Lab 1

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You should have RStudio installed to edit this file. You will write code in places marked "TO-DO" to complete the problems. Some of this will be a pure programming assignment. The tools for the solutions to these problems can be found in the class practice lectures. I want you to use the methods I taught you, not for you to google and come up with whatever works. You won't learn that way.

To "hand in" the homework, you should compile or publish this file into a PDF that includes output of your code. Once it's done, push by the deadline to your repository in a directory called "labs".

• Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
options(digits=11)
pi
```

[1] 3.1415926536

• Sum up the first 103 terms of the series $1 + 1/2 + 1/4 + 1/8 + \dots$

```
sum(1/(2<sup>(0:102))</sup>)
```

[1] 2

• Find the product of the first 37 terms in the sequence 1/3, 1/6, 1/9 ...

```
#prod(1/(3*(1:37))) there's a better way
prod(1/seq(from=3,by=3,length.out=37))
```

[1] 1.613528728e-61

• Find the product of the first 387 terms of 1 * 1/2 * 1/4 * 1/8 * ...

```
prod(1/2<sup>(0:386)</sup>)
```

[1] 0

Is this answer *exactly* correct?

It's not exactly correct because it is a very small positive number. The number was too small and we experienced numerical underflow so R defaulted to 0.

• Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
-\log(2)*sum((0:386))
## [1] -51771.856063
  • Create the sequence x = [Inf, 20, 18, \ldots, -20].
x \leftarrow c(Inf, seq(from=20, to=-20, by=-2))
    [1] Inf
             20
                 18
                      16
                          14
                              12
                                  10
                                                                       -8 -10 -12 -14
## [20] -16 -18 -20
Create the sequence x = [log_3(Inf), log_3(100), log_3(98), ... log_3(-20)].
x \leftarrow c(Inf, seq(from=100, to=-20, by=-2))
x = log(x, base=3)
## Warning: NaNs produced
##
    [1]
                  Inf 4.19180654858 4.17341725189 4.15464876786 4.13548512895
    [6] 4.11590933734 4.09590327429 4.07544759936 4.05452163807 4.03310325630
## [11] 4.01116871959 3.98869253500 3.96564727304 3.94200336639 3.91772888179
## [16] 3.89278926071 3.86714702345 3.84076143031 3.81358809222 3.78557852143
## [21] 3.75667961083 3.72683302786 3.69597450568 3.66403300988 3.63092975357
## [26] 3.59657702662 3.56087679501 3.52371901429 3.48497958377 3.44451784579
## [31] 3.40217350273 3.35776278143 3.31107361282 3.26185950714 3.20983167673
## [36] 3.15464876786 3.09590327429 3.03310325630 2.96564727304 2.89278926071
  [41] 2.81358809222 2.72683302786 2.63092975357 2.52371901429 2.40217350273
  [46] 2.26185950714 2.09590327429 1.89278926071 1.63092975357 1.26185950714
## [51] 0.63092975357
                                -Inf
                                                                             NaN
                                                NaN
                                                              NaN
## [56]
                  NaN
                                 NaN
                                                NaN
                                                              NaN
                                                                             NaN
## [61]
                  NaN
                                 NaN
```

Comment on the appropriateness of the non-numeric values.

As x approaches 0, $\log(x)$ approaches -Inf. So when x = 0 in this case, it shows that $\log(0) = -\text{Inf.} \log(0)$ technically does not exist but the answer is appropriate enough. As x approaches Inf, then $\log(x)$ approaches Inf so this is appropriate. Log does not exist for negative values of x, so R gives us a NaN, which is maybe not as appropriate as "NA" since $\log(-x)$ is not available/applicable rather than not a number.

• Create a vector of booleans where the entry is true if x[i] is positive and finite.

```
y = !is.nan(x) & is.finite(x) & x > 0
```

• Locate the indices of the non-real numbers in this vector. Hint: use the which function. Don't hesitate to use the documentation via ?which.

```
which(!y) #finding the falses in y (non-reals)
```

[1] 1 52 53 54 55 56 57 58 59 60 61 62

```
# or which(y == FALSE)
```

• Locate the indices of the infinite quantities in this vector.

```
which(is.infinite(x))
```

```
## [1] 1 52
```

Locate the indices of the min and max in this vector. Hint: use the which.min and which.max functions.

```
which.min(x)
```

[1] 52

```
which.max(x)
```

[1] 1

• Count the number of unique values in x.

```
length(unique(x))
```

[1] 53

• Cast x to a factor. Do the number of levels make sense?

as.factor(x)

```
[1] Inf
                          4.19180654857877
                                             4.1734172518943
                                                               4.15464876785729
##
    [5] 4.13548512895119
                          4.11590933734319
                                             4.09590327428938
                                                               4.07544759935851
   [9] 4.05452163806914 4.03310325630434
                                            4.01116871959141
                                                               3.98869253500376
## [13] 3.96564727304425
                          3.94200336638929
                                             3.91772888178973
                                                               3.89278926071437
## [17] 3.86714702345081
                          3.84076143030548
                                             3.81358809221559
                                                               3.78557852142874
## [21] 3.75667961082847
                          3.72683302786084
                                             3.69597450568212
                                                               3.66403300987579
                          3.59657702661571
                                                               3.52371901428583
## [25] 3.63092975357146
                                             3.56087679500731
  [29] 3.48497958377173
                          3.44451784578705
                                             3.40217350273288
                                                               3.3577627814323
## [33] 3.31107361281783
                          3.26185950714291
                                             3.20983167673402
                                                               3.15464876785729
## [37] 3.09590327428938
                          3.03310325630434
                                             2.96564727304425
                                                               2.89278926071437
## [41] 2.8135880922156
                          2.72683302786084
                                             2.63092975357146
                                                               2.52371901428583
## [45] 2.40217350273288
                          2.26185950714291
                                             2.09590327428938
                                                               1.89278926071437
                          1.26185950714291
## [49] 1.63092975357146
                                            0.630929753571457 -Inf
## [53] NaN
                          NaN
                                             NaN
                                                               NaN
## [57] NaN
                          NaN
                                             NaN
                                                               NaN
## [61] NaN
                          NaN
## 53 Levels: -Inf 0.630929753571457 1.26185950714291 ... NaN
```

• Cast x to integers. What do we learn about R's infinity representation in the integer data type?

```
as.integer(x) # INFs and NaN converted to NA
## Warning: NAs introduced by coercion to integer range
                                   4
   [1] NA
                4 4 4 4 4
                              4
                                4
                                     3 3
                                                    3 3 3 3
## [26]
                   3 3 3 3
                              3
                                3 3 3
          3
             3
                3
## [51]
       O NA NA NA NA NA NA NA NA NA NA
```

• Use x to create a new vector y containing only the real numbers in x.

```
y = x[(!is.nan(x) & is.finite(x) & x > 0)]
y

## [1] 4.19180654858 4.17341725189 4.15464876786 4.13548512895 4.11590933734
## [6] 4.09590327429 4.07544759936 4.05452163807 4.03310325630 4.01116871959
## [11] 3.98869253500 3.96564727304 3.94200336639 3.91772888179 3.89278926071
## [16] 3.86714702345 3.84076143031 3.81358809222 3.78557852143 3.75667961083
## [21] 3.72683302786 3.69597450568 3.66403300988 3.63092975357 3.59657702662
## [26] 3.56087679501 3.52371901429 3.48497958377 3.44451784579 3.40217350273
## [31] 3.35776278143 3.31107361282 3.26185950714 3.20983167673 3.15464876786
## [36] 3.09590327429 3.03310325630 2.96564727304 2.89278926071 2.81358809222
## [41] 2.72683302786 2.63092975357 2.52371901429 2.40217350273 2.26185950714
## [46] 2.09590327429 1.89278926071 1.63092975357 1.26185950714 0.63092975357
```

• Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle width size 1e-6.

```
sum(seq(from=0,to=1-1e-6,by=1e-6)^2)*1e-6
```

```
## [1] 0.33333283333
```

• Calculate the average of 100 realizations of standard Bernoullis in one line using the sample function.

```
mean(sample(c(0,1),size=100,replace=TRUE))
```

```
## [1] 0.53
```

• Calculate the average of 500 realizations of Bernoullis with p = 0.9 in one line using the sample and mean functions.

```
mean(sample(c(0,1),size=100,replace=TRUE,prob=c(0.1,0.9)))
```

```
## [1] 0.89
```

• Calculate the average of 1000 realizations of Bernoullis with p = 0.9 in one line using rbinom.

```
mean(rbinom(n=1000,size=1,prob=0.9))
```

[1] 0.9

• In class we considered a variable x_3 which measured "criminality". We imagined L = 4 levels "none", "infraction", "misdimeanor" and "felony". Create a variable x_3 here with 100 random elements (equally probable). Create it as a nominal (i.e. unordered) factor.

```
x_3 = as.factor(sample(c("none", "infraction", "misdimeanor", "felony"), size=100, replace=TRUE))
x_3
```

```
##
     [1] felony
                                  infraction
                                                           infraction infraction
                     none
                                              none
##
     [7] misdimeanor misdimeanor none
                                              felony
                                                           felony
                                                                       felony
    [13] misdimeanor none
                                  felony
                                              misdimeanor misdimeanor misdimeanor
##
    [19] none
                     infraction
                                  none
                                              felony
                                                           none
                                                                       infraction
##
    [25] none
                     felony
                                  felony
                                              felony
                                                                       felony
                                                           none
##
    [31] none
                     felony
                                  none
                                              none
                                                           none
                                                                       none
##
    [37] misdimeanor misdimeanor misdimeanor felony
                                                           none
                                                                       felony
##
    [43] infraction misdimeanor infraction
                                              felony
                                                           misdimeanor felony
    [49] misdimeanor felony
##
                                  infraction
                                              none
                                                           none
                                                                       misdimeanor
    [55] felony
                                  infraction misdimeanor infraction
                     none
                                                                       felony
   [61] felony
##
                                                           misdimeanor none
                     none
                                  none
                                              none
    [67] felony
##
                     infraction
                                  felony
                                              misdimeanor none
                                                                       felony
##
   [73] misdimeanor none
                                              misdimeanor none
                                                                       misdimeanor
                                  infraction
   [79] misdimeanor felony
                                  infraction
                                              infraction felony
                                                                       none
##
   [85] misdimeanor misdimeanor none
                                                           misdimeanor infraction
                                              none
    [91] none
                     none
                                              infraction
                                                           none
                                                                       felony
                                  none
  [97] none
                                              misdimeanor
                     misdimeanor none
## Levels: felony infraction misdimeanor none
```

• Use x_3 to create x_3_bin, a binary feature where 0 is no crime and 1 is any crime.

```
x_3_bin = x_3 != "none"
x_3_bin
```

```
##
     [1]
          TRUE FALSE
                      TRUE FALSE
                                   TRUE
                                         TRUE
                                               TRUE
                                                      TRUE FALSE
                                                                  TRUE
                                                                        TRUE
                                                                               TRUE
##
    [13]
          TRUE FALSE
                      TRUE
                            TRUE
                                  TRUE
                                         TRUE FALSE
                                                      TRUE FALSE
                                                                  TRUE FALSE
                                                                               TRUE
    [25] FALSE
                TRUE
                      TRUE
                             TRUE FALSE
                                         TRUE FALSE
                                                      TRUE FALSE FALSE FALSE
##
    [37]
          TRUE
                TRUE
                      TRUE
                            TRUE FALSE
                                         TRUE
                                               TRUE
                                                      TRUE
                                                            TRUE
                                                                  TRUE
                                                                        TRUE
                                                                               TRUE
##
    [49]
          TRUE
               TRUE
                      TRUE FALSE FALSE
                                         TRUE
                                               TRUE FALSE
                                                            TRUE
                                                                  TRUE
                                                                        TRUE
                                                                               TRUE
##
    [61]
          TRUE FALSE FALSE FALSE
                                  TRUE FALSE
                                               TRUE
                                                      TRUE
                                                            TRUE
                                                                  TRUE FALSE
                                                                               TRUE
   [73]
          TRUE FALSE
                      TRUE
                             TRUE FALSE
                                         TRUE
                                               TRUE
                                                      TRUE
                                                            TRUE
                                                                  TRUE
                                                                        TRUE FALSE
##
    [85]
          TRUE
                TRUE FALSE FALSE
                                   TRUE
                                         TRUE FALSE FALSE FALSE
                                                                  TRUE FALSE
                                                                              TRUE
    [97] FALSE
               TRUE FALSE
                            TRUE
```

• Use x 3 to create x 3 ord, an ordered factor variable. Ensure the proper ordinal ordering.

```
x_3_ord = factor(x_3,levels=c("none", "infraction", "misdimeanor", "felony"),ordered=TRUE)
x_3_ord
```

```
##
     [1] felonv
                    none
                                infraction none
                                                        infraction infraction
##
    [7] misdimeanor misdimeanor none
                                            felony
                                                        felony
                                                                    felony
                                            misdimeanor misdimeanor misdimeanor
##
   [13] misdimeanor none
                                felony
##
  [19] none
                    infraction none
                                            felony
                                                                    infraction
                                                        none
   [25] none
                    felony
                                felony
                                            felony
                                                        none
                                                                    felony
  [31] none
##
                    felony
                                none
                                            none
                                                        none
                                                                    none
  [37] misdimeanor misdimeanor misdimeanor felony
                                                        none
                                                                    felony
## [43] infraction misdimeanor infraction felony
                                                        misdimeanor felony
   [49] misdimeanor felony
                                infraction
                                            none
                                                        none
                                                                    misdimeanor
##
  [55] felony
                    none
                                infraction misdimeanor infraction felony
  [61] felony
                    none
                                none
                                            none
                                                        misdimeanor none
  [67] felony
                                            misdimeanor none
##
                    infraction felony
                                                                    felony
## [73] misdimeanor none
                                infraction misdimeanor none
                                                                    misdimeanor
## [79] misdimeanor felony
                                infraction infraction felony
                                                                    none
## [85] misdimeanor misdimeanor none
                                            none
                                                        misdimeanor infraction
## [91] none
                    none
                                            infraction none
                                                                    felony
                                none
## [97] none
                    misdimeanor none
                                            misdimeanor
## Levels: none < infraction < misdimeanor < felony
```

• Convert this variable into three binary variables without any information loss and put them into a data matrix.

```
inf = as.numeric(x 3 ord == "infraction")
inf
  [38] 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 0 0 1 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
 [75] 1 0 0 0 0 0 1 1 0 0 0 0 0 0 1 0 0 0 1 0 0 0 0 0
mis = as.numeric(x_3_ord == "misdimeanor")
mis
  fel = as.numeric(x_3_ord == "felony")
fel
  X = matrix(data=NA,nrow=100,ncol=3)
colnames(X) = c("infraction", "misdimeanor", "felony")
X[, "infraction"] = inf
X[, "misdimeanor"] = mis
X[, "felony"] = fel
```

infraction misdimeanor felony

##

шш	Γ4 J	^	0	4
## ##	[1,]	0	0	1
##	[2,]	1	0	0
##	[3,]	0	0	0
##	[4,] [5,]	1	0	0
		1		
##	[6,]		0 1	0
##	[7,]	0		0
##	[8,]	0	1	0
##	[9,]	0	0	0
##	[10,]	0	0	1
##	[11,]	0	0	1
##	[12,]	0	0	1
##	[13,]	0	1	0
##	[14,]	0	0	0
##	[15,]	0	0	1
##	[16,]	0	1	0
##	[17,]	0	1	0
##	[18,]	0	1	0
##	[19,]	0	0	0
##	[20,]	1	0	0
##	[21,]	0	0	0
##	[22,]	0	0	1
##	[23,]	0	0	0
##	[24,]	1	0	0
##	[25,]	0	0	0
##	[26,]	0	0	1
##	[27,]	0	0	1
##	[28,]	0	0	1
##	[29,]	0	0	0
##	[30,]	0	0	1
##	[31,]	0	0	0
##	[32,]	0	0	1
##	[33,]	0	0	0
##	[34,]	0	0	0
##	[35,]	0	0	0
##	[36,]	0	0	0
##	[37,]	0	1	0
##	[38,]	0	1	0
##	[39,]	0	1	0
##	[40,]	0	0	1
##	[41,]	0	0	0
##	[42,]	0	0	1
##	[43,]	1	0	0
##	[44,]	0	1	0
##	[45,]	1	0	0
##	[46,]	0	0	1
##	[47,]	0	1	0
##	[48,]	0	0	1
##	[49,]	0	1	0
##	[50,]	0	0	1
##	[51,]	1	0	0
##	[52,]	0	0	0
##	[53,]	0	0	0
##	[54,]	0	1	0

##	[55,]	0	0	1
##	[56,]	0	0	0
##	[57,]	1	0	0
##	[58,]	0	1	0
##	[59,]	1	0	0
	[60,]	0		
##			0	1
##	[61,]	0	0	1
##	[62,]	0	0	0
##	[63,]	0	0	0
##	[64,]	0	0	0
##	[65,]	0	1	0
##	[66,]	0	0	0
##	[67,]	0	0	1
##	[68,]	1	0	0
##	[69,]	0	0	1
##	[70,]	0	1	0
##	[71,]	0	0	0
##	[72,]	0	0	1
##	[73,]	0	1	0
##	[74,]	0	0	0
##	[75,]	1	0	0
##	[76,]	0	1	0
##	[77,]	0	0	0
##	[78,]	0	1	0
##	[79,]	0	1	0
##	[80,]	0	0	1
##	[81,]	1	0	0
##	[82,]	1	0	0
##	[83,]	0	0	1
##	[84,]	0	0	0
##	[85,]	0	1	0
##	[86,]	0	1	0
##	[87,]	0	0	0
##	[88,]	0	0	0
##	[89,]	0	1	0
##	[90,]	1	0	0
##	[91,]	0	0	0
##	[92,]	0	0	0
##	[93,]	0	0	0
##	[94,]	1	0	0
##	[95,]	0	0	0
	[96,]	0	0	1
##				
##	[97,]	0	0	0
##	[98,]	0	1	0
##	[99,]	0	0	0
##	[100,]	0	1	0

• What should the sum of each row be (in English)?

