorityQueue<>(
        Comparator.comparingInt(LLNode<Integer> a -> a.value)
    );

    for (LLNode<Integer> head : lists) {
        if (head != null) {
            pq.offer(head);
        }
    }

    LLNode<Integer> dummy = new LLNode<Integer>(value: -1);
    dummy.next = null;
    LLNode<Integer> temp = dummy;

    while (!pq.isEmpty()) {
        LLNode<Integer> min = pq.poll();
        temp.next = min;
        temp = temp.next;

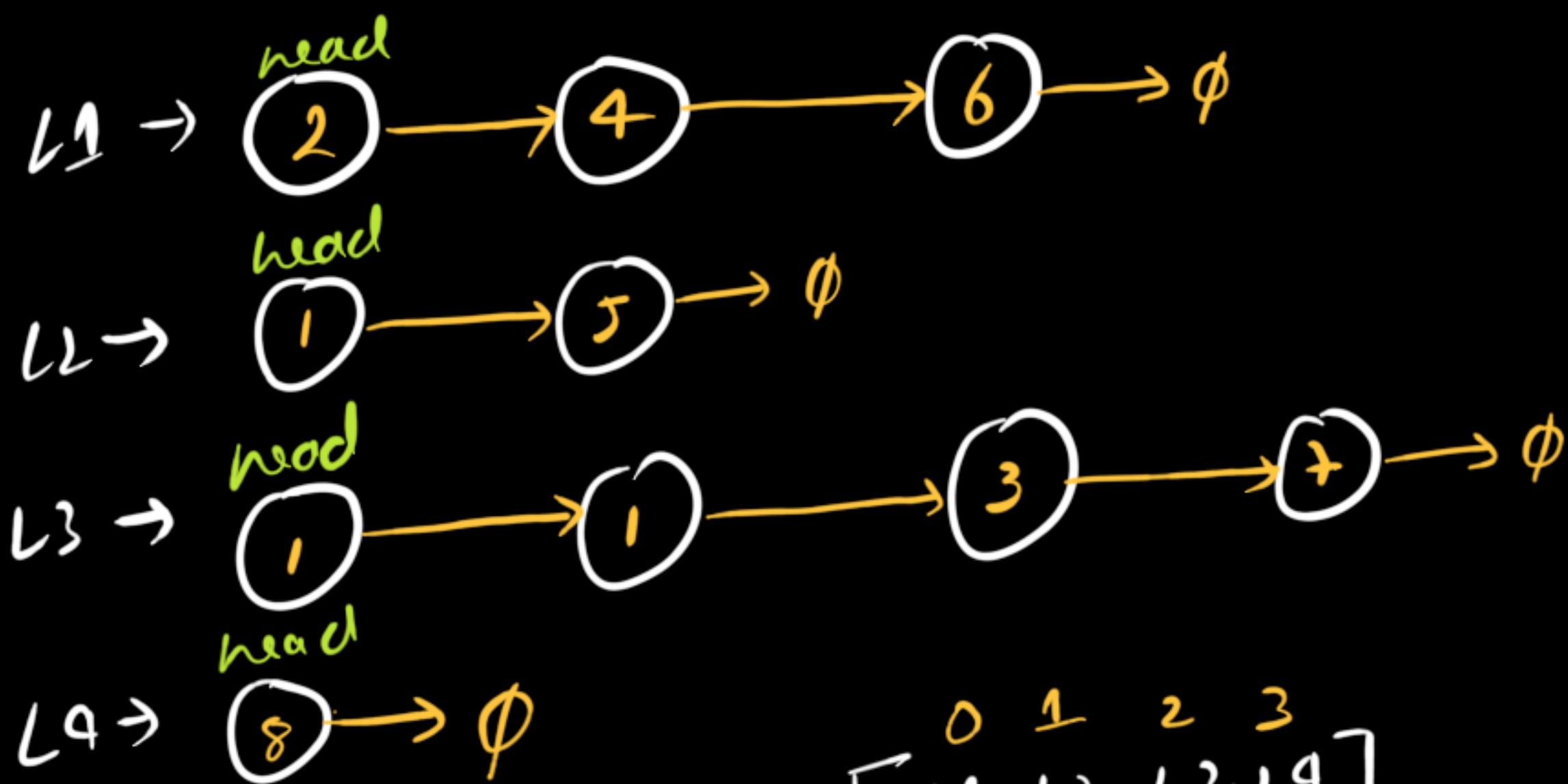
        if (min.next != null) {
            pq.offer(min.next);
        }
    }

