

# Solving 3D frictional contact problems: Formulations and comparisons of numerical methods.

RESEARCH

REPORT

N° 123456789

September 5, 2017

Project-Team Bipop



# Solving 3D frictional contact problems: Formulations and comparisons of numerical methods.

Project-Team Bipop

Research Report n° 123456789 — September 5, 2017 — 104 pages

Abstract: TBW

**Key-words:** Multibody systems, nonsmooth Mechanics, unilateral constraints, Coulomb friction, impact, numerical methods

RESEARCH CENTRE GRENOBLE – RHÔNE-ALPES

Inovallee

655 avenue de l'Europe Montbonnot

38334 Saint Ismier Cedex

# Sur la résolution du problème de frottement tridimensionnel. Formulations and comparaisons des méthodes numériques.

Résumé: TBW

**Mots-clés :** Systèmes multi-corps, Mécanique non régulière, contraintes unilatérales, frottement de Coulomb, impact, Schémas numériques de résolution

#### Contents

1	${ m LMGC\_100\_PR\_PerioBox}$	4
2	LMGC_945_SP_Box_PL	16
3	LMGC Aqueduc PR	27
4	LMGC Bridge PR	38
5	LMGC LowWall FEM	49
6	LMGC Cubes H8	61
7	Capsules	72
8	Chain	83
g	KanlasTower	94

# $1 \quad LMGC\_100\_PR\_PerioBox$

/	figure/VI/UpdateRule/time/profil	e-LMGC_100_PR_PerioBox.pd	f
/ RR n° 123456789	figure/VI/UpdateRule/time/profil	e-LMGC_100_PR_PerioBox_le	gend.pdf

	/figure/NSGS/LocalSolver/time/profile-LMGC_100_PR_PerioBox.pdf	
RR n° 12345	/figure/NSGS/LocalSolver/time/profile-LMGC_100_PR_PerioBox_legend.p	df

_	
	/figure/NSGS/LocalTol/time/profile-LMGC_100_PR_PerioBox.pdf
RR n° 12345	/figure/NSGS/LocalTol/time/profile-LMGC_100_PR_PerioBox_legend.pdf

_	
	/figure/NSGS/Shuffled/time/profile-LMGC_100_PR_PerioBox.pdf
RR n° 12345	/figure/NSGS/Shuffled/time/profile-LMGC_100_PR_PerioBox_legend.pdf

	/figure/PSOR/time/profile-LMGC_100_PR_PerioBox.pdf
RR n° 1234	/figure/PSOR/time/profile-LMGC_100_PR_PerioBox_legend.pdf

_	
	/figure/NSN/time/profile-LMGC_100_PR_PerioBox.pdf
RR n° 123456'	/figure/NSN/time/profile-LMGC_100_PR_PerioBox_legend.pdf

/figure/OPTI/time/profile-LMGC_100_PR_PerioBox.pdf /figure/OPTI/time/profile-LMGC_100_PR_PerioBox_legend.pdf		
/figure/OPTI/time/profile-LMGC_100_PR_PerioBox_legend.pdf		/figure/OPTI/time/profile-LMGC_100_PR_PerioBox.pdf
RR n° 123456789	RR n° 12345	

	$/figure/PROX/Internal Solvers/time/profile-LMGC\_100\_PR\_PerioBox.pdf$	
RR n° 12345	/figure/PROX/InternalSolvers/time/profile-LMGC_100_PR_PerioBox_lege	nd.pdf

	/figure/PROX/Parameters/time/profile-LMGC_100_PR_PerioBox.pdf
	/figure/PROX/Parameters/time/profile-LMGC_100_PR_PerioBox_legend.pdf
RR n° 12345	6789

	/figure/COMP/large/time/profile-LMGC_100_PR_PerioBox.pdf
	/figure/COMP/large/time/profile-LMGC_100_PR_PerioBox_legend.pdf
RR n° 12345	6789

/figure/COMP/zoom/time/profile-LMGC_100_PR_PerioBox.pdf /figure/COMP/zoom/time/profile-LMGC_100_PR_PerioBox_legend.pdf		
		/figure/COMP/zoom/time/profile-LMGC_100_PR_PerioBox.pdf
NN II 123430189	RR n° 1234	