The row represents a person and each of their columns represents if that was the highest crime that they committed. So the sum of the row can only be 1 or 0. This means that the sum of the row represents if an individual committed ANY crime whatsoever.

Verify that.

as.matrix(rowSums(X), nrow=100)

```
##
           [,1]
     [1,]
##
             1
##
     [2,]
              0
##
     [3,]
              1
##
     [4,]
              0
##
     [5,]
              1
     [6,]
##
##
     [7,]
              1
     [8,]
##
              1
##
     [9,]
              0
##
    [10,]
##
    [11,]
              1
##
    [12,]
              1
##
    [13,]
              1
    [14,]
##
##
    [15,]
              1
##
    [16,]
              1
##
    [17,]
              1
##
    [18,]
              1
    [19,]
##
              0
##
    [20,]
              1
##
    [21,]
##
    [22,]
              1
##
    [23,]
              0
##
    [24,]
              1
    [25,]
##
              0
##
    [26,]
              1
##
    [27,]
              1
##
    [28,]
              1
    [29,]
##
              0
##
    [30,]
              1
    [31,]
##
              0
##
    [32,]
              1
##
    [33,]
              0
##
    [34,]
              0
    [35,]
##
              0
##
    [36,]
              0
##
    [37,]
              1
##
    [38,]
              1
##
    [39,]
              1
##
    [40,]
##
    [41,]
              0
    [42,]
##
              1
##
    [43,]
              1
##
    [44,]
    [45,]
##
              1
    [46,]
##
              1
##
   [47,]
              1
##
   [48,]
              1
## [49,]
              1
## [50,]
```

```
[51,]
##
               1
##
     [52,]
               0
     [53,]
##
               0
     [54,]
##
                1
##
     [55,]
               1
##
     [56,]
               0
##
     [57,]
               1
     [58,]
##
                1
##
     [59,]
               1
##
     [60,]
                1
##
     [61,]
                1
##
     [62,]
               0
##
     [63,]
               0
##
     [64,]
               0
##
     [65,]
                1
##
     [66,]
               0
##
     [67,]
                1
     [68,]
##
               1
##
     [69,]
               1
     [70,]
##
               1
##
     [71,]
               0
##
     [72,]
               1
##
     [73,]
                1
##
     [74,]
               0
##
     [75,]
                1
##
     [76,]
               1
##
     [77,]
               0
##
     [78,]
               1
##
     [79,]
##
     [80,]
                1
##
     [81,]
                1
##
     [82,]
                1
##
     [83,]
               1
##
     [84,]
               0
     [85,]
##
               1
##
     [86,]
               1
##
     [87,]
##
     [88,]
               0
##
     [89,]
               1
     [90,]
##
                1
##
     [91,]
               0
##
     [92,]
               0
##
     [93,]
               0
##
     [94,]
                1
##
     [95,]
               0
     [96,]
##
                1
##
     [97,]
               0
##
     [98,]
     [99,]
               0
##
## [100,]
```

• How should the column sum look (in English)?

The column sum represents the total number of a certain crime that everyone in the data set has committed.

For example, if 20 people committed a felony, then the sum of the felony column is 20. Verify that.

```
colSums(X)
```

```
## infraction misdimeanor felony
## 16 25 25
```

• Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column in exponential with lambda of 9, the fifth column is binomial with n = 20 and p = 0.12 and the sixth column is a binary variable with exactly 24% 1's dispersed randomly. Name the rows the entries of the fake_first_names vector.

```
fake first names = c(
  "Sophia", "Emma", "Olivia", "Ava", "Mia", "Isabella", "Riley",
  "Aria", "Zoe", "Charlotte", "Lily", "Layla", "Amelia", "Emily",
  "Madelyn", "Aubrey", "Adalyn", "Madison", "Chloe", "Harper",
  "Abigail", "Aaliyah", "Avery", "Evelyn", "Kaylee", "Ella", "Ellie",
  "Scarlett", "Arianna", "Hailey", "Nora", "Addison", "Brooklyn",
  "Hannah", "Mila", "Leah", "Elizabeth", "Sarah", "Eliana", "Mackenzie",
  "Peyton", "Maria", "Grace", "Adeline", "Elena", "Anna", "Victoria",
  "Camilla", "Lillian", "Natalie", "Jackson", "Aiden", "Lucas",
 "Liam", "Noah", "Ethan", "Mason", "Caden", "Oliver", "Elijah",
  "Grayson", "Jacob", "Michael", "Benjamin", "Carter", "James",
  "Jayden", "Logan", "Alexander", "Caleb", "Ryan", "Luke", "Daniel",
  "Jack", "William", "Owen", "Gabriel", "Matthew", "Connor", "Jayce",
  "Isaac", "Sebastian", "Henry", "Muhammad", "Cameron", "Wyatt",
  "Dylan", "Nathan", "Nicholas", "Julian", "Eli", "Levi", "Isaiah",
  "Landon", "David", "Christian", "Andrew", "Brayden", "John",
  "Lincoln"
)
Y = matrix(data=NA, nrow=100,ncol=6)
rownames(Y) = fake_first_names
?rnorm
```

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```
Y[,1] = rnorm(n=100,mean=17,sd=sqrt(38))
?runif
Y[,2] = runif(n=100,min=-10,max=10)
?rpois
Y[,3] = rpois(n=100,lambda=6)
?rexp
Y[,4] = rexp(n=100,rate=9)
?rbinom
Y[,5] = rbinom(n=20,size=100,p=0.12)
Y[,6] = rbinom(n=100,size=1,p=0.24)
Y
```

[,1] [,2] [,3] [,4] [,5] [,6]

```
## Sophia
             10.91861876543 -4.097394072451
                                                  6 0.01234750516920
                                                                              0
                                                                        14
## Emma
              15.83154338879 -4.321016655304
                                                  4 0.01622077119019
                                                                        12
                                                                              1
## Olivia
              15.91442099575 -5.472529665567
                                                  3 0.20993376687891
                                                                        14
##
                              4.904534891248
  Ava
             27.24053754303
                                                  6 0.32886607009819
                                                                         8
                                                                              0
##
  Mia
              18.37069867801
                              7.861592834815
                                                  2 0.26157304125783
                                                                        16
                                                                              0
##
             20.39793837183 -9.979295795783
                                                  6 0.81935421414145
                                                                              0
  Isabella
                                                                        13
## Riley
              22.31304681125
                              2.353761158884
                                                  5 0.00097520683640
                                                                        11
                                                                              0
## Aria
              14.08692403011
                              0.685578994453
                                                  4 0.23941259320870
                                                                        13
                                                                              1
##
   Zoe
              21.48317001033
                              7.119872537442
                                                  6 0.13858579347064
                                                                         9
                                                                              0
##
   Charlotte 26.10421764337 -4.216666910797
                                                 12 0.03739220007426
                                                                         8
                                                                              0
              6.45400846640 -6.544662918895
                                                  8 0.08544390358392
                                                                              0
   Lily
                                                                        11
   Layla
             -0.80709892028
                              5.576190194115
                                                   0.07128832432338
                                                                        11
                                                                              0
              19.29558821057
                              0.548814330250
                                                  6 0.04487050164284
##
   Amelia
                                                                        11
                                                                              0
              14.15304667879
   Emily
                              6.000881744549
                                                  3 0.02567854358090
                                                                        10
              12.81404936657 -3.863396327943
## Madelyn
                                                  5 0.14354394675904
                                                                        14
                                                                              0
   Aubrey
             21.62990376212
                              4.245483372360
                                                   0.03465824181007
                                                                        12
                                                                              0
   Adalyn
                                                  4 0.05172419411206
                                                                        16
                                                                              0
##
              18.27366457527
                              2.851941566914
  Madison
                                                  3 0.03716211938101
             12.53437973421
                              7.491714912467
##
  Chloe
             24.56431343792 -1.629586699419
                                                  5 0.21608689198786
                                                                        14
                                                                              0
## Harper
              11.59023615958 -1.476277317852
                                                  6 0.16243064701894
##
  Abigail
              6.75414348257
                              5.908799632452
                                                  9 0.12885072806176
                                                                        14
                                                                              0
## Aaliyah
             20.50419567831 -8.953183884732
                                                  5 0.00031601450886
## Avery
              6.56302486164 -8.422682061791
                                                  8 0.05603115109393
                                                                        14
                                                                              0
## Evelyn
             13.20481125051
                              8.421457801014
                                                  6 0.14256558960044
                                                                         8
                                                                              0
## Kaylee
              13.39043612149 -6.077099931426
                                                  5 0.00829849816445
                                                                        16
                                                                              0
## Ella
              24.56096653907
                              6.665602279827
                                                  7 0.03302398370579
                                                                        13
                                                                              1
## Ellie
              18.99076507771
                              2.535851267166
                                                  4 0.05151304556057
                                                                        11
                                                                              1
   Scarlett
             21.40655670907 -0.504435314797
                                                  6 0.48084990368469
                                                                        13
                                                                              0
   Arianna
             24.25281726944 -2.192661357112
                                                  9 0.02368054352701
                                                                         9
                                                                              0
## Hailey
              7.14977957083
                              9.512943918817
                                                  7 0.03488503603472
                                                                         8
                                                                              0
##
  Nora
              14.46477593762
                              9.569652336650
                                                  7 0.06471871377693
                                                                        11
                                                                              1
   Addison
              18.45072299369
                              1.996409213170
                                                  5 0.21152726870338
                                                                        11
                                                                              0
   Brooklyn
              9.42283407256
                              4.304349203594
                                                  2 0.10718394494666
              16.35465728807
  Hannah
                              5.227468637750
                                                  4 0.04702946740306
                                                                        10
                                                                              1
  Mila
              16.24735606561
                             -8.421867601573
                                                  2 0.04247614617149
##
                                                                        14
## Leah
              23.69092478058
                              4.116982151754
                                                  4 0.03228555866852
                                                                        12
                                                                              0
## Elizabeth 12.19392780690
                              5.412375028245
                                                  7 0.00274754222482
## Sarah
                                                  3 0.00578148924162
              18.00557872139
                              7.113266144879
                                                                         8
                                                                              1
## Eliana
              18.95954997659 -9.999384502880
                                                  5 0.12210056621759
                                                                        14
## Mackenzie 6.20819060692 -6.340586673468
                                                  7 0.08527980765068
                                                                         9
                                                                              0
## Peyton
             17.36424865467
                              7.184893097728
                                                  7 0.25182350620055
                                                                        14
## Maria
              25.17838372839
                              8.152099400759
                                                  9 0.06083976699867
                                                                        12
                                                                              1
##
  Grace
              17.63824421202
                              4.811713369563
                                                  3 0.12790883929698
                                                                        14
                                                                              1
                                                                              0
   Adeline
              6.75217432625
                              6.777169569395
                                                  4 0.12858806901869
                                                                         8
## Elena
              18.22405395450 -1.008109096438
                                                  4 0.02554333432474
                                                                        16
                                                                              0
              19.29324600138 -4.414599454030
## Anna
                                                  4 0.03280237724797
                                                                        13
                                                                              0
  Victoria
             18.73241535812 -8.356434949674
                                                  3 0.09329353644977
                                                                        11
                                                                              0
   Camilla
              31.42337921064
                              5.004761335440
                                                  4 0.00369865840508
                                                                        13
              15.00611096845 -1.270415247418
## Lillian
                                                  7 0.04585436549006
                                                                         9
                                                                              0
## Natalie
              19.60619309146
                              5.160495946184
                                                  6 0.06760437041521
                                                                         8
   Jackson
             14.64428130426 -1.893939487636
                                                  6 0.14666798337827
                                                                              0
                                                                        11
## Aiden
              19.14421519870
                              8.636615863070
                                                  5 0.41373680079011
                                                                        11
                                                                              0
## Lucas
              10.36430077822 -4.377955114469
                                                  6 0.14004885239267
                                                                              0
                                                                        11
## Liam
             15.68045781048
                              2.717919591814
                                                  8 0.08878630885595
```