    return dummy.next;
}

```

$T_C: N \log(k)$
 $S_C: O(k)$

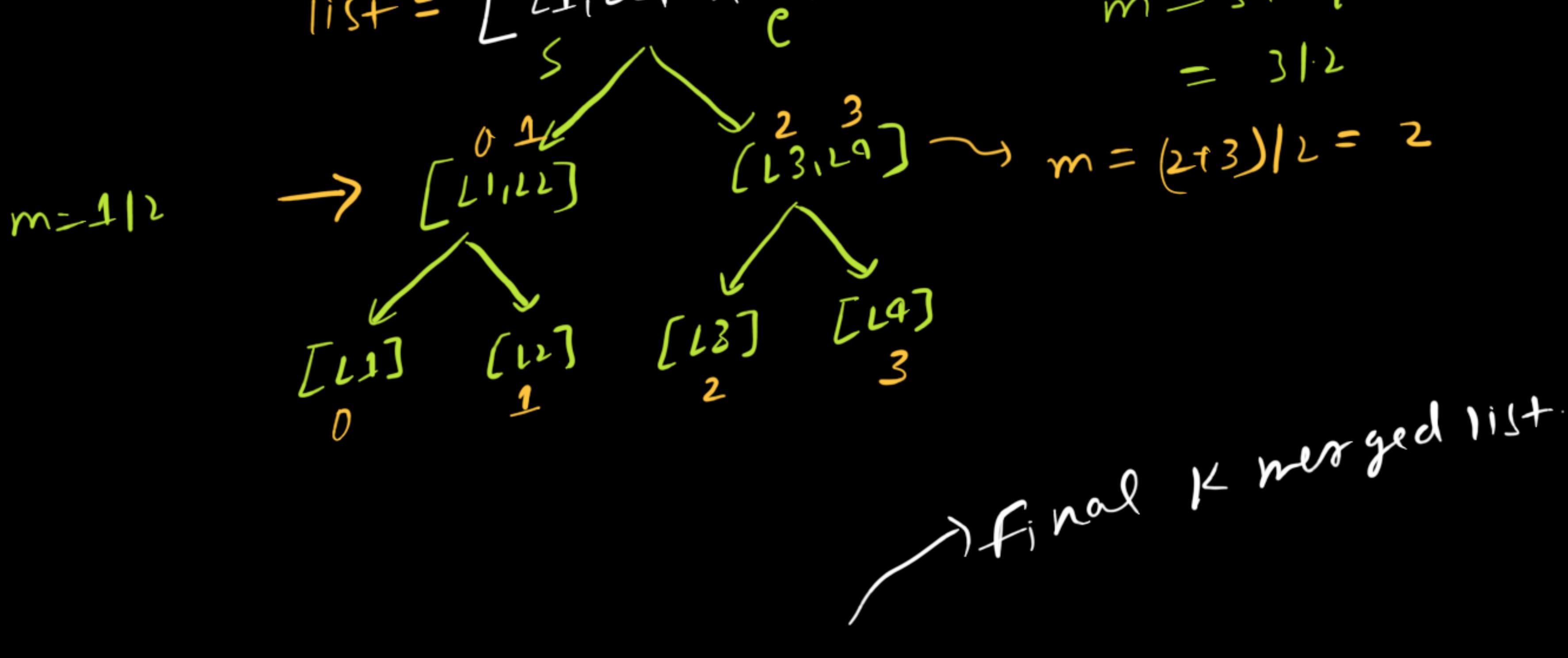
→ Approach-3

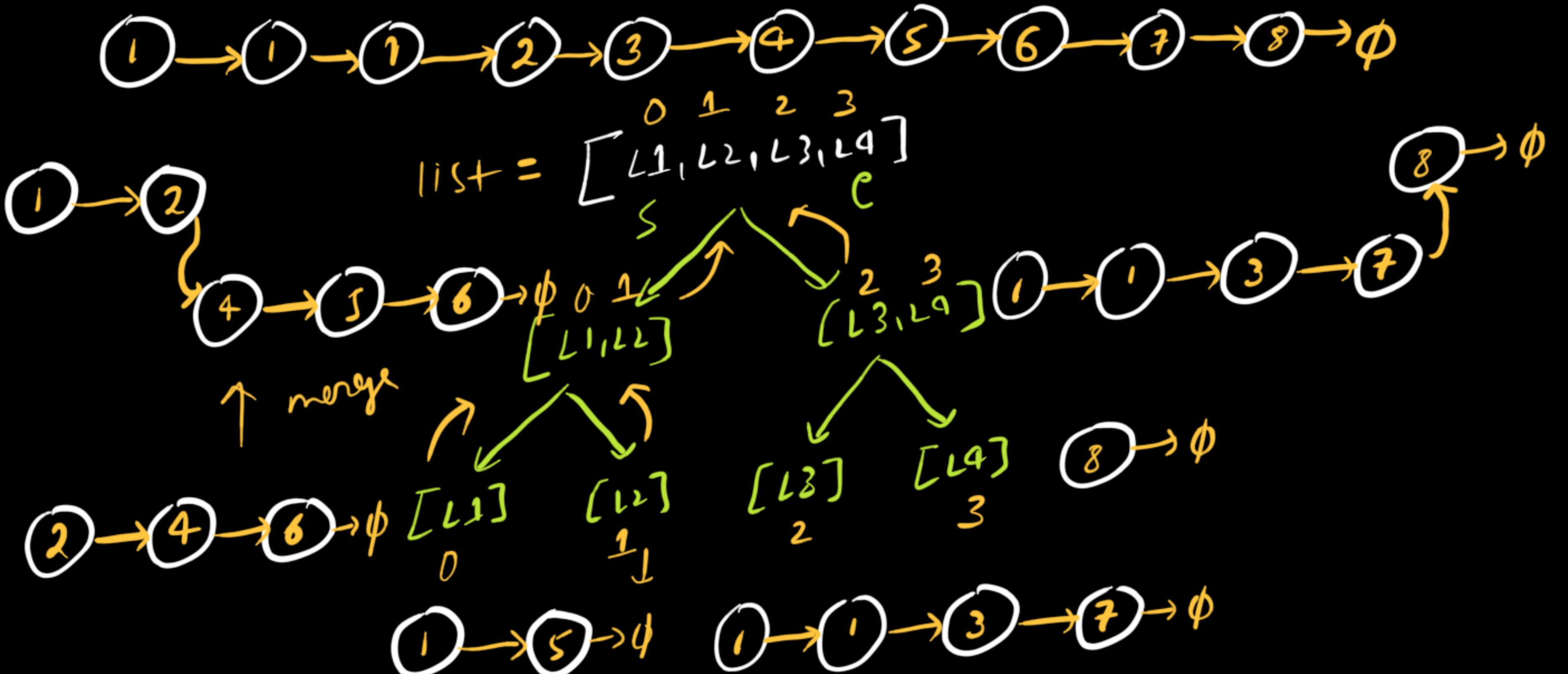


$$\text{list} = [L_1, L_2, L_3, L_4]$$

$$m = \lceil \frac{s}{2} \rceil$$

$$= 3/2$$