## $2 \quad LMGC\_945\_SP\_Box\_PL$

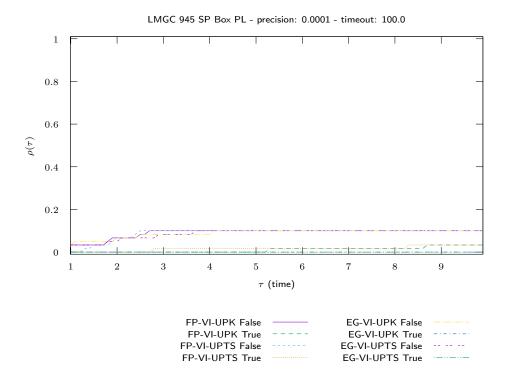


Figure 12: LMGC\_945\_SP\_Box\_PL time VI/UpdateRule

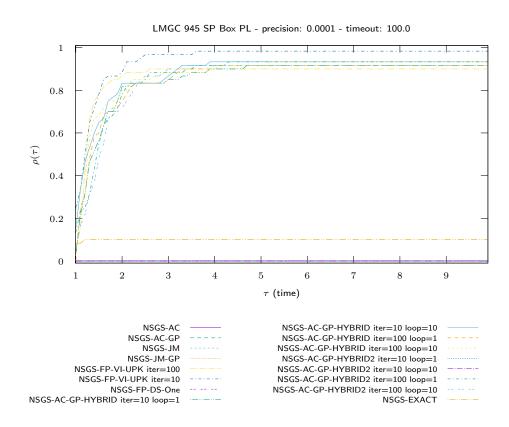


Figure 13: LMGC\_945\_SP\_Box\_PL time NSGS/Local Solver

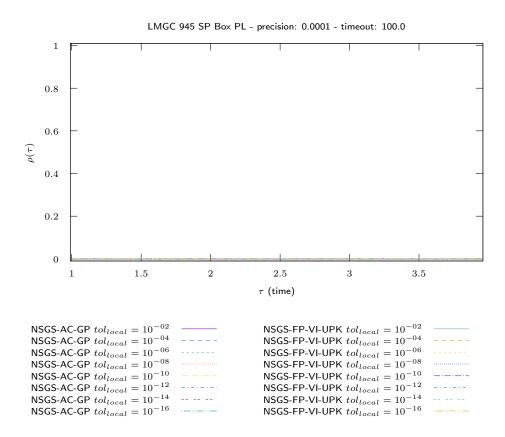


Figure 14: LMGC\_945\_SP\_Box\_PL time NSGS/LocalTol

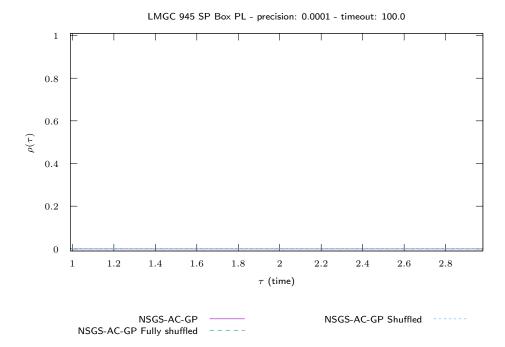


Figure 15: LMGC\_945\_SP\_Box\_PL  $\,$  time NSGS/Shuffled

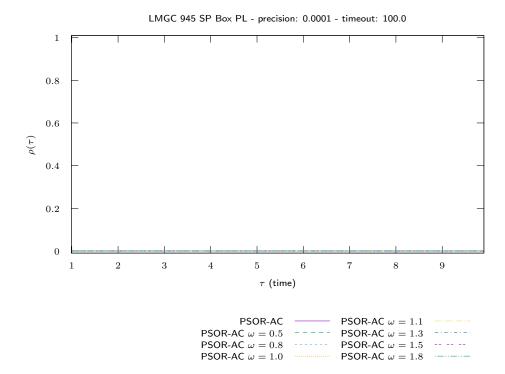


Figure 16: LMGC\_945\_SP\_Box\_PL time PSOR

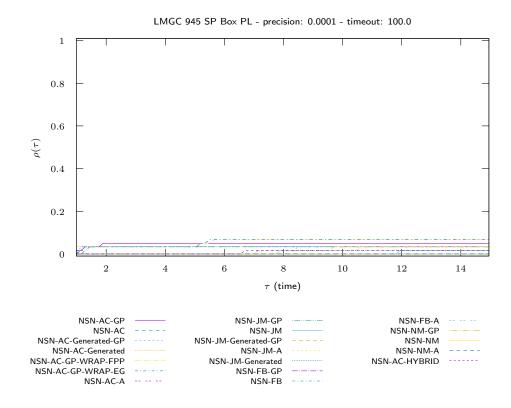


Figure 17: LMGC\_945\_SP\_Box\_PL  $\,$  time NSN

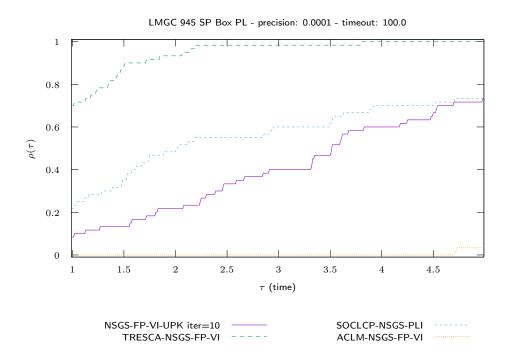


Figure 18: LMGC\_945\_SP\_Box\_PL time OPTI

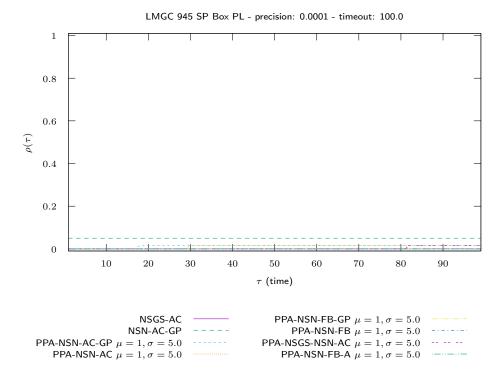


Figure 19: LMGC\_945\_SP\_Box\_PL time PROX/Internal Solvers

/figure/PROX/Parameters/time/profile-LMGC_945_SP_Box_PL.pdf
/figure/PROX/Parameters/time/profile-LMGC_945_SP_Box_PL_legend.pdf

