Week 3 - Sorting Algorithms

AD 325 - Brenden West

Contents

Reading & Videos

- Carrano & Henry, Chapters 15 16, Interlude 5 Generics
- https://www.coursera.org/learn/algorithms-part1/home/week/2 Elementary Sorts
- https://www.coursera.org/learn/algorithms-part1/home/week/3
- https://algs4.cs.princeton.edu/20sorting/ (review)
- https://www.geeksforgeeks.org/sorting-algorithms/ (review)

Learning Outcomes

- Elementary sorting algorithms
- Comparable interfaces
- Advanced sorting algorithms
- Performance considerations for sorting

Key Concepts

- comparable data to be sorted must be comparable e.g. implement Java's Comparable interface
- recursion The process in which a function calls itself directly or indirectly.
 Can achieve results similar to loop, but with different memory usage.
- cost model number of compares and exchanges (or array accesses).
- best, worst, average cases a sorting algorithm's performance can vary in different cases - e.g. whether input data is already sorted.
- memory usage in-place sorting algorithms use constant extra space by modifying elements in the existing array or list. Others use extra memory to hold another copy of the array to be sorted.

Key Concepts, cont.

- stability output from a stable sorting algorithm has objects with equal values
 in the same order as in the original input.
 - https://www.geeksforgeeks.org/stability-in-sorting-algorithms/
- **divide-and-conquer** is an algorithmic paradigm that solves a problem using following three steps:
 - Divide: Break the given problem into subproblems of same type.
 - Conquer: Recursively solve these subproblems
 - Combine: Appropriately combine the answers

Comparable Data

- Data items being sorted must be comparable
- In Java, this means Objects to sort must support the Comparable interface and implement a compareTo() method
- Some built-in comparable types Integer, Double, String, Date
- Comparable methods must:
 - Support total order (antisymmetry, transivity, totality)
 - Return a negative integer, zero, or a positive integer
 - Throw an exception for incompatible types

Key Sorting Algorithms

Elementary

- Selection sort
- Insertion sort
- Shell sort

Advanced

- Mergesort
- Quicksort

Selection Sort

Select the smallest item in the array, and exchange it with the first entry. Then, find the next smallest item and exchange it with the second entry. Continue in this way until the entire array is sorted.

- average case: uses ~N²/2 compares and N exchanges
- Running time insensitive to input. Quadratic time, even if input is sorted

Insertion Sort

Consider items one at a time, swapping the current item with larger items to the left.

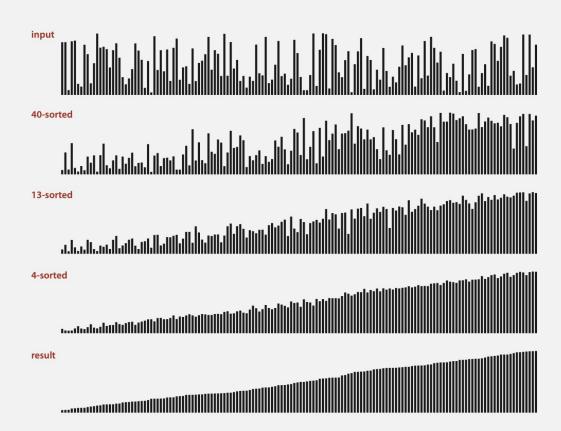
- average case: for randomly ordered arrays, uses ~N²/4 compares and ~N²/4 exchanges.
- worst case: for array sorted in descending order. ~ N²/2 compares and ~ N²/2 exchanges
- best case: for array sorted in ascending order. N-1 compares and 0 exchanges
- works well for certain types of non-random arrays. E.g. for partially sorted arrays insertion sort runs in linear time

Shell Sort

A simple extension of insertion sort that gains speed by exchanging entries that are far apart (*h*-sorting).

- produces partially sorted arrays that can be efficiently sorted, eventually by insertion sort.
- h-sorting is repeated with smaller values of h until the array is fully sorted.
- Optimal increment sequence is 3x + 1
- **Worst case**: number of compares used with 3x+1 increments is $\sim O(N^{3/2})$

Shellsort: visual trace



Mergesort

- A simple recursive method to sort an array by:
 - dividing it into two halves,
 - sorting each half (recursively),
 - merging the results
- Worst case: sorts an array of N items in time proportional to N lg N
- uses extra space proportional to N
- Mergesort improvements:
 - Use Insertion Sort for sub-arrays with < 7 items
 - Stop if already sorted

Mergesort: trace

```
10
     merge(a, aux, 0, 0,
     merge(a, aux, 2, 2, 3)
   merge(a, aux, 0, 1, 3)
     merge(a, aux, 4,
                      4, 5)
     merge(a, aux, 6, 6, 7)
   merge(a, aux, 4, 5, 7)
     ge(a, aux, 0, 3, 7) E E G M
merge(a, aux, 8, 8, 9) E E G M
 merge(a, aux, 0, 3, 7)
     merge(a, aux, 10, 10, 11)
   merge(a, aux, 8, 9, 11)
     merge(a, aux, 12, 12, 13)
     merge(a, aux, 14, 14, 15)
   merge(a, aux, 12, 13, 15)
 merge(a, aux, 8, 11, 15)
merge(a, aux, 0, 7, 15)
```

result after recursive call

Quicksort

- Works well for a variety of different kinds of input data, and is substantially faster than any other sorting method in typical applications.
- Quicksort is a divide-and-conquer method for sorting. It works by partitioning an array into two parts, then sorting the parts independently.
- It uses in-place swaps and requires time proportional to NlogN on the average to sort N items
- Quicksort uses ~2NInN compares (and one-sixth that many exchanges) on the average to sort an array of length N with distinct keys.
- Quicksort uses ~N²/2 compares in the worst case, but random shuffling protects against this case.

Stability

A **stable** sort preserves the relative order of items with equal keys.

Insertion sort and mergesort are stable.