```

XXII.java

public static @Nullable LLNode<Integer> mergeKList(LLNode<Integer> @NotNull [] lists) {
    if (lists.length == 0) {
        return null;
    }

    return mergeK(lists, 0, lists.length - 1);
}

private static LLNode<Integer> mergeK(LLNode<Integer>[] lists, int s, int e) { 3 usage
    if (s == e) return lists[s];
    int mid = (s + e) / 2;

    LLNode<Integer> left = mergeK(lists, s, mid);
    LLNode<Integer> right = mergeK(lists, mid + 1, e);

    return merge(left, right);
}

private static LLNode<Integer> merge(LLNode<Integer> list1, LLNode<Integer> list2) {
    LLNode<Integer> newList = new LLNode<~> (value: 0);
    LLNode<Integer> temp = newList;

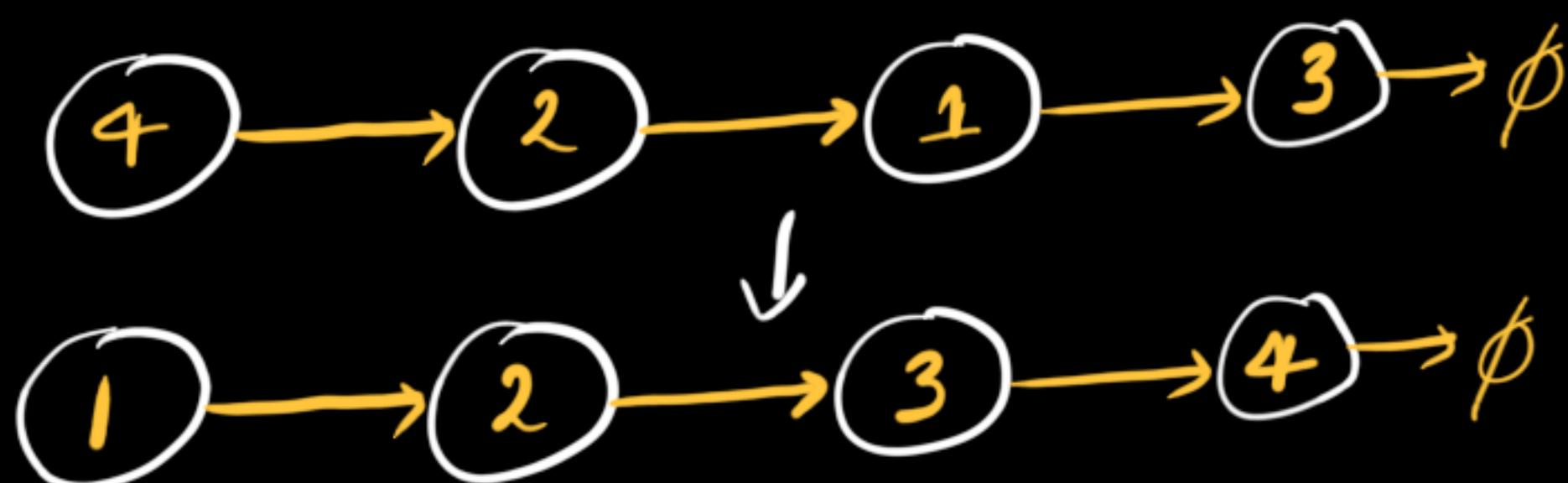
    while (list1 != null && list2 != null) {
        if (list1.value >= list2.value) {
            temp.next = list2;
            list2 = list2.next;
        } else {
            temp.next = list1;
            list1 = list1.next;
        }
        temp = temp.next;
    }

    temp.next = list1 != null ? list1 : list2;
    return newList.next;
}

```

$T_C: O(N \log K)$
 $S_C: O(N)$
 \downarrow
 Recursive
 Stack Space

→ Sort - List



→ Approach-1 (Brute)

↳ APPLY Bubble-Sort

Tc: $O(n^2)$

Sc: $O(1)$