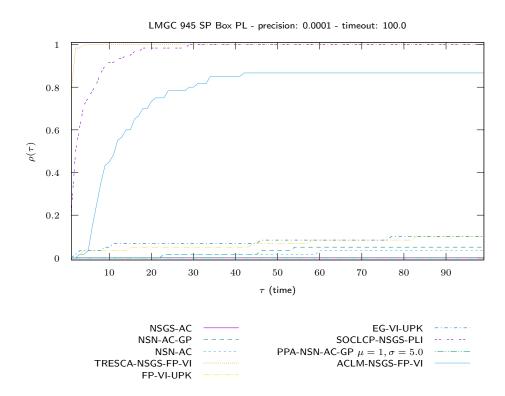


Figure 21: LMGC\_945\_SP\_Box\_PL time COMP/large

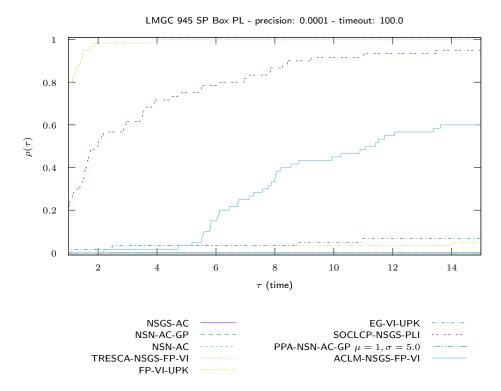


Figure 22: LMGC\_945\_SP\_Box\_PL time COMP/large

### ${\bf 3}\quad {\bf LMGC\ Aqueduc\ PR}$

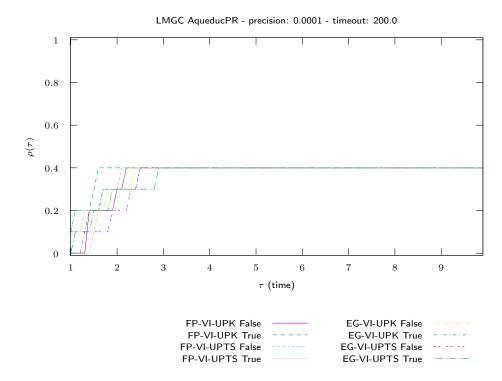


Figure 23: LMGC Aqueduc PR  $\,$  time  $\,$  VI/UpdateRule

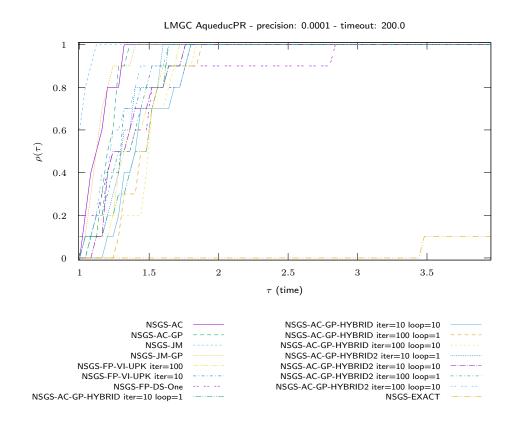


Figure 24: LMGC Aqueduc PR time NSGS/LocalSolver

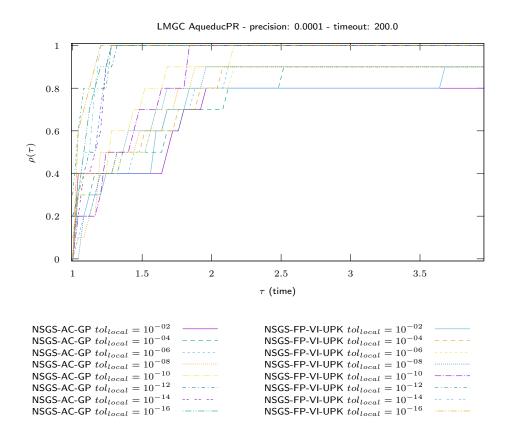


Figure 25: LMGC Aqueduc PR time NSGS/LocalTol

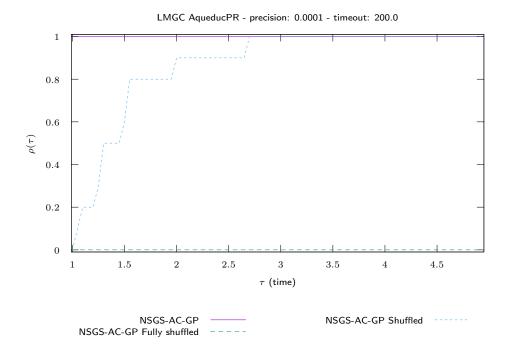


Figure 26: LMGC Aqueduc PR  $\,$  time NSGS/Shuffled

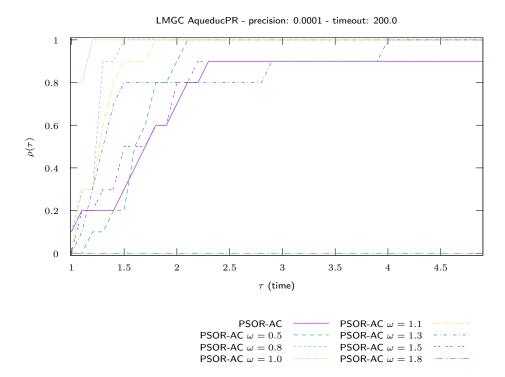


Figure 27: LMGC Aqueduc PR time PSOR

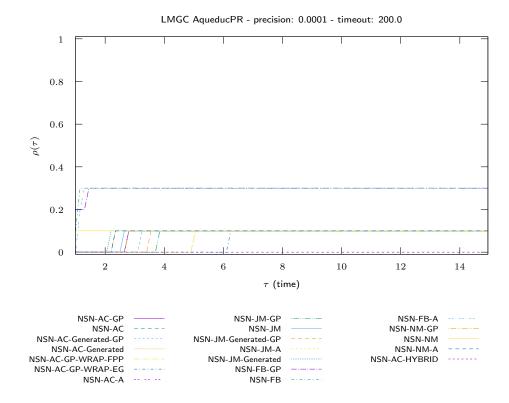


Figure 28: LMGC Aqueduc PR  $\,$  time NSN

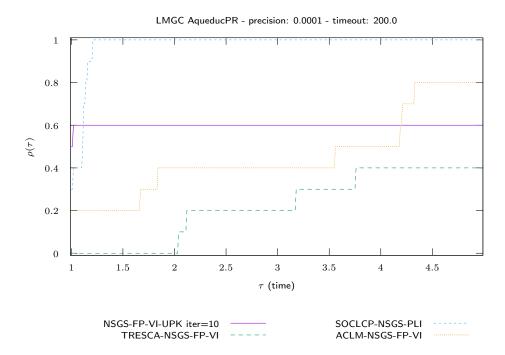


Figure 29: LMGC Aqueduc PR time OPTI

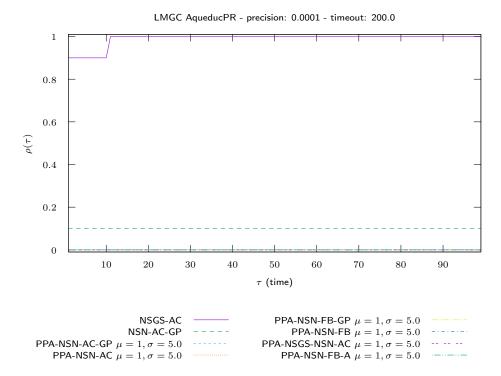


Figure 30: LMGC Aqueduc PR  $\,$  time PROX/InternalSolvers

	/figure/PROX/Parameters/time/profile-LMGC_AqueducPR.pdf
	/figure/PROX/Parameters/time/profile-LMGC_AqueducPR_legend.pdf
RR n° 12345	6789

