LECTURE NO. 5 |LINEAR **MATH 205** CASSIAN ELIMINATION: (FCHELON A MATRIX HAVING THE FORM FOLLOWING PROPERTIES IS SAID TO BE IN ROW- ECHELON FORM. (1) IF A ROW DOES NOT CONSIST ENTIRELY OF ZEROS, THEN THE FIRST NONZERO NUMBER IN THE ROW IS A 1. ( WE CALL THIS A LEADING 1). (2) IF THERE ARE ANY ROWS THAT CONSIST ENTIRELY OF ZEROS THEN THEY ARE GROUPED TOGE-THER AT THE BOTTOM OF THE MATRIX. (3) IN ANY (TWO SUCCESSIVE ROWS THAT DO NOT CONSIST ENTIRELY OF ZEROS, THE LEADING I IN THE LOWER

ROW OCCURS FARTHER TO

THE RIGHT THAN THE

ROW.

LEADING II IN THE HIGHER

2

EXAMPLES: THE FOLLOWING

MATRICES ARE IN ROW-ECHELON

FORM.

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NOTE: IN THIS SECTION

WE SHALL DISCUSS A

PROCEDURE FOR SOLVING

SYSTEMS OF LINEAR EQU
ATIONS BY REDUCING THE

AUGMENTED MATRIX TO

ROW-ECHELON FORM.

CONSIDER THE FOLLOWING

EXAMPLE:

3

EXAMPLE: SOLVE THE FOLLOWING SYSTEM BY GAUSSIAN EUMINAT-ION (ECHELON FORM) METHOD.

> $3x_1 + 4x_2 + 5x_3 = 12$   $x_1 - x_2 + 2x_3 = 2$  $2x_1 + x_2 + 3x_3 = 6$

SOLUTION: WE SHALL REDUCE THE AUCMENTED MATRIX TO ECHELON FORM, CONSIDER

 $\sim R_{1} \leftarrow 7R_{2} \begin{bmatrix} 1 & -1 & 2 & 2 \\ 3 & 4 & 5 & 12 \\ 2 & 1 & 3 & 6 \end{bmatrix}$ 

## NOTES:

- (1) IN ROW REDUCTION PROCESS DON'T PERFORM ANY SE STEPS BY WHICH YOUT PERFORM ANY ALREADY).
- (2) IF POSSIBLE THEN AVOID

  THE FORMATION OF

  FRACTIONS.

## ASSIGNMENT NO. 2

(a) UNDER WHAT CONDITIONS

AB = BA, WHERE

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}, B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}$$

(b) IF A IS A MATRIX THEN

A" A" = A" FOR SUS POSI-

TIVE INTEGERS. IS THIS RESULT TRUE FOR NEGA-TIVE INTEGERS ALSO? JUSTIFY YOUR ANSWER. (c) IF  $A = \begin{bmatrix} 0 & 1 \\ 0 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} 1 & 1 \\ 3 & 4 \end{bmatrix}$ AND C = [2 5] THEN AB=AC= [3 4] BUT B + C,

WHY? Q. no.2

USING THE TECHNIQUE OF FOR-MING A BLOCK MATRIX [A/I] AND PERFORMING E.R.O.S SUCH THAT

[A I] E.R.O.S [I A]

FIND THE INVERSE OF THE

FOLLOWING WHERE A IS GIVEN BY

(a) 
$$\begin{bmatrix} 1 & 0 & 2 \\ 2 & -1 & 3 \\ 4 & 1 & 8 \end{bmatrix}$$
 (b)  $\begin{bmatrix} 1 & 2 & -4 \\ -1 & -1 & 5 \\ 2 & 7 & -3 \end{bmatrix}$ 

[a.no.3]

SOLVE THE FOLLOWING SYSTEM OF EQUATIONS BY REDUCING THEM TO ECHELON FORM (CAUSSIAN ELIMINATION METHOD)

x + y + 23 = 9 2x + 4y - 33 = 1 3x + 6y - 53 = 0

Q.no.4

SOLVE THE FOLLOWING SYST-EM BY GAUSS-JORDAN ELIM-INATION (REDUCED ROW-ECH-ELON FORM)

> $2x_1 + 2x_2 + 2x_3 = 0$   $-2x_1 + 5x_2 + 2x_3 = 1$  $8x_1 + x_2 + 4x_3 = -1$

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Q.no.5
REDUCE [2 1 3 TO 3 TO 3 4 5]
 REDUCED ROW ECHELON FORM
WITHOUT INTRODUCING ANY
 FRACTIONS.
      Q. no. 6
 FIND TWO DIFFERENT
ROW. ECHELON FORMS OF
      [2 ]
   TRY Q. no. 25 (P.22)
         (8th EDITION)
         OR
       Q.no. 25 (P.23)
           7th ED.
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Q.17, P.22 (7THED.) / P.21 (BTH ED.)