

CIND123 Winter 2018 - Assignment #2

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This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see <http://rmarkdown.rstudio.com>.

Use RStudio for this assignment. Edit the file `assignment-2.Rmd` and insert your R code where you see the string "INSERT YOUR ANSWER HERE"

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document.

When you are done with your answers and before submitting, save the file with the following naming convention :your **Lastname_firstname**

Submit **both** the rmd and the pdf output(or word or html) files, failing to submit **both** will be subject to mark deduction.

This assignment may make use of data provided by the ISwR package.

```
library(ISwR)
```

Sample Question and Solution

Use `seq()` to create the vector (1,2,3, ...,10).

```
seq(1,10)
```

```
## [1] 1 2 3 4 5 6 7 8 9 10
```

Question 1 (50%)

Consider the probability distribution associated with rolling 3 fair dice. We can label the faces of a single die using the numbers from 1 to 6. We can therefore label the simple events in this distribution by triples of numbers from 1 to 6. Let d_1 , d_2 , and d_3 represent the labels on each of the dice.

a) Set d_1 to the sequence (1,2,...,6) repeated 36 times.

```
d1 = rep(1:6, times = 36)
```

b) Set d_2 to the sequence consisting of 6 repetitions of the sequence in which each of the numbers (1,2,...,6) is repeated 6 times.

```
d2 = rep(1:6, each = 6, times = 6)
```

- c) Set d3 to the sequence in which each of the numbers (1,2,...,6) is repeated 36 times.

```
d3 = rep(1:6, each = 36)
```

- d) Create a new data frame three.dice from d1, d2, and d3 and print it. Visually confirm that there are $6 \times 6 \times 6 = 216$ rows and each row contains a unique combination of dice labels.

```
three.dice = data.frame(d1, d2, d3)  
print(three.dice)
```

```
##      d1 d2 d3  
## 1     1  1  1  
## 2     2  1  1  
## 3     3  1  1  
## 4     4  1  1  
## 5     5  1  1  
## 6     6  1  1  
## 7     1  2  1  
## 8     2  2  1  
## 9     3  2  1  
## 10    4  2  1  
## 11    5  2  1  
## 12    6  2  1  
## 13    1  3  1  
## 14    2  3  1  
## 15    3  3  1  
## 16    4  3  1  
## 17    5  3  1  
## 18    6  3  1  
## 19    1  4  1  
## 20    2  4  1  
## 21    3  4  1  
## 22    4  4  1  
## 23    5  4  1  
## 24    6  4  1  
## 25    1  5  1  
## 26    2  5  1  
## 27    3  5  1  
## 28    4  5  1  
## 29    5  5  1  
## 30    6  5  1  
## 31    1  6  1  
## 32    2  6  1  
## 33    3  6  1  
## 34    4  6  1  
## 35    5  6  1  
## 36    6  6  1  
## 37    1  1  2
```