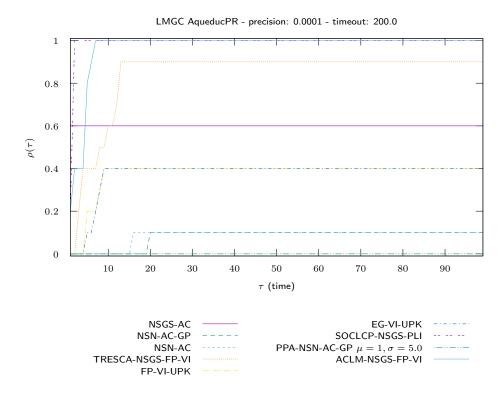


Figure 32: LMGC Aqueduc PR  $\,$  time COMP/large

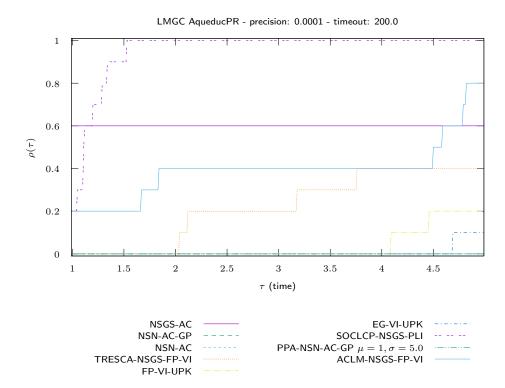


Figure 33: LMGC Aqueduc PR  $\,$  time COMP/large

## 4 LMGC Bridge PR

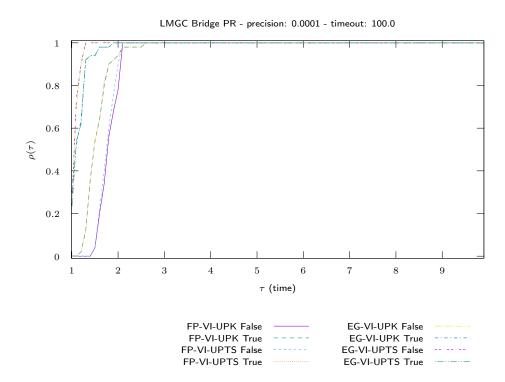


Figure 34: LMGC Bridge PR  $\,$  time  $\,$  VI/UpdateRule

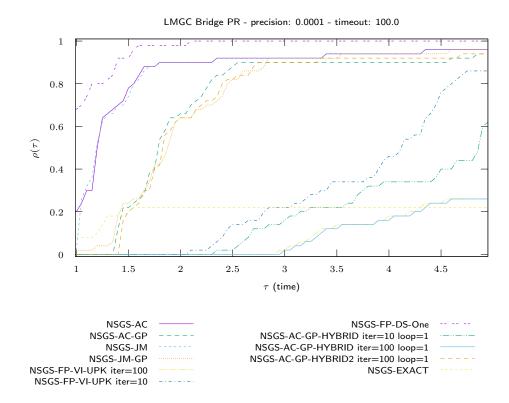


Figure 35: LMGC Bridge PR  $\,$  time NSGS/LocalSolver

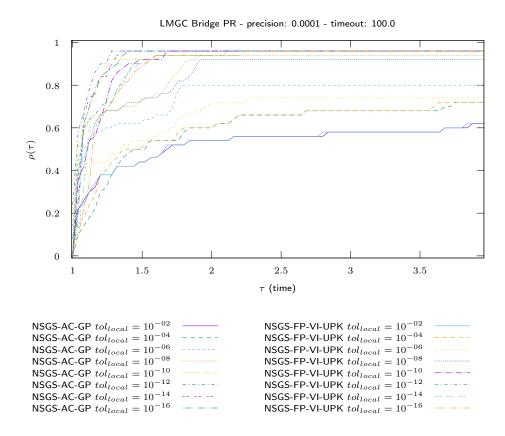


Figure 36: LMGC Bridge PR time NSGS/LocalTol

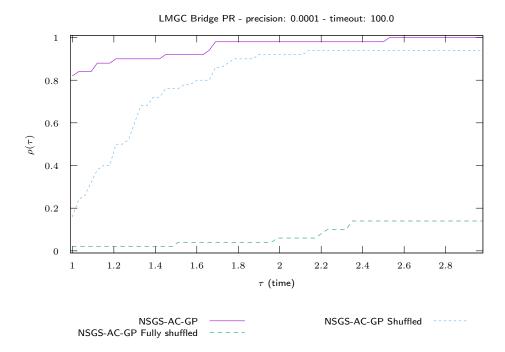


Figure 37: LMGC Bridge PR  $\,$  time NSGS/Shuffled

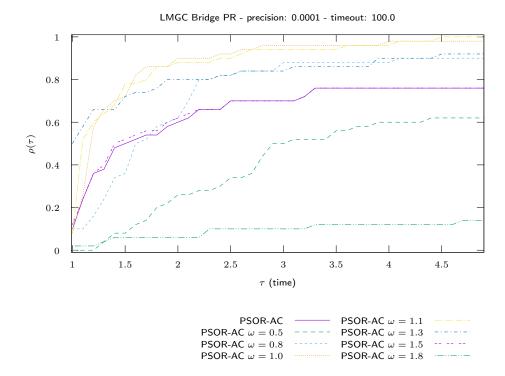


Figure 38: LMGC Bridge PR  $\,$  time PSOR

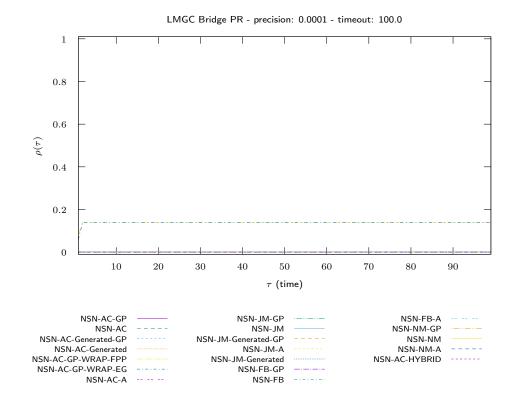


Figure 39: LMGC Bridge PR  $\,$  time NSN  $\,$ 

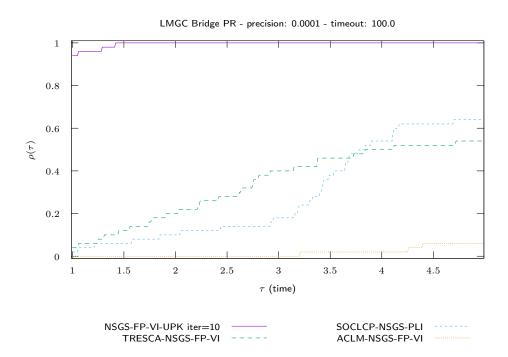
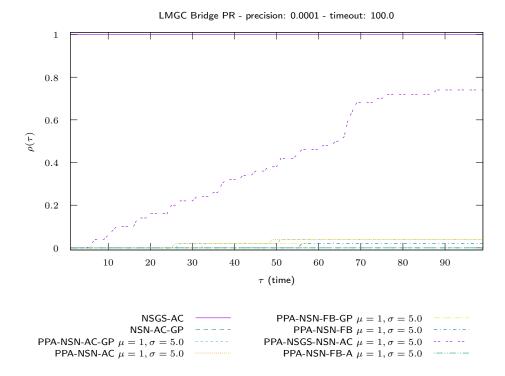


Figure 40: LMGC Bridge PR time OPTI



Figure~41:~LMGC~Bridge~PR~~time~PROX/Internal Solvers

/figure/PROX/Parameters/time/profile-LMGC_Bridge_PR.pdf/figure/PROX/Parameters/time/profile-LMGC_Bridge_PR_legend.pdf		
/figure/PROX/Parameters/time/profile-LMGC_Bridge_PR_legend.pdf		
		/figure/PROX/Parameters/time/profile-LMGC_Bridge_PR.pdf
RR n° 123456789		/figure/PROX/Parameters/time/profile-LMGC_Bridge_PR_legend.pdf
RR n° 123456789		
	RR n° 12345	6789

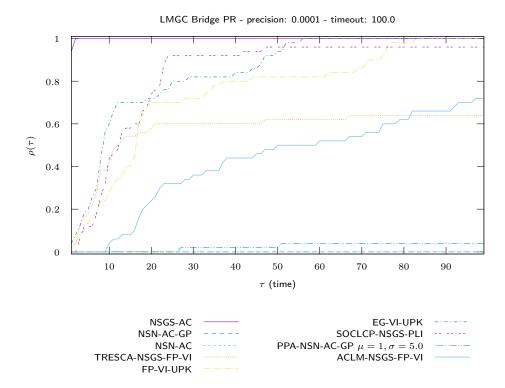


Figure 43: LMGC Bridge PR  $\,$  time COMP/large

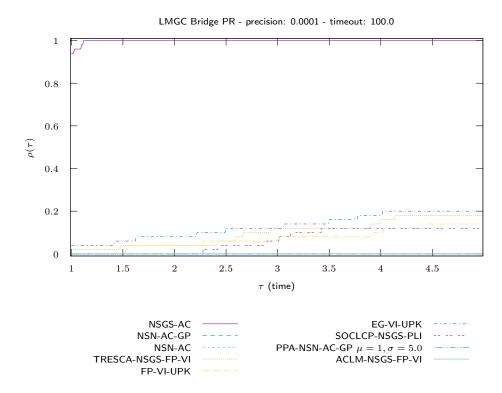


Figure 44: LMGC Bridge PR  $\,$  time COMP/large

## 5 LMGC LowWall FEM

_	
	$/ figure/VI/Update Rule/time/profile-LMGC\_LowWall\_FEM.pdf$
RR n° 12345	/figure/VI/UpdateRule/time/profile-LMGC_LowWall_FEM_legend.pdf

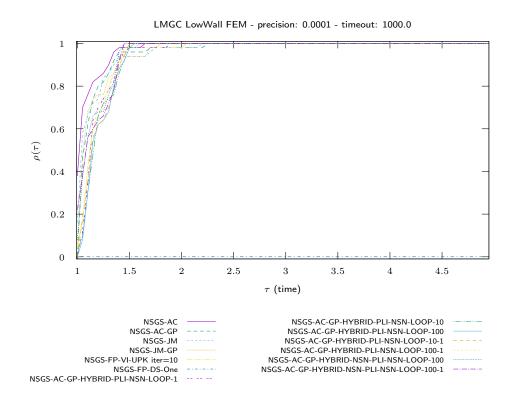


Figure 46: LMGC LowWall FEM  $\,$  time NSGS/LocalSolver

/figure/NSGS/LocalTol/time/profile-LMGC_LowWall_FEM.pdf
$/figure/NSGS/LocalTol/time/profile-LMGC\_LowWall\_FEM\_legend.pdf$ $RR\ n^\circ\ 123456789$

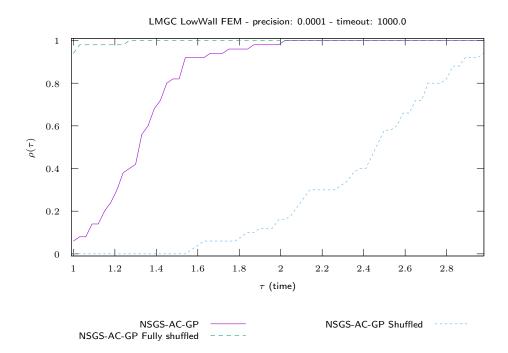


Figure 48: LMGC LowWall FEM  $\,$  time NSGS/Shuffled

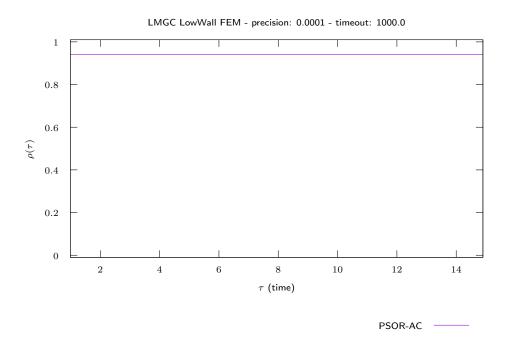


Figure 49: LMGC LowWall FEM time PSOR

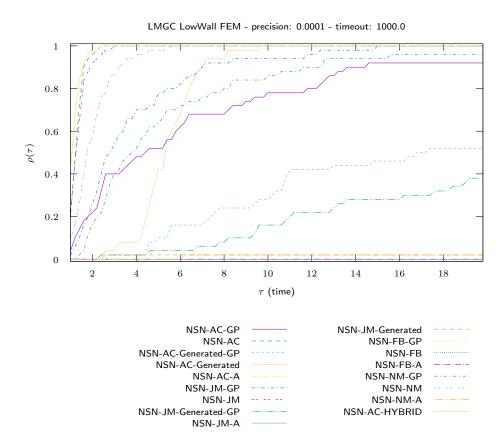


Figure 50: LMGC LowWall FEM time NSN

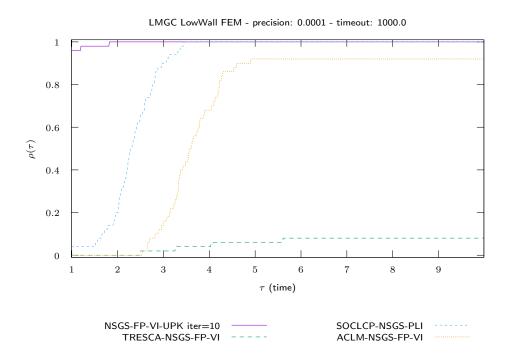


Figure 51: LMGC LowWall FEM time OPTI

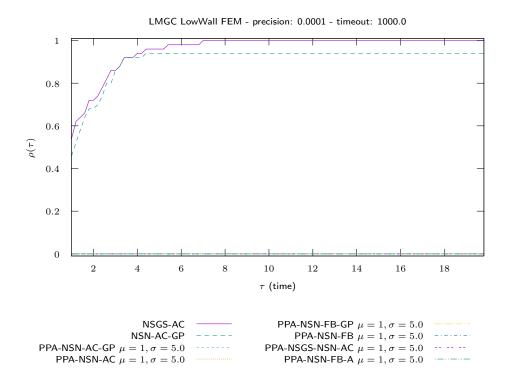


Figure 52: LMGC LowWall FEM  $\,$  time PROX/Internal Solvers

	/figure/PROX/Parameters/time/profile-LMGC_LowWall_FEM.pdf
	/figure/PROX/Parameters/time/profile-LMGC_LowWall_FEM_legend.pdf
RR n° 12345	6789