```
## Noah
             19.48875918133 -8.591755125672
                                                 3 0.13767253979574
                                                                              0
                                                                       14
## Ethan
             18.27429031769 -3.379811751656
                                                 4 0.13145331189397
                                                                       12
                                                                              0
## Mason
             10.91525167552
                              0.869053024799
                                                 5 0.06717220693827
                                                                       16
## Caden
             11.72416568009 -2.957678493112
                                                 6 0.07567201673778
                                                                        8
                                                                              0
## Oliver
             26.85378109997
                              6.385708604939
                                                 5 0.13450372398584
                                                                       14
                                                                              1
## Elijah
             23.55184544769 -8.929673475213
                                                 5 0.19725006817838
                                                                        9
                                                                              0
## Grayson
             27.86921766736
                              7.521594711579
                                                 9 0.03450234606862
                                                                       14
                                                                              0
## Jacob
             13.38504670778 -6.187579929829
                                                 9 0.03921541732012
                                                                       12
                                                                              0
## Michael
              8.99627498985
                              7.181904441677
                                                 6 0.23936242753688
                                                                       14
                                                                              0
## Benjamin
             26.65274963166
                              5.410105343908
                                                 1 0.07010230085709
                                                                        8
                                                                              1
## Carter
             31.69735378744 -7.117239637300
                                                 8 0.15254732945260
                                                                       16
                                                                              0
   James
             17.11864828143
                              7.514688153751
                                                 1 0.03912136134693
                                                                       13
                                                                              0
              6.81327736439
##
   Jayden
                              0.099926758558
                                                 9 0.16468768146508
                                                                       11
                                                                              0
## Logan
             10.33088232434
                              3.078130716458
                                                 6 0.12357123123222
                                                                       13
                                                                              0
## Alexander 25.33791828663 -7.011408857070
                                                 5 0.09179956403405
                                                                        9
                                                                              0
## Caleb
             19.34659512862 -8.805055189878
                                                 8 0.16477847802037
                                                                        8
                                                                              1
## Ryan
                              1.699982136488
                                                10 0.10335311644968
                                                                              0
             16.90438651634
                                                                       11
## Luke
              2.59986726627
                              8.177500320598
                                                 5 0.03032431497963
                                                                       11
                                                                              1
## Daniel
             22.40454797152 4.482135707512
                                                 8 0.30263913814648
                                                                       11
                                                                              0
## Jack
             12.03560596211 -0.660762507468
                                                 2 0.36010579431839
                                                                       10
                                                                              0
## William
              3.76983488360
                              3.439841615036
                                                 8 0.32720050805134
                                                                       14
                                                                              0
## Owen
             21.15878699193
                              6.471642786637
                                                 8 0.08975977541103
                                                                       12
                                                                              1
## Gabriel
             15.49329462354
                              6.489480631426
                                                 3 0.18194802932336
                                                                       16
                                                                              0
## Matthew
              7.87417182900 -6.574119939469
                                                 5 0.10596404172427
                                                                        8
                                                                              0
## Connor
             24.95496512144 -4.209469961934
                                                 6 0.09673158265184
                                                                       14
                                                                              0
  Jayce
             14.95035341172
                              8.618910745718
                                                 6 0.12689958905541
                                                                        9
                                                                              0
## Isaac
              9.01025742371 -9.398923846893
                                                 4 0.15450666281653
                                                                       14
                                                                              0
##
  Sebastian 14.34427320101 -5.192441097461
                                                 8 0.01265541652461
                                                                       12
                                                                              0
## Henry
             12.10676658013
                              2.994423443452
                                                 6 0.04277192144137
                                                                       14
                                                                              0
## Muhammad
                                                 6 0.00950273284434
                                                                        8
             14.53271932656
                              6.665337597951
                                                                              0
  Cameron
             20.10938388170
                              8.401928213425
                                                 5 0.12988704432163
                                                                       16
                                                                              0
## Wyatt
             29.45893479336 -1.227905107662
                                                 1 0.02449569178538
                                                                       13
                                                                              0
## Dylan
             15.94941071677
                              9.614281305112
                                                 6 0.11154009394683
                                                                              1
## Nathan
             13.27879950546 -0.843189782463
                                                10 0.00381051247112
                                                                       13
                                                                              0
## Nicholas
             22.63344143031
                              9.032058115117
                                                 4 0.05121938211636
                                                                        9
                                                                              0
## Julian
             17.01246781981 -3.148652738892
                                                 3 0.01673957379535
                                                                        8
                                                                              0
## Eli
             27.56566710586 -7.942494899035
                                                12 0.03769843978807
                                                                       11
                                                                              0
## Levi
             14.58347265933 -5.371569073759
                                                 6 0.02647660030872
                                                                       11
                                                                              0
              7.68544084136 -7.090637353249
                                                 5 0.27198711884774
## Isaiah
                                                                       11
                                                                              0
## Landon
             22.44025724949 -7.464286964387
                                                 7 0.16852859137681
                                                                       10
                                                                              0
## David
              6.99393462789
                              8.387943576090
                                                 6 0.45686142040773
                                                                       14
                                                                              0
                                                 8 0.21981266822974
## Christian 23.59389591992 -8.007079488598
                                                                       12
                                                                              1
## Andrew
             18.08660121816
                              1.125044655055
                                                 7 0.16969588294520
                                                                       16
                                                                              1
                                                                              0
## Brayden
              8.65734128520
                              2.733864123002
                                                 9 0.09869872420805
                                                                        8
## John
             17.42536724215 -9.343861499801
                                                 8 0.06260052188817
                                                                       14
                                                                              0
             18.97768447955 -5.839329333976
                                                 7 0.06919418435751
                                                                        9
                                                                              0
## Lincoln
```

• Create a data frame of the same data as above except make the binary variable a factor "DOMESTIC" vs "FOREIGN" for 0 and 1 respectively. Use RStudio's View function to ensure this worked as desired.

```
Y_frame = data.frame(Y)
Y_frame[,6] = ifelse(Y_frame[,6] == 1, "FOREIGN", "DOMESTIC")
View(Y_frame)
```

• Print out a table of the binary variable. Then print out the proportions of "DOMESTIC" vs "FOREIGN".

```
table(Y_frame[,6])
##
## DOMESTIC
             FOREIGN
##
         81
                   19
table(Y_frame$X6, Y_frame$X6) / 100
##
##
               DOMESTIC FOREIGN
##
     DOMESTIC
                   0.81
                            0.00
##
     FOREIGN
                   0.00
                            0.19
```

Print out a summary of the whole dataframe.

```
Y_frame$X6 = factor(Y_frame$X6, labels = c("DOMESTIC", "FOREIGN"))
summary(Y_frame)
```

```
##
          Х1
                                Х2
                                                       ХЗ
##
   Min.
           :-0.80709892
                                 :-9.99938450
                                                      : 1.00
                          Min.
                                                 Min.
   1st Qu.:12.17213750
                          1st Qu.:-5.23722309
                                                 1st Qu.: 4.00
##
  Median :17.06555805
                          Median : 0.99704884
                                                 Median: 6.00
                                 : 0.46137572
##
   Mean
           :16.67938917
                          Mean
                                                 Mean
                                                        : 5.75
##
   3rd Qu.:21.22072942
                          3rd Qu.: 6.09708846
                                                 3rd Qu.: 7.00
##
   Max.
           :31.69735379
                          Max.
                                 : 9.61428131
                                                 Max.
                                                        :12.00
          Х4
##
                                  Х5
                                                    Х6
           :0.00031601451
                                   : 8.00
                                             DOMESTIC:81
## Min.
                            Min.
  1st Qu.:0.03733467990
                            1st Qu.: 9.75
                                             FOREIGN:19
## Median :0.08927304213
                            Median :11.50
## Mean
           :0.11972911324
                            Mean
                                    :11.70
##
   3rd Qu.:0.15303716279
                            3rd Qu.:14.00
## Max.
           :0.81935421414
                            Max.
                                   :16.00
```

• Let n=50. Create a n x n matrix R of exactly 50% entries 0's, 25% 1's 25% 2's. These values should be in random locations.

```
R = matrix(sample(
   c(0,1,2),
   size = 50,
   replace = TRUE,
   prob = c(.50, .25, .25)
), nrow = 50, ncol = 50)
table(R)
```

```
## R
## 0 1 2
## 1250 750 500
```

 Randomly punch holes (i.e. NA) values in this matrix so that an each entry is missing with probability 30%.

```
R[sample(1:length(R), length(R)*0.3)] <- NA
table(R)</pre>
```

R ## 0 1 2 ## 876 525 349

R

[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] ## [1,] NANA NANA [2,] NA NANA## NANA## [3,] NA NANA NA NA ## [4,]NANA NANANANA NA## [5,] NA NANA NA ## [6,] NA NA NA ## [7,] NANANA NA ## [8,] NA NA NA[9,] ## NANANA[10,] ## NANANA## [11,]NANA ## [12,]NANANA NA ## [13,] NANA NANANA NA[14,]## NA NA## [15,] NA NA NANANA## [16,]NANA NA NA NANA[17,]NANA## ## [18,] NANA NA## [19,]NA NANA## [20,] NANA NA NA## [21,] NANANANA ## [22,] NA NA [23,]NA NA ## NA [24,]NA NANA NA NANA NA [25,]NA## ## [26,] NANA NANANA## [27,] NANA NA## [28,] NA NA## [29,] NA NA [30,] ## NANA[31,]## NA NANA NANA [32,]NANA## NANANANA## [33,] NANANA NANA[34,]## NANANANA ## [35,] NANA NANA NA NA## [36,] NANANA## [37,] NA NANA NANA [38,] ## NA NANA## [39,] NA NANA NANANA NA ## [40,]NANA NANA

##	[41,]	NA	0	0 1	VA (O NA	0	0	0	0	0	NA	0
	[42,]	1	1	1 I	NA NA	A 1	1	1	1	NA	1	1	NA
##	[43,]	0	NA	0	O NA	A NA	0	NA	0	0	0	0	0
	[44,]	1	1	1	1 NA		1	NA	1	1	1	NA	NA
	[45,]	1	NA	1		1 1	NA	NA	1	1	1	NA	1
##	[46,]	0	NA	0		O NA	0	0	0	0	0	0	0
##	[47,]	1	NA			1 NA	1	1	NA	1	1	1	NA
##	[48,]	1	NA	1	1 NA		NA	NA	NA	NA	1	1	1
##	[49,]	NA	NA	NA		1 NA	1	1	1	1	1	1	NA
##	[50,]	NA	NA	NA	0 (NA	0	0	0	0	0	NA
##	F4 7	[,14]	[,15]	[,16]	[,17]		[,19]	[,20]	[,21]	[,22]	[,23]	[,24]	[,25]
##	[1,]	NA	NA	2	2	2	2	NA	2	2	2	2	2
##	[2,]	NA	NA	0	0	0	0	NA	NA	NA	0	0	0
##	[3,]	NA	0	0	0	NA	0	0	NA	NA	NA	0	0
##	[4,]	O	NA	0	0	NA	0	0	NA	0	NA	NA	NA
## ##	[5,] [6,]	NA O	NA	2	2	2	2	2	2	2	2	2	NA
##	[7,]	NA	0	0	NA	0	0	0	0	0	0	0	0
##	[8,]	0	0	NA	0	NA	0	NA	0	0	0	0	0
##	[9,]	NA	0	0	0	0	0	0	0	NA	0	0	0
##	[10,]	NA	2	2	NA	2	NA	NA	2	2	NA	2	2
##	[11,]	1	1	1	1	1	1	1	NA	1	1	1	1
##	[12,]	2	NA	NA	2	2	2	NA	NA	2	2	2	2
##	[13,]	2	2	2	2	NA	2	2	2	2	2	2	2
##	[14,]	1	1	1	1	1	1	1	1	1	1	NA	1
##	[15,]	NA	0	0	0	0	0	0	0	0	0	0	0
##	[16,]	1	1	1	1	1	1	1	1	1	NA	1	NA
##	[17,]	2	2	NA	2	2	NA	2	NA	NA	2	2	2
##	[18,]	1	NA	1	1	NA	1	1	1	1	1	1	1
##	[19,]	NA	0	NA	0	NA	NA	0	0	0	NA	NA	NA
##	[20,]	2	2	NA	NA	2	NA	2	2	NA	2	NA	2
##	[21,]	0	0	0	0	0	NA	0	NA	0	0	0	NA
##	[22,]	NA	0	0	0	0	0	NA	0	0	0	0	0
##	[23,]	2	2	2	2	2	2	2	NA	2	NA	2	NA
##	[24,]	NA	1	1	NA	NA	NA	NA	1	1	NA	1	1
##	[25,]	1	1	NA	NA	NA	1	1	1	NA	NA	1	1
##	[26,]	2	2	2	2	2	2	2	2	2	2	NA	2
	[27,]	0	0	0	0	0	0	NA	0	0	0	NA	0
##	[28,]	0	0	0	NA	NA	NA	0	0	NA	0	0	0
## ##	[29,]	NA NA	0	O N A	O NA	0	O M A	NA O	0	0	NA	O M A	O N A
##	[30,] [31,]	NA O	0	NA O	NA NA	0	NA O	NA	0	0	NA O	NA NA	NA O
	[32,]	0	0	NA	0	0	NA	0	0	0	0	NA	NA
##	[33,]	1	NA	NA	1	1	1	1	1	1	NA	1	1
##	[34,]	0	NA	0	0	0	0	NA	0	NA	0	0	0
##	[35,]	NA	0	0	0	NA	0	NA	0	0	0	NA	0
##	[36,]	1	NA	1	1	1	NA	1	1	NA	1	NA	1
##	[37,]	1	1	1	ΝĀ	1	NA	1	NA	1	1	NA	1
##	[38,]	NA	2	2	NA	2	2	NA	2	2	2	2	2
##	[39,]	0	NA	0	NA	0	0	0	0	0	0	0	0
##	[40,]	0	NA	NA	0	0	0	0	0	0	NA	NA	0
##		0	0	0	0	0	0	0	0	0	0	NA	0
##	[42,]	NA	1	NA	NA	NA	1	NA	1	1	1	NA	1
##	[43,]	NA	0	0	0	0	0	0	0	0	0	0	NA

##	[44,]	1	1	NA	1	1	1	1	NA	NA	NA	1	1
##	[45,]	1	NA	1	NA	1	NA	1	1	NA	NA	1	NA
##	[46,]	0	0	0	0	NA	0	0	0	NA	NA	0	NA
	[47,]	1	NA	NA	NA	NA	1	NA	1	NA	1	1	1
##	[48,]	1	1	1	NA	1	1	1	1	1	1	NA	1
##	[49,]	1	1	NA	NA	NA	1	1	NA	NA	NA	1	1
##	[50,]	NA	NA	0	0	0	NA	NA	0	0	0	0	0
##	F4 7	[,26]	[,27]	[,28]	[,29]	[,30]	[,31]		[,33]	[,34]		[,36]	[,37]
## ##	[1,] [2,]	2	2	2	2	2 NA	2	2 NA	NA O	2	2	2	2
##	[3,]	0	NA	NA	0	0	0	NA NA	0	0	0	0	0
##	[4,]	0	NA	0	NA	0	0	NA NA	0	0	0	0	0
##	[5,]	NA	2	NA	2	2	NA	2	2	2	NA	2	NA
##	[6,]	NA	NA	0	0	0	NA	0	0	0	0	0	0
##	[7,]	0	NA	NA	0	NA	NA	NA	0	NA	NA	NA	0
##	[8,]	0	0	0	0	0	0	NA	NA	0	0	0	NA
##	[9,]	0	0	0	0	0	NA	0	0	0	NA	NA	0
##	[10,]	2	2	2	2	NA	NA	2	2	2	2	NA	NA
##	[11,]	NA	1	1	1	1	NA	1	1	NA	1	1	NA
##	[12,]	2	2	2	2	NA	NA	NA	NA	2	2	2	2
##	[13,]	2	2	NA	2	2	2	NA	2	NA	2	2	2
##	[14,]	1	1	1	1	1	1	1	1	1	1	1	1
##	[15,]	0	0	NA	0	0	0	0	0	0	0	NA	0
##	[16,]	1	NA	1	1	NA	NA	1	1	1	1	1	1
##	[17,]	NA	2	2	2	2	2	2	2	2	NA	NA	NA
##	[18,]	NA	NA	NA	1	1	1	1	1	1	1	1	1
##	[19,]	0	0	0	NA	0	0	NA	0	0	0	NA	NA
##	[20,]	2	2	2	2	2	2	2	NA	2	2	2	2
##	[21,]	0	NA	0	NA	NA	NA	NA	NA	0	0	0	0
##	[22,]	0	O	NA	NA	0	NA	0	O	NA	0	0	0
## ##	[23,] [24,]	NA NA	NA 1	2 1	2 NA	NA NA	2 1	2 1	NA NA	NA 1	2 1	2 1	NA 1
##	[25,]	1	1	NA	1	1	NA	NA	1	1	1	1	1
##	[26,]	2	2	NA	2	2	NA	2	2	2	2	2	2
##	[27,]	NA	0	0	0	0	0	NA	0	0	0	0	0
##	[28,]	NA	0	0	0	NA	0	0	0	0	0	0	0
##	[29,]	0	0	0	0	NA	NA	0	0	NA	0	NA	NA
##	[30,]	0	NA	NA	NA	0	NA	0	0	0	0	NA	0
	[31,]	0	0	0	NA	0	0	0	0	NA	0	0	0
##	[32,]	NA	0	0	0	0	0	0	NA	NA	NA	0	0
##	[33,]	1	1	1	1	NA	1	1	1	1	1	1	1
	[34,]	0	0	NA	0	0	0	NA	0	0	0	NA	0
	[35,]	0	0	0	0	0	0	0	NA	0	0	NA	NA
##	[36,]	1	NA	1	1	NA	1	1	1	1	1	NA	1
##	- ,-	NA	NA	1	1	1	1	1	NA	1	1	NA	NA
##	[38,]	2	2	2	NA	2	2	2	2	2	2	2	2
##	[39,]	0	0	0	0	NA	0	0	0	NA	0	0	0
##	[40,]	NA	0	0	NA	0	NA	0	NA	0	NA	0	0
##	[41,]	O M A	0	NA 1	O M A	NA 1	0	NA NA	0	0	0	NA 1	NA 1
## ##	[42,]	NA O	1 N A	1 NA	NA O	1 0	1 N A	NA O	1 0	1	1	1 0	1
	[43,] [44,]	NA	NA 1	NA 1	NA	1	NA NA	1	1	NA	1	1	0 1
	[45,]	1	NA	NA	1	NA	1	1	NA	1	NA	1	1
	[46,]	NA	NA	NA	NA	NA	NA	0	NA	0	NA	NA	NA
	- ,-												

##	[47,]	NA	1	1	1	1	1	1	1	1	1	1	1
##	[48,]	1	1	1	NA	1	NA	NA	1	1	NA	NA	1
##	[49,]	NA	1	1	NA	1	1	NA	1	NA	NA	1	1
##	[50,]	0	0	0	0	0	0	NA	0	NA	NA	0	0
##		[,38]	[,39]	[,40]	[,41]	[,42]	[,43]	[,44]		[,46]		[,48]	[,49]
##	[1,]	2	NA	2	NA	2	NA	2	NA	2	2	2	2
##	[2,]	0	0	0	0	0	NA	NA	0	0	0	0	0
##	[3,]	0	0	NA	0	0	0	0	0	0	0	0	NA
##	[4,]	0	0	NA	NA	0	0	0	NA	NA	0	0	0
##	[5,]	2	2	NA	2	2	2	2	2	2	2	2	2
##	[6,]	0	0	0	0	NA	0	0	NA	0	0	NA	NA
##	[7,]	0	0	0	NA	NA	NA	0	NA	NA	0	NA	NA
##	[8,]	NA	0	0	0	0	0	0	NA	0	0	0	0
##	[9,]	NA	0	0	0	0	0	NA	0	0	0	NA	0
##	[10,]	NA	2	NA	NA	2	NA	2	NA	NA	2	NA	NA
##	[11,]	1	NA	NA	NA	1	1	1	NA	1	1	NA	NA
##	[12,]	2	2	2	NA	2	NA	2	2	NA	NA	2	NA
##	[13,]	2	NA	2	2	NA	NA	2	2	NA	2	NA	NA
##	[14,]	1	1	1	1	1	NA	1	1	1	1	1	1
##	[15,]	0	0	0	0	0	NA	0	NA	0	0	0	NA
##	[16,]	NA	1 NA	1	NA	1 NA	1	1	NA	1 NA	1	NA	1
##	[17,]	2 NA	NA	2	2	NA	2	2	2	NA	2	NA	2
##	[18,]	NA	1	NA	1	1	1	1	NA	1 NA	1	NA	1 N A
##	[19,]	NA NA	O	NA	0 2	0	0 2	0	0	NA	O N A	0	NA NA
##	[20,]	NA	NA	2		2		2	NA	2	NA NA	2	NA NA
## ##	[21,] [22,]	0	0	NA O	O NA	0	O NA	0	0	0	NA O	0	NA NA
##	[23,]	NA	2	2	NA NA	NA	NA	NA	2	NA	2	2	2
##	[24,]	NA 1	1	NA	NA 1	NA NA	NA NA	1 1	NA	NA NA	1	NA	1
##	[25,]	1	1	1	1	1	1	NA	1	1	NA	1	1
##	[26,]	2	2	NA	2	NA	2	2	NA	NA	2	2	NA
##	[27,]	NA	0	NA	NA	0	0	0	0	0	0	0	0
##	[28,]	0	NA	0	0	0	0	0	NA	0	0	0	NA
##	[29,]	0	NA	0	0	0	0	NA	0	0	0	0	NA NA
##	[30,]	0	0	0	NA	0	0	NA	0	0	0	NA	0
##	[31,]	NA	0	0	NA	0	NA	0	0	0	0	0	0
##	[32,]	NA	0	0	0	NA	NA	0	NA	0	0	0	0
	[33,]	1	1	1	NA	1	1	1	1	1	1	1	1
	[34,]	0	0	NA	0	0	NA	0	NA	0	0	0	NA
	[35,]	NA	NA	NA	0	0	0	NA	0	0	0	0	0
	[36,]	1	1	NA	1	1	1	1	1	NA	NA	NA	1
	[37,]	1	1	1	1	1	1	1	1	1	1	NA	1
	[38,]	2	2	2	2	2	2	2	2	NA	2	2	NA
	[39,]	0	NA	0	NA	0	0	0	NA	NA	0	NA	0
	[40,]	0	0	NA	0	NA	0	0	0	0	NA	0	0
	[41,]	0	0	0	0	0	0	0	0	NA	NA	NA	NA
	[42,]	1	NA	1	NA	1	NA	1	NA	1	1	NA	NA
	[43,]	NA	0	NA	0	NA	0	NA	0	0	0	NA	NA
	[44,]	1	1	1	NA	1	1	NA	1	1	1	1	1
	[45,]	1	1	1	1	NA	NA	NA	1	NA	1	1	1
	[46,]	NA	0	0	0	0	NA	0	0	0	NA	NA	0
	[47,]	1	NA	1	1	1	1	NA	NA	NA	1	1	1
	[48,]	NA	NA	1	1	NA	1	1	1	NA	NA	1	1
	[49,]	1	1	1	1	1	1	1	NA	1	1	1	1

