Section 2: summarizing single variables

STOR 155.02, Spring '21

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What you will learn

- sample distributions
- plots: bar graphs, histograms
- centrality statistics: mean, median
- spread statistics: range, percentiles (aka quantile), variance and standard deviation

Resources

• Textbook ch 1.6.2-1.6.5 and 1.10

Looking at data

Definition: sample distribution

The sample distribution of a variable tells us what values it takes and how often it takes these values in our dataset.

this is about the values a variable actually has in your data

does *not* tell you about all possible values your variable could have if you got more or different data

frequency statistics

- **frequency** of a category is the **number of observations** in that category
- relative frequency is number of observations in a category / total number of observations

distributions: categorical

- given by **relative frequencies** of each category
- think of it as the chance a randomly chosen observation falls in that category
- e.g. relative frequency of 0.1 for category 'A' means 10 percent of observations of type 'A'

distributions: quantitative

- given by **relative frequencies in a range** of possible values
- think of as the chance a randomly chosen observation falls in the range
- will evaluate with **histogram** plots

Looking at sample distributions: depends on the variable type

Categorical:

Numeric/quantitative:

bar graphs

histograms

pie charts

Looking at categorical data

bar graph

- bar height represents frequency or relative frequency for each category
- the frequency must first be computed

pie chart

- area of a pie slice represents the relative frequency of a category
- these can be **hard to read** because areas are difficult to estimate by eye
- can be used **only for** counts adding to the total number of observations, or percentages adding to 100

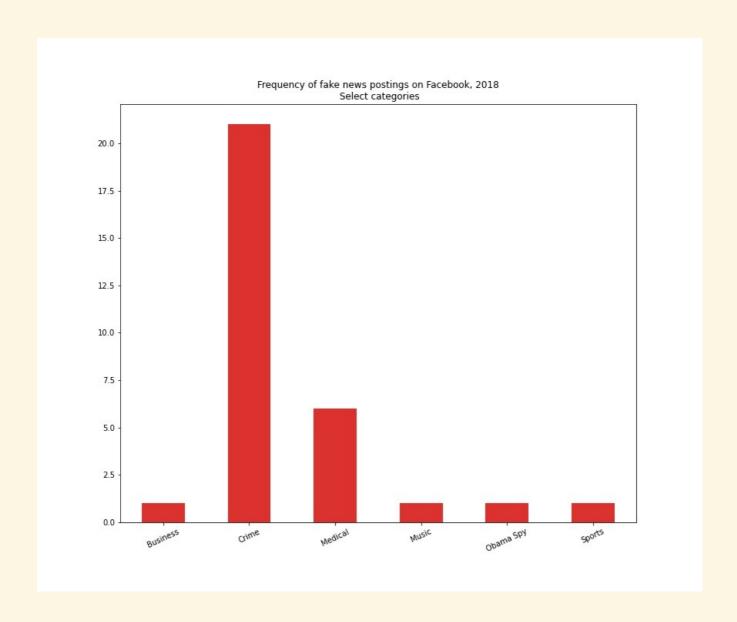
Example: Fake news on facebook

dataset

- data on Facebook popularity of posts by fake news websites in 2018
- identified and collected by Buzzfeed News
- Biggest fake news hits on Facebook in 2018
- source: Buzzfeed github site
- dataset on our course github page as well