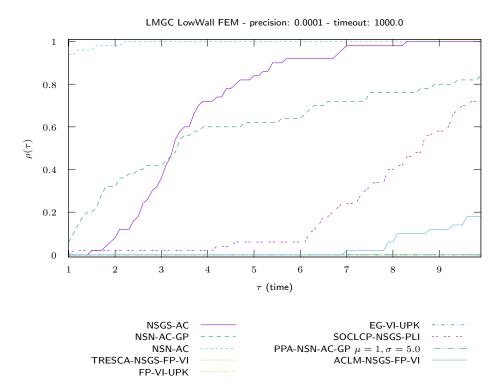


Figure 54: LMGC LowWall FEM  $\,$  time COMP/large

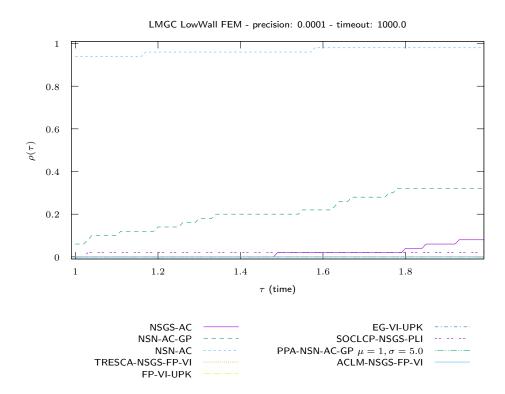


Figure 55: LMGC LowWall FEM  $\,$  time COMP/large

## 6 LMGC Cubes H8

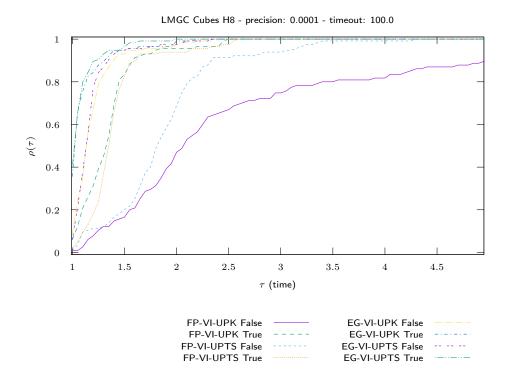


Figure 56: LMGC Cubes H8 time VI/UpdateRule

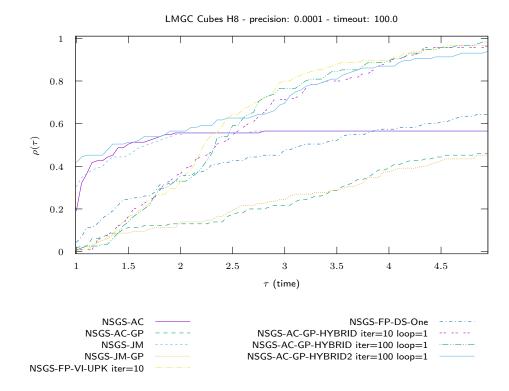


Figure 57: LMGC Cubes H8 time NSGS/LocalSolver

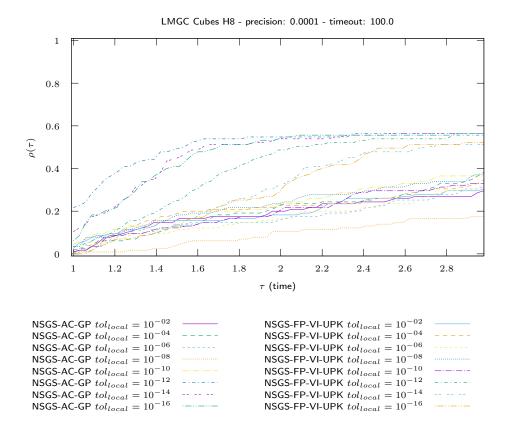


Figure 58: LMGC Cubes H8 time NSGS/LocalTol

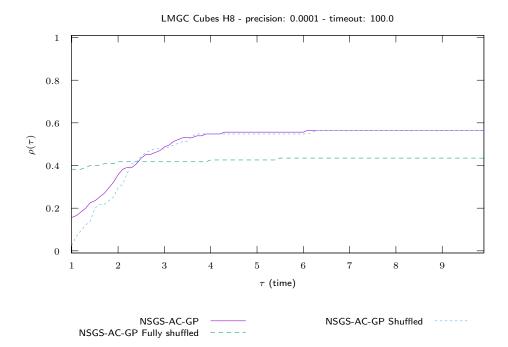


Figure 59: LMGC Cubes H8 time NSGS/Shuffled

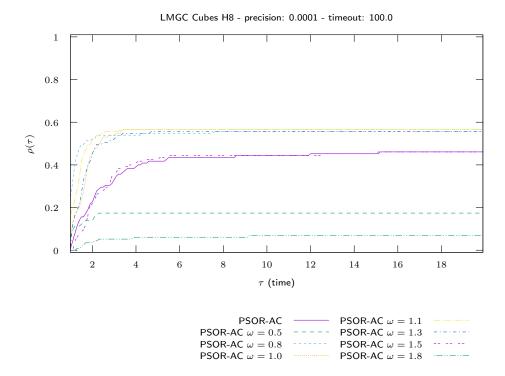


Figure 60: LMGC Cubes H8  $\,$  time PSOR

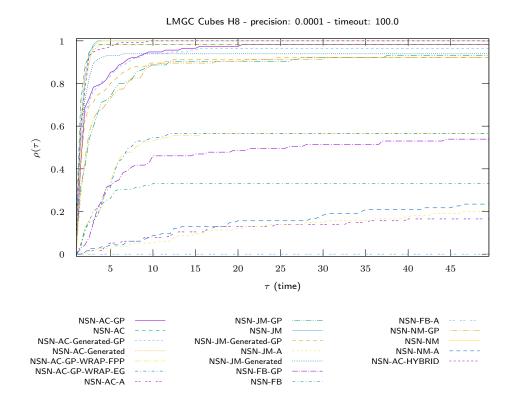


Figure 61: LMGC Cubes H8 time NSN

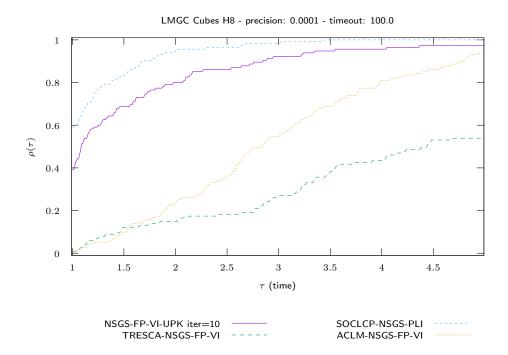


Figure 62: LMGC Cubes H8 time OPTI

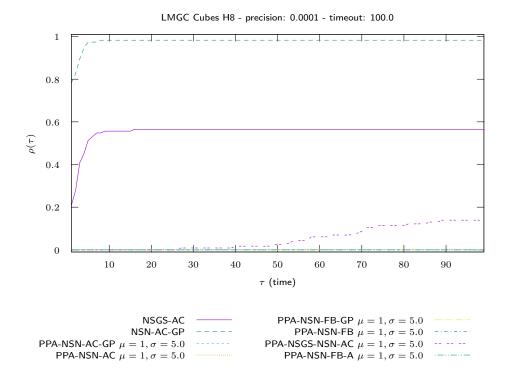


Figure 63: LMGC Cubes H8  $\,$  time PROX/InternalSolvers

	/figure/PROX/Parameters/time/profile-LMGC_Cubes_H8.pdf
RR n° 12345	/figure/PROX/Parameters/time/profile-LMGC_Cubes_H8_legend.pdf

