

BE1M13VES

Manufacturing of Electrical Components

Michal Brejcha

CTU in Prague

Prague, 2017

Overview

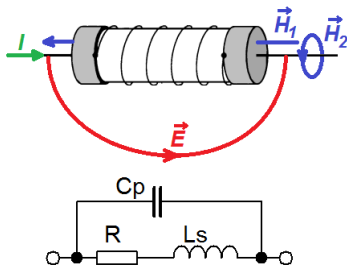
- 1 Frequency dependency of resistors
- 2 Frequency dependency of capacitors
- 3 Frequency dependency of inductors
- 4 Notes

TOPIC

- 1 Frequency dependency of resistors
- 2 Frequency dependency of capacitors
- 3 Frequency dependency of inductors
- 4 Notes

Equivalent Circuit

For AC circuits the parasitic serial inductance and parallel capacity must be taken into account. The frequency dependence of the resistors is caused especially by its construction.



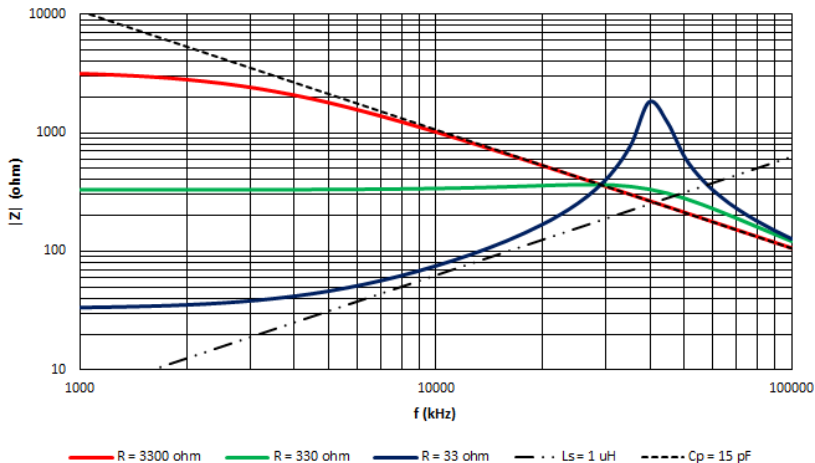
- $H_1, H_2 \dots$ magnetic field from resistive track and leads.
- $E \dots$ electric field (capacitance) between opposite sides of package and leads.

Technology Overview

- Parasitic capacitance is dominant for higher values of resistance ($> \text{k}\Omega$).
- Parasitic inductance is dominant only for small values of resistance ($< 100\Omega$) and frequencies smaller than resonant frequency.
- Larger packages have larger parasitic inductance
 - power resistors (resistive wire) - worst
 - small smd thin film resistors - best



Impedance Plot Example



Equivalent Circuit Analysis

Impedance:

$$\hat{Z} = \frac{R - \frac{j}{\omega C_p} \cdot \left(\omega^2 L_s C_p \cdot (\omega^2 L_s C_p - 1) + (\omega C_p R)^2 \right)}{(1 - \omega^2 L_s C_p)^2 + (\omega C_p R)^2}$$

Low frequencies ($\omega \rightarrow 0$): **resistivity**

$$\hat{Z} \approx R$$

High frequencies ($\omega \gg \omega_{REZ}$): **parasitic capacitance effect**

$$\hat{Z} \approx \frac{1}{j\omega C_p}$$

Equivalent Circuit Analysis - Resonance

Resonance frequency:

$$\omega_{REZ} = \sqrt{\frac{1}{L_s C_p} - \left(\frac{R}{L_s}\right)^2}$$

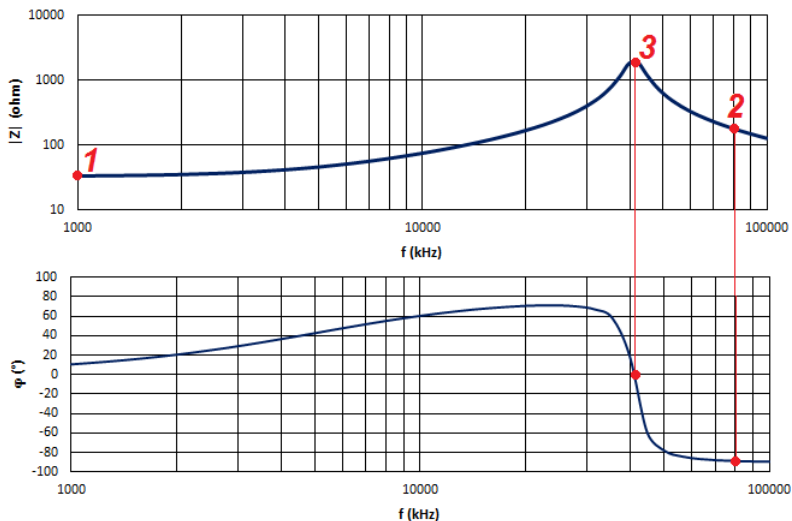
Impedance at ω_{REZ}

$$\hat{Z}_{REZ} = \frac{Z_0^2}{R}$$

Where Z_0 has the same definition as wave impedance:

$$Z_0 = \sqrt{\frac{L_s}{C_p}}$$

Analysis Example



Analysis Example

1 Resistance:

$$R = 33\Omega$$

2 Capacitance (**15 pF**):

$$C_p \approx \frac{1}{\omega \cdot |Z|} = \frac{1}{503 \cdot 10^6 \cdot 180} = 11pF$$

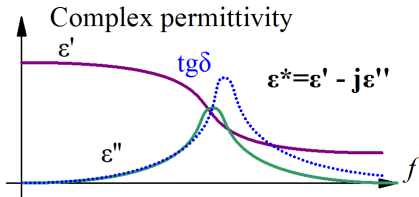
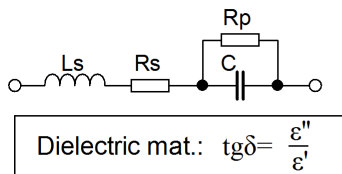
3 Inductance (**1 μ H**):

$$L \approx Z_{REZ} \cdot R \cdot C_p = 1900 \cdot 33 \cdot 15 \cdot 10^{-12} = 940\mu H$$

TOPIC

- 1 Frequency dependency of resistors
- 2 Frequency dependency of capacitors**
- 3 Frequency dependency of inductors
- 4 Notes

Equivalent Circuit



Frequency dependence due to package properties:

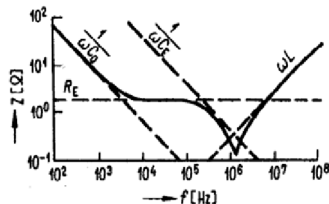
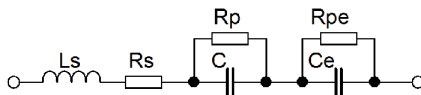
- Parasitic inductance of the leads and electrodes L_s .
- Parasitic resistance of the leads R_s .

Frequency dependence due to material properties (complex permittivity):

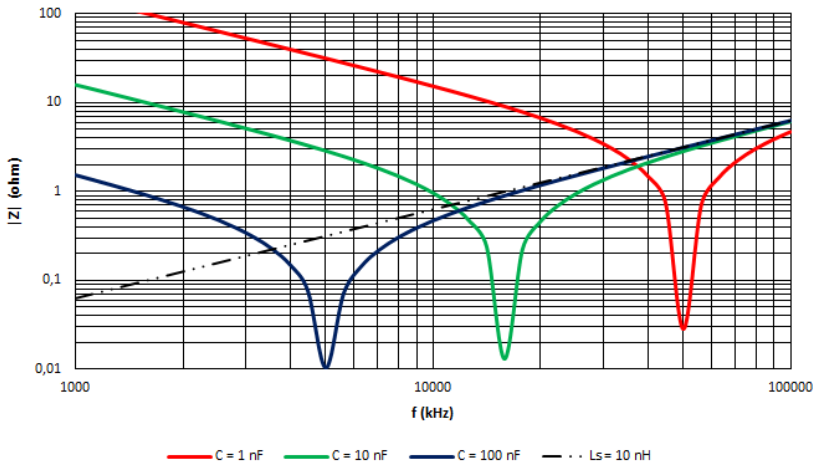
- Change in dielectric power dissipation R_p (ϵ'') - dissip. factor (D).
- Change in capacity C (ϵ').