```
## [50,]
                   NA
                                  0
                                         0
                                               0
                                                             0
                                                                   0
                                                                          0
                                                                                 0
                                                                                      NA
              0
                           0
                                                     NA
          [,50]
##
    [1,]
##
             NA
    [2,]
##
              0
##
    [3,]
             NA
##
    [4,]
              0
##
    [5,]
              2
    [6,]
##
              0
##
    [7,]
             NA
##
    [8,]
              0
##
    [9,]
              0
## [10,]
             NA
## [11,]
              1
              2
## [12,]
## [13,]
              2
## [14,]
              1
## [15,]
              0
## [16,]
              1
## [17,]
             NA
## [18,]
             NA
## [19,]
              0
## [20,]
              2
## [21,]
              0
## [22,]
              0
## [23,]
             NA
## [24,]
              1
## [25,]
              1
## [26,]
              2
## [27,]
              0
## [28,]
             NA
## [29,]
             NA
## [30,]
              0
## [31,]
              0
## [32,]
              0
## [33,]
              1
## [34,]
              0
## [35,]
             NA
## [36,]
             NA
## [37,]
             NA
## [38,]
              2
## [39,]
              0
## [40,]
             NA
## [41,]
             NA
## [42,]
              1
## [43,]
              0
## [44,]
             NA
## [45,]
              1
## [46,]
              0
## [47,]
              1
## [48,]
              1
## [49,]
              1
## [50,]
```

• Sort the rows in matrix R by the largest row sum to lowest. Be careful about the NA's!

##		[,1]	[,2]		[,4]			[,7]			[,10]	[,11]	[,12]	[,13]
##	[1,]	2	2	2	NA	2	2	2	2	NA	NA	2	2	2
##	[2,]	2	NA	2	2	NA	NA	2	2	2	NA	2	2	2
##	[3,]	2	NA	2	2	NA	2	NA	2	2	2	NA	2	2
##	[4,]	2	NA	2	NA	2	2	NA	NA	2	2	2	NA	2
##	[5,]	2	2	2	2	2	2	NA	2	NA	2	2	2	2
##	[6,]	NA	2	NA	2	2	2	2	2	NA	2 NA	2	NA NA	2
## ##	[7,]	2 NA	NA 2	2	NA NA	NA 2	2 NA	2 2	NA NA	2 2	NA 2	2 2	NA 2	2 2
##	[8,] [9,]	NA 2	2	2	NA NA	2	NA NA	2	NA 2	2	2	NA	2	2
##	[10,]	2	2	NA	2	NA	2	2	NA	2	2	2	2	2
##	[11,]	1	1	1	1	1	1	1	1	1	1	NA	NA	1
##	[12,]	NA	NA	1	NA	1	1	1	1	1	1	1	NA	NA
##	[13,]	1	1	1	1	1	1	1	1	1	NA	1	1	1
##	[14,]	1	1	1	1	1	1	NA	1	1	1	NA	1	1
##	[15,]	NA	1	1	1	1	1	1	1	NA	1	1	1	NA
##	[16,]	NA	1	NA	NA	NA	NA	1	NA	1	1	1	1	1
##	[17,]	NA	1	1	1	1	NA	NA	1	1	1	1	1	1
##	[18,]	1	1	1	1	NA	1	1	NA	1	1	1	NA	NA
##	[19,]	1	1	1	NA	NA	NA	1	1	1	1	1	NA	NA
##	[20,]	1	NA	NA	NA	1	NA	1	1	NA	1	1	1	NA
##	[21,]	NA	NA	NA	1	1	NA	1	1	1	1	1	1	NA
##	[22,]	1	NA	1	1	NA	1	NA	NA	NA	NA	1	1	1
##	[23,]	1	1	1	NA	NA	1	1	1	1	NA	1	1	NA
##	[24,]	1	NA	1	1	1	1	NA	NA	1	1	1	NA	1
##	[25,]	NA	1	1	NA	NA	1	1	NA	1	NA	1	NA	NA
##	[26,]	0	0	NA	0	0	0	0	NA	0	NA	NA	0	NA
##	[27,]	0	0	0	0	0	NA	0	NA	NA	NA	0	O	NA
## ##	[28,] [29,]	NA O	0	0	NA O	0	NA O	NA O	0	NA O	O NA	0	NA NA	NA NA
##	[30,]	NA	NA	0	0	0	0	NA	0	NA	0	0	0	0
##	[31,]	0	NA	0	0	0	0	0	NA	0	0	0	NA	0
##	[32,]	0	0	0	NA	0	0	0	0	0	NA	NA	0	0
##	[33,]	NA	0	0	0	0	0	0	0	NA	NA	NA	NA	0
##	[34,]	0	0	0	0	0	0	0	0	NA	0	NA	NA	0
##	[35,]	NA	0	NA	0	0	0	0	0	NA	0	NA	0	0
##	[36,]	0	NA	0	0	0	0	0	0	0	0	NA	0	0
##	[37,]	0	NA	0	NA	NA	0	0	0	0	0	0	0	0
##	[38,]	0	0	0	NA	0	0	0	0	0	0	0	NA	0
##	[39,]	0	0	0	0	NA	0	0	NA	0	0	0	0	0
##	[40,]	0	0	0	0	0	0	0	0	NA	NA	0	0	0
##	[41,]	0	0	NA	0	0	0	NA	0	NA	NA	NA	0	0
##	[42,]	NA	NA	0	0	NA	0	NA	NA	0	0	0	0	NA
##	[43,]	NA	NA	NA	0	0	0	0	0	0	0	0	NA	0
##	[44,]	0	NA	NA	0	0	0	NA	NA	0	NA	0	0	NA
##	[45,]	NA	0	0	NA	NA	NA	NA	0	0	0	0	0	0
##	[46,]	NA	NA	0	NA	0	NA	0	0	NA	0	0	0	NA
##	[47,]	NA	O M A	0	NA	O N. A	NA	0	O N. A	0	0	0	NA	0
##	[48,]	0	NA	0	0	NA	NA	0	NA	0	0	0	0	0
##	[49,]	0	NA	0	0	0	NA	0	0	0	0	0	0	0

##	[50,]	NA	NA	NA	0 (NA	0	0	0	0	0	NA
##		[,14]			[,17]			[,20]	[,21]	[,22]	[,23]	[,24]	[,25]
##	[1,]	NA	2	2	NA	2	2	NA	2	2	2	2	2
##	[2,]	NA	NA	2	2	2	2	NA	2	2	2	2	2
##	[3,]	NA	NA	2	2	2	2	2	2	2	2	2	NA
##	[4,]	2	2	2	2	2	2	2	2	2	2	NA	2
##	[5,]	2	2	NA	2	2	NA	2	NA	NA	2	2	2
##	[6,]	2	2	NA	NA	2	NA	2	2	NA	2	NA	2
##	[7,]	2	2	2	2	NA	2	2	2	2	2	2	2
##	[8,]	2	NA	NA	2	2	2	NA	NA	2	2	2	2
##	[9,]	2	2	2	2	2	2	2	NA	2	NA	2	NA
##	[10,]	NA	2	2	NA	2	NA	NA	2	2	NA	2	2
##	[11,]	1	1	1	1	1	1	1	1	1	1	NA	1
##	[12,]	1	NA	NA	1	1	1	1	1	1	NA	1	1
##	[13,]	1	1	NA	NA	NA	1	1	1	NA	NA	1	1
##	[14,]	1	1	1	1	1	1	1	NA	1	1	1	1
##	[15,]	1	NA	1	1	NA	1	1	1	1	1	1	1
##	[16,]	1 1	1 NA	1 1	1 1	1 1	1 NA	1 1	1 1	1 N A	NA 1	1 NA	NA 1
## ##	[17,] [18,]	1	1	NA	1	1	1	1	NA	NA NA	NA	1	1
##	[19,]	1	1	1	NA	1	NA	1	NA NA	1	1	NA	1
##	[20,]	1	NA	NA	NA	NA	1	NA	1	NA	1	1	1
##	[21,]	1	1	NA	NA	NA	1	1	NA	NA	NA	1	1
##	[22,]	1	1	1	NA	1	1	1	1	1	1	NA	1
##	[23,]	NA	1	NA	NA	NA	1	NA	1	1	1	NA	1
##	[24,]	1	NA	1	NA	1	NA	1	1	NA	NA	1	NA
##	[25,]	NA	1	1	NA	NA	NA	NA	1	1	NA	1	1
##	[26,]	NA	NA	0	0	0	0	NA	NA	NA	0	0	0
##	[27,]	NA	0	0	0	NA	0	0	NA	NA	NA	0	0
##	[28,]	0	NA	0	0	NA	0	0	NA	0	NA	NA	NA
##	[29,]	0	0	0	0	0	0	0	0	0	0	0	0
##	[30,]	NA	0	0	NA	0	0	0	0	0	0	0	0
##	[31,]	0	0	NA	0	NA	0	NA	0	0	0	0	0
##	[32,]	NA	0	0	0	0	0	0	0	NA	0	0	0
##	[33,]	NA	0	0	0	0	0	0	0	0	0	0	0
##	[34,]	NA	0	NA	0	NA	NA	0	0	0	NA	NA	NA
##	[35,]	0	0	0	0	0	NA	0	NA	0	0	0	NA
##	[36,]	NA	0	0	0	0	0	NA	0	0	0	0	0
##	[37,]	0	0	0	0	0	0	NA	0	0	0	NA	0
##	[38,]	0	0	0	NA	NA	NA	0	0	NA	0	0	0
##	[39,]	NA	0	0	0	0	0	NA	0	0	NA	0	0
##	[40,]	NA	0	NA	NA	0	NA	0	0	0	NA	NA	NA
	[41,]	0	0	0	NA	0	0	NA	0	0	0	NA	0
	[42,]	0	0	NA	0	0	NA	0	0	0	0	NA	NA
	[43,]	0	NA	0	0	0	0	NA	0	NA	0	0	0
	[44,]	NA	0	0	0	NA	0	NA	0	0	0	NA	0
	[45,]	0	NA	0	NA	0	0	0	0	0	0	0	0
	[46,]	0	NA	NA	0	0	0	0	0	0	NA	NA	0
	[47,]	0	0	0	0	0	0	0	0	0	0	NA	0
##	[48,]	NA	0	0	0	0	0	0	0	0	0	0	NA
##	[49,]	0	0	0	0	NA	0	0	0	NA	NA	0	NA
##	[50,]	NA Coci	NA L 071	0	0	0	NA L 243	AN Local	0	0	0	0	0
##	[4]	[,26]		[,28]		[,30]		[,32]		[,34]		[,36]	[,37]
##	[1,]	2	2	2	NA	2	2	2	2	2	2	2	2

	го л	0	0	0	0	0	0	0	37.4	0	0	0	0
##	[2,]	2	2	2	2	2	2	2 2	NA	2	2	2	2
##	[3,]	NA 2	2	NA	2	2	NA	2	2 2	2	NA	2 2	NA
##	[4,]		2 2	NA	2	2	NA	2	2	2	2		2
##	[5,]	NA		2 2	2	2	2	2			NA	NA 2	NA
##	[6,]	2	2				2		NA	2	2		2
##	[7,]	2	2	NA	2	2	2	NA	2	NA	2	2	2
##	[8,]	2	2	2	2	NA	NA	NA	NA	2	2	2	2
##	[9,]	NA	NA	2	2	NA	2	2	NA	NA	2	2	NA
##	[10,]	2	2	2	2	NA	NA	2	2	2	2	NA	NA
##	[11,]	1	1	1	1	1	1	1	1	1	1	1	1
##	[12,]	1	1	1	1	NA	1	1	1	1	1	1	1
##	[13,]	1	1	NA	1	1	NA	NA	1	1	1	1	1
##	[14,]	NA	1	1	1	1	NA	1	1	NA	1	1	NA
##	[15,]	NA	NA	NA	1	1	1	1	1	1	1	1	1
##	[16,]	1	NA	1	1	NA	NA	1	1	1	1	1	1
##	[17,]	1	NA	1	1	NA	1	1	1	1	1	NA	1
##	[18,]	NA	1	1	NA	1	NA	1	1	NA	1	1	1
##	[19,]	NA	NA	1	1	1	1	1	NA	1	1	NA	NA
##	[20,]	NA	1	1	1	1	1	1	1	1	1	1	1
##	[21,]	NA	1	1	NA	1	1	NA	1	NA	NA	1	1
##	[22,]	1	1	1	NA	1	NA	NA	1	1	NA	NA	1
##	[23,]	NA	1	1	NA	1	1	NA	1	1	1	1	1
##	[24,]	1	NA	NA	1	NA	1	1	NA	1	NA	1	1
##	[25,]	NA	1	1	NA	NA	1	1	NA	1	1	1	1
##	[26,]	0	0	0	0	NA	0	NA	0	0	0	0	0
##	[27,]	0	NA	NA	0	0	0	NA	0	0	0	0	0
##	[28,]	0	NA	0	NA	0	0	NA	0	0	0	0	0
##	[29,]	NA	NA	0	0	0	NA	0	0	0	0	0	0
##	[30,]	0	NA	NA	0	NA	NA	NA	0	NA	NA	NA	0
##	[31,]	0	0	0	0	0	0	NA	NA	0	0	0	NA
##	[32,]	0	0	0	0	0	NA	0	0	0	NA	NA	0
##	[33,]	0	0	NA	0	0	0	0	0	0	0	NA	0
##	[34,]	0	0	0	NA	0	0	NA	0	0	0	NA	NA
##	[35,]	0	NA	0	NA	NA	NA	NA	NA	0	0	0	0
##	[36,]	0	0	NA	NA	0	NA	0	0	NA	0	0	0
##	[37,]	NA	0	0	0	0	0	NA	0	0	0	0	0
##	[38,]	NA	0	0	0	NA	0	0	0	0	0	0	0
	[39,]	0	0	0	0	NA	NA	0	0	NA	0	NA	NA
	[40,]	0	NA	NA	NA	0	NA	0	0	0		NA	0
	[41,]	0	0	0	NA	0	0	0	0	NA	0	0	0
	[42,]	NA	0	0	0	0	0	0	NA	NA	NA	0	0
	[43,]	0	0	NA	0	0	0	NA	0	0	0	NA	0
	[44,]	0	0	0	0	0	0	0	NA	0	0	NA	NA
	[45,]	0	0	0	0	NA	0	0	0	NA	0	0	0
	[46,]	NA	0	0	NA	0	NA	0	NA	0	NA	0	0
	[47,]	0	0	NA	0	NA	0	NA	0	0	0	NA	NA
	[48,]	0	NA	NA	0	0	NA	0	0	0	0	0	0
	[49,]	NA	NA	NA	NA	NA	NA	0	NA	0	NA	NA	NA
	[50,]	0	0	0	0	0	0	NA	0	NA	NA	0	0
##		[,38]			[,41]				[,45]		[,47]		[,49]
##	[1,]	2	2	2	2	2	2	2	2	NA	2	2	NA
##	[2,]	2	NA	2	NA	2	NA	2	NA	2	2	2	2
##	[3,]	2	2	NA	2	2	2	2	2	2	2	2	2
##	[4,]	2	2	NA	2	NA	2	2	NA	NA	2	2	NA

##	[5,]	2	NA	2	2	NA	2	2	2	NA	2	NA	2
##	[6,]	NA	NA	2	2	2	2	2	NA	2	NA	2	NA
##	[7,]	2	NA	2	2	NA	NA	2	2	NA	2	NA	NA
##	[8,]	2	2	2	NA	2	NA	2	2	NA	NA	2	NA
##	[9,]	NA	2	2	NA	NA	NA	NA	2	NA	2	2	2
##	[10,]	NA	2	NA	NA	2	NA	2	NA	NA	2	NA	NA
##	[11,]	1	1	1	1	1	NA	1	1	1	1	1	1
##	[12,]	1	1	1	NA	1	1	1	1	1	1	1	1
##	[13,]	1	1	1	1	1	1	NA	1	1	NA	1	1
##	[14,]	1	NA	NA	NA	1	1	1	NA	1	1	NA	NA
##	[15,]	NA	1	NA	1	1	1	1	NA	1	1	NA	1
##	[16,]	NA	1	1	NA	1	1	1	NA	1	1	NA	1
##	[17,]	1	1	NA	1	1	1	1	1	NA	NA	NA	1
##	[18,]	1	1	1	NA	1	1	NA	1	1	1	1	1
##	[19,]	1	1	1	1	1	1	1	1	1	1	NA	1
##	[20,]	1	NA	1	1	1	1	NA	NA	NA	1	1	1
##	[21,]	1	1	1	1	1	1	1	NA	1	1	1	1
##	[22,]	NA	NA	1	1	NA	1	1	1	NA	NA	1	1
##	[23,]	1	NA	1	NA	1	NA	1	NA	1	1	NA	NA
##	[24,]	1	1	1	1	NA	NA	NA	1	NA	1	1	1
##	[25,]	1	1	NA	1	NA	NA	1	NA	NA	1	NA	1
##	[26,]	0	0	0	0	0	NA	NA	0	0	0	0	0
##	[27,]	0	0	NA	0	0	0	0	0	0	0	0	NA
##	[28,]	0	0	NA	NA	0	0	0	NA	NA	0	0	0
##	[29,]	0	0	0	0	NA	0	0	NA	0	0	NA	NA
##	[30,]	0	0	0	NA	NA	NA	0	NA	NA	0	NA	NA
##	[31,]	NA	0	0	0	0	0	0	NA	0	0	0	0
##	[32,]	NA	0	0	0	0	0	NA	0	0	0	NA	0
##	[33,]	0	0	0	0	0	NA	0	NA	0	0	0	NA
##	[34,]	NA	0	NA	0	0	0	0	0	NA	0	0	NA
##	[35,]	0	0	NA	0	0	0	0	0	0	NA	0	NA
##	[36,]	O N A	0	0	NA NA	0	NA O	0	0	0	0	0	NA
## ##	[37,] [38,]	NA O	O NA	NA O	N A O	0	0	0	NA	0	0	0	O NA
##	[39,]	0	NA NA	0	0	0	0	NA	0	0	0	0	NA
##	[40,]	0	0	0	NA	0	0	NA	0	0	0	NA	0
	[41,]	NA	0	0	NA	0	NA	0	0	0	0	0	0
	[42,]	NA	0	0	0	NA	NA	0	NA	0	0	0	0
	[43,]	0	0	NA	0	0	NA	0	NA	0	0	0	NA
	[44,]	NA	NA	NA	0	0	0	NA	0	0	0	0	0
	[45,]	0	NA	0	NA	0	0	0	NA	NA	0	NA	0
	[46,]	0	0	NA	0	NA	0	0	0	0	NA	0	0
	[47,]	0	0	0	0	0	0	0	0	NA	NA	NA	NA
	[48,]	NA	0	NA	0	NA	0	NA	0	0	0	NA	NA
##	[49,]	NA	0	0	0	0	NA	0	0	0	NA	NA	0
##	[50,]	0	NA	0	0	0	0	NA	0	0	0	0	NA
##		[,50]											
##	[1,]	2											
##	[2,]	NA											
##	[3,]	2											
##	[4,]	2											
##	[5,]	NA											
##	[6,]	2											
##	[7,]	2											