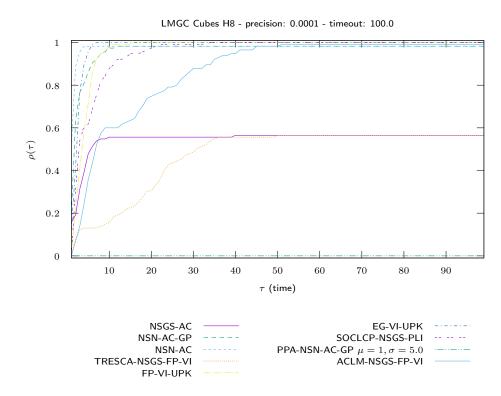


Figure 65: LMGC Cubes H8 time COMP/large

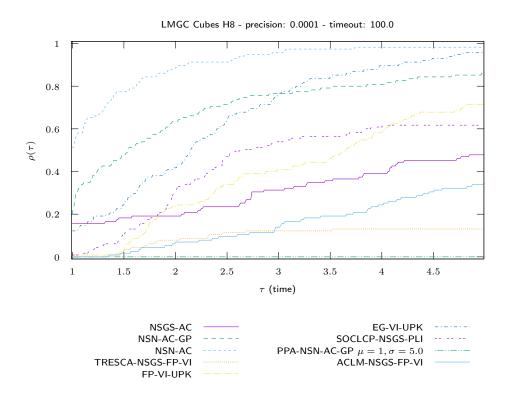


Figure 66: LMGC Cubes H8 time COMP/large

## 7 Capsules

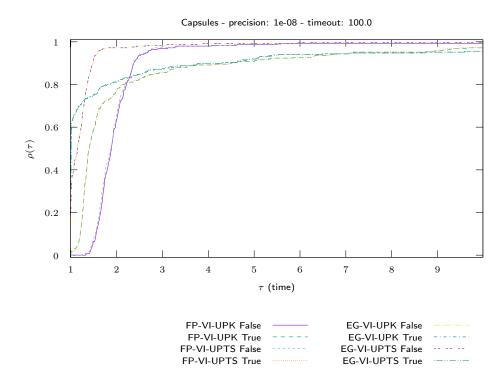


Figure 67: Capsules time VI/UpdateRule

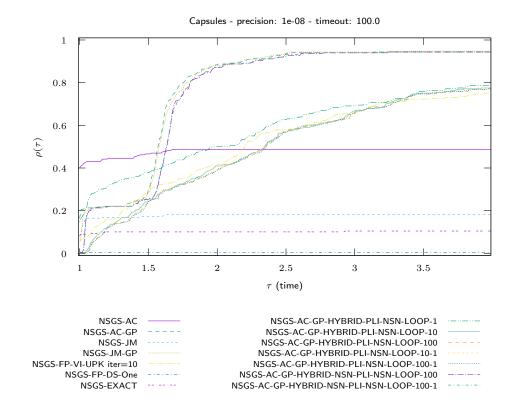


Figure 68: Capsules time NSGS/LocalSolver

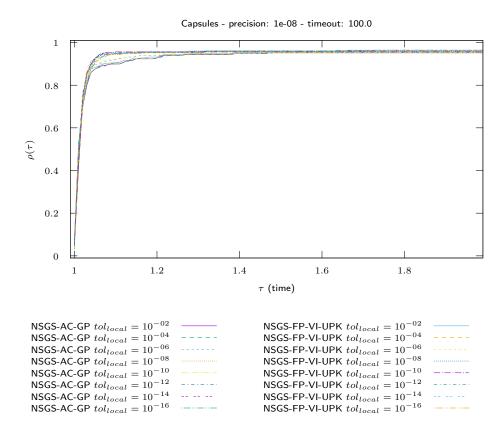


Figure 69: Capsules time NSGS/LocalTol

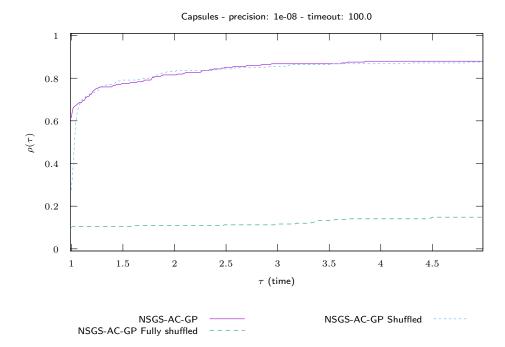


Figure 70: Capsules time NSGS/Shuffled

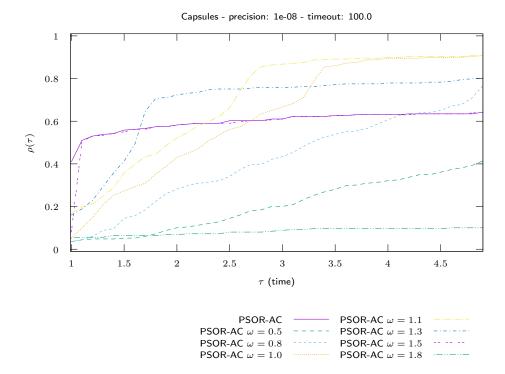


Figure 71: Capsules time PSOR

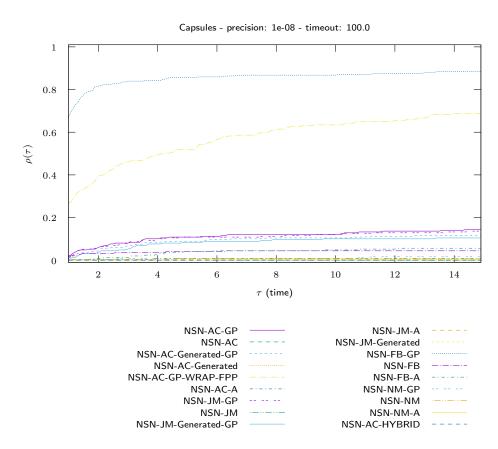


Figure 72: Capsules time NSN

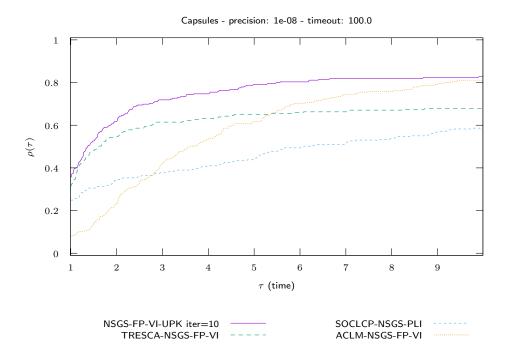


Figure 73: Capsules time OPTI

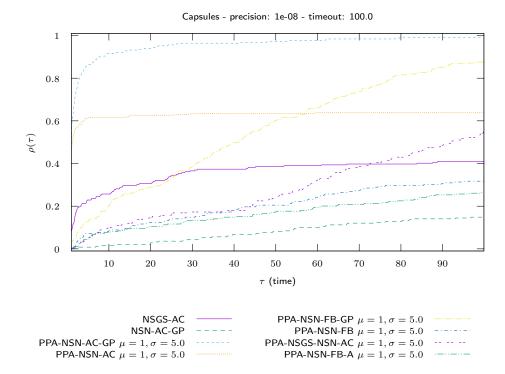


Figure 74: Capsules time PROX/InternalSolvers

/figure/PROX/Parameters/time/profile-Capsules.pdf
/figure/PROX/Parameters/time/profile-Capsules_legend.pdf

