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1.3 Risk and Capital

- Risk-Weighted Assets
- Risk Weights
- Capital
- Minimum Capital

1.4 Expenses and Earnings

- Expenses
- Risk Costs
- Taxes
- Earnings

- Retained Earnings
- Dividends
- Capital Raise

2 Introduction to Banks

2.1 Nature of Banking

- Commercial Banking:
 - Taking deposits and making loans (wholesale or retail).
 - Money center banks operate in the wholesale market and often fund loans by borrowing.

• Investment Banking:

- Raising debt and equity for companies.
- Advice on mergers and acquisitions, restructurings, trading, etc.

2.2 Structure of Banking in the US

- Large international banks (small number).
- Regional banks (several hundred).
- Small community banks (several thousand).

2.3 History of Bank Regulation in the US

- McFadden Act (1927, 1933).
- Douglas Amendment (1956).
- Bank Holding Companies Act (1970).
- Riegel-Neal Interstate Banking and Branching Efficiency Act (1994).

2.4 Example of Simple Bank Balance Sheet (End 2023)

- Assets:
 - Cash: 5.
 - Marketable Securities: 10.
 - Loans: 80.
 - Fixed Assets: 5.
 - Total: 100.

• Liabilities:

- Deposits: 90.
- Subordinated Long Term Debt: 5.
- Equity Capital: 5.
- Total: 100.

2.5 Income Statement (2023)

- Net Interest Income: 3.00.
- Provision for Loan Losses: -0.80.
- Non-Interest Income: 0.90.
- Non-Interest Expense: -2.50.
- Pre-Tax Operating Income: 0.60.

2.6 Year 2024 Scenario

• Similar to 2023, except provision for loan losses increases to 4.0 from 0.8.

2.7 Deposit Insurance

- Insures depositors against losses up to a certain level.
- In the US, FDIC has provided protection since 1933.
- Coverage increased from \$2,500 (1933) to \$250,000 (2008).
- Raises the question: Why might deposit insurance encourage risk-taking?

2.8 Investment Banking

- Methods of raising debt or equity:
 - Public Offering.
 - Private Placement.
 - Best Efforts.
 - Firm Commitment.

2.9 Initial Public Offering (IPO)

- Often done on a best efforts basis.
- Banks set offering price low to ensure sales.
- Shares often rise in price post-IPO.

2.10 Securities Trading

- Exchange-traded vs Over-the-Counter (OTC).
- Brokerage Services:
 - Full Service.
 - Discount.
 - Online.

2.11 Potential Conflicts of Interest

- Bank recommending securities it is trying to sell.
- Passing confidential client information between commercial and investment banks.
- Stock recommendations influenced by investment banking business goals.

2.12 The Originate-to-Distribute Model

- Popular for handling mortgages (2000–2007).
- Banks originate loans and package them into products sold to investors.
- Frees up funds for further lending.

3 Securitization and the Global Financial Crisis

3.1 What Happened

- Starting in 2000, mortgage originators in the US relaxed lending standards and created large numbers of subprime first mortgages.
- Low interest rates increased the demand for real estate, leading to rising prices.
- Market features included:
 - 100% mortgages, ARMs, teaser rates.
 - NINJAs, liar loans, non-recourse borrowing.
- In 2007, the bubble burst:
 - Borrowers struggled to afford payments after teaser rates ended.
 - Negative equity led borrowers to exercise put options.
 - Real estate prices fell, and products previously thought safe became risky.
- A "flight to quality" ensued, with increased credit spreads.

3.2 Asset-Backed Securities (ABS)

- Structured with a "waterfall" for allocating cash flows to tranches.
- Example structure:
 - Senior Tranche: \$75 million, Return = 6%.
 - Mezzanine Tranche: \$20 million, Return = 10%.
 - Equity Tranche: \$5 million, Return = 30%.

3.3 ABS CDOs or Mezz CDOs

- Composed of subprime mortgages:
 - Senior Tranche: 75%, rated AAA.
 - Mezzanine Tranche: 20%, rated BBB.
 - Equity Tranche: 5%, not rated.
- Loss distributions varied based on subprime portfolio performance.