| | | | |
|-------|---|---|---|
| ## 38 | 2 | 1 | 2 |
| ## 39 | 3 | 1 | 2 |
| ## 40 | 4 | 1 | 2 |
| ## 41 | 5 | 1 | 2 |
| ## 42 | 6 | 1 | 2 |
| ## 43 | 1 | 2 | 2 |
| ## 44 | 2 | 2 | 2 |
| ## 45 | 3 | 2 | 2 |
| ## 46 | 4 | 2 | 2 |
| ## 47 | 5 | 2 | 2 |
| ## 48 | 6 | 2 | 2 |
| ## 49 | 1 | 3 | 2 |
| ## 50 | 2 | 3 | 2 |
| ## 51 | 3 | 3 | 2 |
| ## 52 | 4 | 3 | 2 |
| ## 53 | 5 | 3 | 2 |
| ## 54 | 6 | 3 | 2 |
| ## 55 | 1 | 4 | 2 |
| ## 56 | 2 | 4 | 2 |
| ## 57 | 3 | 4 | 2 |
| ## 58 | 4 | 4 | 2 |
| ## 59 | 5 | 4 | 2 |
| ## 60 | 6 | 4 | 2 |
| ## 61 | 1 | 5 | 2 |
| ## 62 | 2 | 5 | 2 |
| ## 63 | 3 | 5 | 2 |
| ## 64 | 4 | 5 | 2 |
| ## 65 | 5 | 5 | 2 |
| ## 66 | 6 | 5 | 2 |
| ## 67 | 1 | 6 | 2 |
| ## 68 | 2 | 6 | 2 |
| ## 69 | 3 | 6 | 2 |
| ## 70 | 4 | 6 | 2 |
| ## 71 | 5 | 6 | 2 |
| ## 72 | 6 | 6 | 2 |
| ## 73 | 1 | 1 | 3 |
| ## 74 | 2 | 1 | 3 |
| ## 75 | 3 | 1 | 3 |
| ## 76 | 4 | 1 | 3 |
| ## 77 | 5 | 1 | 3 |
| ## 78 | 6 | 1 | 3 |
| ## 79 | 1 | 2 | 3 |
| ## 80 | 2 | 2 | 3 |
| ## 81 | 3 | 2 | 3 |
| ## 82 | 4 | 2 | 3 |
| ## 83 | 5 | 2 | 3 |
| ## 84 | 6 | 2 | 3 |
| ## 85 | 1 | 3 | 3 |
| ## 86 | 2 | 3 | 3 |
| ## 87 | 3 | 3 | 3 |

| | | | |
|--------|---|---|---|
| ## 88 | 4 | 3 | 3 |
| ## 89 | 5 | 3 | 3 |
| ## 90 | 6 | 3 | 3 |
| ## 91 | 1 | 4 | 3 |
| ## 92 | 2 | 4 | 3 |
| ## 93 | 3 | 4 | 3 |
| ## 94 | 4 | 4 | 3 |
| ## 95 | 5 | 4 | 3 |
| ## 96 | 6 | 4 | 3 |
| ## 97 | 1 | 5 | 3 |
| ## 98 | 2 | 5 | 3 |
| ## 99 | 3 | 5 | 3 |
| ## 100 | 4 | 5 | 3 |
| ## 101 | 5 | 5 | 3 |
| ## 102 | 6 | 5 | 3 |
| ## 103 | 1 | 6 | 3 |
| ## 104 | 2 | 6 | 3 |
| ## 105 | 3 | 6 | 3 |
| ## 106 | 4 | 6 | 3 |
| ## 107 | 5 | 6 | 3 |
| ## 108 | 6 | 6 | 3 |
| ## 109 | 1 | 1 | 4 |
| ## 110 | 2 | 1 | 4 |
| ## 111 | 3 | 1 | 4 |
| ## 112 | 4 | 1 | 4 |
| ## 113 | 5 | 1 | 4 |
| ## 114 | 6 | 1 | 4 |
| ## 115 | 1 | 2 | 4 |
| ## 116 | 2 | 2 | 4 |
| ## 117 | 3 | 2 | 4 |
| ## 118 | 4 | 2 | 4 |
| ## 119 | 5 | 2 | 4 |
| ## 120 | 6 | 2 | 4 |
| ## 121 | 1 | 3 | 4 |
| ## 122 | 2 | 3 | 4 |
| ## 123 | 3 | 3 | 4 |
| ## 124 | 4 | 3 | 4 |
| ## 125 | 5 | 3 | 4 |
| ## 126 | 6 | 3 | 4 |
| ## 127 | 1 | 4 | 4 |
| ## 128 | 2 | 4 | 4 |
| ## 129 | 3 | 4 | 4 |
| ## 130 | 4 | 4 | 4 |
| ## 131 | 5 | 4 | 4 |
| ## 132 | 6 | 4 | 4 |
| ## 133 | 1 | 5 | 4 |
| ## 134 | 2 | 5 | 4 |
| ## 135 | 3 | 5 | 4 |
| ## 136 | 4 | 5 | 4 |
| ## 137 | 5 | 5 | 4 |