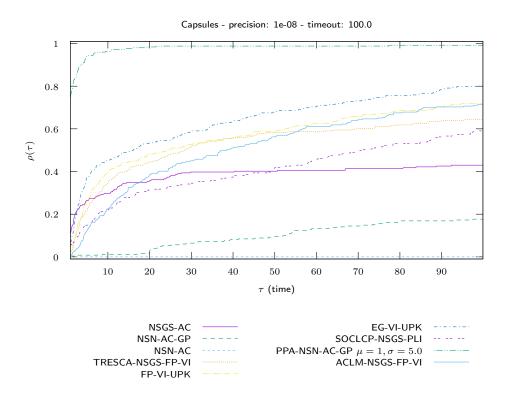


Figure 76: Capsules time COMP/large

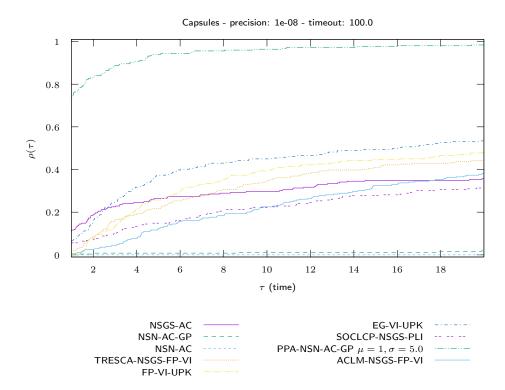


Figure 77: Capsules time COMP/large

## 8 Chain

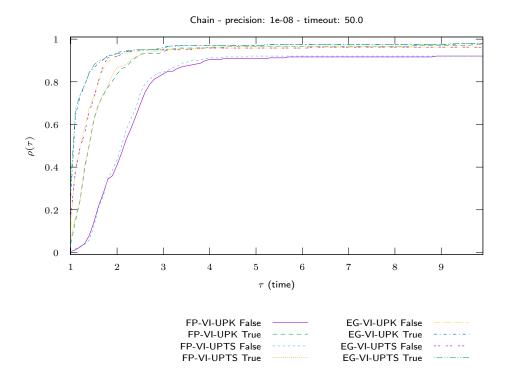


Figure 78: Chain time VI/UpdateRule

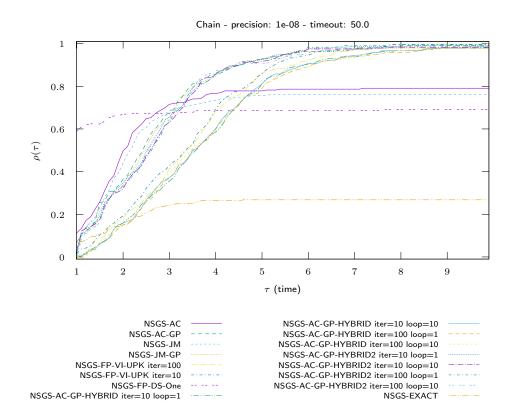


Figure 79: Chain time NSGS/LocalSolver

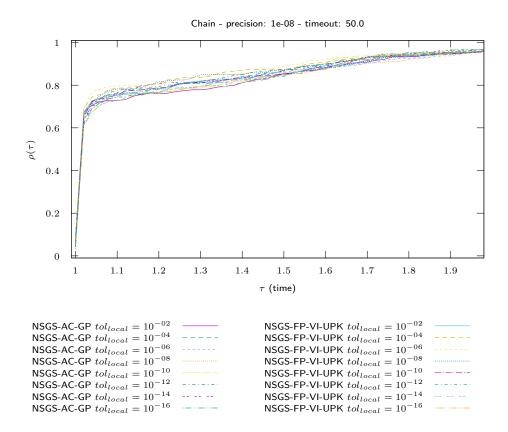


Figure 80: Chain time NSGS/LocalTol

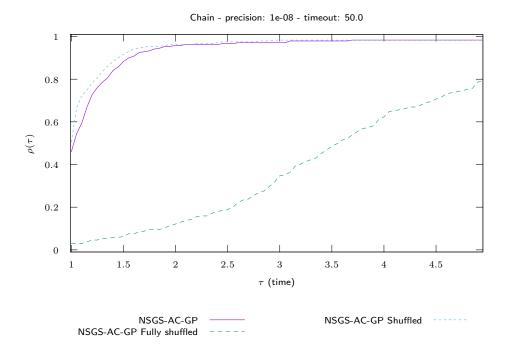


Figure 81: Chain time NSGS/Shuffled

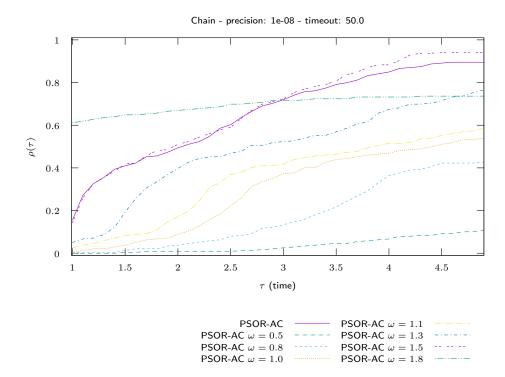


Figure 82: Chain time PSOR

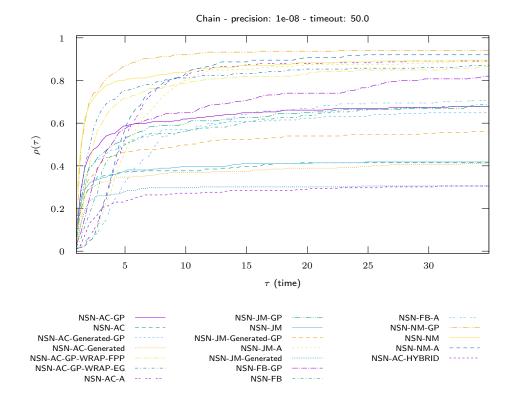


Figure 83: Chain time NSN

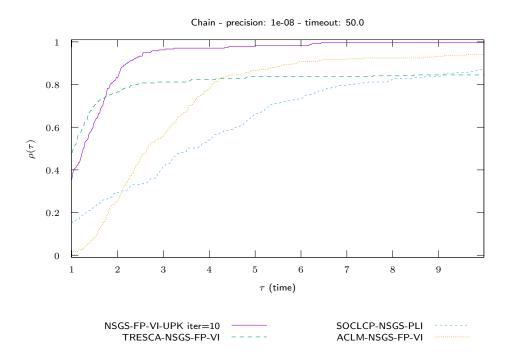


Figure 84: Chain time OPTI

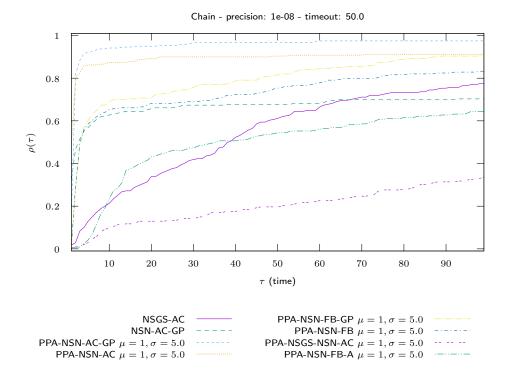


Figure 85: Chain time PROX/InternalSolvers

	/figure/PROX/Parameters/time/profile-Chain.pdf
	/figure/PROX/Parameters/time/profile-Chain_legend.pdf
RR n° 12345	