3.4 Regulatory Arbitrage

• Capital requirements for securities created from mortgage portfolios were significantly lower than keeping mortgages on balance sheets.

3.5 Role of Incentives

- Valuers, ABS creators, and rating agencies contributed to the crisis through flawed incentives.
- Compensation plans for traders encouraged short-term decision-making.

3.6 Importance of Transparency

- ABSs and ABS CDOs were complex, inter-related products.
- Once perceived as risky, AAA tranches became difficult to trade due to a lack of understanding.
- Simpler credit-related products, like credit default swaps, continued to trade during the crisis.

3.7 Lessons from the Global Financial Crisis

- Beware of irrational exuberance.
- Do not underestimate default correlations in stressed markets.
- Recovery rates depend on default rates.
- Compensation structures must align with proper incentives.
- \bullet Deals too good to be true (e.g., AAA earning LIBOR + 100 bp) likely are.
- Do not rely solely on ratings.
- Transparency is crucial in financial markets.
- Resecuritization was fundamentally flawed.

4 Operational Risk

4.1 Definition of Operational Risk

"Operational risk is the risk of loss resulting from inadequate or failed internal processes, people, and systems, or from external events."

– Basel Committee, Jan 2001

4.2 What It Includes

- People risks.
- Technology and processing risks.
- Physical risks.
- Legal risks.

Exclusions: Reputation risk and strategic risk.

4.3 The Biggest Risk?

- Operational risk is difficult to quantify but regarded as the biggest risk facing banks.
- Cyber risk is a significant concern for financial institutions.
- Compliance risks can lead to substantial losses (e.g., BNP Paribas, \$9 billion in 2014).

4.4 Categories of Operational Risk

- Internal fraud.
- External fraud.
- Employment practices and workplace safety.
- Clients, products, and business practices.
- Damage to physical assets.
- Business disruption and system failures.
- Execution, delivery, and process management.

4.5 Loss Severity vs Loss Frequency

- Loss frequency estimation:
 - Based on the bank's own data.
 - Often modeled using a Poisson distribution.
- Loss severity estimation:
 - Based on internal and external historical data.
 - Often modeled using a lognormal distribution.

4.6 Monte Carlo Simulation

- 1. Sample from the frequency distribution to determine the number of loss events (n).
- 2. Sample n times from the severity distribution to determine the loss severity for each event.
- 3. Sum the loss severities to determine total loss.

4.7 SMA (Standard Measurement Approach)

- Business Indicator (BI):
 - Reflects net interest income, other operating income, and net P&L.
 - BI Component (BIC) is a piecewise linear function of BI.
- Loss Component (LC):
 - 15 times the average annual operational risk losses over the last 10 years.

- Transition period allows for 5 years of losses if 10 years are unavailable.
- Internal Loss Multiplier (ILM):

$$ILM = \ln \left[e^{-1} + \left(\frac{LC}{BIC} \right)^{0.8} \right]$$

- Capital Requirements:
 - Equal to BIC for small banks.
 - Product of BIC and ILM for large banks.
 - National regulators may adjust these requirements.

4.8 Loss Prevention

- Establish causal relationships.
- Risk Control Self-Assessment (RCSA).
- Key Risk Indicators (KRI).
- Educate employees on appropriate communication (emails and phone calls).
- Allocate operational risk capital to encourage risk reduction.

4.9 Power Law

$$Prob(v > x) = Kx^{-a}$$

- Effective for modeling operational risk losses.
- Distributions with heavy tails (low a) define the 99.9% worst-case scenario.

4.10 Insurance

- Design factors:
 - Moral hazard.
 - Adverse selection.
- Risk management tools:
 - Deductibles.
 - Co-insurance provisions.
 - Policy limits.

4.11 Sarbanes-Oxley Act

- CEOs and CFOs held accountable for financial statements.
- Increased SEC powers.
- Prohibited auditors from performing significant non-audit tasks.
- Required audit committees to consider alternative accounting treatments.
- Mandated return of bonuses if financial statements are restated.

5 Liquidity Risk

5.1 Types of Liquidity Risk

- Liquidity Trading Risk.
- Liquidity Funding Risk.