```
PartXXIII.java
public static LLNode<Integer> sortList(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;

    LLNode<Integer> temp = head;

    while (temp != null){
        LLNode<Integer> secTemp = temp.next;

        while (secTemp != null){
            if (temp.value > secTemp.value){
                Integer t = temp.value;
                temp.value = secTemp.value;
                secTemp.value = t;
            }
            secTemp = secTemp.next;
        }

        temp = temp.next;
    }
    return head;
}
```

→ Approach-2 (Better)

① Traverse the list, put all elements into an ArrayList
② Sort the list & overwrite the value of the original list;

Tc: $O(2N) + N \log N$
 $\approx O(N \log N)$

Sc: $O(N)$

```
PartXXIII.java
public static LLNode<Integer> sortListBetter(LLNode<Integer> head) {
    if (head == null || head.next == null) return head;

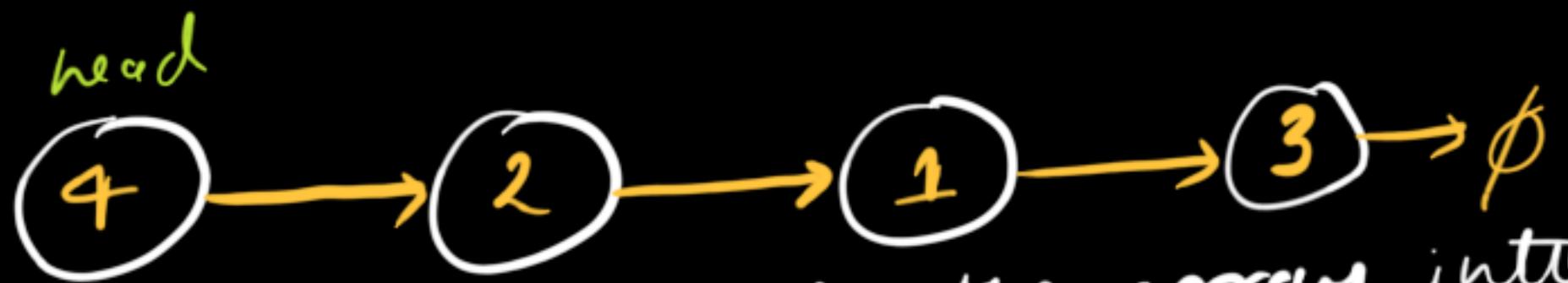
    LLNode<Integer> temp = head;
    List<Integer> l = new ArrayList<>();

    while (temp != null){      O(N)
        l.add(temp.value);
        temp = temp.next;
    }

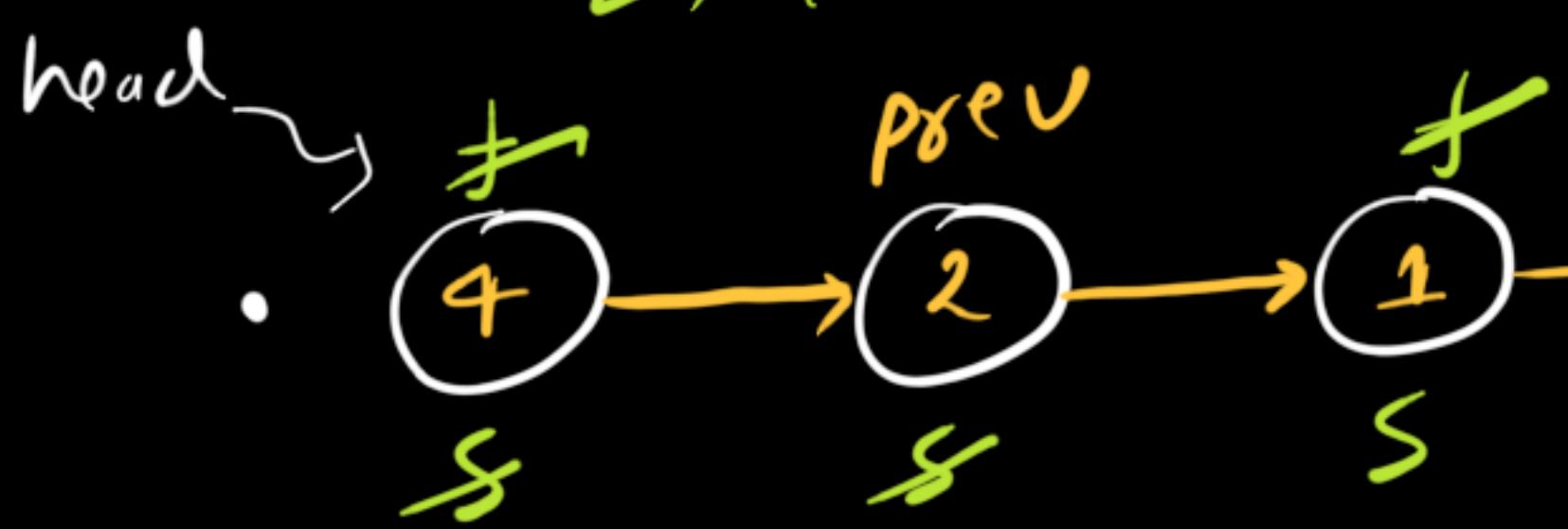
    Collections.sort(l);      O(N log N)
    temp = head;
    for (Integer e : l){      O(N)
        temp.value = e;
        temp = temp.next;
    }

