## Introduction to Analysis Notes

## Brendan Burkhart

## Contents

1 Sets and Lists 2

## 1 Sets and Lists

**Definition 1.1.** A set is an unordered group of distinct elements.

**Definition 1.2.** The empty set (denoted  $\varnothing$ ) is the unique set having no elements.

While sets are unordered groups of distinct elements, lists (also called n-tuples) are ordered groups of elements which are not necessarily distinct. An ordered pair (a, b) is a list of a length two (a tuple), where a, and b are elements of some set.

**Definition 1.3.** An ordered pair (a, b) is a tuple of elements of some set.

Ordered pairs (and *n*-tuples more generally) can be represented as sets themselves - the pair (a, b) can be represented as the set  $\{a, \{a, b\}\}\$ .

**Definition 1.4.** The Cartesian product of two sets A and B is denoted  $A \times B$ . It is equal to  $\{(a,b) \mid a \in A, b \in B\}$ .