



HABIB UNIVERSITY

Data Structures & Algorithms

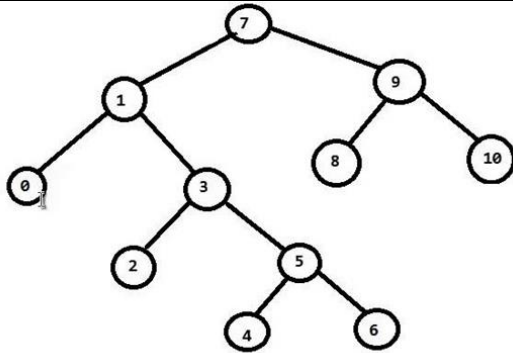
CS/CE 102/171 Spring 2023

Instructor: Maria Samad

Binary Tree Representation – Array-Based

Student Name: _____

For the given trees, define them using Array Based Representation (implemented using Lists), and answer the specified questions



Tree Representation:

$T = [7, 1, 9, 0, 3, 8, 10, \text{None}, \text{None}, 2, 5, \text{None}, \text{None}, \text{None}, \text{None}, \text{None}, \text{None}, \text{None}, 4, 6, \text{None}, \text{None}, \text{None}, \text{None}, \text{None}, \text{None}, \text{None}, \text{None}]$

Parent of Node 5 (Use formula on the list to evaluate):

$$\begin{aligned}\text{Parent Position} &= \text{floor}[(f(p) - 1) / 2] \\ &= \text{floor}[(10 - 1) / 2] \\ &= \text{floor}(9/2) \\ &= \text{floor}(4.5) \\ &= 4\end{aligned}$$

Thus, Parent Node = Node 3

Left Child of Node 8 (Use formula on the list to evaluate):

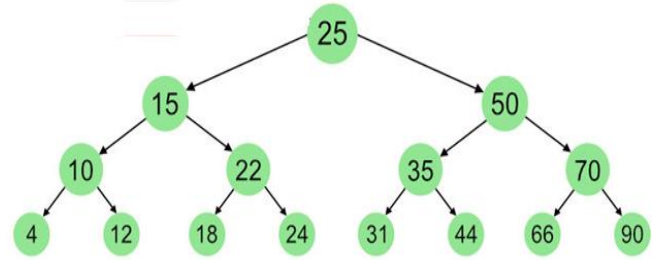
$$\begin{aligned}\text{Left Child Position} &= 2f(p) + 1 \\ &= 2(5) + 1 \\ &= 10 + 1 \\ &= 11\end{aligned}$$

Thus, Left Child = None i.e. no left child

Right Child of Node 9 (Use formula on the list to evaluate):

$$\begin{aligned}\text{Right Child Position} &= 2f(p) + 2 \\ &= 2(2) + 2 \\ &= 4 + 2 \\ &= 6\end{aligned}$$

Thus, Right Child = Node 10



Tree Representation:

$T = [25, 15, 50, 10, 22, 35, 70, 4, 12, 18, 24, 31, 44, 66, 90]$

Parent of Node 35 (Use formula on the list to evaluate):

$$\begin{aligned}\text{Parent Position} &= \text{floor}[(f(p) - 1) / 2] \\ &= \text{floor}[(5 - 1) / 2] \\ &= \text{floor}(4/2) \\ &= \text{floor}(2) \\ &= 2\end{aligned}$$

Thus, Parent Node = Node 50

Left Child of Node 70 (Use formula on the list to evaluate):

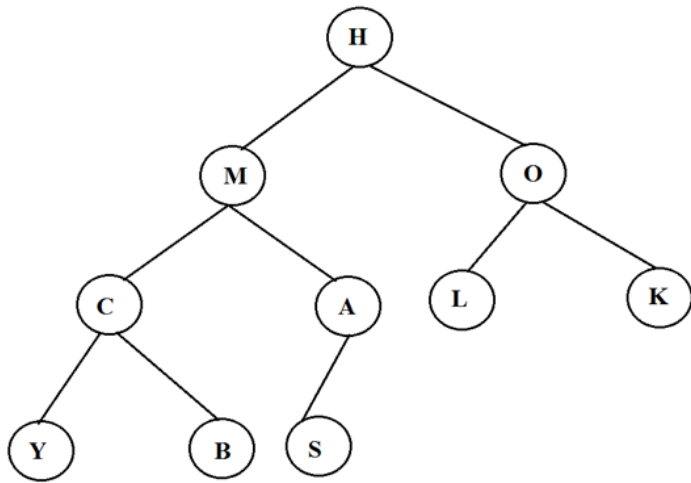
$$\begin{aligned}\text{Left Child Position} &= 2f(p) + 1 \\ &= 2(6) + 1 \\ &= 12 + 1 \\ &= 13\end{aligned}$$