    return head;
}
```

→ Approach-3 (merge-sort)



- How do we divide the array into two equal part
↳ Tortoise & hare Algorithm

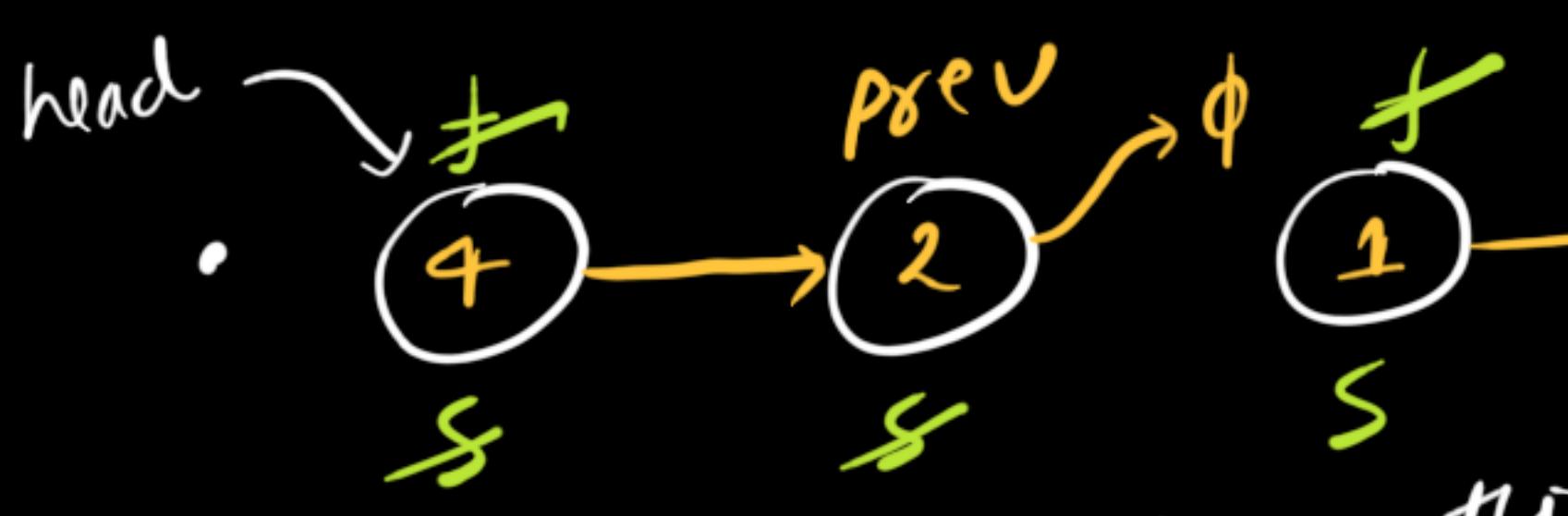


position + → divide the linked
list in two part

→ ③ → ϕ

prev.next = next

= list



p8(v) + → Two list:
3 → φ
1. head
2. slows

- recursively keep doing this until a single rock remains,
that will be our base case. \hookrightarrow when single rock
remains head next
Base-case \hookrightarrow = - rock

$T_1: O(nwgn)$

Sc: $\sigma(N)$

↓
steaks paul.

```
PartXXIII.java

public static LLNode<Integer> sortListOpt( @NotNull LLNode<Integer> head) { 3 usages
    if (head.next == null) return head;

    LLNode<Integer> f = head;
    LLNode<Integer> s = head;
    LLNode<Integer> prev = null;

    while (f != null && f.next != null){
        prev = s;
        s = s.next;
        f = f.next.next;
    }
    prev.next = null;