```
## [8,]
              2
  [9,]
##
             NA
## [10,]
             NA
## [11,]
              1
## [12,]
              1
## [13,]
              1
## [14,]
              1
## [15,]
             NA
## [16,]
              1
## [17,]
             NA
## [18,]
             NA
## [19,]
             NA
## [20,]
              1
## [21,]
## [22,]
              1
## [23,]
              1
## [24,]
              1
## [25,]
              1
## [26,]
              0
## [27,]
             NA
## [28,]
              0
## [29,]
              0
## [30,]
             NA
## [31,]
              0
## [32,]
              0
## [33,]
              0
## [34,]
              0
## [35,]
              0
## [36,]
              0
## [37,]
              0
## [38,]
             NA
## [39,]
             NA
## [40,]
              0
## [41,]
              0
## [42,]
              0
## [43,]
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## [44,]
             NA
## [45,]
              0
## [46,]
             NA
## [47,]
             NA
## [48,]
              0
## [49,]
              0
## [50,]
              0
```

R # R was unchanged

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
##
##
    [1,]
             2
                  NA
                        2
                              2
                                   NA
                                        NA
                                               2
                                                     2
                                                          2
                                                                        2
                                                                               2
                                                                                      2
                                                                NA
    [2,]
##
             0
                   0
                       NA
                                    0
                                         0
                                                    NA
                                                          0
                                                                NA
                                                                       NA
                                                                               0
                                                                                    NA
    [3,]
##
             0
                   0
                         0
                              0
                                    0
                                               0
                                                         NA
                                                                        0
                                                                               0
                                        NA
                                                    NA
                                                                NA
                                                                                    NA
##
    [4,]
            NA
                   0
                         0
                             NA
                                    0
                                        NA
                                              NA
                                                     0
                                                          NA
                                                                 0
                                                                        0
                                                                              NA
                                                                                    NA
##
    [5,]
             2
                         2
                              2
                                         2
                                              NA
                                                     2
                                                          2
                                                                 2
                                                                       NA
                                                                               2
                                                                                     2
                  NA
                                   NA
##
    [6,]
             0
                   0
                         0
                              0
                                    0
                                          0
                                               0
                                                     0
                                                          0
                                                                NA
                                                                        0
                                                                              NA
                                                                                    NA
                                                     0
##
    [7,]
                         0
                              0
                                    0
                                          0
                                              NA
                                                                 0
                                                                        0
                                                                               0
                                                                                      0
            NA
                  NA
                                                         NA
```

##	[8,]	0	NA	0	0	0	0	0	NA	0	0	0	NA	0
##	[9,]	0	0	0	NA	0	0	0	0	0	NA	NA	0	0
##	[10,]	2	2	NA	2	NA	2	2	NA	2	2	2	2	2
##	[11,]	1	1	1	1	1	1	NA	1	1	1	NA	1	1
##	[12,]	NA	2	2	NA	2	NA	2	NA	2	2	2	2	2
##	[13,]	2	NA	2	NA	NA	2	2	NA	2	NA	2	NA	2
##	[14,]	1	1	1	1	1	1	1	1	1	1	NA	NA	1
##	[15,]	NA	0	0	0	0	0	0	0	NA	NA	NA	NA	0
##	[16,]	NA	1	NA	NA	NA	NA	1	NA	1	1	1	1	1
##	[17,]	2	2	2	2	2	2	NA	2	NA	2	2	2	2
##	[18,]	NA	1	1	1	1	1	1	1	NA	1	1	1	NA
##	[19,]	0	0	0	0	0	0	0	0	NA	0	NA	NA	0
##	[20,]	NA	2	NA	2	2	2	2	2	NA	2	2	NA	2
##	[21,]	NA	0	NA	0	0	0	0	0	NA	0	NA	0	0
##	[22,]	0	NA	0	0	0	0	0	0	0	0	NA	0	0
##	[23,]	2	2	2	NA	2	NA	2	2	2	2	NA	2	2
##	[24,]	NA	1	1	NA	NA	1	1	NA	1	NA	1	NA	NA
##	[25,]	1	1	1	1	1	1	1	1	1	NA	1	1	1
##	[26,]	2	NA	2	NA	2	2	NA	NA	2	2	2	NA	2
##	[27,]	0	NA	0	NA	NA	0	0	0	0	0	0	0	0
##	[28,]	0	0	0	NA	0	0	0	0	0	0	0	NA	0
##	[29,]	0	0	0	0	NA	0	0	NA	0	0	0	0	0
##	[30,]	0	0	0	0	0	0	0	0	NA	NA	0	0	0
##	[31,]	0	0	NA	0	0	0	NA	0	NA	NA	NA	0	0
##	[32,]	NA	NA	0	0	NA	0	NA	NA	0	0	0	0	NA
##	[33,]	NA	NA	1	NA	1	1	1	1	1	1	1	NA	NA
##	[34,]	NA	NA	NA	0	0	0	0	0	0	0	0	NA	0
##	[35,]	0	NA	NA	0	0	0	NA	NA	0	NA	0	0	NA
##	[36,]	NA 1	1	1	1	1	NA	NA 1	1	1	1	1	1 N A	1 N A
##	[37,]	1	1	1 2	NA	NA	NA 2	1	1	1	1	1	NA	NA
##	[38,]	2	2		NA	2		2	2	NA	NA	2	2	2
##	[39,] [40,]	NA NA	O NA	0	NA NA	NA O	NA NA	NA O	0	O NA	0 0	0 0	0 0	O N: A
## ##	[41,]	NA NA	0	0	NA	0	NA NA	0	0	0	0	0	NA	NA O
##	[42,]	1	1	1	NA	NA	1	1	1	1	NA	1	1	NA
##	[43,]	0	NA	0	0	NA	NA	0	ΝA	0	0	0	0	0
##	[44,]	1	1	1	1	NA	1	1	NA	1	1	1	NA	NA
	[45,]	1	ΝA	1	1	1	1	NA	NA	1	1	1	NA	1
	[46,]	0	NA	0	0	0	NA	0	0	0	0	0	0	0
	[47,]	1	NA	NA	NA	1	NA	1	1	NA	1	1	1	NA
	[48,]	1	NA	1	1	NA	1	NA	NA	NA	NA	1	1	1
##	[49,]	NA	NA	NA	1	1	NA	1	1	1	1	1	1	NA
##	[50,]	NA	NA	NA	0	0	0	NA	0	0	0	0	0	NA
##	[00,]	[,14]		[,1		,17] [[,19]	[,20]		[,22]		[,24]	[,25]
##	[1,]	NA	NA	-,	2	2	2	2	NA		2			2
##	[2,]	NA	NA		0	0	0	0	NA		NA			0
##	[3,]	NA	0		0	0	NA	0	0		NA			0
##	[4,]	0	NA		0	0	NA	0	0	NA	0			NA
##	[5,]	NA	NA		2	2	2	2	2		2			NA
##	[6,]	0	0		0	0	0	0	0	0	0	0	0	0
##	[7,]	NA	0		0	NA	0	0	0	0	0	0	0	0
##	[8,]	0	0		NA	0	NA	0	NA	0	0	0	0	0
##	[9,]	NA	0		0	0	0	0	0	0	NA	0	0	0
##	[10,]	NA	2		2	NA	2	NA	NA	2	2	NA	2	2

