
`%Problem 2`

`echo on`

`% Problem statement: Consider hypotehsis test with $H_0: x \sim N[s_0, \sigma^2 I]$ and
% $H_1: x \sim N[s_1, \sigma^2 I]$, Assume $L_{00}=L_{11}=0$ and $L_{01}=2*L_{10}$. Determine
% α ,
% β , η , and k for a minimax test. Carry out computations for d^2
% $=$
% $(s_1-s_0)T(s_1-s_0)/\sigma^2 = 0.1$ and 10 . For both cases, determine
% nature's
% least favorable prior.
echo off`

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echo off`

`For $d^2=0.1$:`

`d = sqrt(0.1);
z=[-1:0.0001:1];
q1=2*erf(z);
q2=erf(z - d);

closest_val = abs(q1+q2-2);
min_idx = find(closest_val == min(closest_val));
min_z = z(min_idx);`

`eta = min_z*d - (d^2)/2
alpha = 1 - erf(min_z)
beta = 1 -2*alpha
k = exp(eta)
echo on
% Nature's least favorable prior:
echo off
p = k/(2+k)`

`eta =`

`0.2045`

`alpha =`

```

0.2551

beta =

0.4898

k =

1.2269

% Nature's least favorable prior:
echo off

p =

0.3802

For d^2 = 10:

d = sqrt(10);
z=[-1:0.0001:1];
q1=2*erf(z);
q2=erf(z - d);

closest_val = abs(q1+q2-2);
min_idx = find(closest_val == min(closest_val));
min_z = z(min_idx);

eta = min_z*d - (d^2)/2
alpha = 1 - erf(min_z)
beta = 1 -2*alpha
k = exp(eta)
echo on
% Nature's least favorable prior:
echo off
p = k/(2+k)

eta =

-1.8377

alpha =

0.1573

beta =

0.6854

```

$k =$

0.1592

*% Nature's least favorable prior:
echo off*

$p =$

0.0737

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