    LLNode<Integer> left = sortListOpt(head);
    LLNode<Integer> right = sortListOpt(s);

    return merge(left , right);
}

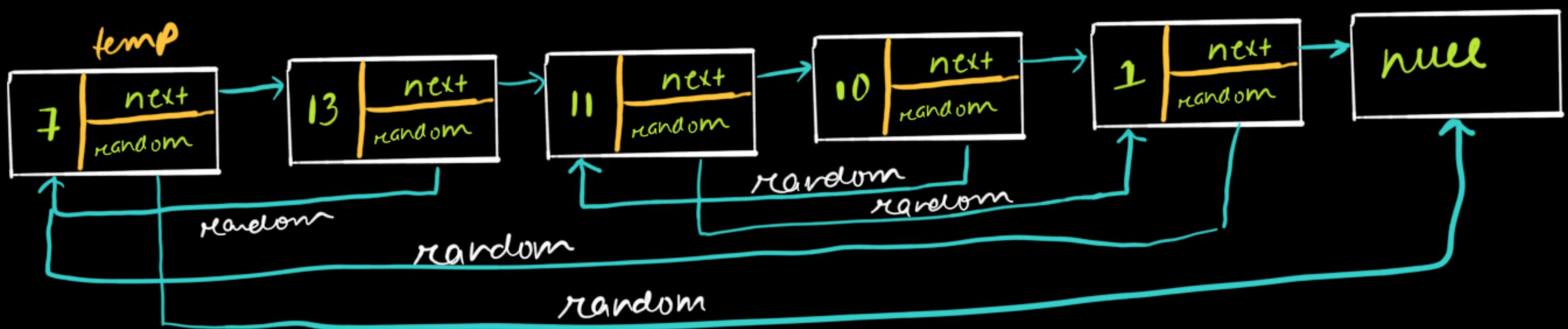
private static LLNode<Integer> merge(LLNode<Integer> list1, LLNode<Integer> list2) {
    LLNode<Integer> newList = new LLNode<~>( value: 0);
    LLNode<Integer> temp = newList;

    while (list1 != null && list2 != null) {
        if (list1.value >= list2.value) {
            temp.next = list2;
            list2 = list2.next;
        } else {
            temp.next = list1;
            list1 = list1.next;
        }
        temp = temp.next;
    }

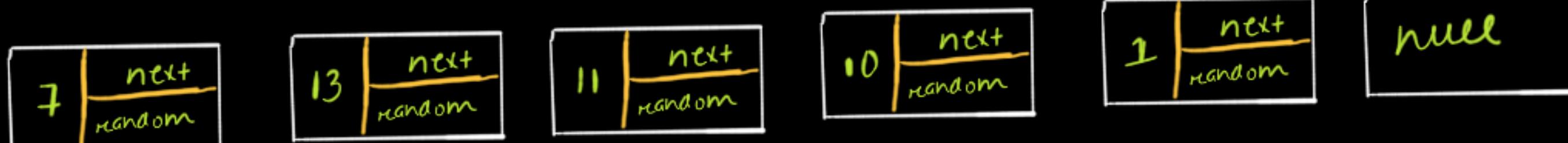
    temp.next = list1 != null ? list1 : list2;
    return newList.next;
}
```

→ Copy list with Random pointer

→ Next: points to the next node
random: points to any random node or null



→ Approach-1



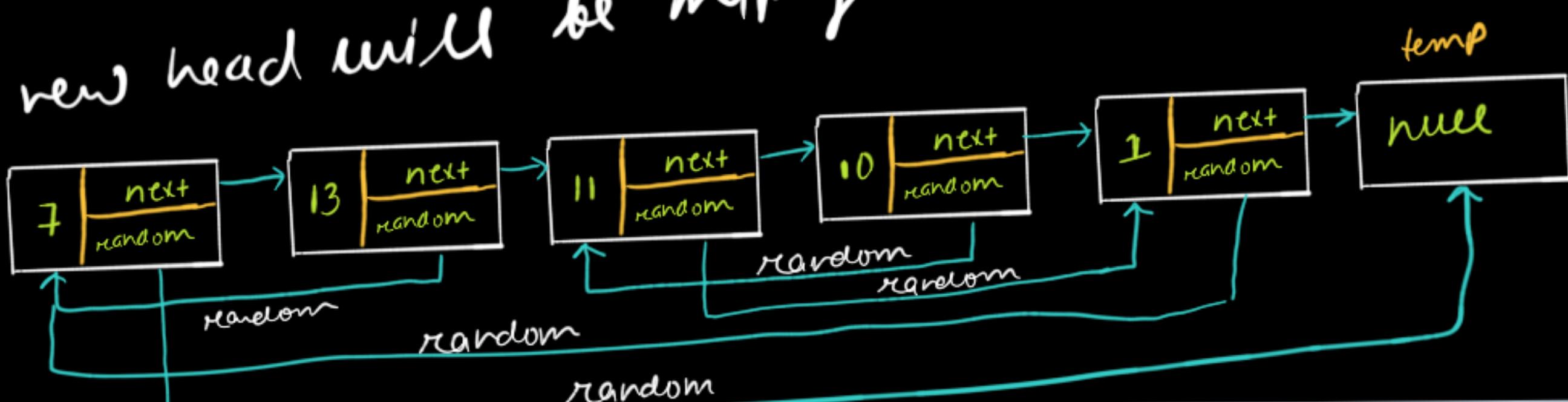
- (1) place temp, push each node into the hash map.
- (2) Again place temp over the head, get the copied node using org-node as key.

Node org = temp;
Node wpy = map.get(temp);
wpy.next = map.get(org.next);
wpy.random = map.get(org.random);

③ The new head will be map.get(head);



Map<Node, Node>
Original Node Copied Node



TC: $O(2N)$

SC: $O(N) + O(N)$

For map For creating the new list.