5.2 Liquidity Trading Risk

- The price received for an asset depends on:
 - The mid-market price.
 - The amount to be sold.
 - How quickly it is to be sold.
 - The economic environment.
- Transparency, as seen during the GFC, is also a factor affecting liquidity.

5.3 Cost of Liquidation in Stressed Markets

• The cost of liquidation is influenced by the mean and standard deviation of the bid-offer spread, as well as the required confidence level.

5.4 Liquidity-Adjusted VaR

- Adjusted Value at Risk (VaR) incorporates liquidity costs into traditional risk measures.
- It accounts for both the dollar bid-offer spread and market price deviations.

5.5 Unwinding a Position Optimally

 Traders aim to minimize costs by optimizing the amounts traded daily, factoring in price impacts and market volatility.

5.6 Other Measures of Trading Liquidity

- Volume of trading per day.
- Price impact of a trade.
- Absolute daily return divided by daily dollar volume (Amihud measure, 2002).
- Research indicates expected asset returns increase as liquidity decreases.

5.7 Liquidity Funding Risk

- Sources of liquidity:
 - Cash and Treasury securities.
 - Liquidation of trading positions.
 - Borrowing ability.
 - Retail and wholesale deposits.
 - Securitization.
 - Central bank borrowing.

5.8 Regulation

- Liquidity Coverage Ratio (LCR): Ensures the bank can survive a 30-day period of acute stress.
- Net Stable Funding Ratio (NSFR): Ensures funding sources align with asset permanence over the long term.

5.9 Liquidity Black Holes

- Occur when most market participants want to take one side of the market, leading to dried-up liquidity.
- Examples:
 - 1987 Market Crash.
 - LTCM collapse.
 - British Insurance Companies.

5.10 Positive and Negative Feedback Trading

- Positive feedback traders:
 - Buy after a price increase.
 - Sell after a price decrease.
- Negative feedback traders:
 - Buy after a price decrease.
 - Sell after a price increase.
- Positive feedback trading can exacerbate liquidity black holes.

5.11 The Leveraging and Deleveraging Cycles

- Leveraging:
 - Increased leverage allows investors to buy more assets.
 - Asset prices rise, reducing leverage.
- Deleveraging:
 - Investors reduce leverage by selling assets.
 - Asset prices decline, increasing leverage.

5.12 Is Liquidity Improving?

- Spreads are narrowing, suggesting improved liquidity.
- However, risks of liquidity black holes may be greater due to lack of diversity in financial market participants.

6 Credit Value at Risk (Credit VaR)

6.1 Rating Transitions

- One-year rating transition probabilities are published by rating agencies.
- Assuming independence of rating transitions between periods, multi-period transitions can be calculated.
- The phenomenon of "ratings momentum" indicates that the independence assumption is not perfectly accurate.

6.2 Rating Transition Matrices

- One-Year Transition Matrix: See Table 19.1.
- Five-Year Transition Matrix: Derived from one-year transitions (Table 19.2).
- One-Month Transition Matrix: Calculated from one-year transitions (Table 19.3).

6.3 Credit VaR

- Defined analogously to Market Risk VaR.
- A one-year Credit VaR at 99.9% confidence represents the loss level not expected to be exceeded within the year.

6.4 Vasicek's Model

• For a large loan portfolio:

$$WCDR = N^{-1} [N^{-1}(PD) + \sqrt{r}N^{-1}(X)]$$

• N^{-1} is the inverse cumulative normal distribution, PD is the probability of default, and r is the Gaussian copula correlation.

6.5 VaR Model

• Credit VaR is calculated as:

$$VaR = LGD \times EAD \times WCDR$$

• Extended by Gordy for more complex portfolios.

6.6 Credit Risk Plus

- Default rate modeled using Poisson distribution.
- If default rate has a gamma distribution, defaults follow a negative binomial distribution.

6.7 Monte Carlo Simulation for Credit Risk Plus

- 1. Sample overall default rate.
- 2. Sample probability of default for each counterparty category.
- 3. Sample number of losses for each category.
- 4. Sample loss size for each default.

5. Calculate total loss from defaults.

Repeated multiple times to create a total loss probability distribution.