| | | | |
|--------|---|---|---|
| ## 138 | 6 | 5 | 4 |
| ## 139 | 1 | 6 | 4 |
| ## 140 | 2 | 6 | 4 |
| ## 141 | 3 | 6 | 4 |
| ## 142 | 4 | 6 | 4 |
| ## 143 | 5 | 6 | 4 |
| ## 144 | 6 | 6 | 4 |
| ## 145 | 1 | 1 | 5 |
| ## 146 | 2 | 1 | 5 |
| ## 147 | 3 | 1 | 5 |
| ## 148 | 4 | 1 | 5 |
| ## 149 | 5 | 1 | 5 |
| ## 150 | 6 | 1 | 5 |
| ## 151 | 1 | 2 | 5 |
| ## 152 | 2 | 2 | 5 |
| ## 153 | 3 | 2 | 5 |
| ## 154 | 4 | 2 | 5 |
| ## 155 | 5 | 2 | 5 |
| ## 156 | 6 | 2 | 5 |
| ## 157 | 1 | 3 | 5 |
| ## 158 | 2 | 3 | 5 |
| ## 159 | 3 | 3 | 5 |
| ## 160 | 4 | 3 | 5 |
| ## 161 | 5 | 3 | 5 |
| ## 162 | 6 | 3 | 5 |
| ## 163 | 1 | 4 | 5 |
| ## 164 | 2 | 4 | 5 |
| ## 165 | 3 | 4 | 5 |
| ## 166 | 4 | 4 | 5 |
| ## 167 | 5 | 4 | 5 |
| ## 168 | 6 | 4 | 5 |
| ## 169 | 1 | 5 | 5 |
| ## 170 | 2 | 5 | 5 |
| ## 171 | 3 | 5 | 5 |
| ## 172 | 4 | 5 | 5 |
| ## 173 | 5 | 5 | 5 |
| ## 174 | 6 | 5 | 5 |
| ## 175 | 1 | 6 | 5 |
| ## 176 | 2 | 6 | 5 |
| ## 177 | 3 | 6 | 5 |
| ## 178 | 4 | 6 | 5 |
| ## 179 | 5 | 6 | 5 |
| ## 180 | 6 | 6 | 5 |
| ## 181 | 1 | 1 | 6 |
| ## 182 | 2 | 1 | 6 |
| ## 183 | 3 | 1 | 6 |
| ## 184 | 4 | 1 | 6 |
| ## 185 | 5 | 1 | 6 |
| ## 186 | 6 | 1 | 6 |
| ## 187 | 1 | 2 | 6 |

```
## 188 2 2 6
## 189 3 2 6
## 190 4 2 6
## 191 5 2 6
## 192 6 2 6
## 193 1 3 6
## 194 2 3 6
## 195 3 3 6
## 196 4 3 6
## 197 5 3 6
## 198 6 3 6
## 199 1 4 6
## 200 2 4 6
## 201 3 4 6
## 202 4 4 6
## 203 5 4 6
## 204 6 4 6
## 205 1 5 6
## 206 2 5 6
## 207 3 5 6
## 208 4 5 6
## 209 5 5 6
## 210 6 5 6
## 211 1 6 6
## 212 2 6 6
## 213 3 6 6
## 214 4 6 6
## 215 5 6 6
## 216 6 6 6
```

- e) Since the dice are fair and independent, each simple event has the same probability, namely $\frac{1}{216}$. Add the column P to the data frame with this value.

```
three.dice$P = 1/216
```