##	Γ11]	1	1	1	1	1	1	1	NA	1	1	- 1	1
##	[11,] [12,]	1 2	NA	1 NA	2	1 2	2	1 NA	NA NA	1 2	1 2	1 2	1 2
##	[13,]	2	2	2	2	NA	2	2	2	2	2	2	2
##	[14,]	1	1	1	1	1	1	1	1	1	1	NA	1
##	[15,]	NA	0	0	0	0	0	0	0	0	0	0	0
##	[16,]	1	1	1	1	1	1	1	1	1	NA	1	NA
##	[17,]	2	2	NA	2	2	NA	2	NA	NA	2	2	2
##	[18,]	1	NA	1	1	NA	1	1	1	1	1	1	1
##	[19,]	NA	0	NA	0	NA	NA	0	0	0	NA	NA	NA
##	[20,]	2	2	NA	NA	2	NA	2	2	NA	2	NA	2
##	[21,]	0	0	0	0	0	NA	0	NA	0	0	0	NA
##	[22,]	NA	0	0	0	0	0	NA	0	0	0	0	0
##	[23,]	2	2	2	2	2	2	2	NA	2	NA	2	NA
##	[24,]	NA	1	1	NA	NA	NA	NA	1	1	NA	1	1
##	[25,]	1	1	NA	NA	NA	1	1	1	NA	NA	1	1
##	[26,]	2	2	2	2	2	2	2	2	2	2	NA	2
##	[27,]	0	0	0	0	0	0	NA	0	0	0	NA	0
##	[28,]	0	0	0	NA	NA	NA	0	0	NA	0	0	0
##	[29,]	NA	0	0	0	0	0	NA	0	0	NA	0	0
##	[30,]	NA	0	NA	NA	0	NA	0	0	0	NA	NA	NA
##	[31,]	0	0	0	NA	0	0	NA	0	0	0	NA	0
##	[32,]	0	0	NA	0	0	NA	0	0	0	0	NA	NA
##	[33,]	1	NA	NA	1	1	1	1	1	1	NA	1	1
##	[34,]	0	NA	0	0	0	0	NA	0	NA	0	0	0
## ##	[35,] [36,]	NA 1	O NA	0	0 1	NA 1	O NA	NA 1	0	O NA	0	NA NA	0 1
##	[37,]	1	1	1	NA	1	NA NA	1	NA	1	1	NA NA	1
##	[38,]	NA	2	2	NA	2	2	NA	2	2	2	2	2
##	[39,]	0	NA	0	NA	0	0	0	0	0	0	0	0
##	[40,]	0	NA	NA	0	0	0	0	0	0	NA	NA	0
##	[41,]	0	0	0	0	0	0	0	0	0	0	NA	0
##	[42,]	NA	1	NA	NA	NA	1	NA	1	1	1	NA	1
##	[43,]	NA	0	0	0	0	0	0	0	0	0	0	NA
##	[44,]	1	1	NA	1	1	1	1	NA	NA	NA	1	1
##	[45,]	1	NA	1	NA	1	NA	1	1	NA	NA	1	NA
##	[46,]	0	0	0	0	NA	0	0	0	NA	NA	0	NA
##	[47,]	1	NA	NA	NA	NA	1	NA	1	NA	1	1	1
	[48,]	1	1	1	NA	1	1	1	1	1	1	NA	1
	[49,]	1	1	NA	NA	NA			NA	NA	NA	1	1
	[50,]	NA	NA	0	0	0		NA		0	0	0	0
##										[,34]			
##	[1,]	2	2	2	2	2		2		2	2	2	2
##	[2,]	0	0	0	0	NA	0	NA	0	0	0	0	0
##	[3,]	0	NA	NA	0	0	0	NA	0	0	0	0	0
##	[4,] [5,]	0	NA	0	NA	0	0	NA 2	0	0	0	0	O N A
## ##	[6,]	NA NA	2 NA	NA O	2	2	NA NA		2	2	NA O	2	NA O
##	[7,]	NA O	NA NA	NA	0	NA	NA NA	NA	0	NA	NA	NA	0
##	[8,]	0	0	0	0	0	0	NA	NA	0	0	0	NA
##	[9,]	0	0	0	0	0	NA	0	0	0	NA	NA	0
##	[10,]	2	2	2	2	NA	NA	2	2	2	2	NA	NA
	[11,]	NA	1	1	1	1	NA	1	1	NA	1	1	NA
	[12,]	2	2	2	2	NA	NA	NA	NA	2	2	2	2
	[13,]	2	2	ΝĀ	2	2	2		2	NA	2	2	2
	• -												

##	[14,]	1	1	1	1	1	1	1	1	1	1	1	1
##	[15,]	0	0	NA	0	0	0	0	0	0	0	NA	0
##	[16,]	1	NA	1	1	NA	NA	1	1	1	1	1	1
##	[17,]	NA	2	2	2	2	2	2	2	2	NA	NA	NA
##	[18,]	NA	NA	NA	1	1	1	1	1	1	1	1	1
##	[19,]	0	0	0	NA	0	0	NA	0	0	0	NA	NA
##	[20,]	2	2	2	2	2	2	2	NA	2	2	2	2
##	[21,]	0	NA	0	NA	NA	NA	NA	NA	0	0	0	0
##	[22,]	0	0	NA	NA	0	NA	0	0	NA	0	0	0
##	[23,]	NA	NA	2	2	NA	2	2	NA	NA	2	2	NA
##	[24,]	NA	1	1	NA	NA	1	1	NA	1	1	1	1
##	[25,]	1	1	NA	1	1	NA	NA	1	1	1	1	1
##	[26,]	2	2	NA	2	2	NA	2	2	2	2	2	2
##	[27,]	NA	0	0	0	0	0	NA	0	0	0	0	0
##	[28,]	NA	0	0	0	NA	0	0	0	0	0	0	0
##	[29,]	0	0	0	0	NA	NA	0	0	NA	0	NA	NA
##	[30,]	0	NA	NA	NA	0	NA	0	0	0	0	NA	0
##	[31,]	0	0	0	NA	0	0	0	0	NA	0	0	0
##	[32,]	NA	0	0	0	0	0	0	NA	NA	NA	0	0
##	[33,]	1	1	1	1	NA	1	1	1	1	1	1	1
##	[34,]	0	0	NA	0	0	0	NA	0	0	0	NA	0
##	[35,]	0	0	0	0	0	0	0	NA	0	0	NA	NA
##	[36,]	1	NA	1	1	NA	1	1	1	1	1	NA	1
##	[37,]	NA	NA	1	1 NA	1	1	1	NA	1	1	NA	NA
## ##	[38,] [39,]	2	2	2	NA O	2 NA	2	2	2	2 NA	2	2	2
##	[40,]	NA	0	0	NA	0	NA	0	NA	0	NA	0	0
##	[41,]	0	0	NA	0	NA	0	NA	0	0	0	NA	NA
##	[42,]	NA	1	1	NA	1	1	NA	1	1	1	1	1
##	[43,]	0	NA	NA	0	0	NA	0	0	0	0	0	0
##	[44,]	NA	1	1	NA	1	NA	1	1	NA	1	1	1
##	[45,]	1	NA	NA	1	NA	1	1	NA	1	NA	1	1
##	[46,]	NA	NA	NA	NA	NA	NA	0	NA	0	NA	NA	NA
##	[47,]	NA	1	1	1	1	1	1	1	1	1	1	1
##	[48,]	1	1	1	NA	1	NA	NA	1	1	NA	NA	1
##	[49,]	NA	1	1	NA	1	1	NA	1	NA	NA	1	1
##	[50,]	0	0	0	0	0	0	NA	0	NA	NA	0	0
##										[,46]			
##	[1,]	2	NA	2	NA	2	NA	2	NA	2	2	2	2
##	[2,]	0	0	0	0	0	NA	NA	0	0	0	0	0
##	[3,]	0	0	NA	0	0	0	0	0	0	0	0	NA
## ##	[4,] [5,]	0 2	0 2	NA NA	NA 2	0 2	0 2	0 2	NA 2	NA 2	0 2	0 2	0 2
##	[6,]	0	0	NA O	0	NA	0	0	NA	0	0	NA	NA
##	[7,]	0	0	0	NA	NA	NA	0	NA	NA	0	NA	NA
##	[8,]	NA	0	0	0	0	0	0	NA	0	0	0	0
##	[9,]	NA	0	0	0	0	0	NA	0	0	0	NA	0
##	[10,]	NA	2	NA	NA	2	NA	2	NA	NA	2	NA	NA
##	[11,]	1	NA	NA	NA	1	1	1	NA	1	1	NA	NA
##	[12,]	2	2	2	NA	2	NA	2	2	NA	NA	2	NA
##	[13,]	2	NA	2	2	NA	NA	2	2	NA	2	NA	NA
##	[14,]	1	1	1	1	1	NA	1	1	1	1	1	1
##	[15,]	0	0	0	0	0	NA	0	NA	0	0	0	NA
##	[16,]	NA	1	1	NA	1	1	1	NA	1	1	NA	1

##	[17,]	2	NA	2	2	NA	2	2	2	NA	2	NA	2
##	[18,]	NA	1	NA	1	1	1	1	NA	1	1	NA	1
##	[19,]	NA	0	NA	0	0	0	0	0	NA	0	0	NA
##	[20,]	NA	NA	2	2	2	2	2	NA	2	NA	2	NA
##	[21,]	0	0	NA	0	0	0	0	0	0	NA	0	NA
##	[22,]	0	0	0	NA	0	NA	0	0	0	0	0	NA
##	[23,]	NA	2	2	NA	NA	NA	NA	2	NA	2	2	2
##	[24,]	1	1	NA	1	NA	NA	1	NA	NA	1	NA	1
##	[25,]	1	1	1	1	1	1	NA	1	1	NA	1	1
##	[26,]	2	2	NA	2	NA	2	2	NA	NA	2	2	NA
##	[27,]	NA	0	NA	NA	0	0	0	0	0	0	0	0
## ##	[28,] [29,]	0	NA NA	0 0	0 0	0 0	0	O NA	NA O	0	0	0 0	NA NA
##	[30,]	0	0	0	NA	0	0	NA	0	0	0	NA	0
##	[31,]	NA	0	0	NA	0	NA	0	0	0	0	0	0
##	[32,]	NA	0	0	0	NA	NA	0	NA	0	0	0	0
##	[33,]	1	1	1	NA	1	1	1	1	1	1	1	1
##	[34,]	0	0	NA	0	0	NA	0	NA	0	0	0	NA
##	[35,]	NA	NA	NA	0	0	0	NA	0	0	0	0	0
##	[36,]	1	1	NA	1	1	1	1	1	NA	NA	NA	1
##	[37,]	1	1	1	1	1	1	1	1	1	1	NA	1
##	[38,]	2	2	2	2	2	2	2	2	NA	2	2	NA
##	[39,]	0	NA	0	NA	0	0	0	NA	NA	0	NA	0
##	[40,]	0	0	NA	0	NA	0	0	0	0	NA	0	0
##	[41,]	0	0	0	0	0	0	0	0	NA	NA	NA	NA
##	[42,]	1	NA	1	NA	1	NA	1	NA	1	1	NA	NA
##	[43,]	NA	0	NA	0	NA	0	NA	0	0	0	NA	NA
##	[44,]	1	1	1	NA 1	1 NA	1 NA	NA NA	1	1 N A	1 1	1 1	1
##	[45,] [46,]	1 NA	1 0	1 0	1 0	NA O	NA NA	NA O	1 0	NA O	NA	NA	1 0
##	[47,]	1	NA	1	1	1	1	NA	NA	NA	1	1	1
##	[48,]	NA	NA	1	1	ΝA	1	1	1	NA	NA	1	1
##	[49,]	1	1	1	1	1	1	1	NA	1	1	1	1
##	[50,]	0	NA	0	0	0	0	NA	0	0	0	0	NA
##		[,50]											
##	[1,]	NA											
##	[2,]	0											
##	[3,]	NA											
##	[4,]	0											
##	[5,]	2											
##	[6,]	0											
##	[7,]	NA											
##	[8,]	0											
## ##	[9,] [10,]	O NA											
	[11,]	1											
	[12,]	2											
	[13,]	2											
	[14,]	1											
	[15,]	0											
	[16,]	1											
	[17,]	NA											
	[18,]	NA											
##	[19,]	0											

```
## [20,]
              2
## [21,]
              0
## [22,]
              0
## [23,]
             NA
## [24,]
              1
## [25,]
              1
## [26,]
              2
## [27,]
              0
## [28,]
             NA
## [29,]
             NA
## [30,]
              0
## [31,]
              0
## [32,]
              0
## [33,]
              1
## [34,]
              0
## [35,]
             NA
## [36,]
             NA
## [37,]
             NA
## [38,]
              2
## [39,]
              0
## [40,]
             NA
## [41,]
             NA
## [42,]
              1
## [43.]
              0
## [44,]
             NA
## [45,]
              1
## [46,]
              0
## [47,]
              1
## [48,]
              1
## [49,]
              1
## [50,]
R = R[order(rowSums(R, na.rm = TRUE), decreasing = TRUE),] # assigning
rowSums(R, na.rm = TRUE)
```

• We will now learn the apply function. This is a handy function that saves writing for loops which should be eschewed in R. Use the apply function to compute a vector whose entries are the standard deviation of each row. Use the apply function to compute a vector whose entries are the standard deviation of each column. Be careful about the NA's! This should be one line.

0 0 0 0

0 0 0 0 0 0

[1] 82 74 74 74 70 70 68 66 62 58 46 40 39 37 37 35 35 35 34 33 33 32 31 31 27

0 0 0 0 0 0 0 0 0

[26]

[1] 0.83219007599 0.78491525276 0.79301947772 0.75602419316 0.77459666924

```
## [6] 0.79599839534 0.78629127444 0.77390598995 0.78000215471 0.78857386432
## [11] 0.78532422798 0.80950789391 0.88006238638 0.75067174219 0.79282496717
## [16] 0.79831171061 0.81704218512 0.84091786587 0.78365433331 0.75996059566
## [21] 0.77755282397 0.82182530102 0.83591400764 0.81867681600 0.78532422798
## [26] 0.82227511432 0.83190353531 0.78000215471 0.83190353531 0.79884051447
## [31] 0.78288136126 0.80833723835 0.75337080350 0.79471941424 0.79301947772
## [36] 0.79705339699 0.74530297810 0.78000215471 0.75833704583 0.79042848102
## [41] 0.77390598995 0.75053323860 0.74238558959 0.81982893820 0.80229555709
## [46] 0.66713998349 0.78863883972 0.82060166754 0.70186240634 0.76477052086
```

```
\# apply(R, MARGIN = c(1,2), sd, na.rm = TRUE) \# all NAs
```

• Use the apply function to compute a vector whose entries are the count of entries that are 1 or 2 in each column. This should be one line.

```
?apply
vec = apply(R > 0, MARGIN = 2, sum, na.rm = TRUE)
vec
```

```
## [1] 17 16 20 14 15 17 18 16 19 18 21 16 17 19 17 16 14 18 18 18 18 17 16 18 21 ## [26] 14 19 19 17 16 19 18 20 20 20 19 19 17 18 16 18 16 20 14 13 20 15 17 17
```