6.8 CreditMetrics

- Calculates Credit VaR based on possible rating transitions.
- Uses a Gaussian copula model to define correlations between rating transitions of different companies.

6.9 Credit Risk in the Trading Book

- Two alternatives for calculating 10-day 99% VaR:
 - Historical simulation to analyze potential credit spread changes.
 - Transition matrix combined with the CreditMetrics approach.

6.10 Constant Level of Risk Assumption

- For a BBB bond with a 3-month liquidity horizon:
 - If the bond deteriorates, it is replaced at the end of each 3-month period.
 - The one-year loss is then represented as four consecutive 3-month losses.

7 Economic Capital and RAROC

7.1 Economic Capital

• Defined as a bank's own assessment of the capital required to cover risks.

7.2 Model Used for Economic Capital

- Similar to the model for regulatory capital.
- Capital is chosen based on a desired confidence level (e.g., 99.98%) and a one-year time horizon.
- AA-rated companies have a 0.02% probability of defaulting in one year.

7.3 Basel II Regulatory Environment

- Risks categorized into:
 - Non-Business Risk (regulatory capital): Credit risk, market risk, operational risk.
 - Business Risk (no regulatory capital): Risk from strategic decisions, reputation risk.

7.4 Characteristics of Risk Distributions

- Market Risk: High variance, zero skewness, low kurtosis.
- Credit Risk: Moderate variance, moderate skewness, moderate kurtosis.
- Operational Risk: Low variance, high skewness, high kurtosis.

7.5 Interactions of Risks

- Credit and market risks influence each other (e.g., LGD and PD depend on market value).
- Operational risks can depend on market moves or credit events.

7.6 Integrated Risk Management

- Economic capital is calculated for different risks and business units.
- Aggregation of risks involves dealing with correlations between them.

7.7 Combining Distributions

- Perfect correlation overstates capital by 40%.
- Assuming normal distributions understates capital by 40%.
- A hybrid approach provides more accurate results.

7.8 Example: Economic Capital Estimates

- Economic capital estimates for two business units:
 - Business Unit 1: Market risk = 30, credit risk = 70, operational risk = 30.
 - Business Unit 2: Market risk = 40, credit risk = 80, operational risk = 90.
- Total economic capital:
 - Business Unit 1: 100.

- Business Unit 2: 153.7.

- Whole bank: 203.2.

7.9 RAROC (Risk-Adjusted Return on Capital)

• Measures return on economic capital allocated to a business unit.

• Calculated as:

$$RAROC = \frac{ExpectedProfit}{EconomicCapital}$$

• Expected profit may include risk-free interest on economic capital.

7.10 Example: Lending in a Region

- AA-rated bank estimates average losses from defaults as 1% of outstanding loans annually.
- Worst-case loss at 99.98% confidence: 5%.
- Economic capital per \$100 of loans = \$4.
- Spread between cost of funds and interest charged = 2.5%, administrative costs = 0.7%.

7.11 Ex-ante vs Ex-post RAROC

- Ex-ante: Used for forecasting and capital allocation.
- Ex-post: Used for performance evaluation, replacing expected loss with realized loss.

8 Climate Risk, ESG, and Sustainability

8.1 Major Cause of Climate Change

- Tens of billions of tons of greenhouse gases are emitted annually due to:
 - Burning fossil fuels.
 - Manufacturing cement, concrete, steel, and plastics.
 - Raising animals for food.
- These gases trap heat, reducing the radiation back into space, leading to global warming.

8.2 Paris and Glasgow Agreements

- Paris Agreement (2015): Aims to limit temperature rise to 1.5°C above pre-industrial levels.
- Glasgow Agreement (2021): Strengthened 2030 targets to achieve netzero emissions by 2050.

8.3 IPCC Sixth Assessment Report (2021)

- Highlights five Shared Socioeconomic Pathways (SSPs):
 - SSP1: CO_2 emissions net zero by 2050, warming: 1.4°C (2081–2100).
 - SSP5: CO_2 emissions triple by 2075, warming: 4.4°C (2081–2100).

