

# Automata Theory

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Spring/Summer 2022

## Abstract

This document stores my Automata Theory notes - which are important to me. Additionally, it serves as a worthy example of how to structure  $\text{\LaTeX}$  files in a VC system like GitHub.

# 1 Symbols, alphabets and languages

Symbols in strings, for example,  $a, b$ , always belong to an alphabet. Hence, we can say an alphabet  $\Sigma$  is a set of characters, for example  $\{a, b\}$ , is formally defined as:

$$\text{Alphabet} = \Sigma = \{a, b\} \quad (1)$$

A language,  $L$ , is a set over a particular alphabet. Hence:

$$\text{Language} = L1(\Sigma) = \{a, aa, b, ab, ba, bba, \dots\} \quad (2)$$

As you may see, the above language  $L1$  is generated over the alphabet  $\Sigma$ , and contains various combinations of the symbols in our alphabet. In theory, it is possible to create an infinite number of such combinations. Therefore, that language is an *infinite* language.

As you might have guessed, there are two main types of languages:

- infinite
- finite

For a language to be finite, we must restrict how symbols are combined. Such restrictions applied to a language produce a grammar,  $G$ . Formally, we say that a grammar  $G$  is a tuple:

$$\text{Grammar} = G = (N, T, P, S) \quad (3)$$

where  $N$  = nonterminals,  $T$  = terminals,  $P$  = productions, or rules, and  $S$  = starting symbol.

## 2 Chapter 2

This is Chapter 2.

## **3 Chapter 3**

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