Technology Overview

- Capacitors with higher capacitance have lower resonant frequency.
- Foil capacitors have larger parasitic inductance L_s .
- Electrolytic capacitors have higher serial parasitic resistance R_s due to electrolyte presence.
- Equivalent scheme of electrolytic capacitor:



Impedance Plot Example



Equivalent Circuit Analysis

Impedance:

$$\hat{Z} = R_s + \frac{R_p}{(1 + (\omega CR_p)^2)} + j \left(\omega L_s - \frac{1}{\omega C} \cdot \frac{(\omega CR_p)^2}{(1 + (\omega CR_p)^2)} \right)$$

Low frequencies ($\omega \ll \omega_{REZ}$): **capacitance**

$$\hat{Z} \approx \frac{1}{j\omega C}$$

High frequencies ($\omega \gg \omega_{REZ}$): **parasitic inductance**

$$\hat{Z} \approx j\omega L_s$$

Equivalent Circuit Analysis - Resonance

Resonance frequency:

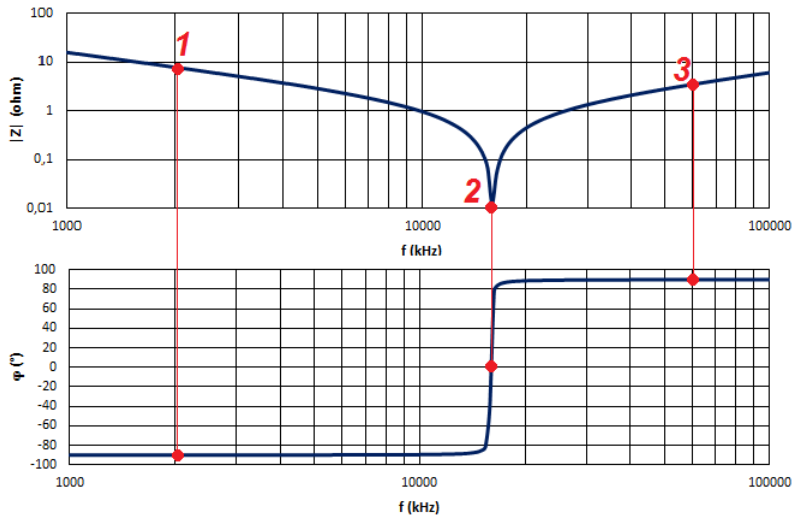
$$\omega_{REZ} = \sqrt{\frac{1}{L_s C} - \left(\frac{1}{R_p C p}\right)^2} \approx \sqrt{\frac{1}{L_s C}}$$

Impedance at ω_{REZ}

$$\hat{Z}_{REZ} = R_s + \frac{Z_0^2}{R_p} \approx R_s$$

- The approximation is made for capacitors with high resistance R_p and value of capacitance $C > 1 \text{ nF}$
- The higher resistance at the resonance is caused by the factor $\frac{Z_0^2}{R_p}$ or by **skin-effect**.
- The parasitic resistances can change due to frequency dependence of complex permittivity.

Analysis Example



Analysis Example

1 Capacitance (**10 nF**):

$$C \approx \frac{1}{\omega \cdot |Z|} = \frac{1}{12.6 \cdot 10^6 \cdot 7.85} = 10.1 nF$$

2 Serial resistance **0.01 Ω**):

$$R_s \approx Z_{REZ} = 0.01 \Omega$$

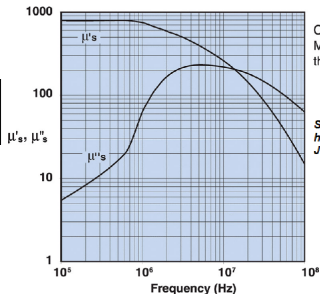
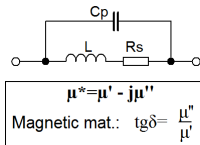
3 Inductance (**10 nH**):

$$L \approx \frac{|Z|}{\omega} = \frac{3.65}{376 \cdot 10^6} = 9.7 nH$$

TOPIC

- 1 Frequency dependency of resistors
- 2 Frequency dependency of capacitors
- 3 Frequency dependency of inductors**
- 4 Notes