8.4 Greenhouse Gas Emissions by Sector

- Transportation: 27%.
- Electricity: 25%.
- Industry: 24%.
- Commercial and Residential: 13%.
- Agriculture: 11%.

8.5 Costly Results of Climate Change

- Rising sea levels.
- Ocean acidification.
- Increased storms, heatwaves, wildfires, hurricanes, and tornadoes.

8.6 Organizations Addressing Climate Risk

- Task Force on Climate-Related Financial Disclosures (TCFD): Led by Michael Bloomberg.
- Glasgow Financial Alliance for Net Zero (GFANZ): Led by Mark Carney.

8.7 Physical vs. Transition Risks

- Physical Risks: Costs from extreme climate events (e.g., floods, hurricanes).
- Transition Risks: Costs of reducing emissions (e.g., carbon taxes, plant closures).

8.8 Impact on Financial Institutions

- Banks: Climate risks affect credit, market, liquidity, operational, and reputational risks.
- Insurance Companies: Challenges for property, casualty, and life insurance sectors.

8.9 Institutional Investors

- Institutional investors significantly influence company climate risk policies.
- Examples: California State Teachers Retirement System, BlackRock.

8.10 ESG (Environmental, Social, and Governance)

- Environmental: Includes climate change and resource use.
- Social: Covers diversity, equity, inclusion, and worker well-being.
- Governance: Involves transparent and socially responsible policies.

8.11 Sustainability

- Defined as meeting present needs without compromising future generations.
- Focus areas include pollution, soil and water contamination, overfishing, and deforestation.

8.12 Greenwashing

- Companies make misleading claims about their environmental friendliness.
- Examples discussed in Section 23.4.

9 Model Risk Management

9.1 Uses of Models

- Credit decisions and exposures.
- Liquidity management.
- Derivatives valuation.
- Calculation of risk measures such as VaR and ES.
- Asset management.
- Fraud detection.

9.2 SR 11-7 Guidance

- Issued by the U.S. Board of Governors, providing guidance on model risk management.
- **Definition of Model Risk:** The potential for adverse consequences due to incorrect or misused model outputs.
- Sources of model risk:
 - Fundamental errors: data, calculations, numerical procedures, assumptions.
 - Inappropriate use of the model.
- Directives include:
 - Model development, testing, and documentation.
 - Role of model validation groups.
 - Use of vendor models.

9.3 Finance vs Physics

- Physics models describe physical processes and are highly accurate with unchanging parameters.
- Finance models describe human behavior and are approximations with parameters that evolve over time.

9.4 Linear Products

- Little uncertainty about the correct model.
- Mistakes still occur (e.g., Kidder Peabody, In Arrears Swaps).
- Monitoring trading patterns is critical; unusual activity may indicate model inaccuracies.

9.5 Models for Pricing Actively Traded Products

- Market prices are often directly available.
- Models serve as communication tools (e.g., implied volatilities) or interpolation tools (e.g., strike prices and maturities).
- Hedging performance depends on model accuracy.

9.6 Models for Less Actively Traded Products

- Models are essential for both pricing and hedging.
- Pricing risks can be managed by:
 - Using multiple models calibrated to actively traded instruments.
 - Establishing reserve accounts to delay profit recognition.
 - Using weighted Monte Carlo to identify consistent pricing models.

9.7 Marking the Prices of an Instrument to Market

- Sources include:
 - Market maker quotes.
 - Recent trades by the financial institution.
 - SEFs or interdealer brokers.
 - Price indications or models.

9.8 Accounting Standards

- FASB 157 and IASB 39 classify instruments as "held for sale" or "held to maturity."
- Mark-to-market requirements:
 - Level 1: Quoted prices in active markets.
 - Level 2: Quoted prices for similar products in active markets.
 - Level 3: Requires valuation assumptions.

9.9 Model Building Missteps

- Common issues:
 - Overfitting.
 - Overparametrization.
 - Excessive complexity, making the model unusable for its intended users.
- Simpler models, like Black-Scholes, succeed due to their practical usability.

10 Value at Risk and Expected Shortfall

10.1 The Question in VaR

"What loss level is such that we are X% confident it will not be exceeded in N business days?"