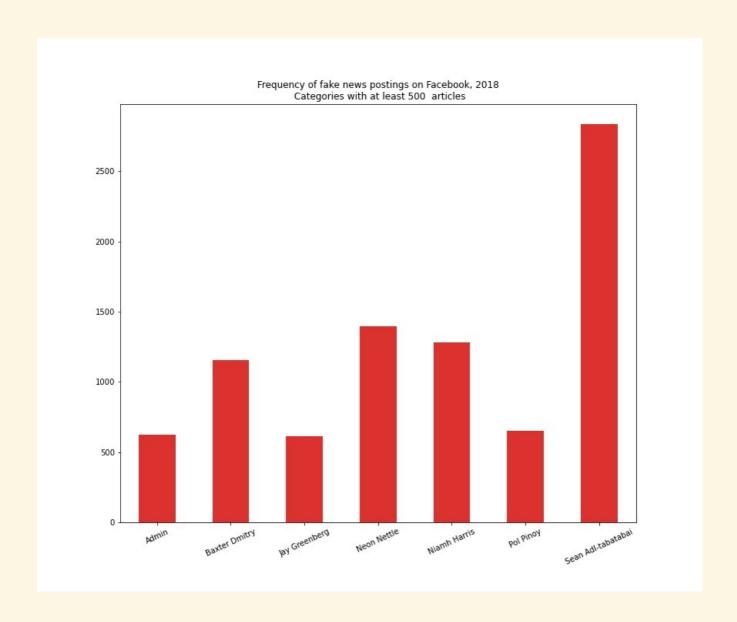
observations and variables

- each row is represents an article
- fb_engagement is essentially number of likes post received
- category is a buzzfeed-created categorical variable



There are too many weird small categories to show nicely, so I picked some I was interested in.

but what does it look like if we isolate the most common posting categories?



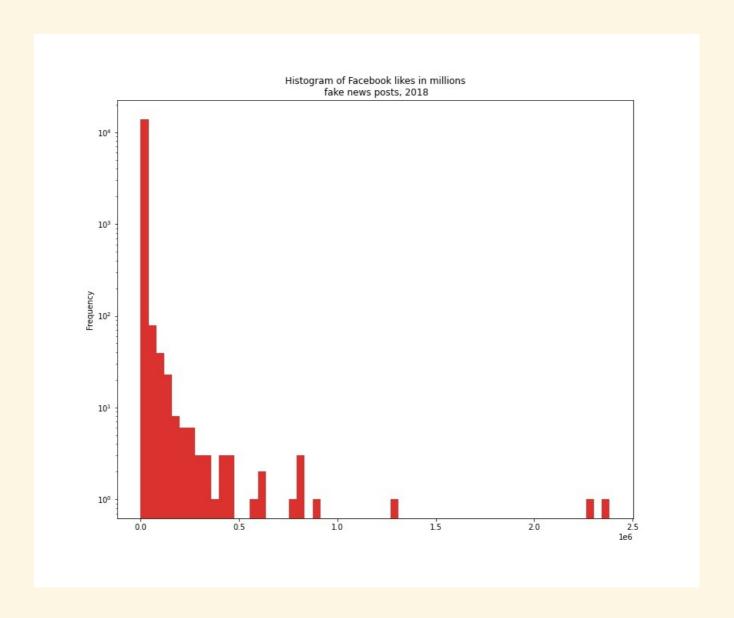
Does this information make sense?

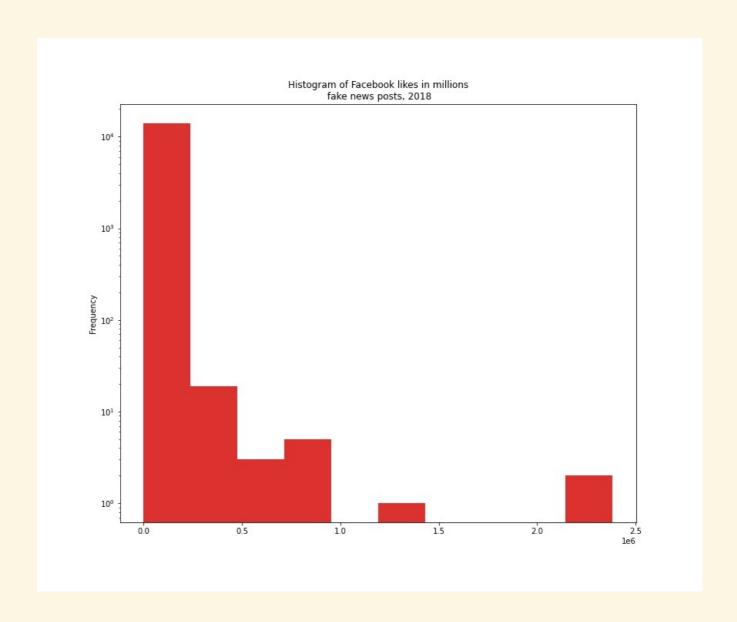
Will investigate a little in the group exercise.