```
PartXXIV.java
public static Node copyRandomList(Node head) {
    if (head == null) {
        return null;
    }

    Map<Node, Node> map = new HashMap<>();
    Node temp = head;

    while (temp != null) {          O(N)
        map.put(temp, new Node(temp.val));
        temp = temp.next;
    }

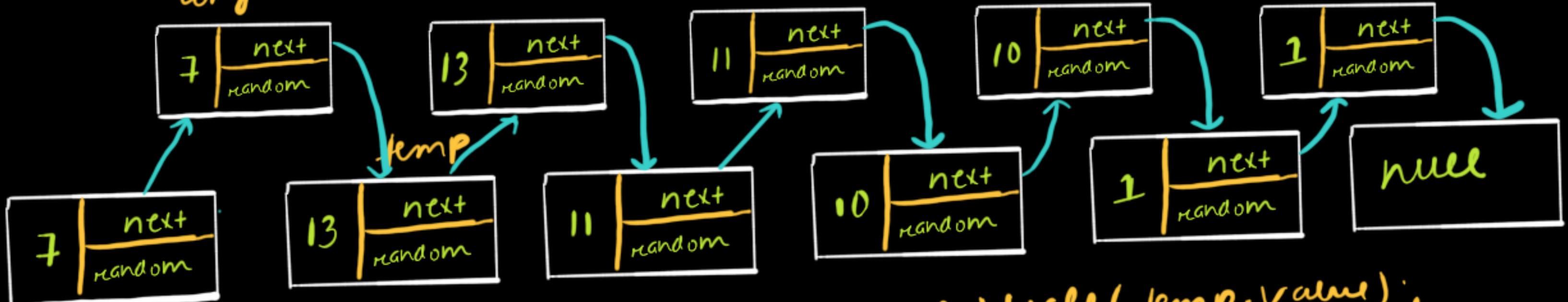
    temp = head;
    while (temp != null) {          O(N)
        Node copy = map.get(temp);
        copy.next = map.get(temp.next);
        copy.random = map.get(temp.random);
        temp = temp.next;
    }

    return map.get(head);
}
```

→ Approach-2

- Insert copy-node in between the current node & current.next node.

copyNode



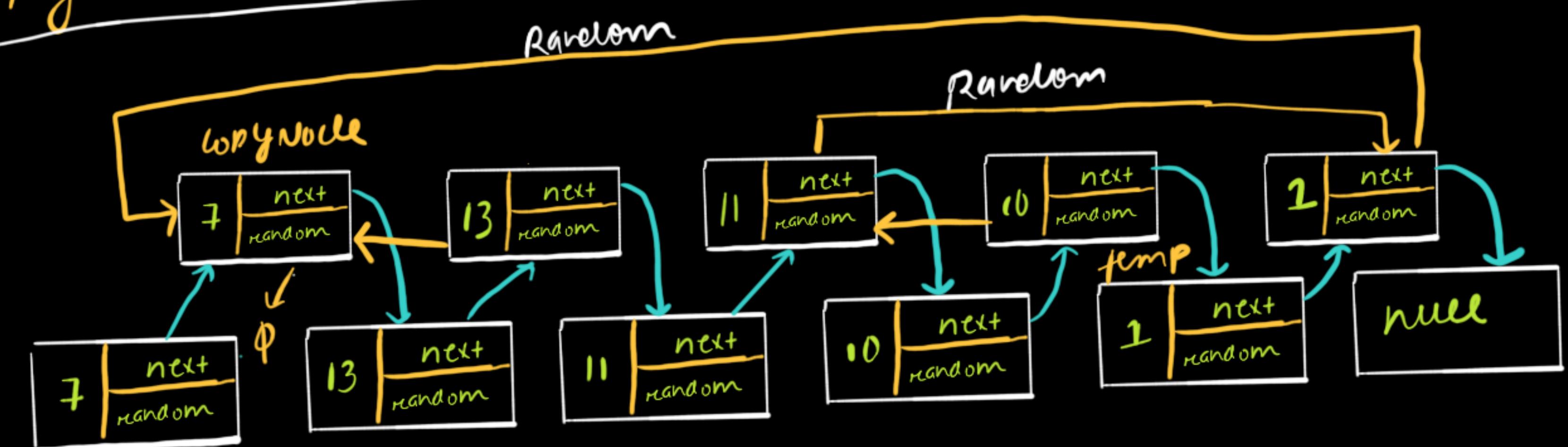
Node copyNode = new Node(temp.value);

copyNode.next = temp.next;

temp.next = copyNode;

temp = temp.next.next;

- Again point temp to head & connect random pointer.



temp
13

Ravelom

next → 7
copy

Ravelom

Node copy = temp.next;

copy.random = temp.random != null ? temp.random;

temp = temp.next.next;

next : null;

so ~ temp.random.next;

- Extract the related copy linked list

copied list

Ravelom

dummy
-1

temp

original list

Node dummy = new Node(-1);
Node res = dummy;

res.next = temp.next;

temp.next = temp.next.next;

res = res.next;

temp = temp.next;

return dummy.next;

TC: $O(3N)$

SC: $O(N)$

for creating the
new copied
Linked List