• Use the split function to create a list whose keys are the column number and values are the vector of the columns. Look at the last example in the documentation ?split.

```
?split
split(R, col(R))
```

```
## $'1'
##
    [1]
               2
                   2
                      2 NA
                            2 NA
                                   2
                                      2
                                         1 NA
                                               1
                                                  1 NA NA NA
                                                               1
                                                                  1
                                                                    1 NA
##
   [26]
                  O NA
                                  O NA
                                         0
                                            0
                                               0
                                                  0
                                                      0
                                                         O NA NA
                                                                  O NA NA NA
                            O NA
## $'2'
##
    [1]
         2 NA NA NA
                      2 2 NA
                               2
                                  2
                                      2
                                        1 NA
                                               1
                                                  1
                                                     1 1 1 1 NA NA NA
                               0
                                  0
                                     O NA NA
                                                         O NA NA NA
   [26]
               0
                  O NA NA
                            0
                                               0
                                                  0
                                                      0
                                                                    O NA O NA NA NA
##
## $'3'
         2
            2
               2
                   2
                      2 NA
                            2
                               2
                                  2 NA
                                         1
                                            1
                                               1
                                                  1
                                                      1 NA
                                                            1
                                                               1
                                                                  1 NA NA
                                                                            1
                                                                               1
##
  [26] NA
               0
                         0
                            0
                               0
                                  O NA
                                         0
                                            0
                                               0
                                                  0
                                                      O NA
                                                            O NA NA
##
## $'4'
    [1] NA
            2
               2 NA
                      2
                         2 NA NA NA
                                      2
                                         1 NA
                                               1
                                                  1
                                                      1 NA
                                                            1
                                                               1 NA NA
                                                                        1
                                                                           1 NA
##
   [26]
                         O NA
                                  0
                                      0
                                         O NA NA
                                                            0
                                                               O O NA NA NA
##
## $'5'
##
    [1]
         2 NA NA
                  2
                      2
                         2 NA
                               2
                                  2 NA
                                                     1 NA
                                                           1 NA NA
                                         1
                                            1
                                               1
                                                  1
                                                                    1
                                                                         1 NA NA
                                  0
                                         O NA
                                               O NA
                                                         O NA
                               0
                                      0
                                                      0
                                                                  O NA
##
## $'6'
   [1]
         2 NA
               2
                   2
                      2
                         2
                            2 NA NA
                                      2
                                                      1 NA NA
                                                               1 NA NA NA 1
                                         1
                                            1
                                               1
                                                  1
                                  0
                                      0
                                         0
                                            0
                                               0
                                                  0
                                                      0
                                                         0
  [26]
         O NA NA
                            0
                               0
                                                               0
                                                                  O NA NA NA NA
##
```

```
## $'7'
## [26] O O NA O NA O O O O O O O O O NA NA O NA NA O O O NA
##
## $'8'
## [26] NA NA O O O NA O O O O O O NA O O NA O O NA O O NA O O
## $'9'
##
## $'10'
## [1] NA NA 2 2 2 2 NA 2 2 2 1 1 NA 1 1 1 1 1 1 1 NA NA 1 NA
##
## $'11'
 [1] 2 2 NA 2 2 2 2 2 NA 2 NA 1 1 NA 1 1 1 1 1 1 1 1 1 1 1
## $'12'
## [1] 2 2 2 NA 2 NA NA 2 2 2 NA NA 1 1 1 1 NA NA 1 1 1 1 NA NA
## [26] O O NA NA O NA O NA NA O O O NA O O O NA O O O NA O O
## $'13'
## [26] NA NA NA NA O O O O O O O O O O NA O NA O NA O O O NA
## $'14'
## [26] NA NA O O NA O NA NA NA O NA O O NA NA O O O NA O O NA O NA
##
## $'15'
## $'16'
## [26] O O O O NA O O NA O O O O NA O NA O O O NA O O O
##
## $'17'
## [1] NA 2 2 2 2 NA 2 2 2 NA 1 1 NA 1 1 1 1 NA NA NA NA NA NA NA NA
##
## $'18'
## [26] O NA NA O O NA O O NA O O O NA O O O NA O O O NA O
##
## $'19'
##
## $'20'
## [1] NA NA 2 2 2 2 2 NA 2 NA 1 1 1 1 1 1 1 1 1 NA 1 1 NA
```

```
##
## $'21'
## $'22'
## [1] 2 2 2 2 NA NA 2 2 2 2 1 1 NA 1 1 1 NA NA 1 NA NA 1 1 NA 1
##
## $'23'
## [1] 2 2 2 2 2 2 2 2 2 NA NA 1 NA NA 1 1 NA 1 1 NA 1 1 NA 1 1 NA NA
##
## $'24'
## [26] O O NA O O O O O NA O O NA O O NA NA NA O NA O NA NA O O
##
## $'25'
## [1] 2 2 NA 2 2 2 2 2 NA 2 1 1 1 1 1 NA 1 1 1 1 1 1 1 NA 1
## $'26'
## [26] O O O NA O O O O O O NA NA O O O NA O O NA O O NA O
## $'27'
##
## $'28'
## [1] 2 2 NA NA 2 2 NA 2 2 2 1 1 NA 1 NA 1 1 1 1 1 1 1 1 NA 1
## [26] O NA O O NA NA NA N
##
## $'29'
## [1] NA 2 2 2 2 2 2 2 2 2 1 1 1 1 1 1 NA 1 1 NA NA NA NA NA NA
## [26] O O NA O O O O O NA NA NA O O O NA NA O O O NA O O NA O
##
## $'30'
## [1] 2 2 2 2 2 2 2 NA NA NA 1 NA 1 1 1 NA NA 1 1 1 1 1 1 NA NA
##
## $'31'
##
## $'32'
## [1] 2 2 2 2 2 2 NA NA 2 2 1 1 NA 1 1 1 1 1 1 1 NA NA NA 1 1
##
## $'33'
## [1] 2 NA 2 2 2 NA 2 NA NA 2 1 1 1 1 1 1 1 NA 1 1 1 1 NA NA
##
```

```
## $'34'
## [1] 2 2 2 2 2 2 NA 2 NA 2 1 1 1 NA 1 1 NA 1 1 NA 1 1 1 1
## [26] O O O O NA O O O O NA O O NA O NA NA O O NA O O O NA
## $'35'
## [26] O O O NA O NA O O O O O O O NA O O NA O O NA NA
## $'36'
## [26] O O O O NA O NA NA NA O O O O NA NA O O NA NA O O NA O NA O
##
## $'37'
## [1] 2 2 NA 2 NA 2 2 2 NA NA 1 1 1 NA 1 1 1 NA 1 1 1 1 1 1
## [26] O O O O NA O O NA O O O NA O O O NA O O NA O NA O NA O
##
## $'38'
## [1] 2 2 2 2 2 NA 2 2 NA NA 1 1 1 1 NA NA 1 1 1 1 1 NA 1 1 1
## [26] O O O O NA NA O NA O O NA O O NA NA O NA O O NA NA O
## $'39'
## [26] O O O O O O O O O O O NA NA O O O NA NA O O O NA
## $'40'
## [26] O NA NA O O O O O NA NA O NA O O O O NA NA O NA O NA
## $'41'
##
## $'42'
## [26] O O O NA NA O O O O O O O O O O NA O O NA O NA O O
## $'43'
## [1] 2 NA 2 2 2 2 NA NA NA NA 1 1 1 1 1 1 1 1 1 1 NA NA NA
##
## $'44'
## [26] NA O O O O NA O O O O O NA NA O O O NA O O NA O NA
##
## $'45'
##
## $'46'
## [26] O O NA O NA O O O NA O O O O O O O O NA O NA O O
##
## $'47'
## [1] 2 2 2 2 2 NA 2 NA 2 2 1 1 NA 1 1 1 NA 1 1 1 NA 1 1 1
```

```
## [26] O O O O O O O O NA O O O O O O O O NA NA O NA O
##
## $'48'
   [1]
        2
          2
                2 NA
                     2 NA
                           2
                             2 NA
                                   1
                                        1 NA NA NA NA
                                                     1 NA 1 1 1 NA 1 NA
                                     1
##
             O NA NA
                     O NA
                           0
                             0
                                0
                                   0
                                      0
                                        O O NA O
                                                   0
                                                      0
                                                        O NA O NA NA NA O
##
## $'49'
##
   [1] NA 2
             2 NA 2 NA NA NA 2 NA 1 1 1 NA
                                             1
                                                1
                                                   1 1
                                                         1
       O NA O NA NA O O NA NA NA NA
                                     O NA NA
                                              0
                                                   O NA
                                                         0
                                                              O NA NA
##
## $'50'
   [1]
##
        2 NA
             2
                2 NA
                     2
                        2
                           2 NA NA
                                  1
                                     1 1 1 NA
                                                1 NA NA NA
                                                           1 1 1
                                                           O NA NA
                O NA
                        0
                          0
                             0
                                0
                                   0
                                      O NA NA
                                              0
                                                0
                                                      O NA
       O NA
                     0
                                                   0
```

• In one statement, use the lapply function to create a list whose keys are the column number and values are themselves a list with keys: "min" whose value is the minimum of the column, "max" whose value is the maximum of the column, "pct_missing" is the proportion of missingness in the column and "first_NA" whose value is the row number of the first time the NA appears.

```
?lapply
?split
lapply(split(R, col(R)), function(X) list(min = min(X, na.rm = TRUE), max = max(X, na.rm = TRUE), pct_m
## $'1'
## $'1'$min
## [1] 0
##
## $'1'$max
## [1] 2
##
## $'1'$pct_missing
## [1] 0.36
## $'1'$first_NA
## [1] 6
##
##
## $'2'
## $'2'$min
## [1] 0
##
## $'2'$max
## [1] 2
## $'2'$pct_missing
## [1] 0.4
##
## $'2'$first_NA
## [1] 2
##
##
## $'3'
## $'3'$min
```

```
## [1] 0
##
## $'3'$max
## [1] 2
## $'3'$pct_missing
## [1] 0.22
##
## $'3'$first_NA
## [1] 6
##
##
## $'4'
## $'4'$min
## [1] 0
##
## $'4'$max
## [1] 2
## $'4'$pct_missing
## [1] 0.36
##
## $'4'$first_NA
## [1] 1
##
##
## $'5'
## $'5'$min
## [1] 0
##
## $'5'$max
## [1] 2
## $'5'$pct_missing
## [1] 0.3
## $'5'$first_NA
## [1] 2
##
##
## $'6'
## $'6'$min
## [1] 0
##
## $'6'$max
## [1] 2
## $'6'$pct_missing
## [1] 0.3
## $'6'$first_NA
## [1] 2
##
```

##

```
## $'7'
## $'7'$min
## [1] 0
##
## $'7'$max
## [1] 2
## $'7'$pct_missing
## [1] 0.28
##
## $'7'$first_NA
## [1] 3
##
## $'8'
## $'8'$min
## [1] 0
##
## $'8'$max
## [1] 2
##
## $'8'$pct_missing
## [1] 0.32
## $'8'$first_NA
## [1] 4
##
## $'9'
## $'9'$min
## [1] 0
##
## $'9'$max
## [1] 2
## $'9'$pct_missing
## [1] 0.3
##
## $'9'$first_NA
## [1] 1
##
##
## $'10'
## $'10'$min
## [1] 0
##
## $'10'$max
## [1] 2
## $'10'$pct_missing
## [1] 0.3
##
## $'10'$first_NA
## [1] 1
```

```
##
##
## $'11'
## $'11'$min
## [1] 0
##
## $'11'$max
## [1] 2
## $'11'$pct_missing
## [1] 0.22
## $'11'$first_NA
## [1] 3
##
##
## $'12'
## $'12'$min
## [1] 0
## $'12'$max
## [1] 2
##
## $'12'$pct_missing
## [1] 0.34
## $'12'$first_NA
## [1] 4
##
##
## $'13'
## $'13'$min
## [1] 0
##
## $'13'$max
## [1] 2
## $'13'$pct_missing
## [1] 0.32
##
## $'13'$first_NA
## [1] 12
##
## $'14'
## $'14'$min
## [1] 0
##
## $'14'$max
## [1] 2
##
## $'14'$pct_missing
## [1] 0.36
##
```

```
## $'14'$first_NA
## [1] 1
##
##
## $'15'
## $'15'$min
## [1] 0
##
## $'15'$max
## [1] 2
## $'15'$pct_missing
## [1] 0.28
##
## $'15'$first_NA
## [1] 2
##
##
## $'16'
## $'16'$min
## [1] 0
##
## $'16'$max
## [1] 2
##
## $'16'$pct_missing
## [1] 0.28
## $'16'$first_NA
## [1] 5
##
##
## $'17'
## $'17'$min
## [1] 0
## $'17'$max
## [1] 2
## $'17'$pct_missing
## [1] 0.32
## $'17'$first_NA
## [1] 1
##
##
## $'18'
## $'18'$min
## [1] 0
## $'18'$max
## [1] 2
##
## $'18'$pct_missing
```

```
## [1] 0.28
##
## $'18'$first_NA
## [1] 7
##
## $'19'
## $'19'$min
## [1] 0
##
## $'19'$max
## [1] 2
## $'19'$pct_missing
## [1] 0.26
##
## $'19'$first_NA
## [1] 5
##
##
## $'20'
## $'20'$min
## [1] 0
## $'20'$max
## [1] 2
##
## $'20'$pct_missing
## [1] 0.32
## $'20'$first_NA
## [1] 1
##
##
## $'21'
## $'21'$min
## [1] 0
##
## $'21'$max
## [1] 2
## $'21'$pct_missing
## [1] 0.22
##
## $'21'$first_NA
## [1] 5
##
##
## $'22'
## $'22'$min
## [1] 0
##
## $'22'$max
```

[1] 2

```
##
## $'22'$pct_missing
## [1] 0.28
##
## $'22'$first_NA
## [1] 5
##
##
## $'23'
## $'23'$min
## [1] 0
## $'23'$max
## [1] 2
##
## $'23'$pct_missing
## [1] 0.32
##
## $'23'$first_NA
## [1] 9
##
##
## $'24'
## $'24'$min
## [1] 0
## $'24'$max
## [1] 2
##
## $'24'$pct_missing
## [1] 0.32
##
## $'24'$first_NA
## [1] 4
##
##
## $'25'
## $'25'$min
## [1] 0
##
## $'25'$max
## [1] 2
## $'25'$pct_missing
## [1] 0.22
##
## $'25'$first_NA
## [1] 3
##
##
## $'26'
## $'26'$min
## [1] 0
```

##

```
## $'26'$max
## [1] 2
##
## $'26'$pct_missing
## [1] 0.34
##
## $'26'$first_NA
## [1] 3
##
##
## $'27'
## $'27'$min
## [1] 0
##
## $'27'$max
## [1] 2
##
## $'27'$pct_missing
## [1] 0.28
## $'27'$first_NA
## [1] 9
##
##
## $'28'
## $'28'$min
## [1] 0
## $'28'$max
## [1] 2
## $'28'$pct_missing
## [1] 0.3
##
## $'28'$first_NA
## [1] 3
##
##
## $'29'
## $'29'$min
## [1] 0
##
## $'29'$max
## [1] 2
## $'29'$pct_missing
## [1] 0.28
##
## $'29'$first_NA
## [1] 1
##
##
## $'30'
## $'30'$min
```

```
## [1] 0
##
## $'30'$max
## [1] 2
## $'30'$pct_missing
## [1] 0.32
##
## $'30'$first_NA
## [1] 8
##
##
## $'31'
## $'31'$min
## [1] 0
##
## $'31'$max
## [1] 2
## $'31'$pct_missing
## [1] 0.38
##
## $'31'$first_NA
## [1] 3
##
##
## $'32'
## $'32'$min
## [1] 0
## $'32'$max
## [1] 2
## $'32'$pct_missing
## [1] 0.34
## $'32'$first_NA
## [1] 7
##
##
## $'33'
## $'33'$min
## [1] 0
##
## $'33'$max
## [1] 2
## $'33'$pct_missing
## [1] 0.26
## $'33'$first_NA
## [1] 2
##
```

##

```
## $'34'
## $'34'$min
## [1] 0
##
## $'34'$max
## [1] 2
## $'34'$pct_missing
## [1] 0.24
##
## $'34'$first_NA
## [1] 7
##
## $'35'
## $'35'$min
## [1] 0
##
## $'35'$max
## [1] 2
## $'35'$pct_missing
## [1] 0.22
## $'35'$first_NA
## [1] 3
##
## $'36'
## $'36'$min
## [1] 0
##
## $'36'$max
## [1] 2
## $'36'$pct_missing
## [1] 0.3
##
## $'36'$first_NA
## [1] 5
##
##
## $'37'
## $'37'$min
## [1] 0
##
## $'37'$max
## [1] 2
## $'37'$pct_missing
## [1] 0.24
##
## $'37'$first_NA
## [1] 3
```

```
##
##
## $'38'
## $'38'$min
## [1] 0
##
## $'38'$max
## [1] 2
## $'38'$pct_missing
## [1] 0.3
## $'38'$first_NA
## [1] 6
##
##
## $'39'
## $'39'$min
## [1] 0
## $'39'$max
## [1] 2
##
## $'39'$pct_missing
## [1] 0.26
## $'39'$first_NA
## [1] 2
##
##
## $'40'
## $'40'$min
## [1] 0
##
## $'40'$max
## [1] 2
## $'40'$pct_missing
## [1] 0.32
##
## $'40'$first_NA
## [1] 3
##
## $'41'
## $'41'$min
## [1] 0
##
## $'41'$max
## [1] 2
##
## $'41'$pct_missing
## [1] 0.32
##
```

```
## $'41'$first_NA
## [1] 2
##
##
## $'42'
## $'42'$min
## [1] 0
##
## $'42'$max
## [1] 2
## $'42'$pct_missing
## [1] 0.24
##
## $'42'$first_NA
## [1] 4
##
##
## $'43'
## $'43'$min
## [1] 0
##
## $'43'$max
## [1] 2
##
## $'43'$pct_missing
## [1] 0.34
## $'43'$first_NA
## [1] 2
##
##
## $'44'
## $'44'$min
## [1] 0
## $'44'$max
## [1] 2
## $'44'$pct_missing
## [1] 0.24
## $'44'$first_NA
## [1] 9
##
##
## $'45'
## $'45'$min
## [1] 0
## $'45'$max
## [1] 2
##
## $'45'$pct_missing
```

```
## [1] 0.4
##
## $'45'$first_NA
## [1] 2
##
## $'46'
## $'46'$min
## [1] 0
##
## $'46'$max
## [1] 2
## $'46'$pct_missing
## [1] 0.34
##
## $'46'$first_NA
## [1] 1
##
##
## $'47'
## $'47'$min
## [1] 0
## $'47'$max
## [1] 2
##
## $'47'$pct_missing
## [1] 0.18
## $'47'$first_NA
## [1] 6
##
##
## $'48'
## $'48'$min
## [1] 0
##
## $'48'$max
## [1] 2
## $'48'$pct_missing
## [1] 0.36
##
## $'48'$first_NA
## [1] 5
##
##
## $'49'
## $'49'$min
## [1] 0
##
## $'49'$max
```