Histogram: looking at quantitative variable distributions

- breaks the range of the values into bins (intervals) of a given width
- displays frequencies or relative frequencies of the observations that fall into each interval
- choose any convenient number of intervals of equal width
- but choice of width might affect how you interpret the data

Example: **fb_engagement** variable histogram with differing bin sizes





A good histogram allows you to guess at key properties of a numeric variable:

- 1. What are the maximum and minimum values?
- 2. What is the 'middle' value?
- 3. What is the average value?
- 4. Are the values concentrated around the average or spread out?
- 5. What is (are) the most common value(s)?

These are all important statistics of a numeric variable.

Let's make these ideas more precise

Sample statistics for numeric variables

Range:

• max value minus min

Nth percentile (aka quantile):

 value defining a cutoff so that N percent (appropximately) of your data is below that value

Median:

• 50th percentile, half of the data is below this value, half above

Mean:

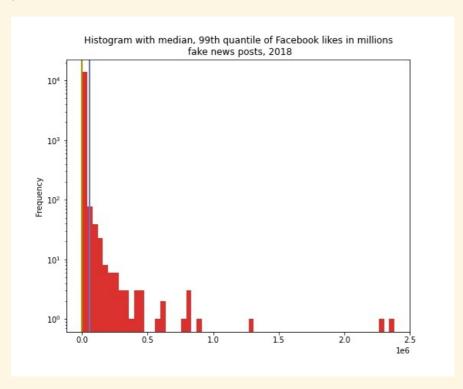
average

Variance:

• average squared distance of values from the mean. A way to think about how *spread out* the data are

Example: Guessing the Nth percentile

Use bar height to guess bin such that N percent of data is below it. Hard to tell with some plots! Remember $(1e6 = 10^6 = 1)$ million.



Math definitions

If I have some number $\(n\)$ data points, I will represent my numeric variable values by $\$X_1, X_2 ... X_n \$$

mean

$x_{X} = \frac{1}{n}\sum_{i=1}^n X_i = X_1 + X_2 + 1 < X_n$

variance

 $\frac{1}{n}\sum_{i=1}^n \left(X_i - \frac{1}{n}\right)^2$

Warning!

For reasons not important to this class, sometimes statistical software will calculate variance with $(\frac{1}{n-1})$ in front instead of $(\frac{1}{n})$.

We'll talk about it in the data homework.

Averages are everywhere. What do they tell us, and not?

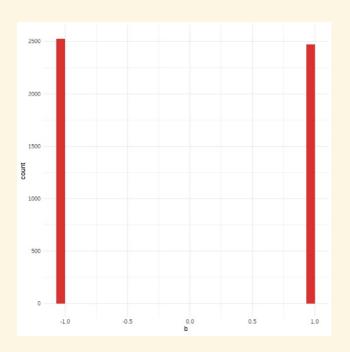
does not tell you

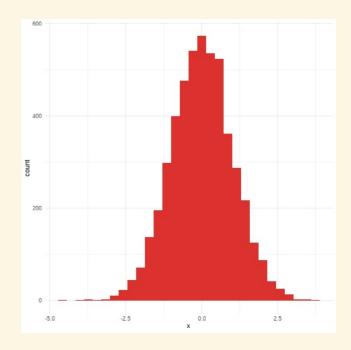
- how evenly values are spread
- min/max
- whether a few extremely big (positive or negative) values are influencing the calculation
- median tells you about the middle but is less sensitive to extreme values

but important because

- a common way to capture the 'middle' value, along with median
- magic of the bell curve: we'll see this later!

These two variables have approximately the same average, \(\bar{X} = O\)





Group breakout exercise

Poll closes at ___!

Poll everywhere link:

https://PollEv.com/surveys/wk1afrjltBXR1J1GQIO

You must be registered to submit a response!

Discuss with group but respond individually