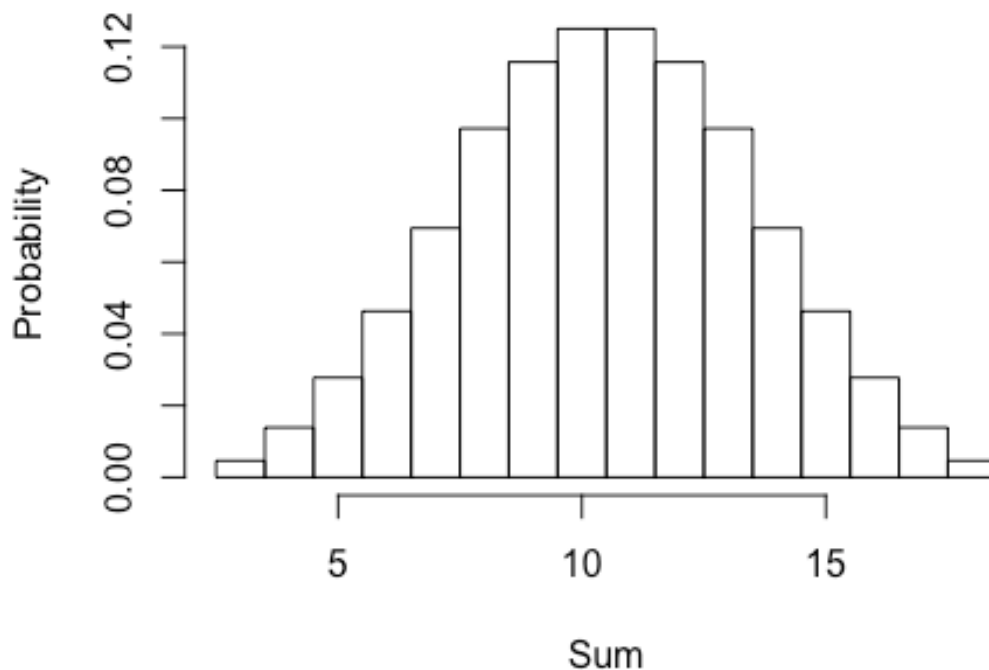
- f) Add a new column sum equal to the sum of the dice labels. Add another new column mean equal to the average of the dice labels.

```
three.dice$sum = d1 + d2 + d3
three.dice$mean = (d1 + d2 + d3)/3
```

- g) Plot a probability histogram of three.dice\$sum.

```
phistogram = hist(three.dice$sum, freq = 0, breaks = 2.5:18.5, main =
"Probability Histogram of the Sums", xlab = "Sum", ylab =
"Probability")
```

Probability Histogram of the Sums



```
phistogram$counts
```

```
## [1] 1 3 6 10 15 21 25 27 27 25 21 15 10 6 3 1
```

h) Compute the probability that the sum of the dice is greater than 12 and less than 18.

HINT: Use `subset()` to select the events and sum P.

```
sum(subset(three.dice, sum > 12 & sum < 18, select = P))
```

```
## [1] 0.2546296
```

i) Compute the probability that the sum is even.

```
sum(subset(three.dice, sum %% 2 == 0, select = P))
```

```
## [1] 0.5
```

j) Compute the probability that the mean is exactly 4.

```
sum(subset(three.dice, mean == 4, select = P))
```

```
## [1] 0.1157407
```

Question 2 (50%)

a) You have two groups of distinctly different items, 10 in the first group and 8 in the second. If you select one item from each group, how many different pairs can you form?

```
n = 10
m = 8
n * m

## [1] 80
```

b) Evaluate the following permutation P_3^5

```
choose(5, 3) * factorial(3)

## [1] 60
```

c) Evaluate the following combinations $C_3^5 + C_2^5$

```
choose(5, 3) + choose(5, 2)

## [1] 20
```

d) In how many ways can you select five people from a group of eight if the order of selection is important?

```
choose(8, 5) * factorial(5)

## [1] 6720
```

e) In how many ways can you select two people from a group of 20 if the order of selection is not important?

```
choose(20, 2)

## [1] 190
```

END of Assignment #2.