[1] 2

```
##
## $'49'$pct_missing
## [1] 0.42
##
## $'49'$first NA
## [1] 1
##
##
## $'50'
## $'50'$min
## [1] 0
##
## $'50'$max
## [1] 2
##
## $'50'$pct_missing
## [1] 0.3
##
## $'50'$first NA
## [1] 2
```

 Set a seed and then create a vector v consisting of a sample of 1,000 iid normal realizations with mean -10 and variance 100.

```
set.seed(1997)
?rnorm
v = rnorm(n=1000,mean=-10,sd=sqrt(100))
v
```

```
##
      [1] -17.675075287345 -0.949106997727 -21.066080455948 -11.120659879294
##
      [5] -27.375027862063 -7.704144076084
                                               2.597498851215 -5.515257599821
##
      [9] -24.460034119716 -22.183513749114 -12.172376580441 -19.932224927593
##
      \begin{bmatrix} 13 \end{bmatrix} \ -40.589574811965 \ \ -4.042791369789 \ \ \ -7.921791907704 \ \ -25.171271034845 
##
     [17] -7.154827257229 -16.242704003329
                                              2.698337308058 -14.112945787479
##
     [21] -19.005216872874 -19.468127109558 -24.795080119834 -14.565484554333
##
     [25] -14.848788652614 -23.276613947575 -23.677226193297 -10.355930014706
##
     [29] -12.986072061446
                            1.102600768017 -6.553384276259 -15.398435755252
##
     [33]
          -7.097227711029 -4.257667013194 -13.818777098701 -10.428719959574
##
     [37]
          -9.935950684218 -5.243923183966 -12.050187835554 -8.347434870727
##
     [41] -17.695521882223 -10.968180101525 -21.473348771507 -23.133052728704
##
     Γ451
          -1.985455782487 -21.626807647293 -8.075617472219
                                                                3.366873499473
##
     [49]
          -3.303425209237
                             2.425684631294
                                               1.801978361841
                                                               -8.584232151446
          -9.314462577062 -22.547805356553 -12.035091979326 -10.950830893286
##
##
     [57] -20.258361001872 -12.651441378184 -7.270835552875
                                                                 4.405994575461
##
     [61] -20.461940104114 -31.414553951163 -25.646675723423 -31.331316067967
##
     [65]
          -7.578754505849 -18.151594301284 -10.930649006001 -31.168901261683
##
     [69]
          -2.477994347714 -22.548255903827 -23.210422435126 11.777299512369
            7.428032727033 -5.911275480957 -4.317293553459 -22.605811929479
##
     [73]
##
     [77]
          -8.099993583120 -2.186213991853 -11.672740794780 -15.936009458596
##
     [81] -18.449909226976 -15.456585208946 14.169397203459 -19.468018594904
##
     [85] -10.366055191468 -15.433842868361 -27.440233126389 -4.100313941819
          -2.966463692549 -14.492620488028 -12.701700545468 -17.541691505294
##
     [89]
##
     [93] -11.180618465129 -1.994373053461 -1.871776046599 -7.378958020688
```

```
##
          -5.978624547935 -0.227992529838 -3.824920429153 -5.263561992652
##
   Γ101]
         -9.201825236459 -20.680259746570 -6.773769442336 -3.421813641457
   [105]
           2.402168586646 -5.364094210864 -6.973390018061 -18.385767173802
   [109] -12.061227688453
                           3.149730197075 -16.061057180708 -2.257612039426
##
   [113]
         -9.936548168969 -12.214717137182 -12.646391042828 -15.476814365295
   [117] -10.719964382217 -4.831423449430 -26.226289884387 11.616078708203
##
   [121] -13.261104492088 -4.484189092450 -10.928835116863 -18.678733363087
           4.432487838495
                          7.326872658389 -3.453592472821 -17.509921130044
##
   [125]
##
   [129] -20.131683878681 -9.600588083671 -15.056258017703 -13.086224561976
##
   Г1331
         -8.617455313744
                         4.112372140495 -6.501328645238 -15.231188029610
   [137] -11.889499314849 -5.878917627878
                                         8.063718289513 -12.826085935949
         -9.572632577052 -28.915863828949 -17.153200677198
##
   [141]
                                                         9.870065789418
##
   [145]
         -1.940388273824 4.702765243513 -17.468046163970 -6.004097269767
         11.808930687967 -12.547324728295 -22.409038918006 -9.845173737171
##
##
   [153] -19.243068174955 -24.848475317706
                                         0.033457003406 -21.738261723065
##
   [157] -25.245306280145 -14.372955851173 -7.624926851233 -12.531633969231
    \begin{bmatrix} 161 \end{bmatrix} \ -15.048875315416 \ \ -9.819212127515 \ \ -16.669332712485 \ \ -10.389585416116 
##
##
   [165] -24.518493496738 -29.667647936582 -9.001201792480 18.699913183824
   [169] -11.523515208863 -17.025039467558 -10.190485663506 -1.964954170292
##
##
   [173]
         10.577590264792 -13.362521187145 -18.038520820021
                                                         -9.770044051213
##
   Γ177]
         -2.497586390317 -11.279282118801 -25.689231809685 -17.734640601634
   [181] -20.479633767396 -4.313128204591 -0.816196578256
                                                         -3.137077767318
   [185] -18.315873095340 -27.045625650228 -12.006588214002
                                                         6.427404185808
##
    [189] -13.762627132292 -5.139469059477 -21.335230825650 -25.701437700320
##
   [193] -16.302337394572 -12.292421632107 -6.170152707879 -14.100263915475
##
   [197] -21.874545053831 -26.410526890184 -10.979108727875
                                                          1.785934892104
##
   ##
   [205]
           4.650885604901 -4.852856029993 -14.431637615470 -20.005374895754
##
   [209]
           0.790701783115
                           2.178876415095 -1.025521151893 -22.143975940735
   [213]
         -5.310478062384 -33.294901729148 -19.660011088052 -28.358201912067
   [217] -10.389592912381 -30.133521718314 -9.985158367923 -14.934985668312
##
##
   [221]
           3.197142077887 -19.581111271523
                                          9.751130885028 -12.962741220576
##
   [225]
          16.609731115238 -19.538412669592
                                         2.086703561310 -13.410858759493
   [229]
           0.364268369458 -22.932200198355 -11.848197017461 -9.736149822799
##
##
   [233] -31.741954663254
                          4.202722956243 -33.994704404213 -9.226817710218
##
           9.890592798578 -3.972847793470 -22.254856962172 -9.280720115976
   [237]
##
   [241] -14.738227349677 -7.964379417245 -26.592598337096 -0.677299560044
##
   [249] -17.123331894326 -15.392392614509
                                          5.023418729435 -4.183555954247
##
##
   [253] -11.223875612457 -3.993167998937 -1.096992059817 -23.582418019742
         -9.761800307751 -27.340710029202 -5.101081082792 -14.113802483831
   [257]
##
   [261]
           6.230270720496 -20.426100423141
                                         3.074772452820 11.653107665237
##
   ##
         -3.431481080231 -2.669263983490 -9.635902077450 -16.387862285020
   [269]
   [273] -13.629913959958 -15.399706528673 -21.411677678622 -7.192973702671
##
   [277]
         -9.719796840692 -23.943799095410 -10.608644583268 -1.864279050982
##
   [281] -17.362904858532 -7.711483441580 -2.987507816457 -16.185621285070
         -7.300760987886 -17.993267567723 -0.869820541584 -4.642587624481
##
   [285]
##
   [289]
         -0.966277954573 -4.521689180411
                                         0.274473021962 -14.045851845721
##
   [293]
           8.685332385166 -6.394307376462 -15.895829683093 -16.098429697997
##
   ##
           2.632572155427 -13.760696656096 -2.662559305228 -12.690014907739
##
   [305] -19.135956878579 -18.220056773777 0.913472322452 -22.122930669266
   [309] -23.942725567812 -8.892440811686 -23.469067746007 -11.142992876375
```

```
##
    [313]
            2.965306046357 -4.409664088108
                                             4.446731609640 17.563713724939
##
           -9.784752606683 -9.368148757915 -24.211164541320 -35.702560240790
    Γ3177
    [321]
##
           -7.939482013140 -6.516497619739 -20.030629940175 10.070250336529
    [325]
           -2.295733075421 -21.892024607116 -24.097162644068 -11.373080851947
##
##
    [329] -15.709581008943 -4.321873730397
                                             -7.525743346105
                                                                5.723427405123
                             5.238354411043
##
    [333]
           -5.804678081388
                                               1.458355619524
                                                              -9.044075696258
##
    [337]
           -9.525746487472 -16.791141888638 -48.773558171947 -10.806989413334
##
    [341]
           -0.893143291288 -15.194890291363 -20.853839009389 -0.514692059810
##
    [345] -21.584089465274 -11.425546879343
                                               2.671230766599 -12.911662560195
##
    [349]
          -6.915935685304 -10.486961142163
                                               3.090580306872
                                                                3.202106743289
    [353] -11.020154543166 -20.169191134749 -1.392838391696
                                                              -5.282976358578
##
     \begin{bmatrix} 357 \end{bmatrix} \ -22.930325496718 \ \ -4.367569658851 \ \ -23.097951559090 \ \ \ -5.129010771743 
##
    [361]
          -9.198866978781 -4.070163709157 -10.514481048732 -17.715207194223
##
          -2.888227858856 -18.517251900259 -12.345561313218 -20.649390250901
##
    [369] -16.953279749864 -13.751822248678 -15.911455213490 -27.458170500670
    [373] -11.631700120767 -8.855348299840 -20.184380708685
##
                                                              -9.881159831317
    [377] -13.408893035642 -13.464154474975 -25.095494127423
##
                                                              -2.749464524350
##
    [381] -19.390047644923 -2.040358131737 -6.373167878764 -14.5355554237514
          -5.675464812310 -6.233932493987 -10.104283638124
##
    [385]
                                                              -3.916170461888
##
    [389]
           -9.430213156515 -12.985485211286 -14.760361187738 -13.118356311670
##
    [393]
           -9.388084506682
                             1.916235917823 -7.228031503635
                                                              -7.727836275254
           -5.237567610826 -10.748695424443 -21.879460534838
##
    [397]
                                                               -2.472554464817
           -5.298320775399 -13.877768994742 -4.753386575356
##
    [401]
                                                               4.397443670378
                           -3.135526270782 -31.680559441996 -20.238193926398
##
    [405] -33.661510175126
##
    [409]
           -1.678197865810 -0.345224422496 -5.917970456579
                                                              -0.197095044759
    [413] -17.552539175191 -1.720355924099
                                               2.666904697729
                                                                7.375745692462
##
          -9.410704904291 -5.580161581670 -19.190156392236 -14.219405784947
    [417]
##
    [421] -18.129578131008
                            4.074238025536
                                             -3.760343990745 -22.713695847586
##
    [425]
          -6.944201733727 -11.980321420525
                                             -8.508423411349
                                                                0.780020973064
##
    [429]
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##
##
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```

```
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##
##
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##
    [789]
##
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##
##
     \hspace{-0.2cm} \begin{bmatrix} 801 \end{bmatrix} \hspace{-0.2cm} -12.191610301876 \hspace{-0.2cm} -23.347693539336 \hspace{-0.2cm} -25.414640207544 \hspace{-0.2cm} -6.269143825294 
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##
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##
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##
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```

```
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    [997] -18.501539379958 -12.463851659622 -13.580793521121 -25.843965795372
##
```

• Repeat this exercise by resetting the seed to ensure you obtain the same results.

```
set.seed(1997)
v = rnorm(n=1000,mean=-10,sd=sqrt(100))
v
```

```
##
      [1] -17.675075287345
                           -0.949106997727 -21.066080455948 -11.120659879294
##
      [5] -27.375027862063
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                                              2.597498851215 -5.515257599821
##
      [9] -24.460034119716 -22.183513749114 -12.172376580441 -19.932224927593
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##
##
     [17]
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                                              2.698337308058 -14.112945787479
##
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##
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##
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           -7.097227711029
                           -4.257667013194 -13.818777098701 -10.428719959574
##
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##
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##
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##
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##
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##
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##
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##
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##
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##
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##
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                                             -9.066324613121 -13.099850723063
##
    [881]
                                                               -1.880561571816
##
            2.517334178585
                           -8.935111102874
                                             -4.313905787717
##
    [885] -13.509723595541 -3.998287082879 -12.637571829360
                                                                0.440133318485
    [889]
##
           14.737675994047 -18.887347223915 -17.166079851847
                                                                9.875921094057
##
    [893]
            9.373452314285 -17.996420211031
                                               0.473297723096
                                                               -2.292451090348
    [897]
            7.393356590663 -18.446689035399
                                             -7.407025308317
                                                               -9.836695468562
##
##
    [901] -24.293850570496
                             3.138795042317 -10.270704585457 -18.338540910022
##
    [905]
           -5.501582012862
                           -6.980088784870 -12.652867380358 -14.781704774933
                                                               -4.112691982488
##
    [909] -25.709052719330
                             3.772261470857
                                             -8.509155007500
##
    [913]
           -9.379344620707
                           -7.012729909946 -18.502162629534
                                                               -9.159802455501
##
    [917]
           -1.840557648498 -11.265947814851 -36.310895501028
                                                                1.246698625679
##
    [921] -20.055574270685 -15.470823427666
                                             -1.038353891399
                                                               -1.667278284115
           -8.861503658918 -14.461051286110
##
    [925]
                                             -6.975857119940
                                                                9.165435780991
    [929]
            2.050150304393 -14.911253673842
                                             -0.181231213955
                                                               -9.144319447371
##
    [933]
                             4.282227599374 -10.023856340859 -18.731177899862
##
           -5.152894343570
##
    [937]
           -3.531176173338
                            -8.633308074774 -20.458867605230
                                                                9.882671510279
##
    [941]
           -9.397524420981
                             3.247688078190
                                              3.454760414189 -19.787317830780
    [945]
           -4.496197793864 -24.693210102616
                                             -9.248832541561 -13.068029744425
##
##
    [949]
            6.766416683629
                             2.148152841838 -11.392572536977
                                                              -3.851279549607
##
    [953] -26.143552739200
                             2.783335997745
                                               1.301441145727 -11.383544876582
           -2.404886994915 -31.007177348761
                                             -8.599015667673
                                                              -6.797852741519
##
    [957]
##
    [961] -12.949516069881
                           -5.885844667457 -12.861530029051 -11.685482842150
##
    [965]
          -7.008156417712 -20.122997520924
                                             -4.986584501372 -6.796762392667
##
    [969]
            0.281175970454
                            -3.671363470527
                                             -8.203528195177 -13.652787032792
                            -6.934206316057 -19.726258607731
                                                                2.922769588320
##
    [973] -16.902457609334
##
    [977] -12.206112040685
                            -0.397556937674 -14.266088631673 -14.723349180514
##
    [981]
           -5.599160138138
                           -1.852944660173 -4.083250181944 -10.845154790800
##
    [985]
           -1.411709968699 -19.781316714126 -22.786275679921
                                                               -8.419756783495
##
    [989]
         -16.313684418112 -15.453658186605 -10.068335210721
                                                               -3.347334682254
           -4.242505656619 -21.359160113491 -9.247988491033 14.831359093131
##
    [993]
##
    [997] -18.501539379958 -12.463851659622 -13.580793521121 -25.843965795372
```

• Find the average of v and the standard error of v.

```
mean(v)

## [1] -9.6941212672

sd(v)
```

• Find the 5%ile of v and use the qnorm function to compute what it theoretically should be. Is the estimate about what is expected by theory?

```
?quantile
quantile(v, 0.05)

## 5%
## -25.41669862

?qnorm
qnorm(0.05, mean=-10, sd=sqrt(100))

## [1] -26.44853627

# The estimate is about the same
```

• What is the percentile of v that corresponds to the value 0? What should it be theoretically? Is the estimate about what is expected by theory?

```
inverse_quantile_obj = ecdf(v)
inverse_quantile_obj(0)
```

[1] 0.848

[1] 9.7639309287

The estimate is about the same when you take the CDF of 0 of this distribution 0.84134475