Equivalent Circuit

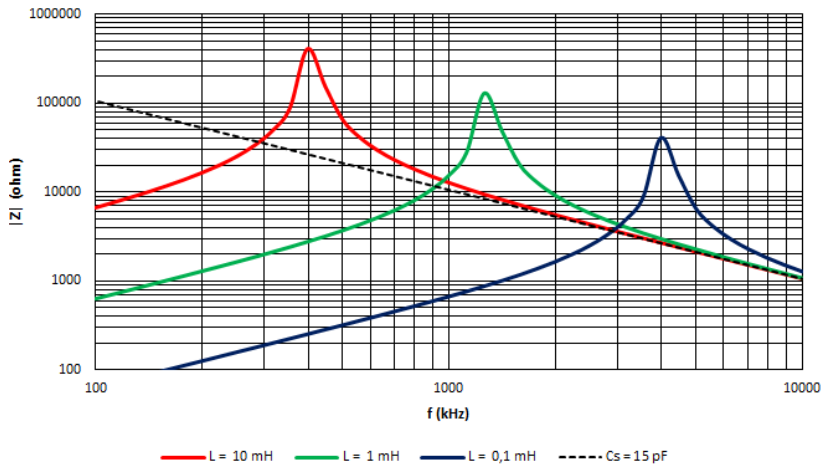


Complex Permeability vs. Frequency
 Measured on a 17/10/6mm toroid using
 the HP 4284A and the HP 4291A.

Source:
http://www.nutsvolts.com/magazine/article/July2015_HamWorkbench

- The same equivalent circuit as in case of resistors.
- The frequency dependence strongly affected by core material properties and skin-effect.
- Coils with high impedance have lower resonant frequencies.

Impedance Plot Example



Equivalent Circuit Analysis

Very low frequencies ($\omega \rightarrow 0$): **parasitic resistivity**

$$\hat{Z} \approx R_s$$

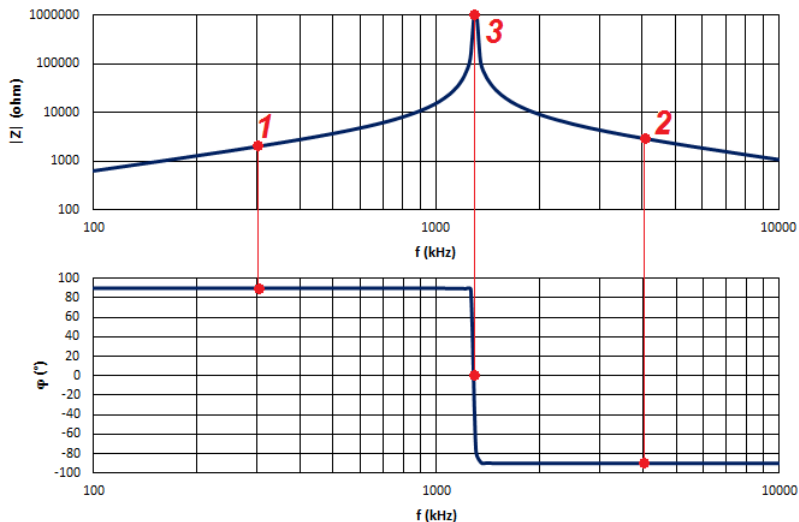
Low frequencies ($\omega \ll \omega_{REZ}$): **inductance**

$$\hat{Z} \approx j\omega L$$

High frequencies ($\omega \gg \omega_{REZ}$): **parasitic capacitance effect**

$$\hat{Z} \approx \frac{1}{j\omega C_p}$$

Analysis Example



Analysis Example

- 1 Inductance (**1 mH**):

$$L \approx \frac{|Z|}{\omega} = \frac{2050}{1885 \cdot 10^3} = 1.1 \text{ mH}$$

- 2 Parallel capacitance (**15 pF**):

$$C \approx \frac{1}{\omega \cdot |Z|} = \frac{1}{25.1 \cdot 10^6 \cdot 2970} = 13 \text{ pF}$$

- 3 Serial resistance **10 Ω**):

$$R_s \approx \frac{Z_0^2}{Z_{REZ}} = \frac{10^{-3}}{1510^{-12} \cdot 10^6} = 6.67 \Omega$$

- **NO!** ... better to find out the serial resistance from DC measurement.

TOPIC

- 1 Frequency dependency of resistors
- 2 Frequency dependency of capacitors
- 3 Frequency dependency of inductors
- 4 Notes**

NOTES

- In case of impedance plot use logarithmic scale for both axis.
- In case of phase plot use logarithmic scale only for frequency.

■

$$\hat{Z} = R + jX$$

■

$$|Z| = \sqrt{R^2 + X^2}$$

■

$$\varphi = \operatorname{arctg} \frac{X}{R}$$

- resonance: $X = 0$, $\varphi = 0$, parallel \Rightarrow high $|Z|$, serial \Rightarrow low $|Z|$