Thus, Left Child = Node 66

Right Child of Node 25 (Use formula on the list to evaluate):

$$\begin{aligned}\text{Right Child Position} &= 2f(p) + 2 \\ &= 2(0) + 2 \\ &= 0 + 2 \\ &= 2\end{aligned}$$

Thus, Right Child = Node 50



Tree Representation:

T = [H, M, O, C, A, L, K, Y, B, S, None, None, None, None, None]

Parent of Node S (Use formula on the list to evaluate):

$$\begin{aligned}
 \text{Parent Position} &= \text{floor}[(f(p) - 1) / 2] \\
 &= \text{floor}[(9 - 1)/2] \\
 &= \text{floor}(8/2) \\
 &= \text{floor}(4) \\
 &= 4
 \end{aligned}$$

Thus, Parent Node = Node A

Left Child of Node O (Use formula on the list to evaluate):

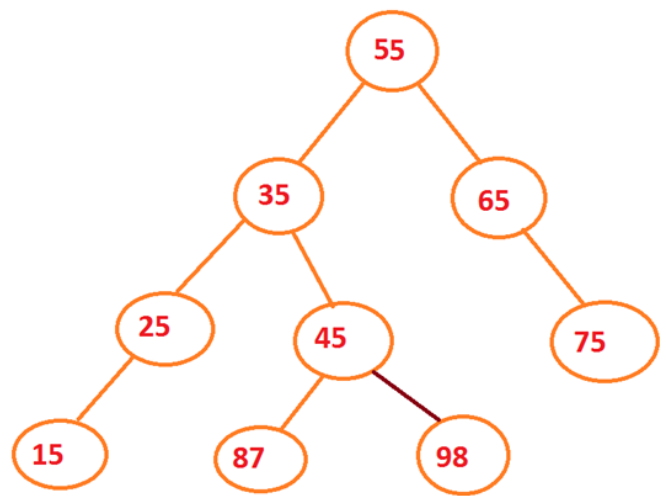
$$\begin{aligned}
 \text{Left Child Position} &= 2f(p) + 1 \\
 &= 2(2) + 1 \\
 &= 4 + 1 \\
 &= 5
 \end{aligned}$$

Thus, Left Child = Node L

Right Child of Node C (Use formula on the list to evaluate):

$$\begin{aligned}
 \text{Right Child Position} &= 2f(p) + 2 \\
 &= 2(3) + 2 \\
 &= 6 + 2 \\
 &= 8
 \end{aligned}$$

Thus, Right Child = Node B



Tree Representation:

T = [55, 35, 65, 25, 45, None, 75, 15, None, 87, 98, None, None, None, None]

Parent of Node 87 (Use formula on the list to evaluate):

$$\begin{aligned}
 \text{Parent Position} &= \text{floor}[(f(p) - 1) / 2] \\
 &= \text{floor}[(9 - 1)/2] \\
 &= \text{floor}(8/2) \\
 &= \text{floor}(4) \\
 &= 4
 \end{aligned}$$

Thus, Parent Node = Node 45

Left Child of Node 25 (Use formula on the list to evaluate):

$$\begin{aligned}
 \text{Left Child Position} &= 2f(p) + 1 \\
 &= 2(3) + 1 \\
 &= 6 + 1 \\
 &= 7
 \end{aligned}$$

Thus, Left Child = Node 15

Right Child of Node 75 (Use formula on the list to evaluate):

$$\begin{aligned}
 \text{Right Child Position} &= 2f(p) + 2 \\
 &= 2(6) + 2 \\
 &= 12 + 2 \\
 &= 14
 \end{aligned}$$

Thus, Right Child = None, i.e. no right child