10.2 VaR and Regulatory Capital

- VaR traditionally used for calculating required regulatory capital.
- Market-risk capital: Based on a 10-day VaR with 99% confidence.
- Credit and operational risk capital: Based on a one-year 99.9% VaR.
- Recently, regulators have shifted to Expected Shortfall (ES) for market risks.

10.3 Advantages of VaR

- Captures risk in a single number.
- Easy to understand.
- Answers the question: "How bad can things get?"

10.4 VaR vs Expected Shortfall

- VaR: The loss level not expected to be exceeded with a given probability.
- ES (Expected Shortfall): Expected loss given that the loss exceeds the VaR level.
- ES is more coherent and satisfies properties such as subadditivity.
- Regulators now use ES for determining market risk capital.

10.5 Spectral Risk Measures

- Assign weights to quantiles of the loss distribution.
- VaR: All weight assigned to the X-th percentile.
- ES: Equal weight assigned to percentiles greater than the X-th percentile.
- Coherent measures require weights to be non-decreasing functions of percentiles.

10.6 Normal Distribution Assumption

- Losses/gains are assumed normally distributed with mean μ and standard deviation σ .
- VaR and ES can be calculated using:

$$VaR = \mu + \sigma Z$$

$$ES = \mu + \frac{\sigma e^{-Z^2/2}}{\sqrt{2\pi}(1-X)}$$

• Z is the X-th percentile of the standard normal distribution.

10.7 Changing the Time Horizon

• For independent, normally distributed daily losses:

$$VaR_{T-day} = \sqrt{T} \times VaR_{1-day}$$

$$ES_{T-day} = \sqrt{T} \times ES_{1-day}$$

• With autocorrelation r, adjust by incorporating autocorrelation terms.

10.8 Aggregating VaRs

• Total VaR can be approximated using:

$$VaR_{total} = \sqrt{\sum_{i} VaR_{i}^{2} + \sum_{i \neq j} \rho_{ij} VaR_{i} VaR_{j}}$$

• ρ_{ij} : Correlation between losses from segments i and j.

10.9 VaR Measures for Portfolios

- Marginal VaR: Sensitivity of VaR to a small change in portfolio weight.
- Incremental VaR: Change in VaR due to inclusion/exclusion of an asset.
- Component VaR: Allocates total VaR to portfolio components.

10.10 Back-testing and Bunching

- Back-testing involves checking how often losses exceed VaR (exceptions).
- Statistical tests, such as those by Christoffersen, can identify bunching (clustering of exceptions).

11 Basel I, Basel II, and Solvency II

11.1 History of Bank Regulation

- Pre-1988: Banks regulated using balance sheet measures such as capital-to-assets ratio.
- 1988: Introduction of BIS Accord (Basel I).
- 1996: Amendment to BIS Accord.
- 1999: Basel II first proposed.

11.2 1988: BIS Accord

- Capital must be at least 8% of risk-weighted assets (RWA).
- At least 50% of capital must be Tier 1 capital.

11.3 Types of Capital

- Tier 1 Capital: Common equity and non-cumulative perpetual preferred shares.
- Tier 2 Capital: Includes cumulative preferred stock, 99-year debentures, and subordinated debt with an original life exceeding 5 years.

11.4 Risk-Weighted Capital

- Risk weights assigned based on asset risk (e.g., 0% for cash, 100% for corporate loans).
- For OTC derivatives and off-balance-sheet commitments:
 - Calculate credit equivalent amount using current exposure method (CEM).
 - Apply a risk weight to the credit equivalent amount.

11.5 Netting

- Netting clauses allow OTC derivatives with a counterparty to be treated as a single transaction in case of default.
- 1995 modification to allow reduction in credit equivalent totals with bilateral netting agreements.

11.6 1996 Amendment

- Implemented in 1998.
- Required capital for market risk for all instruments in the trading book (on and off-balance-sheet).

11.7 Basel II

- Implemented in 2007.
- Three Pillars:
 - Pillar 1: New capital requirements for credit and operational risk.
 - Pillar 2: Supervisory review for uniform enforcement.
 - Pillar 3: Market discipline with increased disclosure requirements.