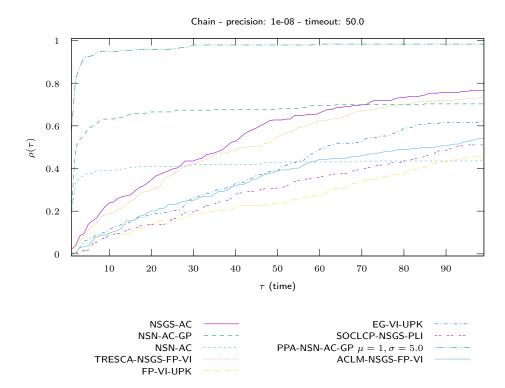


Figure 87: Chain time COMP/large

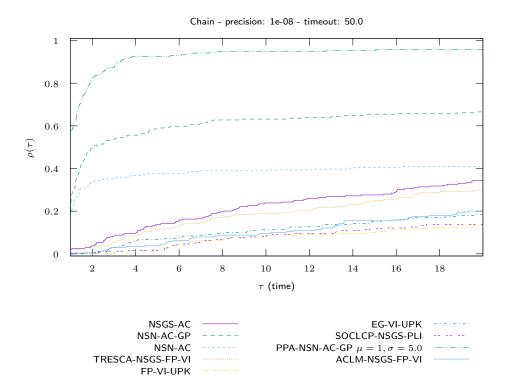


Figure 88: Chain time COMP/large

## 9 KaplasTower

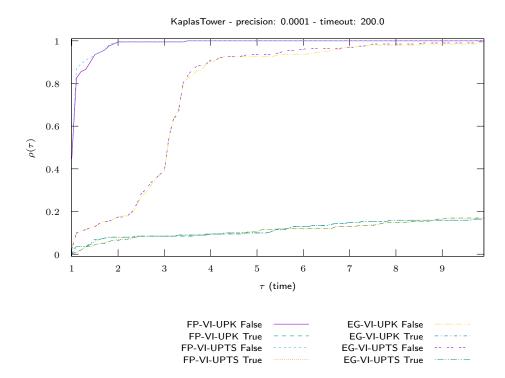


Figure 89: KaplasTower time VI/UpdateRule

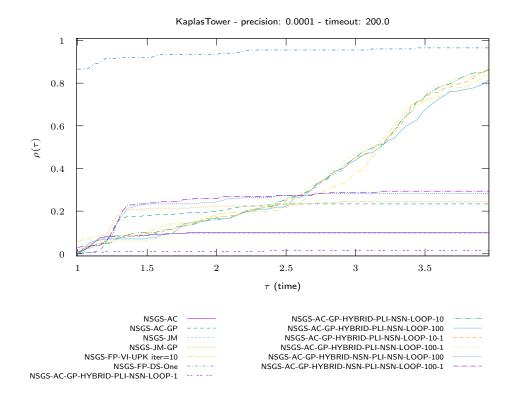


Figure 90: KaplasTower time NSGS/LocalSolver

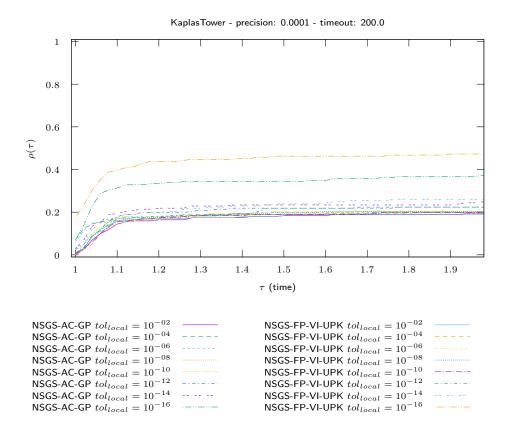


Figure 91: KaplasTower time NSGS/LocalTol

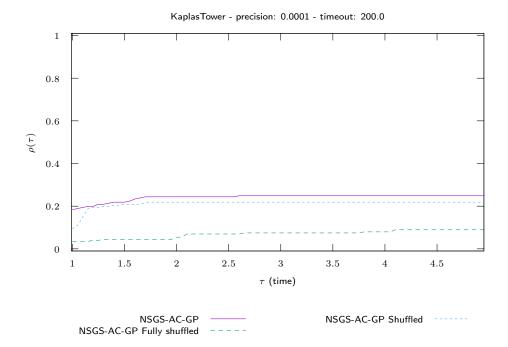


Figure 92: KaplasTower time NSGS/Shuffled

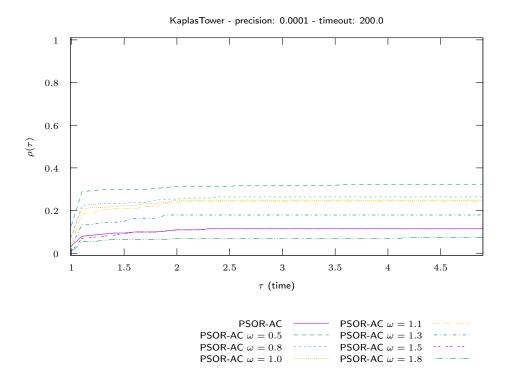


Figure 93: KaplasTower time PSOR

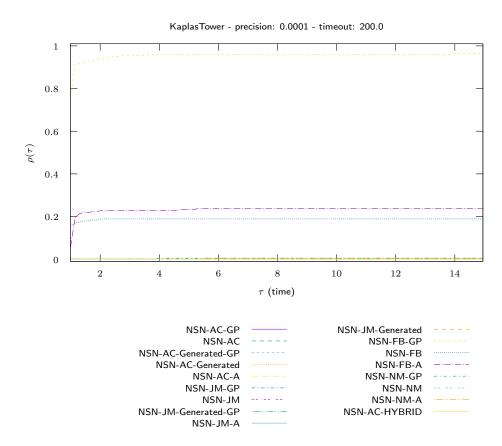


Figure 94: Kaplas Tower  $\,$  time NSN

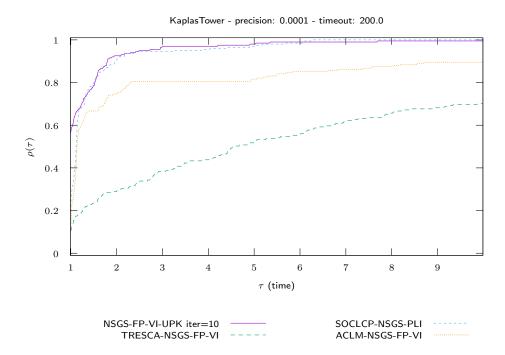
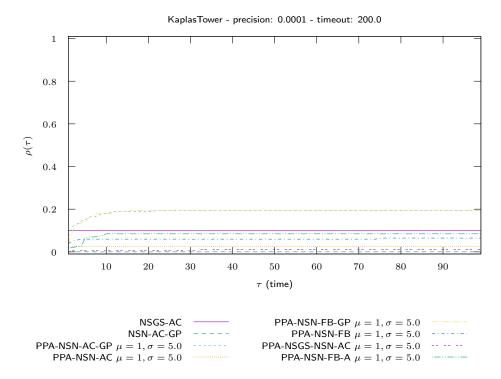


Figure 95: KaplasTower time OPTI



Figure~96:~KaplasTower~time~PROX/InternalSolvers

	/figure/PROX/Parameters/time/profile-KaplasTower.pdf
RR n° 12345	/figure/PROX/Parameters/time/profile-KaplasTower_legend.pdf

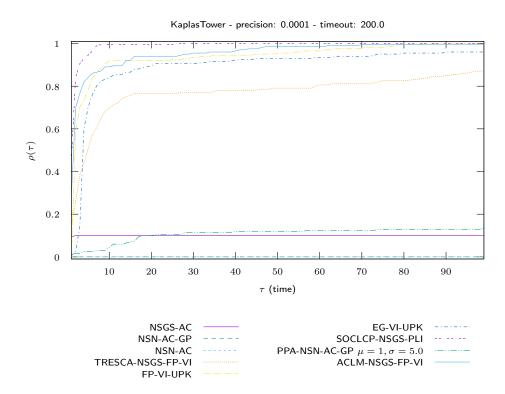


Figure 98: Kaplas Tower  $% \left( 1,...,N\right) =1$  time COMP/large

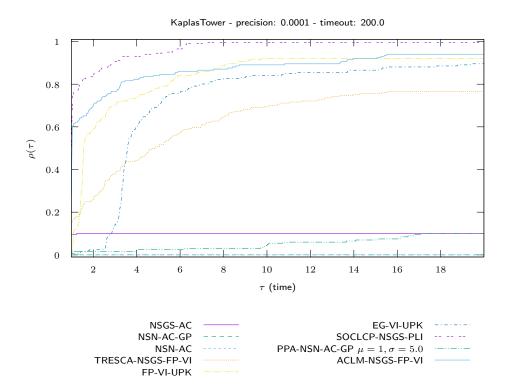


Figure 99: Kaplas Tower  $% \left( 1,...,N\right) =1$  time COMP/large



RESEARCH CENTRE GRENOBLE – RHÔNE-ALPES

Inovallée

655 avenue de l'Europe Montbonnot

38334 Saint Ismier Cedex

Publisher Inria Domaine de Voluceau - Rocquencourt BP 105 - 78153 Le Chesnay Cedex inria.fr