Assumption: successful war results in  $v_i=1,\; \pmb{\tau}_i=\pmb{1} \implies \hat{G}_i'=0$ 

War costs are specific to the directed dyad ( $\hat{c}_{ji}$  is j's relative cost for attacking i) and is a realization of a random varible from a known aggressor-specific distribution. These are held as private information to the aggressor. Government j prefers not to attack i so long as

$$(1 - \tilde{\chi}_{ji}(\boldsymbol{Z};\boldsymbol{\theta}_m)) \, \hat{G}_j(\hat{\boldsymbol{\tau}};\hat{\boldsymbol{h}}) + \tilde{\chi}_{ji}(\boldsymbol{Z};\boldsymbol{\theta}_m) \hat{G}_j(\hat{\boldsymbol{\tau}}_i';\hat{\boldsymbol{h}}_i') - \hat{c}_{ji} \leq \hat{G}_j(\hat{\boldsymbol{\tau}};\hat{\boldsymbol{h}})$$
$$\hat{c}_{ji}^{-1} \leq \left(\tilde{\chi}_{ji}(\boldsymbol{Z};\boldsymbol{\theta}_m) \left(\hat{G}_j(\hat{\boldsymbol{\tau}}_i';\hat{\boldsymbol{h}}_i') - \hat{G}_j(\hat{\boldsymbol{\tau}};\hat{\boldsymbol{h}})\right)\right)^{-1}$$

Let inverse war costs be distributed Frechét,

$$\Pr\left(\frac{1}{\hat{c}_{ji}} \le \frac{1}{\hat{c}}\right) = F_j\left(\frac{1}{\hat{c}}\right) = \exp\left(-C_j\hat{c}^{\eta}\right)$$

where  $C_j$  is an aggressor-specific cost shifter and  $\eta$  is a global shape parameter.

From this, we can calculate the probability that no government finds it profitable to attack i, which is given by

$$H_{i}(\hat{\bar{\tau}}; \boldsymbol{Z}, \boldsymbol{\theta}_{m}) = \prod_{j \neq i} F_{j} \left( \left( \tilde{\chi}_{ji}(\boldsymbol{Z}; \boldsymbol{\theta}_{m}) \left( \hat{G}_{j}(\hat{\tau}'_{i}; \hat{\boldsymbol{h}}'_{i}) - \hat{G}_{j}(\hat{\bar{\tau}}; \hat{\bar{\boldsymbol{h}}}) \right) \right)^{-1} \right)$$

$$= \exp \left( -\sum_{j \neq i} C_{j} \left( \tilde{\chi}_{ji}(\boldsymbol{Z}; \boldsymbol{\theta}_{m}) \left( \hat{G}_{j}(\hat{\tau}'_{i}; \hat{\boldsymbol{h}}'_{i}) - \hat{G}_{j}(\hat{\bar{\tau}}; \hat{\bar{\boldsymbol{h}}}) \right) \right)^{\eta} \right)$$

A prospective policy-chooser then confronts the following objective function

$$\hat{\hat{G}}_i\left(\hat{\hat{\boldsymbol{\tau}}},\hat{\hat{\boldsymbol{h}}}\right) = H_i(\hat{\hat{\boldsymbol{\tau}}},\hat{\hat{\boldsymbol{h}}};\boldsymbol{Z},\boldsymbol{\theta}_m)\hat{G}_i\left(\hat{\hat{\boldsymbol{\tau}}},\hat{\hat{\boldsymbol{h}}}\right)$$

where implicitly i's utility is zero with probability  $1 - H_i(\hat{\tau}, \hat{h}; \mathbf{Z}, \boldsymbol{\theta}_m)$ . We solve this best response by imposing the constraints

$$\hat{ ilde{m{h}}} = \hat{m{h}}(\hat{ ilde{m{ au}}})$$

(equilibrium ge constraints) and

$$\hat{\boldsymbol{h}}_i' = \hat{\boldsymbol{h}}(\boldsymbol{1}_i; \hat{\tilde{\boldsymbol{ au}}}_{-i})$$

(conquest ge constraints)

<sup>&</sup>lt;sup>1</sup>Higher  $\eta$  correspond to more concentrated cost draws.