11.8 New Capital Requirements

- Two approaches for risk weighting:
 - Standardized Approach: Based on external credit ratings.
 - IRB Approach: Based on internal ratings (Advanced and Foundation IRB).
- Separate capital charge for operational risk.

11.9 Operational Risk Capital

- Basic Indicator Approach: 15% of gross income.
- Standardized Approach: Multiplicative factors for gross income per business line.
- Internal Measurement Approach: Capital equals 99.9% VaR minus expected one-year loss.

11.10 Solvency II

- Three pillars similar to Basel II:
 - Pillar 1: Specifies Minimum Capital Requirement (MCR) and Solvency Capital Requirement (SCR).
 - Pillar 2: Supervisory review.
 - Pillar 3: Market discipline.
- Internal models vs standardized approach.
- Capital charge for investment risk, underwriting risk, and operational risk.

12 Basel II.5, Basel III, and Other Post-Crisis Changes

12.1 Basel II.5 (Implemented December 31, 2011)

- Stressed VaR:
 - Calculated over a one-year period of stressed market conditions.
 - Capital requirement:

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Capital = \max(VaR_{t-1}, mc \times VaR_{avg}) + \max(sVaR_{t-1}, ms \times sVaR_{avg})
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- Incremental Risk Charge: Ensures similar capital requirements for trading book and banking book products.
- Comprehensive Risk Measure: Addresses capital for instruments dependent on credit default correlations.

12.2 Basel III

• Full implementation by 2022.

• Key Components:

- Capital definition and requirements.
- Capital conservation buffer.
- Countercyclical buffer.
- Leverage ratio.
- Liquidity ratios.
- Capital for CVA (Credit Valuation Adjustment) risk.

12.3 Capital Definition and Requirements

• Types of Capital:

- Common Equity Tier 1 (CET1): $\geq 4.5\%$ of RWA.
- Tier 1: $\geq 6\%$ of RWA.
- Tier 1 + Tier 2: \geq 8% of RWA.

12.4 Capital Buffers

- Capital Conservation Buffer: 2.5% extra CET1 in normal times to absorb stress losses.
- Countercyclical Buffer: Up to 2.5% CET1, left to national regulators, to account for cyclicality in bank earnings.

12.5 Leverage Ratio

- Minimum Tier 1 capital to total exposure ratio: $\geq 3\%$ (higher in some jurisdictions).
- Exposure includes all on-balance-sheet items, derivatives, securities financing, and off-balance-sheet items.

12.6 Liquidity Risk Ratios

- Liquidity Coverage Ratio (LCR): Ensures sufficient high-quality liquid assets to cover 30-day cash outflows during acute stress.
- Net Stable Funding Ratio (NSFR): Promotes stable funding over a one-year time horizon.

12.7 G-SIBs and D-SIBs

- Global Systemically Important Banks (G-SIBs):
 - Required to hold 1-3.5% additional Tier 1 capital.
 - Subject to Total Loss Absorbing Capacity (TLAC) requirements.
- Domestic Systemically Important Banks (D-SIBs):
 - Additional capital, disclosure, and stress testing requirements.
 - In the U.S., banks with assets over \$50 billion are classified as D-SIBs.

12.8 Contingent Convertible Bonds (CoCos)

- Convert to equity under specific conditions, e.g.:
 - Tier 1 equity falls below 7% of RWA.
 - Regulatory determination of need for public sector support.

12.9 Dodd-Frank Act

- Introduced new systemic risk monitoring bodies (FSOC and OFR).
- Imposed the Volcker Rule to restrict proprietary trading.
- Required central clearing for OTC derivatives.
- Mandated "living wills" for large financial institutions.
- Increased capital requirements for Systemically Important Financial Institutions (SIFIs).
- Prohibited use of external credit ratings for regulatory purposes.

12.10 Global Regulatory Changes

- UK: Financial Services (Banking Reform Act) implemented in 2013.
- European Union: New regulations proposed in 2012 by the Liikanen Committee.

12.11 Key Issues Addressed by Regulators

- Central clearing and use of electronic trading platforms.
- Restrictions or insulation of proprietary trading from other activities.
- Enhanced transparency through living wills.
- Compensation reform (less stringent in the U.S.).