```
PartXXIV.java
public static Node copyRandomListOpt(Node head) {
    if (head == null) return null;

    Node temp = head;

    while (temp != null) {
        Node copy = new Node(temp.val);
        copy.next = temp.next;
        temp.next = copy;          O(N)
        temp = copy.next;
    }

    temp = head;
    while (temp != null) {
        if (temp.random != null) {
            temp.next.random = temp.random.next;
        }
        temp = temp.next.next;      O(N)
    }

    Node dummy = new Node(val: 0);
    Node res = dummy;
    temp = head;

    while (temp != null) {
        res.next = temp.next;
        res = res.next;           O(N)

        temp.next = temp.next.next;
        temp = temp.next;
    }

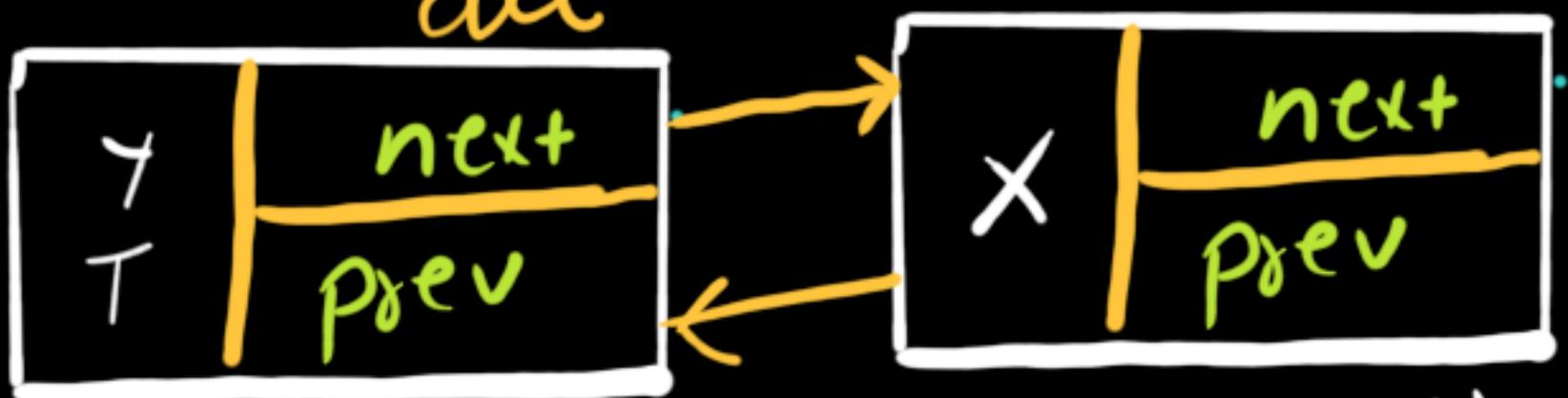
    return dummy.next;
}
```

→ Design Browser History

- `BrowserHistory(homepage)`, → visit homepage
- `visit(url)`, → visit new url
- `back(steps)`, → go back steps time in history
- `forward(steps)`, → go forward steps time in history

Double linked list

→ `visit()` call



```
newNode = new Node(url);  
dll.next = newNode;  
newNode.prev = dll;  
dll = dll.next;
```

TC: $O(2 \text{ steps})$

SC: $O(N)$

{
No. of `visit()` calls
↓
each call adds
one node.

```
BrowserHistory.java  
public class BrowserHistory { no usages new *  
private Node dll; 12 usages  
@Contract(pure = true)  
public BrowserHistory(String homepage) { no u  
this.dll = new Node(homepage);  
}  
  
public void visit(String url) { no usages new  
Node node = new Node(url);  
dll.next = node;  
node.prev = dll;          O(1)  
dll = node;  
}  
  
public String back(int steps) { no usages new  
while (steps > 0){  
if (dll.prev != null) dll = dll.prev;  
else break;  
steps--;}           O(steps)  
return dll.url;  
}  
  
public String forward(int steps) { no usages i  
while (steps > 0){  
if (dll.next != null) dll = dll.next;  
else break;  
steps--;}           O(steps)  
return dll.url;  
}  
  
private class Node { 6 usages new *  
public String url; 3 usages  
public Node next; 4 usages  
public Node prev; 4 usages  
  
@Contract(pure = true)  
public Node(String url){ 2 usages new *  
this.url = url;  
this.next = null;  
this.prev = null;  
}  
}
```